\(\alpha\)-decay-correlated mass measurement of \(^{206,207g,m_1}\)Ra using an \(\alpha\)-TOF detector equipped multireflection time-of-flight mass spectrograph system


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The atomic masses of the isotopes \(^{206,207}\)Ra have been measured via decay-correlated mass spectroscopy using a multireflection time-of-flight mass spectrograph equipped with an \(\alpha\)-TOF detector. The Ra isotopes were produced as fusion-evaporation products in the \(^{51}\text{V}+^{159}\text{Tb}\) reaction system and delivered by the gas-filled recoil ion separator GARIS-II at RIKEN. The \(\alpha\)-TOF detector provides for high-accuracy mass measurements by correlating time-of-flight signals with subsequent \(\alpha\)-decay events. The masses of \(^{206}\)Ra and \(^{207}\)Ra were directly measured using a multireflection time-of-flight mass spectrograph equipped with an \(\alpha\)-TOF detector. The mass excesses of \(^{206,207}\)Ra and the excitation energy of \(^{207}\)Ra were determined to be \(\text{MB} = 3540(50)\text{ keV/}	ext{c}^2\), \(3538(15)\text{ keV/}	ext{c}^2\), and \(E_{\gamma} = 552(42)\text{ keV}\), respectively. The \(\alpha\)-decay branching ratio of \(^{207}\)Ra, \(b_\alpha = 0.26(20)\), was directly determined from decay-correlated time-of-flight signals, and the reduced \(\alpha\) width of \(^{207}\)Ra was calculated to be \(\delta^2 = 43(36)\text{ keV}\) from the branching ratio. The spin-parity of \(^{207}\)Ra was confirmed to be \(J^\pi = 13/2^+\) from decay correlated mass measurement results.

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I. INTRODUCTION

The structures of heavy and superheavy nuclides are strongly influenced by shell effects, and investigations of the ground and excited state properties provide us important information for the understanding of these nuclides. The binding energy of the ground state nuclide, as a direct mapping of the nucleus structure, is of utmost importance for understanding these nuclides. The binding energy provides us information about the nuclear force and the effect of shell effects. Investigations of the atomic masses have strongly influenced by shell effects, and investigations of the atomic masses have been performed with REXTRAP at CERN/ISOLDE for conversion to the atomic mass standard and the atomic mass excess standard.

\(^{150}\text{Ho}\) by Penning-trap mass spectrometry at CERN/ISOLDE, wherein it was found that the indirect measurements, from \(\beta\)-decay spectroscopy, had an 800 keV discrepancy due to a misidentification of the excited and ground states [1,2].

The structure of \(\gamma\)-transitioning isomers has been studied with high precision based on \(\gamma\)-ray spectroscopy. However, there are still many nuclides in which the isomeric states undergo direct \(\alpha\) or \(\beta\) decay, precluding the application of \(\gamma\)-ray spectroscopy. Separately, there have been a number of decay spectroscopy measurements assisted by mass separation, utilizing both Penning traps and multireflection time-of-flight mass spectrometers (MRTOF-MS). The first experiment where such trap-assisted decay spectroscopy was performed with REXTRAP at CERN/ISOLDE for conversion to the atomic mass standard and the atomic mass excess standard.

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electron studies [3]. Since then, several experiments have been performed using high-resolution mass separators coupled with a decay station [4–8]. Apart from an effort to measure half-lives using variable storage time in an ion trap connected to an MRTOF [9], until now when performing trap-assisted decay spectroscopy the mass determinations and decay measurements were performed independently; the mass spectrometers have always been employed as high-resolution mass separators.

Recently, we developed a novel detector, which we refer to as an α-TOF [10], that can simultaneously measure ion implantation (to deduce time of flight) and subsequent α-decay events from implanted ions. From these correlated signals, we can perform mass and decay spectroscopy for multiple nuclides simultaneously. We have previously described the use of this decay-correlated mass spectroscopy to suppress background. Other nuclear properties can be inferred using the detector; the lifetime of each nuclide, for instance, can be determined from the time intervals between the time-of-flight signal and the decay signal. In this paper, we report on the decay-correlated mass spectroscopy of $^{206}$Ra using an MRTOF-MS equipped with an α-TOF detector, demonstrating several capabilities beyond atomic mass determination.

