

The physics of the intergalactic medium

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Intergalactic space is filled with a pervasive medium of ionized gas, the intergalactic medium (IGM). A residual neutral fraction is detected in the spectra of quasistellar objects at both low and high redshifts, revealing a highly fluctuating medium with temperatures characteristic of photoionized gas. The statistics of the fluctuations are well reproduced by numerical gravity-hydrodynamics simulations within the context of standard cosmological structure formation scenarios. Thus, the study of the IGM offers an opportunity to probe the nature of the primordial density fluctuations on scales unavailable to other methods. The simulations also suggest that the IGM is the dominant reservoir of baryons produced by the Big Bang, and so the principal source of the matter from which galaxies formed. The detection of metal systems within the IGM shows that it was enriched by evolved stars early in its history, demonstrating an intimate connection between galaxy formation and the IGM. A comprehensive review of the current understanding of the structure and physical properties of the IGM and its relation to galaxies is presented, concluding with comments on prospects for furthering the study of the IGM using future ground-based facilities and space-based experiments.

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old, adiabatic expansion cooling brought the temperature of the primordial plasma down until the hydrogen and helium recombined. The radiation last scattered at this time appears today as the cosmic microwave background (CMB). The search for the intergalactic medium (IGM) began well before the discovery of the CMB with an attempt by [Field \(1959a\)](#) to detect the hyperfine 21 cm absorption signature from hydrogen along the line of sight to the extragalactic radio galaxy Cygnus A. Although no detection was made, combination of the optical depth with the measured temperature of the CMB discovered in 1965 would have been sufficient to exclude the possibility that the Universe was closed by baryons, with an upper limit on the baryon density of only 20% of the closure density required for an Einstein–de Sitter (flat) universe.¹

Nearly coincident with the discovery of the CMB, however, a considerably improved measurement of the density of intergalactic neutral hydrogen was made. Soon after the discovery of the first quasistellar object (QSO) ([Hazard et al., 1963](#); [Schmidt, 1963](#)), [Gunn and Peterson \(1965\)](#) reported a small decrement in a QSO spectrum shortward of its Ly- α emission line. Attributing the decrement to the Ly- α resonance scattering of radiation from the QSO by intergalactic neutral hydrogen, Gunn and Peterson demonstrated that the cosmic mass density of neutral hydrogen was very much smaller than the Einstein–de Sitter density. In fact, it was far smaller than the spatially averaged hydrogen density of all the stars in the Universe. If the Big Bang theory was correct, this meant either that galaxy formation was an extraordinarily efficient process, sweeping up all but a tiny residue of the primordial hydrogen, or that the gas was reionized.

These two themes, the detection of intergalactic gas through the 21 cm signature in the radio or through Lyman resonance scattering lines in the optical or ultraviolet (UV), continue to dominate studies of the IGM. To date, almost all that is known about the structure of the IGM has been derived from optical and UV data. This situation is expected to change dramatically in the near future with the development of low-frequency radio arrays like the low frequency array (LOFAR),² the Murchison widefield array (MWA),³ the primeval structure telescope (PaST/21CMA),⁴ the precision array to probe the epoch of reionization (PAPER),⁵ and a possible square kilometre array (SKA).⁶ A primary scientific driver of these instruments is the direct imaging of the IGM prior to the completion of the epoch of reionization ([Madau et al., 1997](#)). Most of this review focuses

on the current understanding of the IGM as determined from optical and UV measurements. Observations have relied almost exclusively on the spectra of QSOs, although IGM absorption features have also been detected in the spectra of gamma-ray bursts (GRBs) ([Totani et al., 2006](#)), and indeed played a key role in establishing the extragalactic character of some bursts ([Metzger et al., 1997](#)).

Almost immediately after Gunn and Peterson publicized their finding, it was recognized that individual Ly- α absorption features should appear from neutral hydrogen concentrated into cosmological structures ([Bahcall and Salpeter, 1965](#); [Wagoner, 1967](#)). Absorption features had in fact been detected in higher-resolution QSO spectra, but these were identified with intervening ionized metal absorption systems ([Bahcall et al., 1968](#)), as was expected if galaxies had hot halos of ionized gas: the lines of sight to background QSOs were expected to pass through such hot halos and intercept any ionized gas clouds within them ([Bahcall and Spitzer, 1969](#)). The features, however, were uncomfortably common, hinting at a class of unknown structures not associated with galaxies. The Ly- α resonance line features continued to prove elusive until 1971, when [Lynds \(1971\)](#) recognized several absorption features shortward of the Ly- α emission line of a QSO as Ly- α lines⁷ arising in a population of discrete absorption systems also showing metal features. The Ly- α lines form a plethora of distinct absorption features in the spectra of high-redshift QSOs; they are collectively known today as the Ly- α forest.

The properties of the Ly- α forest came under increasing scrutiny, with the first systematic survey conducted several years later by [Sargent et al. \(1980\)](#) demonstrating through the homogeneity of the observed properties of the absorbers their intergalactic origin, as opposed to being clouds ejected by the observed QSOs. Although limited by the resolution of the spectrograph, the measured velocity widths of the Ly- α features corresponded to gas temperatures of a few to several 10^4 K, characteristic photoionization temperatures for gas of a primordial composition, for which there is no significant cooling by metals. The number of features per comoving length was shown to increase with redshift, demonstrating that the systems were evolving ([Young et al., 1982](#)).

The past decade has witnessed a dramatic improvement in precision studies of the Ly- α forest with the advent of 8–10 m class telescopes, particularly the Keck 10 m and the 8.2 m very large telescope (VLT). For the first time, the individual absorption features in the Ly- α forest were spectroscopically resolved over their full range. Velocity widths of ~ 25 km s⁻¹ are typical. The neutral hydrogen column densities of the absorbers range from roughly 10^{12} to 10^{22} cm⁻². The highest-column-density systems, the damped Ly- α absorbers (DLAs), are of particular interest for galaxy formation,

¹This conclusion requires the assumptions (reasonable at the time) that hydrogen was all neutral and that the hyperfine structure levels of hydrogen were in thermal equilibrium with the CMB.

²<http://www.lofar.org>

³<http://www.haystack.mit.edu/ast/arrays/mwa/>

⁴<http://web.phys.cmu.edu/~past/>

⁵<http://astro.berkeley.edu/~dbacker/eor/>

⁶<http://www.skatelescope.org>

⁷These are not true absorption features involving the net destruction of a photon, but the scattering out of the line of sight of resonance line photons.

as they are suspected of containing the neutral gas that formed the bulk of the stars in present-day galaxies.

As the number per length of absorption systems increases along a line of sight with increasing redshift, so does the mean flux decrement in a background QSO spectrum due to Ly- α scattering. The QSO spectra measured as part of the Sloan digital sky survey⁸ (SDSS) show a rapid rise in the flux decrement at $z \gtrsim 5.5$, suggesting that the epoch of H I reionization may lie not far beyond $z \approx 6$. Many of the hydrogen features also show absorption lines from metals, including carbon, silicon, nitrogen, oxygen, magnesium, iron, and others. The abundances of the metals, however, are at most about 10% of solar abundance at low redshifts, and as low as 1% at high redshifts, indicating that the absorption systems are comprised largely of primordial material. The primordial nature of the gas received further important confirmation in 1994 with the discovery by [Jakobsen et al. \(1994\)](#) of intergalactic helium using the Hubble space telescope (HST) through the detection of He II Ly- α absorption.

Because the baryons in the IGM are detected only through their absorption signatures, the physical structures that give rise to the features must be modeled. Early models characterized the systems as discrete clouds of gas, with most of the focus on clouds either pressure confined by a hot medium ([Sargent et al., 1980](#)), or gravitationally confined in a dark matter halo ([Ikeuchi, 1986](#); [Rees, 1986](#)). At the time it was believed that the absorption systems accounted for only a few percent of the baryons produced in the Big Bang, much like galaxies, their visible counterparts. A paradigm shift in the models occurred in the mid-1990s. Measurements of coincident absorption features along neighboring lines of sight suggested sizes of tens to hundreds of kiloparsecs for the absorbers ([Smette et al., 1992](#); [Bechtold et al., 1994](#); [Dinshaw et al., 1997](#)), much larger than expected for clouds confined by pressure or dark matter halos. A radical transformation in the understanding of the nature and structure of the IGM was initiated by numerical simulations of cosmological structure formation. Today, essentially all baryons produced in the Big Bang are believed to have undergone the same gravitational instability process initiated by primordial density fluctuations that was responsible for the formation of galaxies. The computation of the structure of the IGM has been converted into an initial value problem similar to that of the CMB fluctuations. Fluctuations in the CMB are solved for by following the gravitational instability growth of a postulated spectrum of primordial dark matter density fluctuations. The growth of structure in the IGM is now treated as the nonlinear extension of these computations. The result is a network of filamentary structures, the so-called cosmic web ([Bond et al., 1996](#)). The Ly- α forest is believed to be a signature of the cosmic web. Early simulations broadly reproduced the statistics of the Ly- α forest well ([Cen et al., 1994](#); [Petitjean et al.,](#)

[1995](#); [Zhang et al., 1995, 1997](#); [Hernquist et al., 1996](#); [Theuns et al., 1998](#)). An immediate conclusion was that at $z \gtrsim 1.5$ some 90% of the baryons produced in the Big Bang are contained within the IGM, with only 10% in galaxies, galaxy clusters, or possibly locked up in an early generation of compact stars.

Soon after the discovery of intervening absorption features, it was recognized that they provided potentially powerful tests of fundamental properties of the Universe. The split in the fine structure lines of the metals was used to set constraints on the variability of the fine structure constant ([Bahcall et al., 1967](#)). The bunching of absorption features near $z \approx 1.9$ (now known to be fortuitous) gave rise to the (re)introduction of a cosmological constant to account for the numerous features as multiple images due to lensing ([Petrosian et al., 1967](#)). The expected primordial composition of the IGM offered the potential of placing constraints on the photon-to-baryon ratio of the Universe through measurements of the intergalactic deuterium abundance. More recently, the success of the models has inspired attempts to exploit the Ly- α forest as a new means to constrain cosmological structure formation models and obtain stringent constraints on the cosmological parameters.

The description of the IGM by simulations, however, is far from complete. There remain many unsolved problems. The current simulations do not reproduce all the observed properties of the IGM. The absorption lines are predicted to be substantially narrower than measured. This likely stems from the principal outstanding missing piece of physics, the reionization of the IGM. Not only must hydrogen be ionized, but helium as well. The ionization heats the gas through the photoelectric effect. Detailed radiative transfer computations are required to recover the temperatures, for which there is still limited success. The sources of the reionization and the epochs of reionization, of both hydrogen and helium, are still not firmly established. The origin of the metal absorption systems in the diffuse IGM is still unknown, although it is widely expected they were deposited by winds from galaxies, possibly driven by intense episodes of star formation. As such, the metal absorption lines in principle offer an important means of studying the history of cosmic star formation. Most fundamentally, the relation of the IGM to the galaxies that form from it is still mostly unknown, but offers perhaps the most exciting prospects for new research directions.

The purpose of this review is to describe the progress made in the understanding of the origin of structure within the IGM, with a view to presenting the underlying physics that determines the structure. An understanding of the physics is necessary for future progress. The past decade has revealed the IGM to be a complex dynamical arena involving interactions between the IGM gas, galaxies, and QSOs. It is becoming increasingly apparent that the separation of these systems into distinct and isolated entities is an artificial construct. Galaxies and QSOs originated from the IGM, and their radiation and outflows impacted upon it. Any complete understanding of the origin of these systems requires a

⁸<http://www.sdss.org>

unified treatment. In this way, the IGM resembles the interstellar medium of disk galaxies in which the gaseous component is intimately linked to the stars and their evolution and impact. Interpretation of the increasingly refined observations requires detailed modeling, which relies on large-scale numerical computations involving gas, radiative processes, and gravity. The physics involved is intermediate in complexity between that of the CMB and galaxy formation, rendering the IGM a bridge between these extreme scales of cosmological structure formation. Unraveling of the processes that led to the formation and structure of the IGM may thus serve as a crucial step in the solution of the much more involved problem of galaxy formation.

A search for papers on the IGM since the [Gunn and Peterson \(1965\)](#) measurement produces close to 6000 references.⁹ While this review does not have the space to describe the observational methods used to measure the IGM, it should be recognized that progress in understanding the properties of the IGM is indebted to advances in observational techniques. This is well illustrated by a plot of the number of refereed publications in the field against time. Periods of relatively steady output are punctuated by four leaps. The first occurs at the end of the 1960s and beginning of the 1970s with the introduction of image tube spectrographs coupled with integrating television systems for photon counting ([Boksenberg, 1972](#); [Morton, 1972](#)), which greatly facilitated the taking of spectra. The next occurs in the mid-1970s with the development of x-ray astronomy following the launch of the UHURU satellite in 1970 and the recognition that galaxy clusters contain an extended and pervasive medium of hot radiating gas ([Kellogg et al., 1973](#); [Lea et al., 1973](#)). Another sharp rise occurs in the early 1990s following the launch of the Hubble space telescope, the installation of EMMI and its echelle spectrograph on the new technology telescope (NTT) ([D’Odorico, 1990](#)), and the delivery of the HIRES spectrometer ([Vogt et al., 1994](#)) to the Keck telescope. The fourth occurred in 2000 with the introduction of the UV and visible echelle spectrograph (UVES) to the VLT ([D’Odorico et al., 2000](#)), the launch of the far ultraviolet spectroscopic explorer (FUSE) ([Moos et al., 2000](#)), and the beginning of operations of the Sloan digital sky survey ([York et al., 2000](#)). The latter in particular triggered a surge of activity in reionization studies following the discovery of high-redshift QSOs ($z > 6$) with spectra indicating a rapid rise in the effective optical depth of the IGM to Ly- α photons, hinting that the epoch of reionization (EOR) was being approached ([Becker et al., 2001](#); [Fan et al., 2002](#)). This is indicated by a rise in IGM reionization papers in Fig. 1, a trend which continues

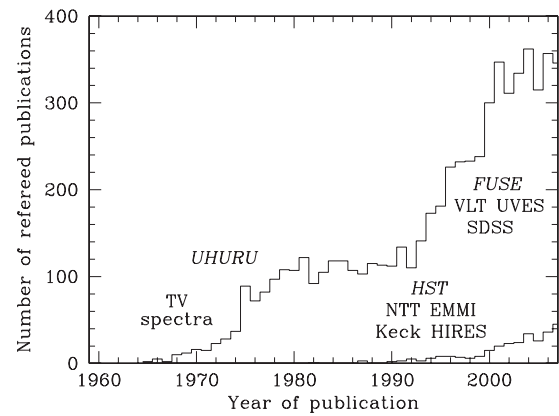


FIG. 1. Number of refereed papers on the intergalactic medium and QSO intervening absorption systems published from 1965 to 2007, as provided by the ADS abstract service (adsabs.harvard.edu). The sharp rises follow key developments in astronomical instrumentation and observations. The lower histogram shows the rise of papers on the reionization and subsequent ionization state of the IGM.

today, fueled in part by the growing interest in the influence of reionization on the CMB fluctuations measured by the Wilkinson microwave anisotropy probe (WMAP) ([Kogut et al., 2003](#)). The next major leap may well come from the anticipated radio measurements.

The rapidly rising tide of IGM studies has brought along with it several reviews. This is fortunate, as it is impossible in a single review to cover all areas thoroughly today. Early reviews of the QSO absorption line literature, now largely historical, were provided by [Strittmatter and Williams \(1976\)](#) and [Weymann et al. \(1981\)](#). [Rauch \(1998\)](#) and [Bechtold \(2003\)](#) provide reviews of the Ly- α forest that are still largely up to date in the sense that most of the topics currently engaging the community are treated, with developments since mostly improvements in accuracy and in the details of the numerical models. Reviews of the low-redshift IGM are provided by [Shull \(2003\)](#) and [Stocke, Shull and Penton \(2006\)](#). [Wolfe et al. \(2005\)](#) reviewed the current understanding of damped Ly- α absorbers, an absorber class of special concern as it represents the closest link to the gaseous component forming present-day galaxies. A new series of reviews followed the recent explosion of activity on the reionization of the IGM in anticipation of the detection of the EOR through its high-redshift 21 cm signature. An early review in this area is by [Loeb and Barkana \(2001\)](#). Since then, current observational and theoretical aspects of reionization have been exhaustively covered by [Fan, Carilli and Keating \(2006\)](#), [Furlanetto et al. \(2006\)](#), and [Barkana and Loeb \(2007\)](#).

Rather than repeating the wide range of IGM phenomenology already covered by previous reviews, I concentrate here on the physics underlying the structure of the IGM. One aim is to describe the physical underpinnings of current numerical simulations as required for future simulations to further progress. As observations are crucial for constraining any models, I begin by giving a broad overview of the current observational situation.

⁹Based on a Boolean search of the astrophysics data system (adsabs.harvard.edu) for all refereed papers with keywords containing (intergalactic and medium) or (quasar and absorption and line). Reionization papers are selected as the subset discussing the reionization of the IGM or the subsequent ionization structure of the IGM.

The next section describes the physics of ionization equilibrium, followed by a discussion of the UV metagalactic background that maintains the ionization of the IGM. A brief review of early models of the Ly- α forest absorbers is then presented, followed by a discussion of current numerical models. The reionization of the IGM is then summarized along with means for its detection. This is followed by a discussion of the connection between galaxies and the IGM before concluding with observational and theoretical prospects for the future.

Unless stated otherwise, the cosmological parameters $\Omega_m=0.3$ and $\Omega_b=0.046$ are assumed for, respectively, the ratios of the present-day matter density and the present-day baryon density to the current Einstein-de Sitter density $\rho_{\text{crit}}(0)=3H_0^2/8\pi G$, a Hubble constant of $H_0=100h \text{ km s}^{-1} \text{ Mpc}^{-1}$ with $h=0.7$ (Mpc=megaparsec $\approx 3.0856 \times 10^{22}$ m), and a baryon density of $\Omega_b h^2=0.022$. These values are consistent within the errors with the current best estimates for a flat Universe based on CMB measurements using year-5 WMAP data of $\Omega_m=0.279 \pm 0.014$, $\Omega_b=0.046 \pm 0.001$, $h=0.701 \pm 0.013$, and $\Omega_b h^2=0.02265 \pm 0.00059$ (Komatsu *et al.*, 2009), or intergalactic D/H measurements, giving $\Omega_b h^2=0.021 \pm 0.001$ (O'Meara *et al.*, 2006).

II. OBSERVATIONS

A. Resonance absorption lines

The IGM is detected through the absorption features it produces in the spectrum of a background bright source of light (typically a QSO). The production of the absorption features is governed by the equation of radiative transfer through the IGM, conventionally expressed in terms of the specific intensity of a background radiation source.

The specific intensity $I_\nu(\mathbf{r}, t, \hat{\mathbf{n}})$ is defined as the rate at which energy crosses a unit area per unit solid angle per unit time as carried by photons of energy $h\nu$ traveling in the direction $\hat{\mathbf{n}}$ relative to some fiducial direction. The equation of radiative transfer for $I_\nu(\mathbf{r}, t, \hat{\mathbf{n}})$ in a medium with attenuation coefficient $\alpha_\nu(\mathbf{r}, t, \hat{\mathbf{n}})$ is

$$\frac{1}{c} \frac{\partial I_\nu(\mathbf{r}, t, \hat{\mathbf{n}})}{\partial t} + \hat{\mathbf{n}} \cdot \nabla I_\nu(\mathbf{r}, t, \hat{\mathbf{n}}) = -\alpha_\nu(\mathbf{r}, t, \hat{\mathbf{n}}) I_\nu(\mathbf{r}, t, \hat{\mathbf{n}}) + j_\nu(\mathbf{r}, t, \hat{\mathbf{n}}). \quad (1)$$

Because of its use later, a radiative source term has been included through the *emission coefficient* $j_\nu(\mathbf{r}, t, \hat{\mathbf{n}})$, which describes the local specific luminosity per solid angle per unit volume emitted by sources. Normally the random orientation of atoms will ensure that j_ν is isotropic, but not always, as, for instance, if the source includes a scattering term, so that a dependence on $\hat{\mathbf{n}}$ is included to account for the possibility of anisotropic sources. A central source like a QSO or galaxy will in fact generally radiate anisotropically.

In general, the attenuation of the radiation field is due to both the absorption of photons and their scattering out of the beam. The attenuation coefficient is then

$$\alpha_\nu(\mathbf{r}, t, \hat{\mathbf{n}}) = \rho(\mathbf{r}, t) \kappa_\nu(\mathbf{r}, t, \hat{\mathbf{n}}) + n(\mathbf{r}, t) \sigma_\nu(\mathbf{r}, t, \hat{\mathbf{n}}), \quad (2)$$

where $\rho(\mathbf{r}, t)$ is the mass density of the medium, $\kappa_\nu(\mathbf{r}, t, \hat{\mathbf{n}})$ is the opacity, which expresses the absorption cross section per unit mass, $n(\mathbf{r}, t)=\rho(\mathbf{r}, t)/\bar{m}$ is the number density of scattering particles of mean mass \bar{m} , and $\sigma_\nu(\mathbf{r}, t, \hat{\mathbf{n}})$ is the scattering cross section. In general, the scattering could arise from more than one type of particle, in which case $n\sigma_\nu$ would be replaced by a sum over particle species i of density n_i and cross section $\sigma_\nu(i)$. In a static medium, $\alpha_\nu(\mathbf{r}, t, \hat{\mathbf{n}})$ is generally isotropic, but not always. As an example, the alignment of atoms in a strong magnetic field would absorb anisotropically. In a moving medium, an anisotropic contribution to the attenuation will be produced by the dependence of Doppler scattering on the relative motion of the radiation and the fluid.

The value of I_ν at any given time t and position s along the direction $\hat{\mathbf{n}}$ will be given by any incoming intensity I_ν^{inc} at position s_0 at time $t_{\text{ret}}=t-(s-s_0)/c$, attenuated by intervening material at positions s' at the retarded times $t'_{\text{ret}}=t-(s-s')/c$, along with contributions from sources at positions s'' that emitted at the retarded times $t''_{\text{ret}}=t-(s-s'')/c$, followed by attenuation. The formal solution to Eq. (1) is then

$$I_\nu(s, t) = (I_\nu^{\text{inc}})_{s_0, t_{\text{ret}}} \exp\left(-\int_{s_0}^s ds' (\alpha_\nu)_{s', t'_{\text{ret}}}\right) + \int_{s_0}^s ds'' (j_\nu)_{s'', t''_{\text{ret}}} \exp\left(-\int_{s''}^s ds' (\alpha_\nu)_{s', t'_{\text{ret}}}\right), \quad (3)$$

as may be verified by direct substitution. In a uniformly expanding (or contracting) medium described by the scale factor $a(t)$, Eq. (1) must be modified to

$$\frac{1}{c} \frac{\partial I_\nu(\mathbf{r}, t, \hat{\mathbf{n}})}{\partial t} + \frac{1}{c} \frac{\dot{a}}{a} \left(3I_\nu(\mathbf{r}, t, \hat{\mathbf{n}}) - \nu \frac{\partial I_\nu(\mathbf{r}, t, \hat{\mathbf{n}})}{\partial \nu}\right) + \hat{\mathbf{n}} \cdot \nabla I_\nu(\mathbf{r}, t, \hat{\mathbf{n}}) = -\alpha_\nu(\mathbf{r}, t, \hat{\mathbf{n}}) I_\nu(\mathbf{r}, t, \hat{\mathbf{n}}) + j_\nu(\mathbf{r}, t, \hat{\mathbf{n}}), \quad (4)$$

where the frequency redshifts according to $\nu \propto a(t)^{-1}$. The solution becomes

$$I_\nu(s, t) = (I_{\nu_0}^{\text{inc}})_{s_0, t_0} \left(\frac{a(t_0)}{a(t)}\right)^3 \exp\left(-\int_{s_0}^s ds' (\alpha_{\nu'})_{s', t'_{\text{ret}}}\right) + \int_{s_0}^s ds'' (j_{\nu''})_{s'', t''_{\text{ret}}} \left(\frac{a(t'')}{a(t)}\right)^3 \times \exp\left(-\int_{s''}^s ds' (\alpha_{\nu'})_{s', t'_{\text{ret}}}\right), \quad (5)$$

where $\nu_0 = \nu a(t)/a(t_0)$, $\nu' = \nu a(t)/a(t')$, and $\nu'' = \nu a(t)/a(t'')$.

In the case of no intermediate sources, $j_\nu=0$ and the received intensity depends only on how the incident intensity is modified by the intervening gas. This is the situation for a single background source such as a QSO. The Lyman absorption features arise from the scattering of resonance line photons received from the background QSO through a medium of scatterers with number den-

sity $n(\mathbf{r}, t)$. The frequency-dependent scattering cross section for a scatterer at rest is given by the Lorentz profile¹⁰

$$\sigma_\nu = \left(\frac{\pi e^2}{m_e c} \right) \left[\frac{1}{4\pi\epsilon_0} \right] f_{lu} \frac{\Gamma_{ul}/4\pi^2}{(\nu - \nu_{lu})^2 + (\Gamma_{ul}/4\pi)^2}, \quad (6)$$

where ν_{lu} is the resonance line frequency, corresponding to the wavelength λ_{lu} , of the transition between an upper level broadened by radiation damping to a sharp lower level (the ground state), $\Gamma_{ul} = (g_l f_{lu}/g_u)[1/4\pi\epsilon_0]8\pi^2 e^2/m_e c \lambda_{lu}^2$ is the damping width of the upper level, where g_l and g_u are the respective statistical weights of the lower and upper levels, f_{lu} is the upward oscillator strength, e is the electric charge of an electron, and m_e is the electron mass.¹¹ The cross section is normalized according to

$$\sigma \equiv \int_{-\infty}^{\infty} d\nu \sigma_\nu = \left(\frac{\pi e^2}{m_e c} \right) \left[\frac{1}{4\pi\epsilon_0} \right] f_{lu}. \quad (7)$$

For λ_{lu} in meters, $\Gamma_{ul} = 6.670 \times 10^{-5} (g_l f_{lu}/g_u) \lambda_{lu}^{-2}$. For the Lyman series,

$$g_l f_{ln} = 2^9 n^5 (n-1)^{2n-4} / 3(n+1)^{2n+4}, \quad (8)$$

where n is the quantum number of the upper state (Menzel and Pekeris, 1935). For the Ly- α transition, $g_l = 2$, $g_u = 6$, and $f_{lu} = 0.4162\dots$. For hydrogen Ly- α , $\lambda_{lu} = 1215.67 \text{ \AA}$ and $\Gamma_{ul} = 6.262 \times 10^8 \text{ s}^{-1}$. For He II Ly- α , λ_{lu} is smaller by a factor of 4, and Γ_{ul} larger by a factor of 16.

In general, the atoms will not be at rest. At the very least they will generally undergo thermal motions described by a Maxwellian velocity distribution corresponding to their temperature T . They may additionally take part in an ordered flow of velocity \mathbf{v} , which may be accounted for by shifting the line center frequency ν to $\nu(1 - v_{\parallel}/c)$, to first-order accuracy in v/c , where v_{\parallel} is the line-of-sight velocity. In addition, there may be a disordered turbulent, or so-called *microturbulent*, component in some collapsed or shocked regions. Ignoring nonthermal velocities, the profile including thermal motions is found by convolving Eq. (6) with a Maxwellian. The result, which neglects additional frequency dependences far from line center, is the Voigt function

¹⁰SI units for electrostatic quantities throughout the text may be accommodated by including the square-bracketed quantity $[1/4\pi\epsilon_0]$, where ϵ_0 is the vacuum permittivity. Without the factor, the expressions correspond to the forms appropriate for cgs units.

¹¹The Lorentz profile neglects the frequency dependence of the scattering cross section far from line center. It does not, for example, recover the low-frequency Rayleigh limit ($\sigma_\nu \propto \nu^4$). The profile, however, is fully adequate for applications to the IGM. Small deviations may become detectable for broad absorption features such as damped Ly- α absorbers at high spectral resolution (Lee, 2003). Such deviations, however, would prove difficult to distinguish from the effects of density inhomogeneities in the absorbing gas and the associated gas velocities, except possibly in a statistical sense over many systems.

$$H(a, x) = \frac{a}{\pi} \int_{-\infty}^{\infty} dy \frac{e^{-y^2}}{(x-y)^2 + a^2}, \quad (9)$$

where $a = \Gamma_{ul}/4\pi\Delta\nu_D$ is the ratio of the damping width to the Doppler width, and $x = (\nu - \nu_{lu})/\Delta\nu_D$ is the frequency shift from the line center in units of the Doppler width $\Delta\nu_D = \nu_{lu}b/c$ with Doppler parameter

$$b = (2k_B T/m_a)^{1/2}, \quad (10)$$

where m_a is the mass of the scattering particle and k_B is Boltzmann's constant. A kinematic component such as microturbulence is often accounted for by adding in quadrature the characteristic kinematic velocity to the thermal component of the Doppler parameter

$$b = (b_{\text{th}}^2 + b_{\text{kin}}^2)^{1/2}, \quad (11)$$

where b_{th} is the thermal contribution from Eq. (10). An expansion approximation for the Voigt function in a is provided by Harris (1948). Fast methods for arbitrary a are described by Humlíček (1979, 1982) and Shippony and Read (1993). Various evaluation methods are compared by Schreier (1992).

The resonance line scattering cross section is

$$\sigma_\nu = \left(\frac{\pi e^2}{m_e c} \right) \left[\frac{1}{4\pi\epsilon_0} \right] f_{lu} \varphi_V(a, \nu) = \sigma \varphi_V(a, \nu), \quad (12)$$

where

$$\varphi_V(a, \nu) = \frac{1}{\Delta\nu_D} \phi_V(a, x) = \frac{1}{\pi^{1/2} \Delta\nu_D} H(a, x) \quad (13)$$

is the Voigt profile, normalized to $\int_{-\infty}^{\infty} d\nu \varphi_V(a, \nu) = 1$. For hydrogen Ly- α , $a \approx 0.0472 T^{-1/2}$. For He II Ly- α , a is larger by a factor of 8.

The intensity of the background QSO is attenuated by the factor $e^{-\tau_\nu}$, where Eq. (5) gives

$$\tau_\nu = \int_{s_0}^s ds' n(s', t') \sigma_{\nu'}. \quad (14)$$

For a homogeneous and isotropic background universe expanding with scale factor $a(t)$, radiation emitted by the source at time t_0 and rest frame frequency $\nu_0 > \nu_{lu}$, where ν_{lu} is the resonance line frequency of a (rest frame) Lyman transition, will be scattered by the medium at epoch t' given by $\nu' = \nu_0 a(t_0)/a(t') = \nu_{lu}$. Thus the received QSO intensity will be attenuated at the time t at all observed frequencies ν in the range $\nu_{lu} > \nu > \nu_{lu} a(t_0)/a(t)$, or wavelengths λ in the range $\lambda_{lu} < \lambda < \lambda_{lu} a(t)/a(t_0)$, where λ_{lu} is the (rest frame) wavelength of the particular Lyman transition, producing a trough in the spectrum of the QSO. This is the Gunn-Peterson effect (Gunn and Peterson, 1965; Scheuer, 1965). Intervening metal absorption, assuming solar abundances distributed uniformly throughout intergalactic space, would produce similar troughs (Shklovskii, 1964, 1965). The corresponding optical depth is given by noting that $ds' = cd t' = c H^{-1}(t') da(t')/a(t')$, where $H(t') = \dot{a}(t')/a(t')$ is the Hubble parameter at time t' . Changing the integration variable to $a' = a(t')$ and setting $z = \nu_{lu}/\nu - 1$, it follows

from Eq. (14) that, taking $\langle n \rangle$ to denote the mean number density of particles in the lower state,

$$\begin{aligned} \tau_\nu &= c \int \frac{da'}{a'} H(a')^{-1} \sigma_{\nu|a'-\nu_{lu}} \langle n(a') \rangle \\ &= \frac{g_u}{g_l} \frac{1}{8\pi} \frac{\lambda_{lu}^3 \Gamma_{ul} \langle n(z) \rangle}{H(z)} \\ &= 1.100 \times 10^4 \frac{(1+z)^3}{[\Omega_m(1+z)^3 + \Omega_K(1+z)^2 + \Omega_v]^{1/2}} \\ &\quad \times \left(\frac{f_{lu} \lambda_{lu}}{506.0 \text{ \AA}} \right) \left(\frac{g_u/g_l}{3} \right) \left(\frac{\langle n \rangle}{\langle n_H \rangle} \right), \end{aligned} \quad (15)$$

after noting from Eq. (7) that $\sigma = (g_u/g_l) \Gamma_{ul} \lambda_{lu}^2 / 8\pi$. The Hubble parameter $H(z)$ at redshift z is related to the value of the Hubble constant today H_0 by $H(z) = H_0 E(z)$, where $E(z) = [\Omega_m(1+z)^3 + \Omega_K(1+z)^2 + \Omega_v]^{1/2}$ (Sargent *et al.*, 1980; Peebles, 1993). Here Ω_m is the mass density of the Universe expressed as a fraction of the Einstein–de Sitter critical density, and Ω_K and Ω_v are similar fractions arising from the curvature and vacuum energy contributions, respectively. They satisfy the identity $\Omega_m + \Omega_K + \Omega_v = 1$. In the last line of Eq. (15), the result was scaled to the present-day mean cosmic hydrogen density $n_H(0) = \rho_H(0)/m_H = (1-Y)\Omega_b\rho_{\text{crit}}(0)/m_H \approx 0.186 \text{ m}^{-3}$, where m_H is the mass of a hydrogen atom, assuming a baryon density of $\Omega_b h^2 = 0.022$ (see Sec. II.B.4) and cosmic helium mass fraction $Y \approx 0.2477 \pm 0.0029$ (Peimbert *et al.*, 2007), and to a Hubble constant of $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Sec. II.B.2). Equation (15) is the inverse of the Sobolev parameter for a homogeneously and isotropically expanding medium, and was first derived in the context of cosmological hydrogen Ly- α photon scattering by Field (1959b).

Observations show that in fact the IGM is not homogeneous, but that the baryons have coalesced, creating a fluctuating density field $n(s, t)$. The discreteness of the absorption lines measured in the spectra of high-redshift QSOs suggests they originate in distinct localized regions. The resulting collection of absorption features, shown in Fig. 2, is known as the Ly- α forest. Denoting the centers of the absorbing regions by the positions s_i , the optical depth becomes $\tau_\nu = \sum_i \tau_\nu(i)$, where

$$\tau_\nu(i) = \int_{s_i - \Delta s/2}^{s_i + \Delta s/2} ds' n(s', t_i) \sigma_{\nu'} \quad (16)$$

Here the integral has been localized to a region of width Δs around s_i , and $\nu' = \nu a(t)/a(t_i)$, where t_i corresponds to the epoch of coordinate s_i in an expanding universe. The absorption features thus probe discrete spatial structures in the IGM. The expression of the optical depth as a sum of discrete absorption systems is, however, an approximation, as the intergalactic gas forms an evolving spatial continuum. Gas distributed over a wide spatial range, and even at different epochs, can therefore affect the same observed frequency ν . However, for $z \lesssim 3.5$, observations show that the discrete absorber approximation provides a good description of the hydrogen Ly- α

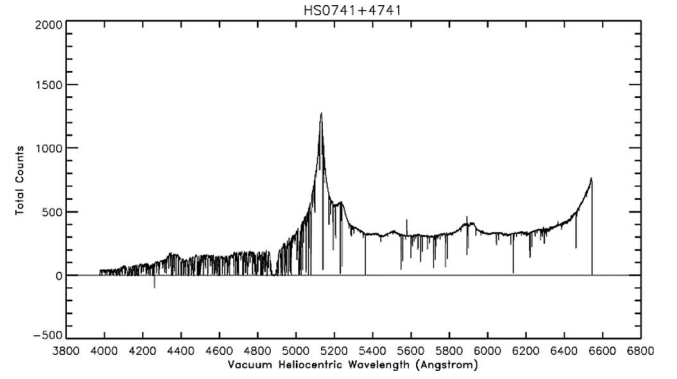


FIG. 2. The Ly- α forest measured in the spectrum of the $z = 3.22$ quasar HS0741+4741. The spectrum was obtained using the HIRES spectrograph on the Keck 10 m telescope. The integration time was 4.0 h with a spectral resolution of $R = 37\,000$ covering 3900 to 6600 \AA with a signal-to-noise ratio of 145 per resolution element. The sharp peak at $\lambda = 5130 \text{ \AA}$ is the Ly- α emission line of the quasar. The Ly- α forest lies toward the blue side of the feature. A damped Ly- α absorber at $z = 3.02$ appears at $\lambda \approx 4890 \text{ \AA}$ (Prochaska *et al.*, 2001). Intervening C IV systems give rise to rarer absorption features longward of the emission line (Songaila, 2006). Figure courtesy of A. Songaila.

forest. Equation (16) may be further simplified to

$$\tau_\nu = \pi^{1/2} \tau_0 \langle \phi_V(a, x) \rangle, \quad (17)$$

where

$$\tau_0 = \frac{N \sigma \lambda_{lu}}{\pi^{1/2} b} = \frac{\sqrt{\pi} e^2}{m_e c} \left[\frac{1}{4\pi \epsilon_0} \right] \frac{N}{b} \lambda_{lu} f_{lu} \quad (18)$$

is the optical depth at line center. Here N is the column density $\int ds' n(s', t')$, and $\langle \phi_V(a, x) \rangle$ is averaged over the line of sight, weighted by the density. This may differ from $\phi_V(a, x)$ when the temperature or large-scale macroscopic velocity field varies along the line of sight. Tabulations of $\lambda_{lu} f_{lu}$ and related atomic data for resonance lines for a variety of elements are available in the literature (Morton, 1991, 2000, 2003). For hydrogen Ly- α ,

$$\tau_0^{\text{H I}} \approx 0.38 \left(\frac{N_{\text{H I}}}{10^{13} \text{ cm}^{-2}} \right) \left(\frac{b}{20 \text{ km s}^{-1}} \right)^{-1}. \quad (19)$$

At redshifts $z > 3.5$, the blending of absorption lines makes it increasingly difficult to attribute the absorption to distinguishable systems. By $z > 5.5$, the individual lines have essentially all merged, forming in effect a Gunn-Peterson trough (though still not corresponding to a completely neutral IGM). Absorption features at intermediate redshifts not easily deblended into subcomponents may be characterized by an equivalent width w_λ . This is defined to be the width, expressed in units of wavelength, a square-well absorption feature with zero flux at its bottom must have to match the integrated area of the detected feature under the continuum

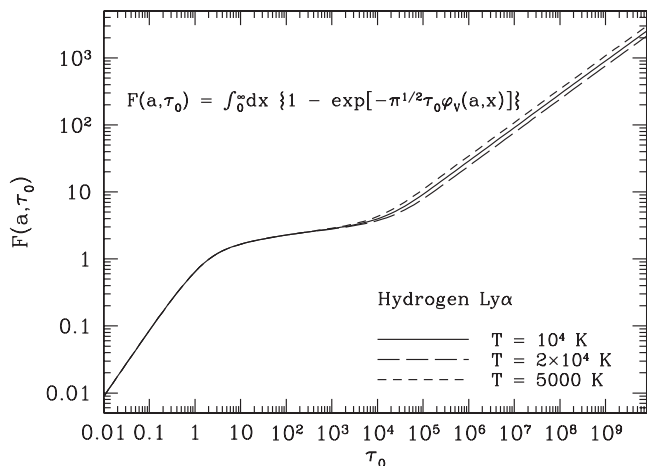


FIG. 3. The function $F(a, \tau_0)$ describing the equivalent width of an absorption feature. Curves are shown for hydrogen Ly- α at three temperatures. Except at large values of τ_0 , the curves are independent of a .

$$w_\lambda = \int_0^\infty d\lambda (1 - e^{-\tau_\nu}) = \frac{\lambda^2}{c} \int_0^\infty d\nu (1 - e^{-\tau_\nu}). \quad (20)$$

For a Voigt profile, the equivalent width is related to the column density through the line-center optical depth according to

$$w_\lambda/\lambda = 2(b/c)F(a, \tau_0), \quad (21)$$

where the function $F(a, \tau_0)$, shown in Fig. 3, is

$$F(a, \tau_0) = \int_0^\infty dx \{1 - \exp[-\pi^{1/2} \tau_0 \phi_V(a, x)]\}. \quad (22)$$

The relationship between the equivalent width and the column density is known as the “curve of growth.” For $\tau_0 < 10^4$, the absorption profiles are well approximated as Doppler in shape, corresponding to $\phi_V(a, x) \approx \pi^{-1/2} e^{-x^2}$, and $F(a, \tau_0)$ may be denoted more simply by $F(\tau_0)$. The function $F(\tau_0)$ may be expressed as the power series (Münch, 1968)

$$F(\tau_0) = \frac{\sqrt{\pi}}{2} \sum_{n=1}^{\infty} (-1)^{n-1} \frac{\tau_0^n}{n! \sqrt{n}}. \quad (23)$$

For very optically thin lines ($\tau_0 \ll 1$), $F(\tau_0) \approx (\sqrt{\pi}/2)\tau_0$, and the equivalent width is related linearly to the column density,

$$\frac{w_\lambda}{\lambda} = \frac{\pi e^2}{m_e c^2} \left[\frac{1}{4\pi \epsilon_0} \right] N \lambda f_{lu} \approx 8.85 \times 10^{-13} N \lambda f_{lu}, \quad (24)$$

where $N\lambda$ has the dimension cm^{-1} . Such features are said to lie on the “linear” part of the curve of growth.