II. EXPERIMENTS

Decay-correlated mass measurements were performed at the SHE-Mass-II facility, jointly operated under the auspices of RIKEN Nishina Center and KEK Wako Nuclear Science Center, within the RIKEN RI Beam Factory. The experimental setup is shown in Fig. 1. A primary beam of $^{51}$V$^{13+}$ was prepared [11], preaccelerated by the RILAC-II linear accelerator, and injected into the RIKEN Ring Cyclotron (RRC) where it was accelerated to 306.0 MeV and impinged upon targets in front of the gas-filled recoil ion separator GARIS-II [12].

Sixteen targets of $^{159}$Tb, produced by sputtering onto 3.0-μm-thick Ti backing foils and having an average thickness of 460 μg/cm², were mounted on a 16-sector rotating target wheel [13], which rotated at 2000 revolutions per minute during the beam irradiation. While the peak cross section for the desired reactions occurs well-below 306.0 MeV, the RRC could not deliver a lower energy beam. Therefore, 12.5-μm Al foil energy degraders were also mounted on the target wheel [14], upstream of the targets. By using the energy degraders, the primary beam energy at target center was 219.1 MeV. To pass $^{207}$Ra the magnetic rigidity of GARIS-II was set to 1.66 Tm; the He-gas pressure was set to 71 Pa. Under this setting, the evaporation residues (ERs) produced in the $^{159}$Tb($^{51}$V, X) reaction were efficiently transported while the unreacted primary beam and other background products were suppressed by GARIS-II.

A secondary beam degrader made from 9.6-μm-thick Mylar foil was installed in the focal plane chamber of GARIS-II. The energy-degraded ERs were then stopped and thermalized in a cryogenic helium gas cell, pressurized to 100 mbar room-temperature equivalent and cooled to 50 K. The thermalized ions were extracted from the gas cell using a traveling wave radio frequency (RF) carpet [15], transferred to an RF ion guide and transported to an RF ion trap suite. After a final cooling process in the “flat trap” [16] (see Fig. 1), the ions were orthogonally ejected from the trap and injected into the MRTOF-MS. In this experiment, the MRTOF-MS was optimized to produce a time focus after 266 laps.

If the mean time between ion implantations is too short compared to the α-decay half-life, subsequent ion implantation may occur prior to α decay. Such events can impede decay correlation and decay spectroscopy. Therefore, for the α-decay correlated measurements of $^{207}$Ra ($t_{1/2} = 59$ ms), the incoming rate of total ions of $^{207}$Ra$^{2+}$ at the MRTOF-MS was limited to about 0.2 cps by reducing the primary beam current to approximately 100 pA, corresponding to an impinging beam of $6.2 \times 10^{12}$ particles per second.

Two measurement runs were performed. The first was six hours in duration, while the second was a 10 hour measurement wherein ions made an extra lap in the MRTOF to confirm identifications. Making measurements at two different numbers of laps ensures that we do not erroneously misattribute TOF peaks from, e.g., stable molecular ions making an arbitrary number of laps and coincidentally having a TOF similar to our analyte. In principle, by making correlations between TOF and subsequent α decay, this precaution is not necessary; however, it does provide an added layer of confirmation.

III. ANALYSIS AND RESULTS

Figure 2 shows the full-range TOF singles spectra for the two runs. In Run #1, the MRTOF-MS timing was configured such that A/q = 103.5 ions would make 266 laps in the MRTOF and A/q = 103 ions would make 267 laps; care was taken to ensure ions of both A/q were not effected by the ejection-side mirror switching [17]. Among the A/q = 103.5 ions, $^{207}$Ra$^{2+}$ and $^{207}$Fr$^{2+}$ were identified, while $^{206}$Ra$^{2+}$ and
were identified among the $A/q = 103$ ions. To exclude misidentification of these ions, in Run #2 the ejection mirror timing was adjusted such that $A/q = 103.5$ ions made 265 laps and $A/q = 103$ ions made 266 laps. As the same identifications were made in this hourlong cross-check measurement, we can be confident of the identifications. The lack of particularly mass selective elements between the gas cell and MRTOF automatically allows for the simultaneous study of multiple $A/q$ chains. The tune of the MRTOF used in this work resulted in the $A/q = 103$ and 103.5 chains having flight lengths differing by one lap, and their relative separation changes only slightly with small variations in the lap number. Other isobaric chains, however, will generally exhibit larger changes in their relative position in the time-of-flight spectrum under small variations in the lap number.