For $6 < \tau_0 < 300$, better than 1% accuracy is provided by the asymptotic series (Münch, 1968)

$$F(\tau_0) \sim (\ln \tau_0)^{1/2} \left(1 + \frac{0.2886}{\ln \tau_0} - \frac{0.1335}{(\ln \tau_0)^2} + \dots \right). \quad (25)$$

For H I Ly- α at a temperature $T = 10^4$ K, $F(a, \tau_0)$ deviates from the logarithmic approximation Eq. (25) by less than 10% for $2 < \tau_0 < 5000$. Such features are said to lie on the “logarithmic” part of the curve of growth. They are also referred to as “saturated” lines since an increase in the column density has only a small change on the shape of the absorption feature. The measurement of accurate column densities is difficult for these features, necessitating the search for higher-order resonance lines on a more linear part of the curve of growth if accurate column densities are desired. On the other hand, the equivalent width is nearly directly proportional to the Doppler width, allowing an accurate determination of the Doppler parameter.

For very large values of τ_0 , the Lorentzian radiation damping wings of the Voigt profile dominate the line profile, which in this limit is given by $\phi_V(a, x) \approx a/\pi x^2$. In this case, the equivalent width is given by

$$\frac{w_\lambda}{\lambda} \approx \frac{2}{c} \left(\lambda^2 N \sigma \frac{\Gamma_{ul}}{4\pi} \right)^{1/2} = 2\pi^{1/4} \frac{b}{c} (a\tau_0)^{1/2}. \quad (26)$$

Because of the square-root dependence on column density, this limit is referred to as the “square-root” part of the curve of growth. While the independence of the equivalent width on the Doppler width of the feature leaves b poorly determined, the stronger dependence on the column density permits a more accurate determination of the column density from the equivalent width, or from line-profile fitting, than is possible for systems on the logarithmic part. The square-root approximation Eq. (26), however, is accurate only for very large values of τ_0 . It is more than 25% too low for $\tau_0 < 10^4$. Better than 1% accuracy is achieved for $\tau_0 > 2 \times 10^5$.

B. Absorption line properties

1. Physical properties of absorption line systems

The absorption features comprising the Ly- α forest are broadly classified into three main types: Ly- α forest systems, DLAs, and Lyman limit systems (LLSs). The classification is based primarily on the physical origin of the features. The Ly- α forest systems, by far the most common, are generally well fitted by Doppler line profiles. The much rarer DLAs have sufficiently high hydrogen column densities that they show the radiation damping wings of the Lorentz profile, and require the Voigt line profile for accurate fitting. The intermediate LLSs have a sufficiently large column density to absorb photons with energies above the photoelectric edge or Lyman limit. The classifications are not strictly exclusive. Damped absorbers of course produce Lyman limit systems. Lower-column-density Lyman limit systems will produce a Ly- α forest feature. For convenience, the features, however, are treated as distinct, corresponding typically to the column density ranges shown in Table I. Recently, a subclass of super Lyman limit systems

TABLE I. Summary of absorption line system properties.

Absorber class	Line parameters		Physical characteristics				$\frac{dN}{dx}^a = N_0(1+z)^\gamma$	
	N_{HI} (cm^{-2})	b^b (km s^{-1})	n^c (m^{-3})	T^c (K)	Size (kpc)	$[M/H]^d$	N_0	γ
Ly- α forest	$\leq 10^{17}$	15–60	0.01–1000	5000–50000	15–1000(?)	–3.5 to –2	6.1	2.47
LLS	$10^{17}–10^{19}$	~ 15	$\sim 10^3–10^4$	~ 30000		–3 to –2	0.3	1.50
Super LLS	$10^{19}–2 \times 10^{20}$	~ 15	$\sim 10^4$	~ 10000		–1 to +0.6	0.03	1.50
DLA	$> 2 \times 10^{20}$	~ 15	$\sim 10^7; \sim 10^4$	$\sim 100; \sim 10000$	$\sim 10–20(?)$	–1.5 to –0.8	~ 0.03	~ 1.5

^aFor the following HI column density and redshift ranges. For the Ly- α forest: $13.64 < \log_{10} N_{\text{HI}} < 17$ and $1.5 < z < 4$; for Lyman limit systems: $\log_{10} N_{\text{HI}} > 17.2$ and $0.32 < z < 4.11$. The same evolution rate is adopted for super Lyman limit systems. The evolution rate of damped Ly- α absorbers over the range $2 < z < 4$ is consistent with that of Lyman limit systems, but poorly constrained by observations.

^bApproximate ranges. Not well determined for most Lyman limit systems and super Lyman limit systems.

^cValues not well constrained by direct observations.

^dApproximate metallicity range, expressed as a logarithmic fraction of solar: $[M/H] = \log_{10}(M/H) - \log_{10}(M/H)_\odot$.

(SLLSs) has been introduced, corresponding to systems with $10^{19} < N_{\text{HI}} < 2 \times 10^{20} \text{ cm}^{-2}$ (Wolfe *et al.*, 2005).¹² These systems are convenient for statistical studies since their column densities are more easily determined than their lower-column-density counterparts because the damping wings begin to appear. They are sometimes also referred to as subdamped absorbers, but there is an important physical distinction between them and the general class of DLAs: the hydrogen in the DLAs is essentially neutral, while the SLLSs are sufficiently penetrated by the UV metagalactic background as to be partially ionized. It is therefore reasonable to distinguish the DLAs as an entirely unique class of absorber.

A great number of surveys of QSO intervening absorption systems have been carried out, building up a large inventory of their statistical properties. Systematic surveys of the Ly- α forest were conducted by Weymann *et al.* (1979), Sargent *et al.* (1980), Bechtold (1994), Hu *et al.* (1995), Storrie-Lombardi *et al.* (1996), Bechtold *et al.* (2002), Kim, Carswell, *et al.* (2002), and Tytler, O’Meara *et al.* (2004). Surveys of Lyman limit systems were conducted by Sargent *et al.* (1989), Lanzetta, Wolf, and Turnshek (1995) and O’Meara *et al.* (2007). Surveys of damped Ly- α absorbers were conducted by Wolfe *et al.* (1986, 1995), Lanzetta *et al.* (1991), Lu *et al.* (1993), Lu and Wolfe (1994), Lanzetta, Wolfe, and Turnshek (1995), Storrie-Lombardi and Wolfe (2000), Ellison *et al.* (2001, 2002), Colbert and Malkan (2002), Akerman *et al.* (2005), Srianand *et al.* (2005), Rao *et al.* (2006), and Jorgenson *et al.* (2006). A radio survey of intervening absorption systems was carried out by Gupta *et al.* (2007). Surveys for galaxies associated with intervening absorption systems were conducted for galaxies associated with diffuse Ly- α absorption systems at $z < 1$ by Lanzetta, Bowen, *et al.* (1995), Chen, Prochaska, *et al.* (2005), Mor-

ris and Jannuzi (2006), and Ryan-Weber (2006), with damped Ly- α absorbers by Chen and Lanzetta (2003) and Cooke *et al.* (2005, 2006) and with metal absorption systems at $z < 1$ by Tumlinson *et al.* (2005), Prochaska *et al.* (2006), Stocke, Penton, *et al.* (2006), and Kacprzak *et al.* (2008), and at $z > 1$ by Adelberger *et al.* (2005).

The neutral hydrogen column densities of the absorbers are measured to range from roughly 10^{12} to 10^{22} cm^{-2} . Lower-column-density systems may exist, but are difficult to detect. An upper cutoff at $(3–5) \times 10^{21} \text{ cm}^{-2}$ is suggested by Prochaska *et al.* (2005). It was early recognized by Tytler (1987a) that the distribution function of the column densities is a near perfect power law, $dN/dN_{\text{HI}} \propto N_{\text{HI}}^{-\beta}$, with $\beta = 1.5–1.7$ (Tytler, 1987a; Hu *et al.*, 1995; Kim, Carswell, *et al.*, 2002). A recent determination for absorption systems in the redshift range $0.5 < z < 1.9$ is shown in Fig. 4 (Janknecht *et al.*, 2006). Although there may be small deviations from a perfect power law (Giallongo *et al.*, 1993; Meiksin and Madau, 1993; Petitjean *et al.*, 1993), the nearness to a single power law over such an enormous dynamic range strongly suggests a single formation mechanism.

The measured Doppler velocities b range over about $10 < b < 100 \text{ km s}^{-1}$, with the majority concentrated between 15 and 60 km s^{-1} (Atwood *et al.*, 1985; Carswell *et al.*, 1991; Rauch *et al.*, 1992; Hu *et al.*, 1995; Lu, Sargent, Womble, and Takada-Hidai, 1996; Kim *et al.*, 1997; Kirkman and Tytler, 1997a). A typical distribution is shown in Fig. 5, using the line list for Q0000-26 from Lu, Sargent, Womble, and Takada-Hidai (1996). Temperatures may in principle be inferred from Eq. (10), but doing so is hampered by two difficulties: (1) the systems may be broadened by a kinematic component and (2) the absorption features may be blends of more than a single system. Evidence for kinematic broadening is found when metal features are also detected. In general, there is no unique fit to an absorption feature, particularly in the presence of blending: several statistically acceptable fits are possible (Kirkman and Tytler, 1997a), and these

¹²Although the SI system is used throughout this review, column densities are expressed with dimensions of cm^{-2} to be consistent with the convention in the literature.

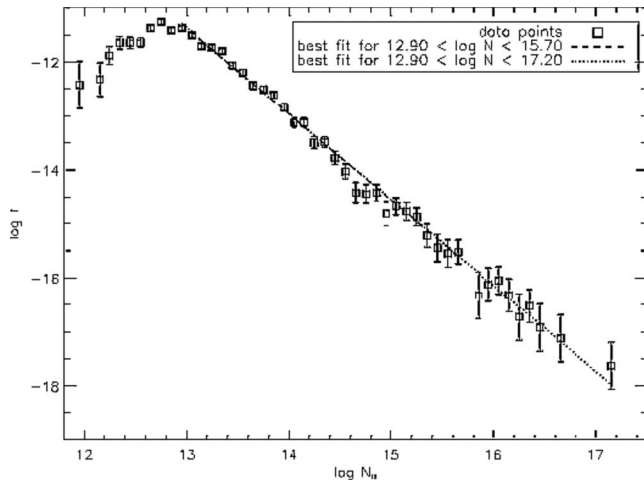


FIG. 4. Distribution of Ly- α forest column densities with fits for different ranges, for absorption systems in the redshift range $0.5 < z < 1.9$. For $12.90 < \log_{10} N_{\text{HI}} < 15.70$, $\beta = 1.60 \pm 0.03$. For $12.90 < \log_{10} N_{\text{HI}} < 17.20$, $\beta = 1.59 \pm 0.02$. From [Janknecht et al., 2006](#). Figure reproduced by permission of *Astronomy & Astrophysics*.

will change as the signal-to-noise ratio or spectral resolution changes ([Rauch et al., 1993](#)). Indeed, Eq. (14) shows that each absorption feature itself may be regarded as the blending of an infinity of smaller features. It is only because of clumpiness of the IGM that the features may be localized [Eq. (16)], yet internal structure is still visible when multiple narrower metal features are detected in a single Ly- α system.

Broadening is also expected from the line finding and fitting procedure. The systematic influence of procedures used to locate and fit the absorption lines on the resulting distributions of Doppler parameters has received limited attention. The potential usefulness of the Doppler parameter distribution for extracting physical information about the IGM, such as its temperature dis-

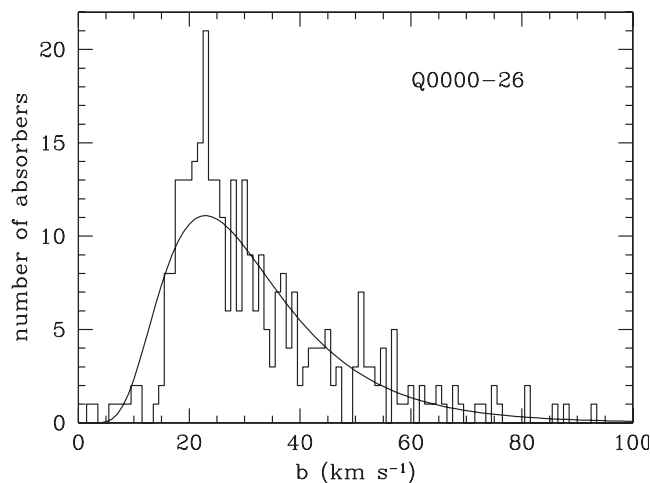


FIG. 5. Distribution of Ly- α forest Doppler parameters for Q0000-26 ([Lu, Sargent, Womble, and Takada-Hidai, 1996](#)). A lognormal distribution (solid line) provides a statistically acceptable fit to the distribution.

tribution, merits further study of the effect of fitting algorithms on the derived distribution. Artificially large b values, for example, have been reproduced through Monte Carlo-simulated spectra with much narrower Gaussian distributions for the b values ([Lu, Sargent, Womble, and Takada-Hidai, 1996](#); [Kirkman and Tytler, 1997](#)). The Monte Carlo models assume Poisson-distributed line centers. Allowing for clustering of the line centers may lead to even broader distributions.

The measured distributions may be fitted by a log-normal function ([Zhang et al., 1997](#); [Meiksin et al., 2001](#)). As an illustration, the best-fitting lognormal function $f(\xi) = \exp(-0.5\xi^2) / \sqrt{2\pi}$, where $\xi = -7.15 + 2.13 \ln(b)$, provides a statistically acceptable description of the b distribution of Q0000-26 ([Lu, Sargent, Womble, and Takada-Hidai, 1996](#)) for systems lying between the rest frame Ly- β and Ly- α wavelengths of the QSO, excluding a small region possibly influenced by the proximity effect (see Sec. IV.C.1). The fit distribution is shown in Fig. 5. The Kolmogorov-Smirnov (KS) test yields a probability for obtaining as large a difference as found between the predicted and measured cumulative distributions of $p_{\text{KS}} = 0.361$. A log-normal distribution will result when the error on a quantity is proportional to the magnitude of the quantity. For example, consider an absorption system with an intrinsic Doppler parameter b . If the iterations of the nonlinear fitting procedure for the remaining features in the spectrum each perturb the first feature by an amount $\Delta b \propto b$, then $\Delta \ln b$ will change by a randomly distributed amount. Fitting several features will then result in a sum of random changes to $\Delta \ln b$. By the central-limit theorem, a normal distribution for $\ln b$ will result. A comparison between the measured b values and their errors from [Lu, Sargent, Womble, and Takada-Hidai \(1996\)](#) showed a positive correlation. The Spearman rank-order correlation coefficient is $r_s = 0.31$, with $p(>r_s) = 9.3 \times 10^{-9}$. A similar result is found for HS 1946+7658 ([Kirkman and Tytler, 1997a](#)), for which a correlation between the Doppler parameters and their errors is found with $r_s = 0.28$ and $p(>r_s) = 7.4 \times 10^{-9}$. A log-normal distribution again provides an acceptable fit to the Doppler parameter distribution. The results for this and several other distributions measured in high-resolution Keck spectra are shown in Table II. In all cases, a log-normal distribution provides a good fit. Although not conclusive, these results suggest that the measured Doppler parameters may in part be induced by a log-normal-generating stochastic process. It is noted that the process need not arise entirely from the line fitting, but could also originate from the physical processes that gave rise to the structures that produce discrete absorption features.

Uncertainty in the origin of the Doppler parameter distribution leaves the physical interpretation of the Doppler parameters with some ambiguity. Although their relation to the gas temperature is not straightforward, the Doppler parameters may usually be used legitimately to set upper limits on the gas temperature. (Even an upper limit is not always guaranteed since

TABLE II. Lognormal fits to the Doppler parameter distributions measured for the Ly- α forest seen in the spectra of Q0000–26 (Lu, Sargent, Womble, and Takada-Hidai, 1996), HS 1946+7658 (Kirkman and Tytler, 1997a), and Q0014+813, Q0302–003, Q0636+680 and Q0956+122 (Hu *et al.*, 1995). The fits are represented in the form $f(b)=\exp(-0.5\xi^2)/\sqrt{2\pi}$, where $\xi=\gamma+\delta\ln(b)$.

QSO name	Z range	No. lines	$\langle b \rangle$ (km s ⁻¹)	γ	δ	p_{KS}
Q0000–26	3.42 < z < 3.98	334	32.8	-7.15	2.13	0.36
Q0014+813	2.70 < z < 3.20	262	33.9	-8.86	2.58	0.99
Q0302–003	2.62 < z < 3.11	266	33.9	-8.75	2.56	0.97
Q0636+680	2.54 < z < 3.03	312	29.3	-7.24	2.23	0.30
Q0956+122	2.62 < z < 3.11	256	31.6	-8.05	2.42	0.53
HS 1946+7658	2.42 < z < 2.98	399	32.5	-7.18	2.16	0.50

noise affecting a weak line may leave it too narrow, or even produce an artificial narrow line.) For pure Doppler broadening, the range 20–60 km s⁻¹ corresponds to temperatures of 2.4×10^4 – 3.8×10^4 K, the range expected from photoionization at the moderate overdensities expected for the absorbers (Meiksin, 1994; Hui and Gnedin, 1997). Cooler temperatures are possible, however, particularly if the gas has been expanding sufficiently fast for adiabatic cooling to be appreciable.

The element of indeterminacy in the measurements of the line parameters has made it difficult to search for evolution in the distribution of Doppler parameters. Evolution is especially interesting in the context of late He II reionization, which may have occurred at $z \approx 3$ – 3.5 . Evolution of the Doppler parameter distribution, however, could also result if absorption systems with different physical characteristics dominate the detected and fitted absorption lines at different epochs. Numerical simulations suggest the systems that give rise to a given H I column density range shift to structures of different gas densities, and therefore different gas temperatures and different sizes as the Universe expands and as the intensity of the photoionizing UV background evolves. The difficulty of interpreting any change in the Doppler parameter distribution in terms of sudden heating is exacerbated by an increase in line blending with increasing redshift. Using an analysis based on the lower cutoff in the Doppler parameter distribution, Schaye, Theuns, *et al.* (2000) reported evolution in the inferred IGM gas temperature over the range $2.0 < z < 4.5$, peaking at $z \approx 3$, consistent with the onset of He II reionization at this redshift. Similar results are obtained from a separate analysis by Ricotti *et al.* (2000). Kim, Cristiani, and D’Odorico (2002) also suggested evolution in the gas temperature based on an increase in the lower cutoff of the Doppler parameter distribution from $z=3.8$ to 3.3 . But the values for the cutoff they derived are discrepant with those of Schaye, Theuns, *et al.* (2000), which casts uncertainty on either interpretation. Kim, Cristiani, and D’Odorico (2002) showed there is considerable sample variance in the cutoff at the same redshift, and attribute the discrepancy with Schaye, Theuns, *et al.* (2000) to this variance. On the other hand, Lehner *et al.* (2007), using the same sample as Kim, Carswell, *et al.* (2002), found no

significant evolution in the b distribution over the redshift range $1.5 < z < 3.6$. This result is confirmed by the nearly identical parameters obtained for the best-fit lognormal distributions between the highest- and lowest-redshift samples in Table II. Lehner *et al.* (2007) did argue for the presence of a second broader population at $z \leq 0.4$. Janknecht *et al.* (2006) found no evidence for evolution in the Doppler parameters over the redshift range $0 < z < 2$.

Damped Ly- α absorbers show a more complex physical structure. Measurements of the 21 cm hyperfine absorption signature produce a range of spin temperatures, from values as low as $T_S \approx 200$ K to lower limits of $T_S \geq 9000$ K, with the lower values occurring only at $z \leq 3$. Kanekar and Chengalur (2003) provided a tabulation from the literature. The presence of high-ionization metal species shows that there is a second warmer component present as well, with $T \approx 10^4$ K. Wolfe *et al.* (2005) suggested a two-component interstellar medium consisting of a warm neutral medium (WNM) at $T \approx 8000$ K in pressure equilibrium with a cold neutral medium (CNM) at $T \approx 100$ K.

A summary of the absorption line properties, as well as of the physical characteristics discussed below, is provided in Table I.

2. Evolution in the number density of the Ly- α forest

The number of absorption systems per unit redshift increases with redshift. Some evolution is expected as a result of the expansion of the Universe. For a proper number density $n_a(z)$ of absorption systems at redshift z , with proper cross section $\sigma_a(z)$, the expected number of absorbers per unit proper length is $dN/dl_p = n_a(z)\sigma_a(z)$. The proper line element is related to redshift according to $dl_p/dz = c/H(z)(1+z)$, where $H(z) = H_0 E(z)$ is the Hubble parameter (see Sec. II.A). For a flat universe ($\Omega_K = 0$) and standard cosmological parameters, $E(z) \approx 0.55(1+z)^{3/2}[1+2.3/(1+z)^3]^{1/2}$. The evolution in the number density is then given by

$$\frac{dN}{dz} \approx (2100 \text{ Mpc}) n_{a,c}(z) \sigma_a(z) (1+z)^{1/2} \times \left(1 + \frac{2.3}{(1+z)^3}\right)^{-1/2}, \quad (27)$$

where $n_{a,c}(z) = n_a(z)(1+z)^{-3}$ is the comoving number density of systems. For a constant comoving number density and fixed proper cross section, only moderate evolution is expected, $dN/dz \propto (1+z)^{1/2}$. At low redshifts, this gives a reasonable description of the evolution. Using Hubble space telescope observations, Weymann *et al.* (1998) found for all systems with equivalent widths above 0.24 \AA , $dN/dz = (32.7 \pm 4.2)(1+z)^{0.26 \pm 0.22}$ for $z < 1.5$. Subsequent higher-spectral-resolution surveys using HST have extended the statistics to systems with equivalent widths below 0.1 \AA at $z < 0.1$ (Penton *et al.*, 2000, 2004). The large survey of Danforth and Shull (2008) obtained $dN/dz = 129^{+6}_{-5}$ down to 0.030 \AA at $z < 0.4$ with $\langle z \rangle = 0.14$.

For $z > 1.5$, however, the number density evolves considerably faster than the constant comoving rate (Tytler, 1987b). Kim, Carswell, *et al.* (2002) obtained $dN/dz = 6.1(1+z)^{2.47 \pm 0.18}$ for systems with column densities in the range $13.64 < \log_{10} N_{\text{HI}} < 17$. This corresponds to considerable evolution in the product $n_{a,c}(z)\sigma_a(z)$. A smooth transition was found over the redshift range $0.5 < z < 1.9$ by Janknecht *et al.* (2006), with a dependence of the evolution rate on column density. High-column-density systems corresponding to Lyman limit systems evolve somewhat more slowly than lower-column-density systems. Stengler-Larrea *et al.* (1995) found for systems with $\tau_L > 1$, $dN/dz = 0.25^{+0.10}_{-0.17}(1+z)^{1.50 \pm 0.39}$ over the redshift range $0.32 < z < 4.11$. Based on a larger higher-redshift sample, Péroux *et al.* (2003) found somewhat more rapid evolution, with $dN/dz = 0.07^{+0.04}_{-0.13}(1+z)^{2.45^{+0.75}_{-0.65}}$ over the redshift range $2.4 < z < 5$. Damped Ly- α absorbers show evolution comparable to that of the Lyman limit systems, with dN/dz increasing by about a factor of 2 from $z = 2.5$ to 4 (Prochaska *et al.*, 2005).

As will be discussed in Sec. VI numerical simulations show that the structure of the IGM evolves, although in the comoving frame the structure is remarkably stable. Because dN/dz is fitted for a fixed HI column density range, the diminishing gas density toward decreasing redshifts will result in fewer systems satisfying the column density threshold, so that dN/dz will decrease toward decreasing redshift. Evolution in the ionizing background will also affect the number of absorption systems lying above the column density threshold, and this is a major factor in the evolution of dN/dz . The slowdown at $z < 1.5$ in the evolution is in fact attributed predominantly to a reduction in the intensity of the ionizing background: as the ionizing rate decreases, fewer systems will slip below the column density threshold than under pure density evolution. As a result, the decrease in dN/dz toward lower z slows down. The difference in the rate of evolution between low- and high-column-

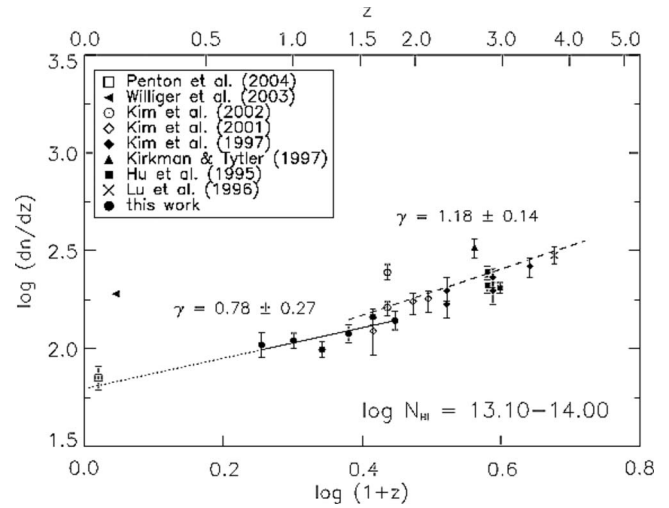


FIG. 6. Evolution of the number density of Ly- α systems with $13.10 < \log_{10} N_{\text{HI}} < 14.00$, including best fits to the solid and open circles over the ranges indicated, as represented by the solid and dashed lines, respectively, taking $dN/dz \propto (1+z)^\gamma$. The dotted line extrapolates the lower redshift fit to $z=0$. From Janknecht *et al.*, 2006. Figure reproduced by permission of *Astronomy & Astrophysics*.

density systems found by Janknecht *et al.* (2006) (compare Figs. 6 and 7) shows that structural evolution in the IGM must also play a role.

3. Characteristic sizes and spatial correlations

Multiple QSOs in proximity to each other on the sky provide an invaluable means for estimating the physical

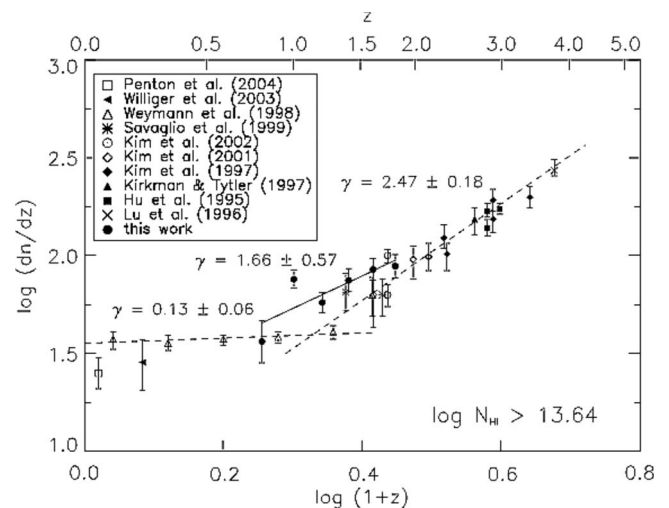


FIG. 7. Evolution of the number density of Ly- α systems with $\log_{10} N_{\text{HI}} > 13.64$, including best fits to the solid and open circles over the ranges indicated, as represented by the solid and dashed lines, taking $dN/dz \propto (1+z)^\gamma$. The additional low-redshift dashed line is the best fit to the open triangles. The open square, left-pointing solid triangle, and stars correspond to systems with $\log_{10} N_{\text{HI}} > 14.00$. From Janknecht *et al.*, 2006. Figure reproduced by permission of *Astronomy & Astrophysics*.

sizes of the regions in the IGM that give rise to the absorption features. Especially useful have been multiply imaged lensed quasars. Using high-resolution spectra of images of a lensed QSO with a separation of 3 arcsecs, [Smette et al. \(1995\)](#) detected a large number of absorbers coincident between the two lines of sight. All clearly detected coincident systems show comparable equivalent widths between the lines of sight, suggesting that the same physical structures are being probed. They set 2σ lower limits of about 70 kpc for weak absorption systems ($\log_{10} N_{\text{HI}} < 14$), and of about 15 kpc for strong systems ($\log_{10} N_{\text{HI}} > 15$), assuming the clouds are spherical. For disklike systems, the lower limits are about twice as large.

Other efforts resulted in similar lower limits ([McGill et al., 1990](#); [Smette et al., 1992](#); [Bechtold et al., 1994](#)). Multiple lines of sight with wider separations of about 1 arcmin suggest still larger sizes of 0.3–1 Mpc ([Crotts and Fang, 1998](#); [Dinshaw et al., 1998](#); [D’Odorico et al., 1998b](#); [Petitjean et al., 1998](#)), and possibly as large as 40 Mpc (comoving) ([Williger et al., 2000](#)). [Smette et al. \(1995\)](#) reported a likely size of about 10–30 kpc for a single damped Ly- α absorber, comparable to the lower limit obtained by direct H I imaging measurements of a separate system by [Briggs et al. \(1989\)](#).

A difficulty with interpreting the larger, megaparsec-scale sizes for the Ly- α forest systems is that the equivalent widths of systems with common redshifts along the neighboring lines of sight do not always match well over these scales. An alternative interpretation of the coinciding redshifts is that they indicate underlying spatial correlations between the absorption systems rather than their spatial coherence. Measurements of the autocorrelation function between absorption systems along single lines of sight suggest correlations on scales of a few hundred km s^{-1} ([Cristiani et al., 1995](#); [Hu et al., 1995](#); [Meiksin and Bouchet, 1995](#)). An anticorrelation at separations of 500–1000 km s^{-1} ([Cristiani et al., 1995](#); [Hu et al., 1995](#); [Meiksin and Bouchet, 1995](#)) has been disputed by [Kim et al. \(1997\)](#) on the basis of the limited lines of sight analyzed, but the issue appears not fully resolved. In the presence of correlations, the error on the correlation function depends on the three- and four-point functions, which are not well measured. A more recent analysis at $z < 2$ detects only weak positive correlations on the few hundred km s^{-1} scale, and no clear anticorrelation ([Janknecht et al., 2006](#)). Transverse positive spatial correlations over comparable scales at $\langle z \rangle = 2.14$ were obtained by [Crotts and Fang \(1998\)](#) and at $0.4 < z < 0.9$ by [Petry et al. \(2006\)](#). Coherence in absorption lines along lines of sight separated by $\sim 2h^{-1}$ Mpc at $2.6 < z < 3.8$ has been detected by [Casey et al. \(2008\)](#).

A characteristic size of 70 kpc for systems with $N_{\text{HI}} \approx 10^{14} \text{ cm}^{-2}$ suggests that a large fraction of the baryons are contained within the Ly- α forest ([Meiksin and Madau, 1993](#)). Taking the size to correspond to a characteristic line-of-sight thickness, the corresponding H I number density is $n_{\text{HI}} \approx 5 \times 10^{-4} \text{ m}^{-3}$. Ionization equilibrium in a UV background, producing an ioniza-

tion rate of $\Gamma_{\text{HI}} \approx \Gamma_{\text{HI},-12} \times 10^{-12}$ H I atoms per second (Sec. [IV.A.2](#)) gives a neutral fraction of $x_{\text{HI}} \approx (1.2n_{\text{HI}}\alpha_A/\Gamma_{\text{HI}})^{1/2} \approx 1.5 \times 10^{-5} N_{\text{HI},14}^{1/2} T_4^{-0.37} \Gamma_{\text{HI},-12}^{-1/2}$, where $\alpha_A \approx 4 \times 10^{-19} \text{ m}^3 \text{ s}^{-1} T_4^{-0.75}$ is the radiative recombination rate for gas at a temperature $T_4 = T/10^4 \text{ K}$ and $N_{\text{HI},14} = N_{\text{HI}}/10^{14} \text{ cm}^{-2}$. The ratio of the baryonic mass density of the Ly- α forest to the critical Einstein–de Sitter density $\rho_{\text{crit}}(z) = \rho_{\text{crit}}(0)H(z)^2/H_0^2$ is

$$\begin{aligned} \Omega_{\text{Ly-}\alpha} &= \frac{1.4m_{\text{H}}}{\rho_{\text{crit}}} \int dN_{\text{HI}} \frac{\partial^2 \mathcal{N}}{\partial N_{\text{HI}} \partial z} \frac{N_{\text{HI}}}{x_{\text{HI}}} \left(\frac{dl_p}{dz} \right)^{-1} \\ &= 1.4m_{\text{H}} \frac{8\pi G}{3cH(z)} (1+z) \int dN_{\text{HI}} \frac{\partial^2 \mathcal{N}}{\partial N_{\text{HI}} \partial z} \frac{N_{\text{HI}}}{x_{\text{HI}}} \\ &\approx 3.0 \times 10^{-5} N_0 h^{-1} \Omega_m^{-1/2} T_4^{0.37} \Gamma_{\text{HI},-12}^{1/2} (1+z)^{\gamma-1/2} \\ &\quad \times \ln \left(\frac{N_{\text{HI,max}}}{N_{\text{HI,min}}} \right) \approx 0.06 T_4^{0.37} \Gamma_{\text{HI},-12}^{1/2} \end{aligned} \quad (28)$$

for $dN/dz = N_0(1+z)^\gamma$ with $N_0 = 6.1$ and $\gamma = 2.47$, and $dN/dN_{\text{HI}} \propto N_{\text{HI}}^{-1.5}$ with $N_{\text{HI,min}} = 10^{13.64} \text{ cm}^{-2}$ and $N_{\text{HI,max}} = 10^{17} \text{ cm}^{-2}$, evaluated at $z = 3$ with $\Omega_m = 0.3$ and $h = 0.7$. This is comparable to estimates for the baryon density of the Universe (see Sec. [II.B.4](#)). The result is not conclusive, however. Since the size estimates are in the transverse direction, a much smaller value for $\Omega_{\text{Ly-}\alpha}$ is possible if the structures are flattened, down by the aspect ratio of the thickness to breadth of the systems ([Rauch and Haehnelt, 1995](#)).

4. Deuterium absorption systems

High-column-density Ly- α absorption systems offer the opportunity to measure the primordial deuterium abundance D/H, a sensitive indicator of the cosmic baryon density, or equivalently the nucleon to photon ratio η , according to Big Bang nucleosynthesis. To date, a relatively limited number of accurate determinations of η from the deuterium abundance have been possible. A line of sight must meet several criteria to be useful for obtaining a clean measurement ([Kirkman et al., 2003](#)): the hydrogen column density must be sufficiently large that deuterium is detectable, the velocity width of the system must be sufficiently narrow so as not to encroach on the 82 km s^{-1} offset deuterium feature; the structure of the system must not be so complicated that a weak interloping H I feature could be mistaken for deuterium, and the background QSO must be sufficiently bright to obtain a high signal-to-noise ratio measurement. These combined criteria whittle down the number of acceptable QSO lines of sight to about 1% of those available at $z = 3$.

Despite the difficulty, several accurate determinations have been made ([Burles and Tytler, 1998a, 1998b](#); [O’Meara et al., 2001, 2006](#); [Pettini and Bowen, 2001](#); [Levshakov et al., 2002](#); [Kirkman et al., 2003](#); [Crighton et al., 2004](#)). The current best estimate for D/H is $\log_{10} \text{D/H} = -4.55 \pm 0.04$ ([O’Meara et al., 2006](#)). Using standard Big Bang nucleosynthesis models, this translates to a baryon density parameter of $\Omega_b h^2$

$=0.0213 \pm 0.0013 \pm 0.0004$, where the 1σ errors refer to the error on the D/H measurement and the uncertainties in the nuclear reaction rates, respectively. This corresponds to a nucleon-to-photon ratio of $\eta = (5.8 \pm 0.3) \times 10^{-10}$. This compares favorably with the determination from the five-year WMAP measurements of the CMB fluctuations, combined with baryonic acoustic oscillations and Type-Ia supernovae constraints, of $\eta \approx (6.2 \pm 0.2) \times 10^{-10}$ (Komatsu *et al.*, 2009).

5. Helium absorption systems

The UV spectral capability of the Hubble space telescope made it possible for the first time to measure intergalactic He II Ly- α $\lambda 304$. Using the spectrum of Q0302-003 at $z_{\text{em}} \approx 3.286$ observed by the faint object camera, Jakobsen *et al.* (1994) found $\tau_{\text{He II}} > 1.7$ (90% confidence) at $z = 3.2$, revised to a 95% confidence interval of $1.5 < \tau_{\text{He II}} < 3.0$ by Hogan *et al.* (1997) and to $\tau_{\text{He II}} > 4.8$ by Heap *et al.* (2000) after more detailed modeling of the absorption trough. Because the same sources which ionize the H I should also ionize He I, virtually all intergalactic helium will be in the form of either He II or He III, depending on whether or not there were sources hard enough to fully ionize helium.

Remarkably, using the spectrum of HS 1700+6416 ($z_{\text{em}} \approx 2.7$) observed by the Hopkins ultraviolet telescope (HUT), Davidsen *et al.* (1996) measured the more moderate optical depth of $\tau_{\text{He II}} \approx 1.00 \pm 0.07$ over the somewhat lower redshift range $z = 2.2 - 2.6$. This led to the speculation that He II was ionized around $z \approx 3$. Subsequent measurements of the spectrum of HE 2347-4342 ($z_{\text{em}} \approx 2.885$) have shown the He II Ly- α optical depth to be very patchy at $z \lesssim 3$, as if a second reionization epoch were being observed, that of He II (Reimers *et al.*, 1997).

Observations of PKS 1935-692 ($z_{\text{em}} \approx 3.18$) using HST (Anderson *et al.*, 1999) and of HE 2347-4342 using the far ultraviolet spectroscopic explorer have detected a He II Ly- α forest (Kriss *et al.*, 2001; Shull *et al.*, 2004; Zheng, Kriss, *et al.*, 2004), permitting more detailed assessments of the fluctuations in the He II to H I column densities. Measurements of the He II Ly- α forest also provide an opportunity to probe the underlying IGM velocity field. Using combined FUSE and VLT data, Zheng, Kriss, *et al.* (2004) were able to identify isolated absorption systems in underdense regions with common H I Ly- α and He II Ly- α features. A comparison between the fitted Doppler parameters gives the ratio $b_{\text{He II}}/b_{\text{H I}} = 0.95 \pm 0.12$. According to Eq. (11), this indicates a velocity field in underdense regions with kinematic motions that dominate the thermal motion.

Subsequent measurements continue to confirm the patchy nature of the He II Ly- α optical depth, including HST observations of HE 2347-4342 (Smette *et al.*, 2002), SDSS J2346-0016 ($z_{\text{em}} \approx 3.50$) (Zheng, Chin, *et al.*, 2004), and Q1157+3143 ($z_{\text{em}} \approx 3.01$) (Reimers *et al.*, 2005), and a FUSE observation of HS 1700+6416 (Fechner *et al.*, 2006). As some of these references point out, and as will be discussed in Sec. IV.C.2, the interpretation in terms of

reionization is not unambiguous: the patchiness may also arise from fluctuations in the radiation field.