The times of flight were determined from TOF spectral peaks by fitting using an asymmetric Gaussian-hybrid function [18]:

$$f(t) = \begin{cases} A_0 \mathcal{N}(t-t_L, \sigma^2) & (t \leq t_L), \\ A e^{-(t-t_L)^2/2\sigma^2} & (t_L < t < t_R), \\ A_0 e^{-(t-t_R)^2/2\sigma^2} & (t \geq t_R), \end{cases}$$

where $A$ is the Gaussian peak height, $t_c$ is the Gaussian centroid (i.e., the time of flight), and $\sigma$ is the standard deviation. The fit function smoothly transitions from Gaussian to exponential on both sides of the peak, with the transition point defined to be $t_L = t_c - \delta t_1$ on the left side and $t_R = t_c + \delta t_2$ on the right side.

The data in Fig. 2 were drift corrected using $^{85}Rb^{+}$ ions from a thermal ion source. These reference ions were measured concomitantly [17] with the analyte ions shown in Fig. 2. The time-of-flight spectra were divided into subsets of 7.5 s duration, each was fitted using Eq. (1), and then the.

![FIG. 2. The full-range time-of-flight singles spectra for two settings of the MRTOF-MS. (a) The upper panel shows the result of the six hour measurement wherein $A/q = 103.5$ ions made 267 laps; (b) the lower panel shows the result of the one hour measurement wherein $A/q = 103.5$ ions made 265 laps. The dashed blue lines indicate the positions of the Fr and Ra isotopes, demonstrating that their relative positions were largely constant under change of lap number between the two runs. Several peaks, presumed to be stable molecular ions extracted from the gas cell, were observed but did not correlate with $\alpha$-decay signals.](image)

206Fr$^{2+}$, 207Ra$^{2+}$, and 206,207Fr were identified among the $A/q = 103$ ions. To exclude misidentification of these ions, in Run #2 the ejection mirror timing was adjusted such that $A/q = 103.5$ ions made 265 laps and $A/q = 103$ ions made 266 laps. As the same identifications were made in this hourlong cross-check measurement, we can be confident of the identifications. The lack of particularly mass selective elements between the gas cell and MRTOF automatically allows for the simultaneous study of multiple $A/q$ chains. The tune of the MRTOF used in this work resulted in the $A/q = 103$ and 103.5 chains having flight lengths differing by one lap, and their relative separation changes only slightly with small variations in the lap number. Other isobaric chains, however, will generally exhibit larger changes in their relative position in the time-of-flight spectrum under small variations in the lap number.

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The masses $m$ of ions with charge $q$ were determined using the single-reference method [19,20]

$$m = \frac{q}{q_{\text{ref}}} \rho m_{\text{ref}} = \frac{q}{q_{\text{ref}}} \left( \frac{t-t_0}{t_{\text{ref}}-t_0} \right)^2 m_{\text{ref}}, \quad (2)$$

where $\rho$ is the time-of-flight ratio between the analyte and reference, and $t_0$ is the delay between the time-to-digital converter start signal and the ejection from the preparation ion trap which sends ions to the MRTOF-MS. When analyte and reference ions are isobaric, the contribution of $t_0$ becomes negligible and can be ignored. The analyte ions were identified from their time-of-flight ratios with the $^{85}Rb^{+}$ ions, using Eq. (2) with $t_0 = 40(4)$ ns. In this work, 206,207Fr$^{2+}$ ions were used as isobaric references in the precise determination of the masses of 206,207Ra, 206,207mRa.

The $\alpha$-singles spectrum measured during Run #1 is shown in Fig 3(a). Directly transported 207Fr, 207/mRa, 206Fr, and 206Ra were observed, along with their Rn, Po, and At isotope decay products. Figures 3(b) and 3(c) show the TOF-correlated $\alpha$-decay spectra for 207Ra$^{2+}$ and 206Ra$^{2+}$, respectively.

The probability of an accidental coincidence is calculated from the ratio of the total coincidence time gate to the total measurement time. In the analysis of 207Ra shown in Fig. 3(b), we selected 180 ms as the coincidence time ($T_c$), which corresponds to three half-lives of 207mRa. According to this coincidence time and the counting of time-of-flight signals, we estimated that 1.8% of the 207Ra produced accidental coincidences. Consequently, the decay-coincidence gated TOF spectrum is contaminated, with 8.6% of the counts being 207mRa. Nonetheless, it can be seen that the isomeric
component is greatly enhanced compared to the singles spectrum.

In the analysis of 206Ra, shown in Fig. 3(c), we selected a coincidence time of \( T_c = 960 \text{ ms} \). The accidental coincidence rate induced by 207Fr, 206Ra, etc. was calculated to be 1.5%. In this case there are no isomeric states to hinder the correlation analysis.

The decay energies of 207Ra and 206Ra were determined to be 7.354(28) and 7.294(23) MeV, respectively, by application of least-square fitting of the TOF-correlated α-decay spectra. To provide a calibration in the determination of absolute decay energy, the α-decay energy of 207Fr was fixed to the literature value of 7.131 MeV [21]. The intensity of 207Fr used in the fitting process was fixed by the calculated number from the α-decay singles spectrum. These results are in agreement with literature values derived from precise α-decay measurements [21,22].

A. 206Ra

Figure 4 shows the time-of-flight spectra measured in the two runs, centered on the ions 206Fr\(^{2+}\) and 206Ra\(^{2+}\). The TOF singles spectra are shown in black, while the 206Ra α-decay correlated TOF spectra are shown in blue. A spurious ion species, presumably a stable molecular ion, can be seen in the tail of the 206Ra\(^{2+}\) case of 267 laps, but it is suppressed by the decay correlation.

Within a region of \( \pm 50 \text{ ns} \) of the center of the 206Ra\(^{2+}\) spectral peaks there were 162 decay-correlated TOF events using \( T_c = 960 \text{ ms} \), out of 327 TOF singles events. The fraction of correlated events, 49.5%, agrees well with the previously reported α-TOF efficiency [10].

The isobaric molecular ions should all have the same peak shape, and therefore we simultaneously fit the two spectra (singles and α-decay correlated) for each run with the width and exponential tail parameters conserved across all peaks. While the spurious intruder ion may exhibit a slightly different shape, its low intensity precludes any minor shape difference resulting in significant biasing of the fit parameters.

A more pressing issue, if we wish to use isobaric referencing, is the isomerism of 206Fr. If all three states were delivered, the second isomer (\( E_{\alpha} = 730 \text{ keV} \)) would be resolvable in the TOF spectra with the mass resolving power of these experimental conditions (\( R_m \approx 178,000 \)), but the first isomer (\( E_{\alpha} = 190 \text{ keV} \)) would be unresolvable. However, if 206Fr were to be delivered as an admixture of ground state and first isomer with comparable intensities, the peak width would be noticeably broadened. As the 206Fr\(^{2+}\) and 206Ra\(^{2+}\) peaks are well reproduced with a shared peak width, we can presume the 206Fr\(^{2+}\) peak is dominated by either the ground state or first isomer. In an experiment conducted at ISOLDE, the population of 206Fr produced by the spallation reaction of UC, was about two times larger than that of 206Fr\(^{2+}\) [23], so we presume 206Fr\(^{2+}\) to be the highly dominant state in our analysis.

Table I summarizes the mass analysis results for 206Ra\(^{2+}\). The weighted average mass excess of 206Ra determined from the TOF singles spectra was ME = 3548(50) keV/\( c^2 \), while the decay-correlated data yielded ME = 3460(92) keV/\( c^2 \). Both of these values are in agreement with the ME_{\text{lit}} = 3566(18) keV/\( c^2 \) literature value [24], confirming the device performance.

In addition to mass measurements, the α-TOF detector allows for determination of half-lives. Figure 5 provides a histogram of the time between ion implantation and subsequent α decay, gated on the 7250 ± 250 keV α-decay energy characteristic of 206Ra in Run #1. By fitting the histogram data to an exponential decay with constant background, a half-life of 206Ra of \( T_{1/2} = 260(55) \text{ ms} \) was determined. From Run #2, totally 21 decay correlated events were obtained. These half-lives were determined to be \( T_{1/2} = 360(100) \text{ ms} \) from
the half-life of $^{206}$Ra was determined to be $T_{1/2} = 283(48)$ ms, which is in good agreement with the $T_{1/2} = 240(20)$ ms literature value [26]. From the experimental results and literature values, a new global half-life of $^{206}$Ra, $T_{1/2} = 248(18)$ ms is obtained.