6. Metal absorption systems

The earliest identifications of intervening absorption systems were for elements heavier than helium, so-called metals (Bahcall *et al.*, 1968). Common are carbon, nitrogen, silicon, and iron, but to date the list extends much further, including oxygen, magnesium, neon, and sulfur (Sargent *et al.*, 1980; Meyer and York, 1987; Cowie *et al.*, 1995; Koehler *et al.*, 1996; Songaila and Cowie, 1996; Lu, Sargent, and Barlow, 1998; Ellison *et al.*, 1999a, 1999b; Schaye, Rauch, *et al.*, 2000; Simcoe *et al.*, 2002, 2004; Richter *et al.*, 2004; Savage *et al.*, 2005). The metals provide invaluable insight into the structure of the IGM in several different ways. The widths of metal absorption features allow direct estimates of the temperature of the IGM and its small-scale velocity structure. The narrow widths of C IV features were used by York *et al.* (1984) to demonstrate that the absorbers had the characteristic temperatures of photoionized rather than collisionally ionized gas. The metal systems probe the impact star formation has had on the IGM, as the metals were most likely transported into the IGM through galactic winds, or introduced *in situ* by local small-scale regions forming first-generation Population III stars. In the nearby Universe, they indicate the presence of shocked gas, as may accompany the formation of galaxy clusters. As such, the metals in principle document the history of cosmic structure and star formation. Ratios of the metal column densities may be used to constrain the spectral shape of the metagalactic ionizing UV background, which in turn puts constraints on the possible sources of the background and their relative contributions. Lastly, metal absorption lines offer a unique opportunity to search for variability in the constants of nature.

Tables of the resonance lines most easily detectable in intervening absorption systems are provided by Morton and York (1989) and Vogel and Reimers (1995). Searches for intervening metal absorbers have been facilitated by the exploitation of atomic line doublets for some of the stronger species. The most common doublets used are Mg II $\lambda\lambda 2796, 2803 \text{ \AA}$ and C IV $\lambda\lambda 1548, 1551 \text{ \AA}$. These are among the strongest lines detected in the Ly- α forest. They also have the important advantage of wavelengths redward of Ly- α , placing them outside the Ly- α forest and avoiding this potential source of confusion. Searches for Mg II absorption systems are by far the most common because of their established connection to galaxies. Mg II absorber surveys were carried out by Lanzetta *et al.* (1987), Tytler *et al.* (1987), Sargent, Steidel, and Boksenberg (1988), Boisse *et al.* (1992), Steidel and Sargent (1992), Aldcroft *et al.* (1993), Le Brun *et al.* (1993), Churchill *et al.* (1999), Nestor *et al.* (2005), Fox *et al.* (2006), Lynch *et al.* (2006), Nestor *et al.* (2006), York *et al.* (2006), and Narayanan *et al.* (2007). Surveys of C IV absorption systems were conducted by Sargent, Boksenberg, and Steidel (1988) and Misawa *et al.* (2002). Absorption features of O VI $\lambda\lambda 1032, 1038 \text{ \AA}$

are more difficult to identify since they lie within the Ly- α forest, and so are not easily distinguished from the forest. Searches have been successful, however, and have moreover discovered a second IGM environment. While at high redshifts the O VI systems probe the component of the IGM containing C VI (Burles and Tytler, 1996, 2002; Kirkman and Tytler, 1997b), at low redshifts they are associated with a warm-hot intergalactic medium (WHIM) (Tripp and Savage, 2000; Savage *et al.*, 2002; Richter *et al.*, 2004; Danforth and Shull, 2005, 2008; Tripp *et al.*, 2008) that is most likely collisionally ionized rather than photoionized. A search for O VI absorption systems as an indicator of a WHIM at high redshift was conducted by Simcoe *et al.* (2002). Efforts are currently under way to detect an intergalactic x-ray absorption line forest using the XMM Newton and Chandra x-ray satellites (Nicastro *et al.*, 2005; Kaastra *et al.*, 2006; Rasmussen *et al.*, 2007). Detections of low-redshift O VIII have been reported by Fang *et al.* (2002, 2007) and Williams *et al.* (2007).

Attempts to infer the origin of the metals, whether distributed by galactic outflows or introduced locally by Population III stars, have led to various efforts to estimate the range in ambient metallicities and to determine their spatial distribution (Bergeron and Stasinska, 1986; Bergeron *et al.*, 1994; Cowie *et al.*, 1995; Songaila and Cowie, 1996; Barlow and Tytler, 1998; Cowie and Songaila, 1998; Ellison *et al.*, 2000; Songaila, 2001, 2005, 2006; Aracil *et al.*, 2004; Pieri *et al.*, 2006; Scannapieco *et al.*, 2006b; Simcoe *et al.*, 2006). Updated solar abundances useful for modeling the abundances of the metal absorption systems are provided by Grevesse and Sauval (1998), Allende Prieto *et al.* (2001, 2002), Holweger (2001), and Asplund (2003). Early attempts to tease out weak metal features were based either on a spectral shift-and-stack approach to generate a high signal-to-noise ratio composite C IV line (Lu, Sarsent, *et al.*, 1998) or through a pixel-by-pixel statistical analysis of the spectra (Songaila and Cowie, 1996; Cowie and Songaila, 1998). A comparison of these two techniques is provided by Ellison *et al.* (2000).

An alternative is to perform long integrations of bright QSOs to obtain high-resolution high-signal-to-noise-ratio spectra. With signal-to-noise ratios of 200–300 per spectral resolution element, Simcoe *et al.* (2004) detected metal lines in 70% of the Ly- α forest systems. Absorption systems with H I column densities as low as $N_{\text{H I}} > 10^{14} \text{ cm}^{-2}$ show C IV features, while systems with $N_{\text{H I}} > 4 \times 10^{13} \text{ cm}^{-2}$ show O VI features. Although the inferred metallicities are model dependent (fixed in part by the assumed spectrum and intensity of the ionizing background), the measurements suggest metallicities as low as 3×10^{-4} that of the Sun. No evidence for a metallicity floor could be discovered. The metallicity distribution inferred is consistent with a log-normal distribution with a mean of 0.006 solar.

The mechanism and degree of metal mixing in the diffuse IGM are unclear. While the mixing of metals in stellar interiors by convection and diffusion may produce a homogeneous composition, preserved in super-

novae ejecta and winds, it is far from clear that the mixing of the ejecta will result in uniform metallicity. The mixing process is still poorly understood in the interstellar medium, and much more so in the IGM. Just as the stirring of a drop of milk in a cup of coffee will result in the mixing and intermingling of the two fluids, so will the stirring produced by dynamical instabilities such as the Kelvin-Helmholtz and Rayleigh-Taylor instabilities mix metal-enriched stellar ejecta with the surrounding primordial gas. Insufficient mixing, however, rather than producing a uniform mixture, will instead result in striations or patches of high-metallicity gas entrained within the primordial gas of essentially zero metallicity. Schaye *et al.* (2007) found evidence for just such inadequate mixing for diffuse absorption systems (with a median upper limit of 13.3 on $\log_{10} N_{\text{H I}}$), at $z \approx 2.3$. By combining C IV measurements with upper limits on H I, C III, Si II, Si III, N V, and O VI, they placed robust constraints on the metallicities and physical properties of the C IV absorption systems, with a median lower limit on the metallicities of $[C/H] > -0.42$ and a median upper limit on the absorber sizes of $R \lesssim 1.5 \text{ kpc}$. They obtained typical median lower and upper limits on the hydrogen densities of $n_{\text{H}} > 100 \text{ m}^{-3}$ and $n_{\text{H}} < 1000 \text{ m}^{-3}$, a range that suggests a cloud size of about 100 pc. The clouds, however, would likely be transient, either quickly dispersing if freely expanding or shorn apart by dynamical instabilities if moving relative to a confining medium, on a time scale of about 10^7 yr . Schaye *et al.* (2007) arrived at a picture in which new clouds are continuously created through dynamical or thermal instabilities. In this picture, nearly all metals in the IGM could be processed through just such a cloud phase. The dispersed clouds would retain their coherence as small patches, but of too low column density to be detectable. The resulting IGM metallicity would persist as patchy, not mixed.

Matching of the metal absorption lines to the corresponding H I Ly- α features frequently reveals multicomponent substructure obscured by the width of the Ly- α feature. An example from QSO 1422+231 is shown in Fig. 8. The C IV systems show evidence for spatial clustering on scales of up to $\sim 300 \text{ km s}^{-1}$ (Rauch *et al.*, 1996; Songaila and Cowie, 1996; D’Odorico *et al.*, 1998a; Pichon *et al.*, 2003). This is consistent with a 2σ lower limit of $\sim 30 \text{ kpc}$ for the clustering of C IV and Mg II systems obtained by Smette *et al.* (1995), based on a statistical analysis of coincident metal systems in neighboring lines of sight to a lensed QSO. An analysis of a triply imaged quasar at $z = 3.9$ by Ellison *et al.* (2004) showed that high-ionization systems such as C IV and Si IV absorbers retain coherence over scales of $\sim 100 \text{ kpc}$. By contrast, low-ionization systems such as Mg II and Fe II absorbers show coherence only over much smaller scales. Assuming a spherical geometry, they are estimated to have sizes of 1.5–4.4 kpc (95% confidence interval). Using similar measurements, Rauch *et al.* (2001) found C IV systems at $1.5 \lesssim z \lesssim 3$ are coherent over scales of about 300 pc, with column densities along neighboring lines of sight differing by 50% for separations of about 1 kpc.

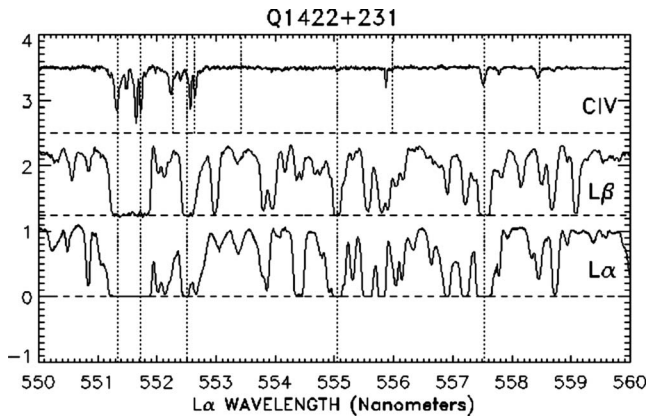


FIG. 8. Portion of the Ly- α forest in the spectrum of Q1422+231 at $z=3.6$ (lower panel) with the corresponding Ly- β systems (middle panel) and $\lambda 1548 \text{ \AA}$ systems of the C IV $\lambda\lambda 1548, 1551 \text{ \AA}$ doublet (upper panel) shifted to coincide. Absorption systems saturated in both Ly- α and Ly- β are indicated by the long vertical dotted lines. The short dotted lines show where the corresponding C IV $\lambda 1551 \text{ \AA}$ line should occur for these systems. From [Songaila and Cowie, 1996](#). Figure reproduced by permission of the American Astronomical Society.

Detectable levels of C IV extend over scales of several kiloparsecs.

Damped Ly- α absorbers show a wide range of metals with both low- and high-ionization states, including boron, carbon, nitrogen, oxygen, magnesium, aluminum, silicon, phosphorus, sulfur, chlorine, argon, titanium, chromium, manganese, iron, cobalt, nickel, copper, zinc, germanium, arsenic, and krypton ([Lu, Sargent, and Barlow, 1996](#); [Wolfe et al., 2005](#); [Dessauges-Zavadsky et al., 2006](#)). The metallicities evolve from about 0.03 solar at $z \approx 4$ to 0.15 solar at $z \approx 1$, with few above 0.3 solar ([Wolfe et al., 2005](#)). No DLA is found with a metallicity smaller than 0.0025 solar, distinguishing them as a population from the Ly- α forest. By contrast, super Lyman limit systems are found to have metallicities ranging from 0.1 solar to supersolar abundances with as much as five times solar in zinc ([Kulkarni et al., 2007](#)). As both these classes of systems are likely related to galaxies, further discussion of them is deferred to Sec. VIII.

The presence of the metal lines in absorbers of all H I column densities in principle offers an opportunity to obtain a nearly model-free measurement of the gas temperature. Allowing for kinetic broadening of the Doppler parameters following Eq. (11), the measurements of the Doppler parameters from features corresponding to two or more elements permit the thermal and kinematic broadening components to be separated. (In principle, instrumental broadening could be incorporated into the kinematic term.) Given total Doppler parameter measurements b_i and b_j for two species i and j of masses m_i and m_j , the temperature may be solved for as

$$T = \frac{m_i m_j (b_i^2 - b_j^2)}{2k_B (m_j - m_i)}. \quad (29)$$

Applying this method to C IV and Si IV features detected in three high-redshift QSOs, and assuming that the C IV and Si IV features trace the same systems with the same temperature and velocity structure, [Rauch et al. \(1996\)](#) obtained a typical temperature of $T \approx 38\,000 \text{ K}$ and typical kinetic motions of $b_{\text{kin}} \approx 6 \text{ km s}^{-1}$ for a select subsample of well-fitted features. The large C IV column densities of the systems [typically exceeding 10^{12} cm^{-2} ([Rauch, 2007](#))], suggest large H I column densities of $N_{\text{H I}} > 10^{15} \text{ cm}^{-2}$ ([Simcoe et al., 2004](#)).

A few other Ly- α systems selected for quiescent velocity fields as part of a program of deuterium abundance measurements yield somewhat cooler temperatures. The Doppler parameters of C IV and Si IV measured by [Kirkman et al. \(2000\)](#) in a system with $\log_{10} N_{\text{H I}} = 16.7$ yield a temperature of $T \approx 30\,000\text{--}32\,000 \text{ K}$. For a Lyman limit system with $\log_{10} N_{\text{H I}} = 17.1$ at $z = 0.7$ ([Tytler et al., 1999](#)), the Doppler parameter measured for Mg II compared with that of H I gives $T \approx 31\,000 \text{ K}$ and $b_{\text{kin}} \approx 13 \text{ km s}^{-1}$, assuming the hydrogen and metals sample the same velocity field, which is not an obvious assumption to make. For a super Lyman limit system with $\log_{10} N_{\text{H I}} = 19.42$, [O'Meara et al. \(2001\)](#) found from a simultaneous fit to O I, N I, and H I $T = 1.15 \pm 0.02 \times 10^4 \text{ K}$ and $b_{\text{kin}} = 2.56 \pm 0.12 \text{ km s}^{-1}$. In all cases, the temperatures obtained are consistent with photoionization-heated gas. Although direct gas density measurements are not possible, models generally suggest that higher-column-density systems correspond to higher densities, especially at these high values. The temperatures support the expected trend of decreasing temperature with increasing density for sufficiently dense absorption systems ([Meiksin, 1994](#)).

The small kinetic contributions to the line broadening are in contrast to what is found for He II absorption systems, which appear to be dominated by kinetic broadening ([Zheng, Kriss, et al., 2004](#)). The He II features, however, were chosen for their clear isolation in the spectrum, and so may probe physically underdense regions, in contrast to the higher-column-density systems discussed above. An attempt to estimate temperatures from a larger sample of He II and H I systems has not been able to produce secure values, but nonetheless shows that only $\sim 45\%$ of the lines are dominated by kinematic broadening ([Fechner and Reimers, 2007](#)).

Intergalactic metal absorption systems may be used to probe the time variability of fundamental physical quantities over cosmological timescales. The excitation of ionic fine structure levels by the CMB allows metal lines in the Ly- α forest to be exploited for measuring the evolution of the CMB temperature ([Bahcall and Wolf, 1968](#)). Because of the possible influence of other excitation mechanisms, the measurements are, strictly speaking, upper limits. Existing excitation temperature measurements are $T = 7.4 \pm 0.8 \text{ K}$ at $z = 1.776$ ([Songaila et al., 1994](#)), $T = 7.9 \pm 1.0 \text{ K}$ at $z = 1.9731$ ([Ge et al., 1997](#)), $T = 15.7 \pm 3.5 \text{ K}$ at $z = 2.34$ ([Ge et al., 2001](#)), and $T = 12.1^{+1.7}_{-3.2} \text{ K}$ (95% confidence interval) at $z = 3.025$ ([Mo-](#)

laro *et al.*, 2002). These values are all consistent with a linearly evolving CMB temperature of $T(z)=T_0(1+z)$, expected for a homogeneous and isotropic expanding universe, with $T_0=2.725$ K (Mather *et al.*, 1999).

Detected resonance line multiplets have been used to place constraints on the time variation of fundamental constants. Bahcall *et al.* (1967) used the fine structure wavelength splittings of the Si II lines near $\lambda 1260$ Å and $\lambda 1527$ Å and the Si IV lines near $\lambda 1394$ Å to show that the fine structure constant ($\alpha=[1/4\pi\epsilon_0]e^2/\hbar c$) varies by less than 5% between $z=0$ and 1.95. Tentative evidence for an evolving fine structure constant in the range $1 < z < 1.6$ of $\Delta\alpha/\alpha \approx (-1.9 \pm 0.5) \times 10^{-5}$ was reported by Webb *et al.* (1999) using measurements of Mg II and Fe II transitions. The value was later revised to $\Delta\alpha/\alpha \approx (-5.7 \pm 1.1) \times 10^{-6}$ over the redshift range $0.2 < z < 4.2$ (Murphy *et al.*, 2004), suggestive of a positive detection of a variation. There is by no means consensus on the detection. Chand *et al.* (2004) and Srianand *et al.* (2004) reported $\Delta\alpha/\alpha \approx (-0.6 \pm 0.6) \times 10^{-6}$ over the redshift range $0.4 < z < 2.3$. Their analysis method has been contested by Murphy *et al.* (2007, 2008), and defended by Srianand *et al.* (2007). In an independent effort using a modified technique designed to eliminate some systematics, Levshakov *et al.* (2007) obtained $\Delta\alpha/\alpha \approx (5.4 \pm 2.5) \times 10^{-6}$ between $z=0$ and 1.7. Inclusion of the hyperfine splitting of the hydrogen 21 cm line permits constraints on the variation of $x \equiv \alpha^2 g_p \mu$, where μ is the electron-to-proton mass ratio and g_p is the proton gyromagnetic ratio. The current best limits are, for a linear fit over the redshift range $0.2 < z < 2.4$, $\dot{x}/x \approx (-1.43 \pm 1.27) \times 10^{-15} \text{ yr}^{-1}$ (Tzanavaris *et al.*, 2005). Combining H I 21 cm data and OH 18 cm data, Kanekar *et al.* (2005) obtained a limit on the effective combination $F \equiv g_p(\alpha^2/\mu)^{1.57}$ of $\Delta F/F \approx (0.44 \pm 0.36^{\text{stat}} \pm 1.0^{\text{sys}}) \times 10^{-5}$ between $z=0$ and $z \approx 0.7$.

C. Direct flux statistics

While the absorption line parameters relate most directly to the physical characteristics of the absorption systems, measuring similar parameters in numerical simulations can be computationally demanding, particularly when building up sufficient statistics to make such a comparison meaningful. More straightforward comparisons may be made using the flux statistics directly. The statistical measures in most use are the mean transmitted flux, the transmitted flux per pixel probability distribution, the flux power spectrum and its Fourier transform, and the flux autocorrelation function. An additional analysis based on wavelets permits a quick means of gauging the distribution of widths of the absorption features.

1. Mean transmitted flux

By far the simplest statistic is the mean transmitted flux through the IGM. Oke and Korycansky (1982) introduced two measurements, D_A , the mean flux of a

background source removed by scattering between the Ly- α and Ly- β transitions in the rest frame of the QSO (but avoiding emission line wings), and D_B , the mean flux removed between Ly- β and the Lyman edge. These definitions are straightforwardly generalized to the fraction of flux removed between each successive pair of Lyman transitions. Removing the effect on higher orders by lower orders, however, is not straightforward but may be accomplished in a statistical sense (Press *et al.*, 1993). The measurement D_A may be evaluated as $D_A = (1 - \langle f_i/c_i \rangle)$, where f_i is the measured flux in pixel i , c_i is the corresponding predicted continuum of the background object, normally a QSO, and the average is carried out over a given wavelength (or corresponding redshift) interval between Ly- α and Ly- β in the rest frame of the QSO. Considerable care must be taken in measuring the contribution at a given redshift from Ly- α alone. Systematics that would bias the result if not corrected for include (1) a low H I fraction near the QSO due to its own ionizing intensity (the ‘‘proximity effect’’); (2) contamination by metal absorption systems; (3) the large stochastic influence of Lyman limit systems and damped Ly- α absorbers, the latter of which produce a divergent mean (Meiksin and White, 2004); and (4) evolution of the absorption in the region measured, including over individual pixels of the spectrum. A detailed discussion is provided by Tytler, Kirkman, *et al.* (2004).

For a spectrum that may be decomposed into individual absorption features with equivalent widths $w(\mathbf{x})$ depending on some set of parameters \mathbf{x} , such as column density or Doppler parameter, the mean of the transmitted flux $\mathcal{T}_\nu \equiv \exp(-\tau_\nu)$ is given by

$$\langle \mathcal{T}_\nu \rangle = \langle \exp(-\tau_\nu) \rangle = \exp(-\tau_l), \quad (30)$$

with the effective optical depth τ_l due to the lines given by

$$\tau_l = \int d\mathbf{x} w(\mathbf{x}) \frac{d\mathcal{N}(\mathbf{x})}{d\lambda} = \frac{1+z}{\lambda_0} \int dw \frac{\partial^2 \mathcal{N}}{\partial w \partial z} w, \quad (31)$$

where $d\mathcal{N}(\mathbf{x})/d\lambda$ is the number of systems per unit rest wavelength per unit volume $d\mathbf{x}$ in parameter space (Spitzer, 1948; Press *et al.*, 1993), here represented in terms of the number per (proper) equivalent width per unit redshift $\partial^2 \mathcal{N}/\partial w \partial z$. The variance $\langle \mathcal{T}^2 \rangle - \langle \mathcal{T} \rangle^2$ of the transmission depends on the details of the line profiles. Expressions for idealized examples are provided by Munch (1968) and Press *et al.* (1993).

It is instructive to consider a comparison between Eq. (31) and the Gunn-Peterson optical depth (15). Using Eq. (27) for the number density evolution given by $dN/dz = \int dw \partial^2 \mathcal{N}/\partial w \partial z$ and Eq. (24) for systems on the linear part of the curve of growth, τ_l may be recast in the form of the Gunn-Peterson optical depth

$$\tau_l = \frac{3}{8\pi} \frac{\lambda_{lu}^3 \Gamma_{ul} \langle n(z) \rangle}{H(z)}, \quad (32)$$

for a mean distributed scattering gas density $\langle n(z) \rangle = n_a(z) \sigma_a(z) \bar{N}(z) = Q_a(z) \bar{n}(z)$, where $\bar{N} = \bar{n}L$ is the mean

column density of the absorption systems with mean atomic density \bar{n} and line-of-sight thickness L , and $Q_a = n_a \sigma_a L$ is the porosity of the absorbers, equivalent to the spatial filling factor of the absorption systems for $Q_a < 1$. For a column density distribution varying like $dN/dN_{\text{HI}} \propto N_{\text{HI}}^{-1.5}$, the effective absorber optical depth (excluding DLAs) is dominated by saturated systems, with $F(\tau_0) \approx 1-2$. In this case, Eq. (21) gives $w/\lambda_0 = 2(b/c)F(\tau_0) \approx 3b/c$. If the absorber velocity widths scale like the Hubble expansion across them, $b \approx fHL$, Eq. (31) gives instead of Eq. (32)

$$\tau_l \approx 2Q_a(z)f(z)F(\tau_0) \approx 3Q_a(z)f(z). \quad (33)$$

In practice, the effective optical depth will scale somewhat between the linear and saturated line limits. It will not in general scale like the Gunn-Peterson optical depth Eq. (15), as is often asserted in the literature. For $dN/dz \propto (1+z)^\gamma$, Eq. (31), instead gives the dependence $\tau_l \propto (1+z)^{1+\gamma}$. This is corroborated by estimates of the mean H I transmission due to Ly- α scattering from all components, whether or not they may be modeled as individual Voigt profile absorption systems. More generally, the mean transmission may be expressed as

$$\langle T \rangle \equiv \exp(-\tau_{\text{eff}}). \quad (34)$$

From an analysis of Ly- α scattering by the IGM in the redshift range $2.5 < z < 4.3$ using moderate resolution spectra, Press *et al.* (1993) obtained $\tau_{\text{eff}} = A(1+z)^{1+\gamma}$ with $A = 0.0175 - 0.0056\gamma \pm 0.0002$ and $\gamma = 2.46 \pm 0.37$. The evolution exponent γ agrees closely with the finding of Kim, Carswell, *et al.* (2002) for dN/dz given above. A similar result was obtained by Kim *et al.* (2001) using high-resolution spectra: $A = 0.0144 - 0.00471\gamma$ and $\gamma = 2.43 \pm 0.17$ [as inferred by Meiksin and White (2004)]. Kim, Carswell, *et al.* (2002) gave the slight variation based on an expanded data set of $A = 0.0032 \pm 0.0009$ and $\gamma = 2.37 \pm 0.20$. Because the implied probability distribution for $\langle T \rangle$ is skewed, the statistical expectation value for the mean transmission must be computed from these expressions for τ_{eff} using Monte Carlo integration (Meiksin and White, 2004). A good fit to the evolution of τ_{eff} based on the data compiled by Meiksin and White (2004), extended to lower redshifts using the data of Kirkman *et al.* (2007), is given by

$$\tau_{\text{eff}} = \begin{cases} 0.0164(1+z)^{1.1}, & 0 < z < 1.2 \\ 0.00211(1+z)^{3.7}, & 1.2 < z < 4 \\ 0.00058(1+z)^{4.5}, & 4 < z < 5.5 \end{cases} \quad (35)$$

(Meiksin, 2006a). The evolution is found to vary from relatively slow at low redshifts, as expected for discrete saturated features, to the more rapid evolution of the Gunn-Peterson effect at high redshifts, as the porosity of the absorption systems approaches unity and increasingly diffuse gas dominates the effective optical depth.

A dip in the evolution of τ_{eff} at $z \approx 3.2$ was reported by Bernardi *et al.* (2003) based on a sample of 1061 moderate-resolution QSO spectra measured by the SDSS. The feature was interpreted as evidence for sud-

den heating due to the onset of He II reionization. This interpretation is not supported by recent simulations (McQuinn *et al.*, 2009). The feature was not confirmed by McDonald *et al.* (2006) using an alternative analysis method applied to 3035 SDSS QSO spectra. Using a sample of 86 high-resolution high-signal-to-noise-ratio spectra, however, Faucher-Giguère, Prochaska, *et al.* (2008) found a feature similar to that reported by Bernardi *et al.* (2003). The existence of the feature appears still not to be entirely secure, but tentatively suggests that a physical change in the state of the IGM occurred at $z \approx 3.2$, possibly reflecting a change in the H I ionization rate, perhaps owing to the growing influence of QSOs (Sec. IV.A.2).

2. Statistics based on pixel fluxes

More detailed transmission information may be extracted from the use of the full spectrum, including the probability distribution of the transmission per pixel, the flux power spectrum, the autocorrelation function of the transmission, and a wavelet decomposition. Because these statistical measures are best interpreted in conjunction with numerical simulations, they are discussed in more detail in Sec. VI. Here they are only defined.

The pixel transmission distribution (PTD) and its variants, such as the transmission flux probability distribution function (TFPDF) (McDonald *et al.*, 2000), simply quantify the frequency of occurrence of a given flux value in each pixel of the spectrum, normalized by the continuum, often expressed in frequency bins. It was introduced by Jenkins and Ostriker (1991) to search for underlying intergalactic absorption in excess of the amount accounted for by discrete absorption systems. Several tabulations are available in the literature: Rauch, Miralda-Escud *et al.* (1997), McDonald *et al.* (2000), Becker *et al.* (2007), Desjacques *et al.* (2007), and Kirkman *et al.* (2007).

Second-order statistics include the flux autocorrelation function and the flux power spectrum, in analogy to similar statistical descriptions of the clustering of galaxies. The flux transmission autocorrelation function was introduced by Zuo and Bond (1994) to investigate properties of the Ly- α forest. For a velocity separation v , it is defined by

$$\xi_F(v) = \langle f(v')f(v'-v) \rangle / \langle f \rangle^2 - 1, \quad (36)$$

where $f(v)$ denotes the pixel flux at velocity v , and $\langle f \rangle$ is the measured mean flux at the relevant redshift.¹³ Sev-

¹³This differs somewhat from the definition of Zuo and Bond (1994), who in place of $\langle f \rangle^2$ in the denominator used the more general form $\langle f(v') \rangle \langle f(v) \rangle$. In most of the literature, it is assumed the mean flux changes negligibly over the velocity separations for which it is computed. This will break down for velocity separations sufficiently large that cosmological expansion becomes a factor, but in this case the physical interpretation of the autocorrelation function becomes less transparent as it would correlate transmissions at different cosmological epochs.

eral estimates of ξ_F are provided by Zuo and Bond (1994), Liske *et al.* (2000), McDonald *et al.* (2000, 2006), Croft, Weinberg, *et al.* (2002), Becker *et al.* (2004), D'Odorico *et al.* (2006), and Kirkman *et al.* (2007). The results generally show significant correlations over scales of a few megaparsecs (comoving). Similar to the flux autocorrelation function is the flux cross-correlation function along neighboring lines of sight to QSOs near each other on the sky (Liske *et al.*, 2000; Becker *et al.*, 2004; D'Odorico *et al.*, 2006). Cross correlations of similar strength to the autocorrelations are found, extending over similar spatial scales.

The flux power spectrum has received considerable attention as a means of constraining cosmological parameters (Croft *et al.*, 1998; Hui *et al.*, 2001). It is a measure of the variance in the amplitude of the Fourier transform coefficients of the transmitted flux. Defining $\delta f = f - \langle f \rangle$ and its Fourier transform

$$\widehat{\delta f}(k) = \frac{1}{\Delta v} \int_{-\Delta v/2}^{\Delta v/2} dv \delta f(v) e^{ikv}, \quad (37)$$

over the velocity interval Δv , the flux power spectrum is

$$P_F(k) = (\Delta v) \langle |\widehat{\delta f}|^2 \rangle / \langle f \rangle^2. \quad (38)$$

The dimensionless form $kP_F(k)/\pi$ is often more convenient. It forms a Fourier transform pair with the flux autocorrelation function through

$$\frac{kP_F(k)}{\pi} = \frac{k}{\pi} \int_{-\Delta v/2}^{\Delta v/2} dv \xi_F(v) e^{ikv}. \quad (39)$$

The reader should be aware that several different conventions for $P_F(k)$ exist in the literature, some without a mean flux normalization, some differing by a factor of 2π , and some referring to an effective three-dimensional (3D) flux power spectrum extracted from the one-dimensional (1D) flux power spectrum in a manner analogous to the relation between the 1D and 3D mass power spectra. Many tabulations of $P_F(k)$ are available: Croft *et al.* (1998, 1999), McDonald *et al.* (2000), Croft, Weinberg, *et al.* (2002), and Kim *et al.* (2004a, 2004b). A substantial effort was made to measure $P_F(k)$ from the spectra of high-redshift quasars discovered by the Sloan digital sky survey (McDonald *et al.*, 2006).

A shortcoming of the Fourier transform is that it loses spatial information. In the case of a spectrum showing the Ly- α forest, the positions of individual absorption features are lost. A wavelet transform is analogous to a Fourier transform, but retains local information, giving in effect a description of the power on different scales as a function of position. A wavelet is a square-integrable function $\psi(x)$ defined in real space such that $\psi_{jk} \equiv 2^{j/2} \psi(2^j x - k)$ (where j and k are integers) forms an orthonormal basis for the set of square-integrable functions. It satisfies $\int_{-\infty}^{\infty} dx \psi(x) = 0$, and is normally concentrated near $x = k2^{-j}$. The wavelet coefficients are defined by $w_{jk} = \int dx f(x) \psi_{jk}(x)$; the original function may be recovered through $f(x) = \sum_{j,k} w_{jk} \psi_{jk}(x)$. The wavelet transform effects a localized multiscale rendition of the data.

Although not commonly used, wavelets are in principle a powerful tool for analyzing the Ly- α forest, producing a statistical description similar to the distribution of b values. The discrete wavelet transform, like the fast Fourier transform, may be computed rapidly, permitting a large number of spectra to be analyzed much more quickly than by performing a full absorption line analysis. This is an advantage over full Voigt profile line fitting for assessing the match of simulations to observations (Meiksin, 2000; Theuns and Zaroubi, 2000; Meiksin and White, 2001; Meiksin *et al.*, 2001; Theuns, Schaye, *et al.*, 2002; Zaldarriaga, 2002).

III. IONIZATION EQUILIBRIUM

A. Ionization

1. Hydrogen and helium

The absorption signatures of the IGM are produced by atoms and ions with bound electrons, through either resonance scattering or photoelectric absorption. The amount of scattering or absorption depends on the ionization structure of the IGM. In this section, the photoionization of hydrogen and helium is discussed. In hot environments such as galaxy clusters, collisional ionization can dominate. Collisional ionization equilibrium may play a particularly important role in the physics of the WHIM (Cen and Ostriker, 1999, 2006; Davé *et al.*, 1999, 2001) and is treated more generally in the section on metal ionization.

Photons with energies exceeding the ionization potential of a bound electron in a hydrogen atom will ionize the neutral hydrogen atoms in the IGM at the rate per neutral atom

$$\Gamma_{\text{H I}} = c \int_{\nu_T}^{\infty} d\nu \frac{u_\nu}{h\nu} a_\nu^{\text{H I}}, \quad (40)$$

where $a_\nu^{\text{H I}}$ is the hydrogen photoelectric cross section, ν_T is the threshold frequency required to ionize hydrogen (the Lyman limit), and u_ν is the specific energy density of the ambient radiation field. The specific energy density is related to the specific intensity of the radiation field $I_\nu(\mathbf{r}, t, \hat{\mathbf{n}})$ by $u_\nu = 4\pi J_\nu / c$, where $J_\nu(\mathbf{r}, t) = (1/4\pi) \oint d\Omega I_\nu(\mathbf{r}, t, \hat{\mathbf{n}})$ is the angle-averaged specific intensity.

Free electrons will be radiatively captured by protons at the rate per proton $n_e \alpha_{\text{H II}}(T)$, where $\alpha_{\text{H II}}$, often referred to as the case A radiative recombination coefficient $\alpha_A(T)$, is the total rate coefficient for radiative capture summed over recombinations to all energy levels. Expressed in terms of the ionization fractions $x_{\text{H I}} = n_{\text{H I}}/n_{\text{H}}$ and $x_{\text{H II}} = n_{\text{H II}}/n_{\text{H}}$, where $n_{\text{H}} = n_{\text{H I}} + n_{\text{H II}}$ is the total hydrogen number density, the ionization rate equations become

$$dx_{\text{H I}}/dt = -x_{\text{H I}} \Gamma_{\text{H I}} + x_{\text{H II}} n_e \alpha_A(T),$$

TABLE III. Case A recombination [α_i ($\text{m}^3 \text{s}^{-1}$)] and recombination cooling [β_i ($\text{J m}^3 \text{s}^{-1}$)] coefficients.

$\alpha_{\text{H II}}$	$2.065 \times 10^{-17} T^{-1/2} \left(6.414 - \frac{1}{2} \ln T + 8.68 \times 10^{-3} T^{1/3} \right)$
$\alpha_{\text{He II}}$	$3.294 \times 10^{-17} \left\{ \left(\frac{T}{15.54} \right)^{1/2} \left[1 + \left(\frac{T}{15.54} \right)^{1/2} \right]^{0.309} \left[1 + \left(\frac{T}{3.676 \times 10^7} \right)^{1/2} \right]^{1.691} \right\}^{-1} + 1.9 \times 10^{-9} (1 + 0.3e^{-9.4 \times 10^4/T}) e^{-4.7 \times 10^5/T} T^{-3/2}$
$\alpha_{\text{He III}}$	$8.260 \times 10^{-17} T^{-1/2} \left(7.107 - \frac{1}{2} \ln T + 5.47 \times 10^{-3} T^{1/3} \right)$
$\beta_{\text{H II}}$	$2.851 \times 10^{-40} T^{1/2} \left(5.914 - \frac{1}{2} \ln T + 0.01184 T^{1/3} \right)$
$\beta_{\text{He II}}$	$1.55 \times 10^{-39} T^{0.3647} + 1.24 \times 10^{-26} (1 + 0.3e^{-9.4 \times 10^4/T}) e^{-4.7 \times 10^5/T} T^{-3/2}$
$\beta_{\text{He III}}$	$1.140 \times 10^{-39} T^{1/2} \left(6.607 - \frac{1}{2} \ln T + 7.459 \times 10^{-3} T^{1/3} \right)$

$$dx_{\text{H II}}/dt = -dx_{\text{H I}}/dt. \quad (41)$$

The time derivatives are Lagrangian so that Eqs. (41) are valid in the presence of velocity flows.

In equilibrium, the neutral fraction will be

$$x_{\text{H I}}^{\text{eq}} = n_e \alpha_A(T) / [\Gamma_{\text{H I}} + n_e \alpha_A(T)]. \quad (42)$$

For a pure hydrogen gas, $n_e = n_{\text{H II}}$, and the rate equation for $x_{\text{H I}}$ becomes

$$dx_{\text{H I}}/dt - t_{\text{rec}}^{-1} x_{\text{H I}}^2 + (\Gamma_{\text{H I}} + 2t_{\text{rec}}^{-1}) x_{\text{H I}} - t_{\text{rec}}^{-1} = 0, \quad (43)$$

where $t_{\text{rec}} = 1/n_e \alpha_A$ is the total radiative recombination time for the gas. The equilibrium neutral fraction may be expressed as

$$x_{\text{H I}}^{\text{eq}} = \left(\frac{1}{2} \phi + 1 \right) - \left[\left(\frac{1}{2} \phi + 1 \right)^2 - 1 \right]^{1/2}, \quad (44)$$

where $\phi = \Gamma_{\text{H I}} t_{\text{rec}}$ denotes the number of photoionizations per neutral atom over a recombination time. It is instructive to consider the case of constant ϕ . Equation (43) then has the general solution

$$x_{\text{H I}} = x_{\text{H I}}^{\text{eq}} - \frac{\eta}{(1 - \delta_0^{-1} \eta) \exp(\eta \tau) - 1}, \quad (45)$$

where $\eta = \phi + 2 - x_{\text{H I}}^{\text{eq}}$, $\tau = t/t_{\text{rec}}$, and $\delta_0 = x_{\text{H I}}(0) - x_{\text{H I}}^{\text{eq}}$ is the initial deviation of the neutral hydrogen fraction from its equilibrium value. For a fast photoionization rate ($\phi \gg 1$), $x_{\text{H I}}^{\text{eq}} \approx \phi^{-1} \ll 1$ and $x_{\text{H I}} \approx x_{\text{H I}}^{\text{eq}} + \delta_0 \exp(-\Gamma_{\text{H I}} t)$. An initial deviation δ_0 from equilibrium decays exponentially. The neutral fraction approaches its equilibrium value on the photoionization rate time scale $\Gamma_{\text{H I}}^{-1}$, regardless of whether equilibrium is established through net photoionizations or net recombinations. Ionization equilibrium will be maintained provided any change to the gas (such as source variability or the expansion of the gas) occurs on a time scale long compared with the photoionization time scale. By contrast, for a slow photoionization rate $\phi \ll 1$, $x_{\text{H I}}^{\text{eq}} \approx 1$ and the neutral fraction approaches equilibrium on the recombination time scale, $x_{\text{H I}} \approx 1 + \delta_0 \exp(-t/t_{\text{rec}})$ for $|\delta_0| \ll 1$ ($\delta_0 < 0$).