### B. $^{207}$Ra

A similar set of analyses was performed for $^{207}$Ra. Figure 6 shows the time-of-flight spectra accumulated in Run #1, with the TOF singles histogram in black and the $^{207}$Ra $\alpha$-decay correlated TOF histogram in blue; due to the incoming rate of $^{207}$Fr$^{2+}$ ($T_{1/2} = 1.38$ s) being higher than the decay rate, it was not possible to perform decay correlations for the ground state. To minimize incidental correlations between $^{207}$Ra$^{2+}$ TOF and $^{207}$Ra $\alpha$ decay, the energy gate had a lower limit of 7.32 MeV ($\sigma_E$ from the $^{207}$Ra $\alpha$-decay energy) resulting in slight reduction in the efficiency. A coincidence time gate of $T_c < 180$ ms, corresponding to approximately three half-lives of $^{207}$Ra, was used. This is shorter than the typical four half-lives, again to suppress the amount incidental coincidence with $^{207}$Ra decays. Despite these efforts we find that 14% of the counts in the decay-correlated TOF spectra (blue histogram in Fig. 6) are derived from $^{207}$Fr$^{2+}$, as noted by the dashed green curve in Fig. 6. The two states of $^{207}$Ra could not be resolved in the singles time-of-flight spectrum alone; the fitting of the two components did not converge, although the peak width indicated multiple components were present.

Similar to the case of $^{206}$Ra, the spectral peaks were fit such that the TOF singles spectral peaks of $^{207}$Fr$^{2+}$ and $^{207}$Ra$^{2+}$, the decay-correlated TOF spectral peak of $^{207}$Fr$^{2+}$, and the incidentally correlated $^{207}$Fr$^{2+}$ had mutually fixed values for the peak-width and exponential tail parameters; the fraction of $^{207}$Fr$^{2+}$ ions in the fit of the decay-correlated spectrum was fixed to 14%. Using the position of the isomeric state determined from decay-correlated events as a fixed parameter when fitting the TOF singles spectrum, the two-component fit reliably converged and the times of flight for the two states could be ascertained.

The masses of $^{207}$Fr$^{2+}$ were determined from the ratio of their times of flight with that of $^{207}$Fr$^{2+}$ using Eq. (2). Decay-correlated spectra were produced using a coincidence time of 180 ms, as previously discussed. From these measurements, the time-of-flight ratios of $^{207}$Fr$^{2+}$ were measured: $\rho_E = 1.000016550(38)$ and $\rho_{\text{int}} = 1.000017983(109)$ with reference species $^{207}$Fr$^{2+}$. The mass excess of $^{207}$Fr and excitation energy of $^{207}$Ra are determined to be $\Delta E = 3538(15)$ keV/$c^2$ and $E_{\text{ex}} = 552(42)$ keV respectively, which are consistent with previous indirectly determined values, $\Delta E_{\text{lit}} = 3510(60)$ keV/$c^2$ and $E_{\text{ex, lit}} = 554(15)$ keV, based on $\alpha$-decay spectroscopy [21, 24].

Additionally, the half-life of $^{207}$Fr was determined using the decay-correlated TOF events. The decay time distribution, determined with an energy gate of $E_{\alpha} \geq 7.32$ MeV applied to the data of Run #1, is shown in Fig. 7. The fitting results show that the half-life of $^{207}$Fr is 55(9) ms, in agreement with the literature value of 59(4) ms. From Run #2, we obtained only one decay-correlated event of $^{207}$Fr. While these are low statistics, it is consistent with the number assumed from the production and $\alpha$ branching ratios (discussed later).