The photoionization equations for helium are analogous to Eqs. (41). Denoting the respective He I, He II, and He III, fractions by $x_{\text{He I}}$, $x_{\text{He II}}$, and $x_{\text{He III}}$, they are given by

$$dx_{\text{He I}}/dt = -x_{\text{He I}} \Gamma_{\text{He I}} + x_{\text{He II}} n_e \alpha_{\text{He II}},$$

$$dx_{\text{He II}}/dt = -dx_{\text{He I}}/dt - dx_{\text{He III}}/dt,$$

$$dx_{\text{He III}}/dt = x_{\text{He II}} \Gamma_{\text{He II}} - x_{\text{He III}} n_e \alpha_{\text{He III}}, \quad (46)$$

where $\alpha_{\text{He II}}$ and $\alpha_{\text{He III}}$ are the total recombination rates to all levels of He I and He II, respectively, and $\Gamma_{\text{He I}}$ and $\Gamma_{\text{He II}}$ are the respective photoionization rates. The total electron density is $n_e = n_{\text{H II}} + n_{\text{He II}} + 2n_{\text{He III}}$.

The Case A radiative recombination coefficient for hydrogenic ions is provided by [Seaton \(1959\)](#), from which the coefficients for $\alpha_{\text{H II}}(T)$ and $\alpha_{\text{He III}}(T)$ may be derived. [In general, the radiative recombination coefficient $\alpha_Z(T)$ for a hydrogenic ion of atomic number Z is related to that of hydrogen by $\alpha_Z(T) = Z \alpha_{\text{H II}}(T/Z^2)$.] For elements He and beyond, the recombination coefficient is the sum of two rates. One is the usual radiative capture term, in which $e^- + X^{n+1} \rightarrow X^n + \gamma$ for a species X with n electrons. The other arises from dielectronic recombination, in which a fast incoming electron excites an ion, which becomes trapped in a weakly bound autoionizing state upon capturing the electron, then decays by the emission of a resonance line photon: $e^- + X^{n+1} \rightarrow X^{n*} \rightarrow X^n + h\nu_{ul}$. The probability for emission of the photon is suppressed by the factor $\exp(-h\nu_{ul}/k_B T)$; usually excitation is followed by the reverse reaction. A form for the radiative recombination rate coefficient contribution to $\alpha_{\text{He II}}(T)$ for $\text{He II} \rightarrow \text{He I}$ is provided by [Verner and Ferland \(1996\)](#), while a form for the dielectronic term is provided by [Aldrovandi and Pequignot \(1973\)](#). The recombination coefficients are listed in [Table III](#). Recombination to He I may also occur through charge transfer, $\text{He}^+ + \text{H}^0 \rightarrow \text{He}^0 + \text{H}^+ + \Delta E$, where ΔE is the energy defect. Where hydrogen is highly ionized, this is a negligible effect compared with radiative recombinations. For partially ionized hydrogen, however, as,

TABLE IV. Ionization cross-section parameters used in Eq. (48). From [Osterbrock, 1989](#).

	a_T (m ²)	ν_T (Hz)	β	s
$a_{\text{H I}}$	6.30×10^{-22}	3.282×10^{15}	1.34	2.99
$a_{\text{He I}}$	7.83×10^{-22}	5.933×10^{15}	1.66	2.05
$a_{\text{He II}}$	1.58×10^{-22}	1.313×10^{16}	1.34	2.99

for example, within a damped Ly- α absorber, or the IGM prior to its complete reionization, the effect may play an important role. The rate coefficient is provided by [Kingdon and Ferland \(1996\)](#). The reverse process, charge transfer ionization, is suppressed by a Boltzmann factor and so is normally negligible except at high temperatures.

The exact photoionization cross section for hydrogenic atoms with atomic number Z in the ground state is ([Heitler, 1954](#))

$$a_Z(\nu) = \frac{A_0}{Z^2} \left(\frac{\nu_T}{\nu} \right)^4 \frac{e^{4-(4 \tan^{-1} \epsilon)/\epsilon}}{1 - e^{-2\pi\epsilon}}, \quad (47)$$

for $h_p \nu > h_p \nu_T = 13.60 Z^2$ eV, the threshold energy for ionization, and where $A_0 = (2^9 \pi / 3 e^4) \alpha \pi a_0^2 = 6.30 \times 10^{-22}$ m², $a_0 = [4\pi\epsilon_0] \hbar^2 / m_e e^2$ is the Bohr radius, $\alpha = [1/4\pi\epsilon_0] (e^2 / \hbar c)$ is the fine structure constant, and $\epsilon = (\nu / \nu_T - 1)^{1/2}$. For most practical applications, however, an approximate form is preferred. The ionization cross sections are well approximated by the form given by [Osterbrock \(1989\)](#),

$$a(\nu) = a_T \left[\beta \left(\frac{\nu}{\nu_T} \right)^{-s} + (1 - \beta) \left(\frac{\nu}{\nu_T} \right)^{-s-1} \right]. \quad (48)$$

The parameters for hydrogen and helium are listed in Table IV. For results requiring very high accuracy, more precise fits to the photoionization cross sections are provided by [Verner et al. \(1996\)](#), including results for an exhaustive list of metals.

2. Metals

The large number of ionization states of metals results in more complex processes involved in their photoionization. These include autoionization and Auger electron production in addition to dielectronic recombination. In an autoionization, an excited ion with one or two electrons lying in the photoionization continuum is produced following a photoionization event in which a deep shell electron is ejected. The excited ion spontaneously ionizes through a radiationless transition and the ejection of multiple Auger electrons. Although there has been considerable progress in accurate estimates of the relevant rate coefficients, many remain poorly determined either experimentally or theoretically, requiring interpolation (and sometimes extrapolation) from coefficients known for related species ([Ferland and Savin, 2001](#)). These uncertainties can affect the predicted metal abundances in the absorption systems. The effect of un-

certainty in the dielectronic recombination rates on commonly measured metal features is discussed by [Savin \(2000\)](#). Some of the methods of approximation are described in the literature for the rate coefficients.

Sophisticated computer codes have been developed to solve for the equilibrium ionization states. A widely used code is CLOUDY ([Ferland et al., 1998](#)), which solves the radiative transfer problem for plane-parallel and spherical geometries. The photoionization of intervening absorption systems has been described by [Verner and Iakovlev \(1990\)](#), whose formulation is followed here.

Denote by x_{ij} the fraction of a particular element i in the j th ionization state so that j runs from 1 (neutral) to Z_i+1 (fully ionized) for an element of atomic number Z_i . Then $\sum_{j=1}^{Z_i+1} x_{ij} = 1$. The general rate equation for x_{ij} is

$$\begin{aligned} \frac{dx_{ij}}{dt} = & -x_{ij} \left(n_e (c_{ij} + a_{ij} + r_{ij-1} + d_{ij-1}) + p_{ij} + n_{\text{H II}} c_{ij}^{\text{H}} \right. \\ & \left. + n_{\text{He II}} c_{ij}^{\text{He}} + \sum_{k=j+2}^{Z_i+1} q_{ijk} + n_{\text{H I}} r_{i,j-1}^{\text{H}} + n_{\text{He I}} r_{i,j-1}^{\text{He}} \right) \\ & + x_{ij+1} [n_e (r_{ij} + d_{ij}) + n_{\text{H I}} r_{ij}^{\text{H}} + n_{\text{He I}} r_{ij}^{\text{He}}] \\ & + x_{ij-1} [n_e (c_{ij-1} + a_{ij-1}) + p_{ij-1} + n_{\text{H II}} c_{ij-1}^{\text{H}} \\ & \left. + n_{\text{He II}} c_{ij-1}^{\text{He}} \right] + \sum_{l=1}^{j-2} x_{il} q_{ilj}, \end{aligned} \quad (49)$$

where c_{ij} is the collisional ionization rate ([Voronov, 1997](#)), a_{ij} is the autoionization rate ([Arnaud and Rothenflug, 1985](#)), p_{ij} is the photoionization rate without positionization Auger-electron ejection ([Verner and Yakovlev, 1995](#); [Verner et al., 1996](#)), r_{ij} is the radiative recombination rate ([Aldrovandi and Pequignot, 1973](#); [Shull and van Steenberg, 1982a, 1982b](#); [Arnaud and Rothenflug, 1985](#); [Verner and Ferland, 1996](#)), d_{ij} is the dielectronic recombination rate ([Nussbaumer and Storey, 1983, 1986, 1987](#)), c_{ij}^{H} is the rate of charge transfer ionization with H II ([Kingdon and Ferland 1996](#)), c_{ij}^{He} is the rate of charge transfer ionization with He II ([Arnaud and Rothenflug, 1985](#)), r_{ij}^{H} is the rate of charge transfer recombination with H I ([Kingdon and Ferland, 1996](#)), and r_{ij}^{He} is the rate of charge transfer recombination with He I ([Arnaud and Rothenflug, 1985](#)). Photoionization from deep shells followed by Auger-electron ejection, resulting in a change from an initial ionization state j to a final state $k \geq j+2$, occurs at the rate q_{ijk} ([Kaastra and Mewe, 1993](#)). The convention that r_{ij} corresponds to recombination to ionization state j and c_{ij} corresponds to collisional ionization of state j is used. Because of the low metallicity of the IGM, the electron density may normally be well approximated by the electrons lost only by hydrogen and helium.

Using the above notation for the various species and taking $i=1$ for hydrogen and $i=2$ for helium, Eqs. (41) and (46) are modified, allowing for collisional ionization and charge transfer reactions, to

$$\begin{aligned} \frac{dx_{11}}{dt} &= -x_{11} \left(p_{11} + n_e c_{11} + \sum_{i \neq 1} \sum_{j=2}^{Z_i+1} r_{ij-1}^H n_{ij} \right) \\ &\quad + x_{12} \left(n_e r_{11} + \sum_{i \neq 1} \sum_{j=1}^{Z_i} c_{ij}^H n_{ij} \right), \\ \frac{dx_{12}}{dt} &= -\frac{dx_{11}}{dt}, \\ \frac{dx_{21}}{dt} &= -x_{21} \left(p_{21} + n_e (c_{21} + a_{21}) + q_{213} \right. \\ &\quad \left. + \sum_{i \neq 2} \sum_{j=2}^{Z_i+1} n_{ij} r_{ij-1}^{\text{He}} \right) \\ &\quad + x_{22} \left(n_e (r_{21} + d_{21}) + \sum_{i \neq 2} \sum_{j=1}^{Z_i} n_{ij} c_{ij}^{\text{He}} \right), \\ \frac{dx_{22}}{dt} &= -\frac{dx_{21}}{dt} - \frac{dx_{23}}{dt}, \\ \frac{dx_{23}}{dt} &= -x_{23} [n_e (r_{22} + d_{22}) + n_{11} r_{22}^H] + x_{21} q_{213} \\ &\quad + x_{22} [n_e (c_{22} + a_{22}) + p_{22} + n_{12} c_{22}^H], \end{aligned} \quad (50)$$

where the first sum of the double sums is over all elements except the excluded one indicated.

By noting that the photoionization rates are proportional to the energy density of the radiation field, it follows from the structure of Eqs. (49) and (50) that the equilibrium fractions are determined by the ratio $U = n_\gamma/n_H$ for a given spectral shape of the radiation field with photon number density n_γ , and for a given set of elemental abundances. The ratio U is known as the *ionization parameter*. Larger values for U generally produce higher ionization stages in the metals, although these also depend on the spectral shape of the radiation field. Comparisons with measured ion column densities may then be used to constrain the nature of the radiation field and absorption systems.

Fitting formulas for collisional ionization, radiative recombination, and dielectronic recombination rate coefficients were provided by Shull and van Steenberg (1982a). Improved values for many of these rates have since then become available, and are referenced above. Power-law fits to collisional and radiative recombination rates involving hydrogen and helium were provided by Abel *et al.* (1997). Fitting formulas to more recent rates for the elements hydrogen through nickel were provided by Mazzotta *et al.* (1998), along with equilibrium ionization fractions for metals in a hot environment, for which collisional ionization will normally dominate photoionization. A comprehensive compilation is available at D. Verner's "Atomic Data for Astrophysics" website,¹⁴ as

¹⁴<http://www.pa.uky.edu/~verner/atom.html>

described in Ferland *et al.* (1998). Since then, improved estimates have been obtained for some rates, including laboratory-measured values of dielectronic recombination rates [Savin *et al.* (2006), and references therein]. A comprehensive review of the atomic physics relevant to x-ray lines, as will arise from a warm-hot IGM, is provided by Kallman and Palmeri (2007).

B. Thermal equilibrium

In the presence of heat transfer at the rate $(G-L)/n$ per particle, where G and L are the thermal gain and loss functions per volume and n is the particle density, the second law of thermodynamics requires the entropy per particle s to change at the rate

$$ds/dt = (G-L)/nT, \quad (51)$$

where T is the temperature of the system. For an ideal gas, the entropy per particle is $s = (\gamma-1)^{-1} k_B \ln(p/\rho^\gamma) + s_0$, where p is the gas pressure, ρ is the mass density, γ is the ratio of specific heats at constant pressure to constant volume ($\gamma=5/3$ for a monatomic gas), k_B is Boltzmann's constant, and s_0 is an arbitrary additive constant. For numerical computations, it is often useful to express the energy equation in its entropic form Eq. (51), but through the entropy parameter

$$S_E \equiv p/\rho^\gamma. \quad (52)$$

It follows from Eq. (51) that

$$dS_E/dt = (\gamma-1)\rho^{-\gamma}(G-L). \quad (53)$$

The gas temperature is related to S_E by

$$T = (\bar{m}/k_B) S_E \rho^{\gamma-1}, \quad (54)$$

where \bar{m} is the mean mass per particle.

Photoionization will provide heat through the excess energy absorbed by an electron above the threshold energy $h_P \nu_T$ required to ionize a given atom. For a single species i of density n_i , the photoionization heating rate is

$$G_i = n_i c \int_{\nu_T^i}^{\infty} \frac{d\nu}{\nu} u_\nu \sigma_i(\nu) (\nu - \nu_T^i), \quad (55)$$

where $h_P \nu_T^i$ is the ionization potential of species i . The total heating rate from all species is

$$G = G_{\text{H I}} + G_{\text{He I}} + G_{\text{He II}}. \quad (56)$$

The contribution due to the photoionization of the metals is normally negligible because of their low abundances.

Cooling is provided by recombinations, collisional excitation of the excited levels in neutral hydrogen, and inverse Compton scattering off CMB photons. At high temperatures, free-free losses and collisionally excited line radiation from atoms and ions other than neutral hydrogen may become important contributions as well. As for heating, all species contribute to cooling, giving the total cooling rate

$$L = L_{\text{H II}} + L_{\text{He II}} + L_{\text{He III}} + L_{e\text{H}} + L_C + L_{\text{line}} + L_{\text{ff}}. \quad (57)$$

For a single species, recombinations radiate the electron energy $\sim k_B T$ as photons at the rate $L_i = n_e n_i \beta_i(T)$. Recombination cooling coefficients $\beta_i(T)$ are provided by [Seaton \(1959\)](#) for recombinations to H I and He II. An expression for the radiative contribution to $\beta_{\text{He II}}$ for recombinations to He I is provided by [Black \(1981\)](#). The dielectronic contribution may be approximated as $\beta_{\text{He II}}^{\text{diel}} = 3 \text{ Ry} \times \alpha_{\text{He II}}^{\text{diel}}$ ([Gould and Thakur, 1970](#)) using the second part of the expression for $\alpha_{\text{He II}}$ in [Table III](#), which expresses the dielectronic component. The total recombination cooling coefficients are provided in [Table III](#).

The cooling rate due to the collisional excitation of H I by electrons is given to an accuracy of 3% over the temperature range $4000 < T < 12\,000$ K by ([Spitzer, 1978](#)).

$$L_{e\text{H}} = 7.3 \times 10^{-32} \text{ J m}^3 \text{ s}^{-1} n_e n_{\text{H I}} e^{-118\,400/T}. \quad (58)$$

For temperatures relevant to the IGM, cooling losses due to collisional ionization of hydrogen and collisional excitation and ionization losses from helium are negligible. Similarly, for the low metallicities encountered in the IGM, radiative losses from metals are normally negligible, although they may possibly be important in the WHIM.

Cooling is also produced by the Compton scattering of CMB photons off the electrons, which is especially important at high redshifts. The cooling rate is ([Weymann, 1965](#))

$$L_C = 4n_e c (\sigma_T / m_e c^2) a T_{\text{CMB}}^4(z) k_B [T - T_{\text{CMB}}(z)], \quad (59)$$

where $\sigma_T = (8\pi/3)(e^2/[4\pi\epsilon_0]m_e c^2)^2 = 6.65 \times 10^{-29} \text{ m}^2$ is the Thomson cross section, a is the radiation density constant, m_e is the electron mass, c is the speed of light, and T_{CMB} is the temperature of the cosmic microwave background.

In the WHIM, cooling by thermal bremsstrahlung radiation, or free-free emission, due to the acceleration of a charge in the Coulomb field of another charge may be significant. For an ion of number density n_i and charge Z_i , the cooling rate is ([Rybicki and Lightman, 1979](#))

$$L_{\text{ff}} = 1.43 \times 10^{-40} \text{ J m}^3 \text{ s}^{-1} T^{1/2} n_e n_i Z_i^2 \bar{g}_B, \quad (60)$$

where \bar{g}_B is a frequency average of the velocity-averaged Gaunt factor, and ranges between 1.1 and 1.5. [Shapiro and Kang \(1987\)](#) provided the fitting formula $\bar{g}_B = 0.794\,64 + 0.1243 \log_{10}(T/Z_i^2)$ for $T/Z_i^2 < 3.2 \times 10^5$ K and $\bar{g}_B = 2.131\,64 - 0.1240 \log_{10}(T/Z_i^2)$ for $T/Z_i^2 > 3.2 \times 10^5$ K. Cooling rates including collisionally excited metallic line losses and their individual emissivities are provided by [Gaetz and Salpeter \(1983\)](#) for solar abundances. Nonsolar values may be interpolated with the zero-metallicity limit for which atomic cooling is determined only by the hydrogen and helium losses.

Photoelectric heating by x rays is automatically included in [Eq. \(55\)](#). X rays, however, may introduce two

other sources of energy exchange: gains through Compton heating and losses through the effect of secondary electrons.

Sources of high-energy radiation, such as a hard x-ray background, may inject additional energy into the IGM through Compton heating ([Arons and McCray 1969](#); [Rees, 1969](#); [Rees and Setti, 1970](#); [Madau and Efstathiou, 1999](#)). For an IGM of electron density n_e and temperature T , an x-ray background with energy density u_ν^X will heat the gas through Compton scatterings at the rate

$$G_C = n_e c \frac{\sigma_T}{m_e c^2} \int_0^\infty d\nu u_\nu^X (h_p \nu - 4k_B T). \quad (61)$$

For photons with energies exceeding 100 keV, Compton scattering takes place in the relativistic regime, requiring the Klein-Nishina instead of the Thomson cross section. The heating rate then becomes ([Blumenthal, 1974](#); [Madau and Efstathiou, 1999](#))

$$G_C = \frac{3}{4} n_e c \sigma_T \int_0^\infty dx u_x^X \frac{1}{x^2} \left(\frac{x^2 - 2x - 3}{2x} \ln(1 + 2x) \right. \\ \left. + \frac{-10x^4 + 51x^3 + 93x^2 + 51x + 9}{3(2 + 3x)^3} \right), \quad (62)$$

where $x = h_p \nu / m_e c^2$. The Compton heating rate G_C should then be added to [Eq. \(56\)](#).

The secondary electrons ejected by x rays have only a small effect on the temperature of highly ionized gas. In partially ionized gas, however, their contribution to the energy losses may become appreciable. They play a particularly important role in the cooling of gas ahead of ionization fronts during the epoch of reionization. Expressions for the energy of a primary electron deposited as heat, further ionizations, and collisional excitations, for both hydrogen and helium, in a partially ionized medium are provided by [Shull and van Steenberg \(1985\)](#).

IV. THE METAGALACTIC UV BACKGROUND

A. Mean energy density of the UV background

1. Origin of the UV background

Since the ionization structure of the IGM is determined by the specific radiation energy density u_ν of the metagalactic ultraviolet photoionizing background, a complete understanding of the structure of the IGM requires an estimate for u_ν . In turn, measured properties of the IGM, like its optical depth to hydrogen- and helium-ionizing photons or the ratios of ionization fractions of metals, place constraints on the shape of the metagalactic UV background.