There are 317 TOF singles events of $^{207}$Fr, and the expected correlated events based on energy gate width and detection efficiency would be 2.6 events. When considering the Poisson
distribution, the probability of getting less than one event when 2.6 events are expected is 27%, which is statistically reasonable. Unfortunately, however, a similar analysis to that of Run #1 data is not possible. Therefore, the data obtained from Run #2 were used primarily to confirm the identity of $^{207}$Fr$^{2+}$ and $^{207}$Ra$^{2+}$ based on their unchanging relative times-of-flight.

The first study of $^{207}$Ra was reported in Heßberger et al. [27]. They estimated the production ratio of $^{207}$Fr$^{2+}$/ $^{207}$Ra to be 0.75/0.25 in the reaction system of $^{58}$Fe + $^{154}$Sm, and that the $\alpha$-branching ratio of $^{207}$Ra was $b_\alpha < 0.25$. Subsequent experiments by Leino et al. [28], have also supported this $\alpha$-decay branching ratio.

Since we can unambiguously determine the ratio of ground state to isomer from the TOF singles spectrum, it is also possible to derive the alpha-decay branching ratio and partial half-life of $^{207}$Ra using the $\alpha$-TOF detector. To determine the $\alpha$-decay branching ratio we must determine the number of $\alpha$-decays from $^{207}$Ra which occurred at the detector and the total number $^{207}$Ra atoms deposited on the detector during the experiment.

While we cannot fully resolve the spectral peaks from $^{206}$Ra and $^{207}$Ra in the alpha singles spectra of Fig. 3(a), the fitting results indicate the total number of $\alpha$-decays $N_{\text{sum}} = N_{^{206}\text{Ra}} + N_{^{207}\text{Ra}} = 305 \pm 21.4$ from $^{206}$Ra and $^{207}$Ra were detected. The TOF-correlated $\alpha$-decay spectrum gated on $^{206}$Ra$^{2+}$ consisted of $N_{^{206}\text{Ra}} = 162 \pm 12.7$. Thus, after correcting $N_{\text{sum}}$ for detector efficiency, we conclude that $N_{^{207}\text{Ra}} = 245 \pm 49.5$ $\alpha$-decays from $^{207}$Ra occurred on the $\alpha$-TOF detector in the course of the measurement.

The total number of $^{207}$Ra deposited on the detector can be determined from the TOF singles spectra (Fig. 6). The two-component fit of the $^{207}$Fr$^{2+}$ spectral peak indicated a ratio of 0.60(2)/0.40(2) for the ground state to isomer yield, similar to the yield ratio observed in the $^{58}$Fe + $^{154}$Sm reaction system. After correcting for the TOF detector efficiency, we determined that 94% $^{207}$Fr$^{2+}$ ions implanted upon the detector during the measurement. Thus, the $\alpha$-decay branching ratio of $^{207}$Ra could be determined to be 26.20(25)%, in agreement with the value of 25% previously reported from $\alpha$-decay spectroscopy [27,28].

IV. DISCUSSION

The spin-parity of $^{207}$Ra has tentatively assigned to $J^\pi = 13/2^+$, based on the systematics of the neighboring nuclei [21]. The single particle level diagrams for odd Ra and Rn nuclides are shown in Fig. 8. The solid red circle in Fig. 8 is the excitation energy of $^{207}$Ra obtained from our decay-correlated mass analysis. It agrees with the prior study from $\alpha$-decay spectroscopy. The systematics continue to suggest that spin-parity is $J^\pi = 13/2^+$. The spin-parity of $^{207}$Ra is assigned to either $J^\pi = 3/2^-$ or $5/2^-$ based on systematics. If $J_\pi = 3/2^-$ then the configuration is $(\pi h_\nu/2)^{\alpha}_{3/2}(\pi p_{3/2})^1$ while if $J_\pi = 5/2^-$ then the configuration would be $(\pi h_\nu/2)^{\alpha}_{5/2}(\pi f_{5/2})^{-1}$ [21]. However, the spin-parity of $^{207}$Ra cannot be determined from this experiment.

From our results, the reduced $\alpha$ width of $^{207}$Ra can be evaluated to $\delta^2 = 40^{+68}_{-34}$ keV according to the Rasmussen prescription [29]. Table II describes the reduced $\alpha$ width of various $^{207}$Ra isotopes.

TABLE II. Summary of the spin-parity, decay properties and reduced $\alpha$ width ($\delta^2$) of odd $^{205-207}$Ra isotopes. $b_\alpha$ is the branching ratio of $\alpha$ decay.

<table>
<thead>
<tr>
<th>Isotope</th>
<th>$J^\pi$</th>
<th>$E_\alpha$ (keV)</th>
<th>$T_{1/2}$ (ms)</th>
<th>$b_\alpha$</th>
<th>$\delta^2$ (keV)</th>
<th>Ref.</th>
</tr>
</thead>
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<tr>
<td>$^{203}$Ra</td>
<td>3/2$^-$</td>
<td>7575(10)</td>
<td>50$^{+90}_{-15}$</td>
<td>1.0</td>
<td>45$^{+137}_{-14}$</td>
<td>[30]</td>
</tr>
<tr>
<td>$^{203}$Ra</td>
<td>13/2$^+$</td>
<td>7607(8)</td>
<td>37$^{+17}_{-12}$</td>
<td>1.0</td>
<td>48$^{+142}_{-16}$</td>
<td>[30]</td>
</tr>
<tr>
<td>$^{205}$Ra</td>
<td>3/2$^-$</td>
<td>7340(20)</td>
<td>210$^{+10}_{-20}$</td>
<td>1.0</td>
<td>50$^{+12}_{-16}$</td>
<td>[26]</td>
</tr>
<tr>
<td>$^{205}$Ra</td>
<td>13/2$^+$</td>
<td>7370(20)</td>
<td>170$^{+10}_{-20}$</td>
<td>1.0</td>
<td>48$^{+27}_{-18}$</td>
<td>[26]</td>
</tr>
<tr>
<td>$^{207}$Ra</td>
<td>3/2$^-$</td>
<td>7313(5)</td>
<td>1380$^{+220}_{-110}$</td>
<td>0.86</td>
<td>37$^{+5}_{-6}$</td>
<td>[26]</td>
</tr>
<tr>
<td>$^{207}$Ra</td>
<td>13/2$^+$</td>
<td>7354(28)</td>
<td>55(9)</td>
<td>0.26(20)</td>
<td>43$^{+68}_{-34}$</td>
<td>this work</td>
</tr>
</tbody>
</table>

$^a$Tentatively assigned 3/2$^-$ or 5/2$^-$. 

FIG. 7. The decay time distribution of $^{207}$Ra, determined with an energy gate of $E_\alpha \geq 7.32$ MeV. The solid red lines indicate the fitted decay curve of $^{207}$Ra, while the dashed green lines indicate the constant background level and the long dashed dotted blue line represents the background-subtracted decay curve. (a) Full range spectrum up to 5 s, linear scale. (b) Focus on the first 500 ms, logarithmic scale.

FIG. 8. The single particle level diagram for odd Ra and Rn nuclei. The closed circle indicates the data from this experiment.
13/2^+ and 3/2^- state in the neighboring nuclei 203Ra and 205Ra. Prior to our study, the reduced α width of 203Ra and 205Ra were reported to be around 60 keV for both states [30]. 207Ra is suggested to be 13/2^+ not only in terms of single-particle level systematics, but also from the reduced α width systematics. The reduced width is consistent with that of the neighboring nuclides, indicating that the α decay of 207Ra is not forbidden.

V. SUMMARY

This work has shown that the correlation of mass and decay properties can be measured by use of an MRTOF-MS equipped with the α-TOF detector, proving that not only the unique determination of the excitation energy of an isomeric state but also its branching ratio and partial half-life can be derived simultaneously. The results are in agreement with the historical α-spectroscopy measurements, and successfully demonstrated the value of simultaneous mass and decay spectroscopy with MRTOF-MS equipped with the α-TOF detector. In particular, the mass of 207Ra and the excitation energy of 207mRa were directly measured for the first time. The nuclear structure could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of the MRTOF-MS could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of the MRTOF-MS could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of the MRTOF-MS could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of the MRTOF-MS could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of the MRTOF-MS could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of the MRTOF-MS could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of the MRTOF-MS could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of the MRTOF-MS could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of the MRTOF-MS could be discussed based on analyses of the decay-correlated time-of-flight spectrum. The exploration of the MRTOF-MS could be discussed based on analyses of the decay-correlated time-of-flight spectrum.


Correction: The J value in the last sentence of the abstract contained an error and has been fixed.