In a homogeneous and isotropic expanding universe, [Eq. \(5\)](#) gives for the integrated specific energy density produced by sources with a total proper emissivity $\epsilon_\nu(z) = 4\pi j_\nu(z)$

$$u_{\nu}(z) = \frac{1}{c} \int_z^{\infty} dz' \frac{dl_p}{dz'} \frac{(1+z)^3}{(1+z')^3} \epsilon_{\nu'}(z') \times \exp[-\tau_{\text{eff}}(\nu, z, z')], \quad (63)$$

where $\tau_{\text{eff}}(\nu, z, z')$ is an effective optical depth due to absorption by the IGM and $\nu' = \nu(1+z)/(1+z')$. For discrete absorption systems, Eq. (31) may be used, adapted to photoelectric absorption by choosing $x = N_{\text{H I}}$ and taking $w = \int d\lambda'' [1 - \exp(-\tau_{\nu''})]$, where $\nu'' = \nu(1+z)/(1+z')$. Then, on replacing $d\lambda'' \partial^2 \mathcal{N} / \partial N_{\text{H I}} \partial \lambda''$ by $dz'' \partial^2 \mathcal{N} / \partial N_{\text{H I}} \partial z''$,

$$\tau_{\text{eff}}(\nu, z, z') = \int_z^{z'} dz'' \int_0^{\infty} dN_{\text{H I}} \frac{\partial^2 \mathcal{N}}{\partial N_{\text{H I}} \partial z''} \times [1 - \exp(-\tau_{\nu''})], \quad (64)$$

where

$$\tau_{\nu''} = N_{\text{H I}} a_{\text{H I}}(\nu'') + N_{\text{He I}} a_{\text{He I}}(\nu'') + N_{\text{He II}} a_{\text{He II}}(\nu''). \quad (65)$$

The emissivity ϵ_{ν} consists of two contributions, isolated radiation sources, such as galaxies and QSOs, and diffuse emission from the IGM itself. Survey estimates for the contributions from isolated sources are discussed later. There are four principal contributions to the diffuse emission capable of photoionizing the IGM (Haardt and Madau, 1996): (1) recombinations to the ground state of He I and He II, (2) He II Ly- α recombination radiation, (3) He II two-photon continuum emission, and (4) He II Balmer continuum emission. The specific recombination emissivity associated with each of these processes may be expressed generally in the form (Haardt and Madau, 1996)

$$\epsilon_{\nu}(z) = h_p \nu f(\nu) B(\nu, z) dz/dl_p, \quad (66)$$

where

$$B(\nu, z) = c \int_0^{\infty} dN_{\text{H I}} \frac{\partial^2 \mathcal{N}}{\partial N_{\text{H I}} \partial z} p_{\text{rec}} p_{\text{esc}}(\nu) \times \int_{\nu_T}^{\infty} d\nu' \frac{u_{\nu'}(z)}{h_p \nu'} w_{\text{abs}}(\nu'), \quad (67)$$

where ν_T refers to the photoionization threshold for ionizing the ground state of an ion of atomic number Z_i . The function $B(\nu, z)$ expresses the escape rate of recombination photons produced by discrete absorption systems in terms of the product of the fraction $w_{\text{abs}}(\nu)$ of photons of energy $h_p \nu$ absorbed by a given ion, the probability p_{rec} that a recombination will result in the particular radiative transition considered, and the probability p_{esc} that the emitted photon will escape the absorption system that produced it. These factors may be computed from detailed radiative transfer computations using a code such as CLOUDY (Haardt and Madau, 1996).

The capture of electrons into the n^2L level of a hydrogenic ion results in the emission of a continuum photon distribution sharply peaked at the photoelectric

edge. The rate of direct recombinations may be computed from the Milne relation between the free-bound recombination cross section $\sigma_{fb}(\nu)$ for an electron moving at velocity ν and the bound-free photoionization cross section $a_n(\nu)$ (Rybicki and Lightman, 1979)

$$\frac{\sigma_{fb}(\nu)}{a_n(\nu)} = \frac{h_p^2 \nu^2}{m_e^2 c^2 \nu^2} \frac{2g_n}{g_i}, \quad (68)$$

where $g_n = 2n^2$ is the statistical weight for the atom with electron in the bound state n and $g_i = 2$ is the statistical weight for the ion. The bound-free cross section from state n in a hydrogenic atom of atomic number Z_i may be expressed as

$$a_n(\nu) = \frac{64\pi}{3^{3/2}} \frac{n}{Z_i^2} \alpha a_0^2 \left(\frac{\nu_T}{\nu} \right)^3 G_n, \quad (69)$$

where G_n is a Gaunt factor and $\alpha = [1/4\pi\epsilon_0]e^2/\hbar c$ is the fine structure constant. The Gaunt factor for the ground state is

$$G_1 = 8\pi 3^{1/2} (1 + \epsilon^2)^{-1} \frac{e^{-(4 \tan^{-1} \epsilon)/\epsilon}}{1 - e^{-2\pi/\epsilon}}, \quad (70)$$

where $\epsilon = (\nu/\nu_T - 1)^{1/2}$ [cf. Eq. (47)]. The photon released following recombination will have energy $h_p \nu = h_p \nu_T + (1/2)m_e \nu^2$, where m_e is the mass of an electron and h_p is Planck's constant. For a Maxwellian velocity distribution $f_M(\nu) = 4\pi(m_e/2\pi k_B T)^{3/2} \nu^2 \exp(-m_e \nu^2/2k_B T)$ for the electrons, the free-bound emissivity due to recombinations to state n in a hydrogenic ion of atomic number Z_i and number density n_i is then

$$\epsilon_n(\nu) = n_e n_i h_p \nu \sigma_{fb}(\nu) \nu f_M(\nu) \frac{d\nu}{d\nu} = \frac{4\pi}{c^2} n_e n_i \left(\frac{h_p^2}{2\pi m_e k_B T} \right)^{3/2} h_p \nu^3 a_n(\nu) 2n^2 \times \exp\left(-\frac{h_p \nu - h_p \nu_T}{k_B T} \right). \quad (71)$$

Recombinations to He II produce hydrogen-ionizing photons ($h_p \nu > 13.6$ eV). The recombinations generally occur to high energy levels, followed by a cascade of bound-bound transitions. Recombinations that populate the 2^2P level of He II result in a He II Ly- α photon of energy 40.8 eV, which photoionizes neutral hydrogen in the Ly- α forest systems. Recombinations that populate the 2^2S level produce He II $2^2S \rightarrow 1^2S$ two-photon emission with a total energy of 40.8 eV and a spectrum peaking at 20.4 eV. Direct recombinations to 2^2S and 2^2P produce He II Balmer continuum emission, for which the threshold photoionization energy is the same as the hydrogen Lyman limit.

2. Sources

QSOs were early recognized as a prominent source of metagalactic ionizing photons (Arons and McCray, 1970a, 1970b; Rees and Setti, 1970). Since then, there

have been numerous estimates of their contribution to the UV metagalactic background (Sargent *et al.*, 1979; Bechtold *et al.*, 1987; Miralda-Escudé and Ostriker, 1990, 1992; Madau, 1992; Meiksin and Madau, 1993; Giroux and Shapiro, 1996; Haardt and Madau, 1996, 2001; Fardal *et al.*, 1998; Shull *et al.*, 1999; Schirber and Bullock, 2003). The QSO luminosity function is conveniently parametrized by a double power-law form (Boyle *et al.*, 1988)

$$\phi(M, z) = \frac{\phi_*}{10^{0.4(1-\beta_1)(M-M^*)} + 10^{0.4(1-\beta_2)(M-M^*)}}, \quad (72)$$

where $\phi(M, z)dM$ describes the spatial density of QSOs at redshift z in the absolute magnitude range M to $M + dM$, ϕ_* is a spatial normalization factor (normally expressed in comoving units), and M^* is a characteristic break magnitude. In a pure luminosity evolution (PLE) model, ϕ_* is held fixed while M^* is allowed to evolve. In a pure density evolution (PDE) model, M^* is held fixed while ϕ_* is allowed to evolve. Although PLE and PDE models well fit the data over limited redshift ranges, Fan *et al.* (2001b) showed that the steepness of the bright end of the luminosity function has evolved between $z < 2$ and $z > 3.6$. Estimates of the QSO luminosity function at $z < 2.1$ are provided by Croom *et al.* (2004) based on the 2-degree field (2dF) redshift survey, and by Richards *et al.* (2005), combining data sets from the 2dF and SDSS. Richards *et al.* (2006) used the SDSS to measure the bright end of the QSO luminosity function and its evolution over the redshift range $0 < z < 5$.

A long-standing uncertainty affecting estimates of the QSO contribution to the UV background at high redshifts ($z > 2$) is the poorly determined number of low-luminosity QSOs. Hunt *et al.* (2004) measured the low-luminosity end of the luminosity function at $z \approx 3$. An estimate of the QSO luminosity function over the redshift range $3 < z < 6$ is provided by Meiksin (2005) based on fitting PLE and PDE models to the results of Fan *et al.* (2001b, 2004), and Hunt *et al.* (2004). An estimate of the bolometric QSO luminosity function over the redshift range $0 < z < 6$ is provided by Hopkins *et al.* (2007).

The QSO emissivity is given by $\epsilon_\nu = \int dM \phi(M) L_\nu(M)$, where $L_\nu(M)$ is the mean specific luminosity corresponding to a QSO of magnitude M . The spectral shape of QSOs, however, is uncertain at frequencies above the H I Lyman edge. Results based on HST data using the faint object spectrograph (FOS) give an intrinsic spectral distribution $f_\nu \propto \nu^{-\alpha_Q}$ with QSO spectral index $\alpha_Q = 1.76 \pm 0.12$ (Telfer *et al.*, 2002) over the rest-frame energies 0.8–1.8 Ry. The sample contains QSOs predominantly in the redshift range $0.3 < z < 2.3$. Distinguishing between radio-quiet and radio-loud QSOs gives $\alpha_Q = 1.57 \pm 0.17$ and 1.96 ± 0.12 , respectively. Results based on FUSE data give instead $\alpha_Q = 0.56^{+0.28}_{-0.38}$ (without distinguishing between radio-quiet and radio-loud QSOs) (Scott *et al.*, 2004). The origin of the discrepancy is unclear. The FUSE sample is at lower redshift ($z < 0.67$) and the sources have lower luminosities, so the differ-

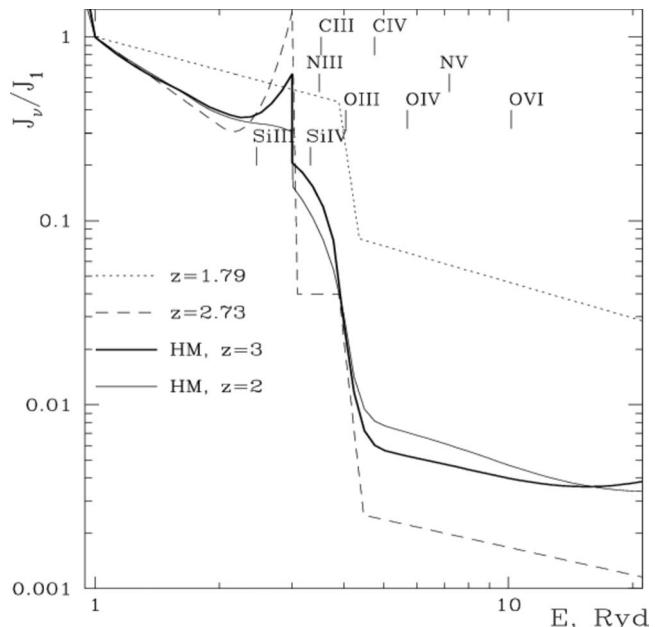


FIG. 9. The UV metagalactic ionizing background intensity J_ν , normalized by the intensity J_1 at 1 Ry, from Haardt and Madau (1996) at $z=3$ (thick line) and 2 (thin line) for a power-law QSO source spectrum $\nu^{-1.5}$ shortward of the H I Lyman edge. The threshold energies required to ionize several commonly detected ions are indicated. Also shown are estimates of the UV background as constrained by metal absorption systems at $z=2.73$ (dashed line) and 1.79 (dotted line). From Agafonova *et al.*, 2007. Figure reproduced by permission of *Astronomy & Astrophysics*.

ence may reflect a hardening with decreasing redshift and/or luminosity, for which there is evidence (Scott *et al.*, 2004). The spectral range used for the power-law fits to the FUSE spectra is restricted to rest-frame energies 0.8–1.4 Ry, similar to the range for the HST sample. The spectral corrections due to absorption by the intervening IGM, however, are smaller for the FUSE sample QSOs than the higher-redshift HST QSOs, so that the FUSE results may be more reliable.

The angle-averaged intensity $J_\nu = cu_\nu/4\pi$ of the UV background determined by Haardt and Madau (1996) based on an earlier assessment of the QSO contribution is shown in Fig. 9 at redshifts $z=2$ and 3. The steps in the background are produced by photoelectric absorption of the source radiation by intervening absorbers at the H I and He II Lyman edges. The comparison with the purely absorbing IGM estimate shows the formation of emission “horns” due to the reprocessing of ionizing radiation by the IGM into redshifted H I and He II Ly- α photons. The redshifted He II Ly- α photons enhance the flux of H I-ionizing photons as does the continuum emission resulting from direct recombinations to the ground levels of H I and He II. At higher redshifts, the UV background more strongly resembles the spectral shape of the sources because the opacity of the IGM becomes so large that the UV background is increasingly dominated by local sources.

TABLE V. Estimates of the H I mean Ly- α transmitted flux (column 2) and H I-ionization rate $\Gamma_{\text{H I}}^{\text{IGM}}$ (in 10^{-12} s^{-1}) required to match the mean Ly- α flux according to Meiksin and White (2004) (column 3) and to Bolton *et al.* (2005) and Bolton and Haehnelt (2007) (column 4). Columns 5 and 6 are the H I ionization rates $\Gamma_{\text{H I}}^{\text{QSO,PLE}}$ and $\Gamma_{\text{H I}}^{\text{QSO,PDE}}$ (in 10^{-12} s^{-1}) from QSOs using the pure luminosity evolution (PLE) and pure density evolution (PDE) models of Meiksin (2005). Column 7 gives the H I ionization rate $\Gamma_{\text{H I}}^{\text{QSO,HRH}}$ using the emissivity from Hopkins *et al.* (2007) and the same attenuation lengths as for the PLE and PDE models. For the PLE and PDE models, the indicated redshift entries $z=3.89, 4.00, 5.00,$ and 6.00 correspond to the ranges $3.6 < z < 3.9, 3.9 < z < 4.4, 4.4 < z < 5.0$ and $z > 5.7$, respectively.

z	$\langle \exp(-\tau) \rangle$	$\Gamma_{\text{H I},-12}^{\text{IGM,MW04}}$	$\Gamma_{\text{H I},-12}^{\text{IGM,B}}$	$\Gamma_{\text{H I},-12}^{\text{QSO,PLE}}$	$\Gamma_{\text{H I},-12}^{\text{QSO,PDE}}$	$\Gamma_{\text{H I},-12}^{\text{QSO,HRH}}$
2.75	0.74 ± 0.04	$0.86^{+0.36}_{-0.24}$			0.64	
3.00	0.70 ± 0.02	$0.88^{+0.14}_{-0.12}$	$0.86^{+0.34}_{-0.26}$	$1.1^{+3.0}_{-0.7}$	$0.44^{+0.39}_{-0.23}$	0.46
3.89	0.48 ± 0.02	$0.68^{+0.08}_{-0.07}$		0.19 ± 0.05	$0.14^{+0.07}_{-0.05}$	0.06
4.00	0.47 ± 0.03	$0.76^{+0.12}_{-0.11}$	$0.97^{+0.48}_{-0.33}$	$0.13^{+0.05}_{-0.03}$	$0.084^{+0.040}_{-0.030}$	0.058
5.00	$0.12^{+0.03}_{-0.04}$	$0.31^{+0.07}_{-0.09}$	$0.52^{+0.35}_{-0.21}$	$0.051^{+0.026}_{-0.018}$	$0.035^{+0.017}_{-0.014}$	0.027
5.50	$0.079^{+0.017}_{-0.013}$	$0.37^{+0.06}_{-0.05}$				0.019
6.00	< 0.006	< 0.14	$< 0.19^{+0.15}_{-0.10}$	$0.012^{+0.013}_{-0.005}$	$0.006^{+0.006}_{-0.002}$	< 0.014

Combining Eq. (40) with Eq. (63), the photoionization rate may be expressed in terms of the emissivity as

$$\Gamma_{\text{H I}} = [\epsilon_L(z) a_T / h_P (3 + \alpha_{\text{MG}})] r_{\text{eff}}, \quad (73)$$

where $\epsilon_L(z)$ is the emissivity at the Lyman edge, α_{MG} is the spectral index of the UV background just shortward of the Lyman edge, r_{eff} is an effective length scale over which the distribution of sources contributes to the radiation field at any given point, the photoionization cross section is approximated as $a_\nu \approx a_T (\nu / \nu_T)^{-3}$, and h_P is Planck's constant. It is well known that in a uniform infinite Euclidean universe with point sources of radiation distributed throughout, the effective length scale is infinite and the local radiation field diverges (Olber's paradox). Cosmological effects, in particular the finite age of the sources and the effects of redshifting, will guarantee convergence, and r_{eff} describes an effective horizon to the sources. Attenuation by a photoelectrically absorbing IGM will shorten the effective length even further, and will dominate at high redshifts. These two extremes, a cosmologically limited length scale and an attenuation limited length scale, may be combined into $r_{\text{eff}} \approx 1 / (1/l_H + 1/r_0)$, where l_H is the length-scale limitation due to cosmological expansion and the finite age of the sources, and r_0 is the length scale due to attenuation by the IGM. For sources turning on at $z = z_{\text{on}}$

TABLE VI. Ratio of $f_\nu(1500 \text{ \AA}) / f_\nu(912 \text{ \AA})$ for starburst galaxies undergoing continuous star formation with a Salpeter stellar initial mass function, over the indicated times for solar ($Z=0.02$) and 1/20 solar ($Z=0.001$) metallicity. Based on the STARBURST99 models of Leitherer *et al.* (1999).

Z	1 Myr	20 Myr	100 Myr	300 Myr	900 Myr
0.02	2.7	4.9	6.2	6.7	6.8
0.001	2.6	4.6	6.2	6.9	7.5

with (comoving) emissivity parametrized as $\epsilon_\nu(z) = \epsilon_L(1+z)^\gamma (\nu / \nu_L)^{-\alpha_S}$, the effective (proper) horizon to the sources is

$$l_H \approx \frac{c}{H_0 \Omega_m^{1/2}} \frac{3 + \alpha_{\text{MG}}}{3 + \alpha_S} (1+z)^{-3/2} \times \frac{1 - [(1+z)/(1+z_{\text{on}})]^{9/2 + \alpha_S - \gamma}}{9/2 + \alpha_S - \gamma} \quad (74)$$

for large z (Meiksin and White, 2003). Values for the attenuation length r_0 are provided by Meiksin and White (2004) based on numerical simulations (see Sec. VI.C.1). The values obtained lie between the medium- and high-attenuation models of Meiksin and Madau (1993) derived from direct absorption line counts.

Resulting values for the QSO contribution to the H I ionization rate are given in Table V at selected redshifts. The estimates are derived from the QSO emissivities of Meiksin (2005) and Hopkins *et al.* (2007) using Eq. (73) and the attenuation lengths r_0 from Meiksin and White (2004), allowing for an extrapolation of the measured Lyman limit system distribution to $z > 4$ (see Sec. VI.C.1). Results for both the pure luminosity evolution model and the pure density evolution models of Meiksin (2005) for the QSO luminosity function are given. The estimate based on the QSO luminosity function of Hopkins *et al.* (2007) uses the emissivity shown in their Fig. 11. All estimates agree within the errors.

Star-forming galaxies are an important potential source of ionizing radiation. While the spectra are likely too soft to produce appreciable He II-ionizing photons, the hot young stars in star-forming galaxies could in principle provide even more hydrogen-ionizing photons than QSOs. An estimate of the contribution of star-forming galaxies to the UV background requires making a variety of assumptions regarding the initial mass function, populations, and ages of the stars as well as the

numbers of faint galaxies below the survey limits. Some of these uncertainties are mitigated using the results of galaxy surveys that measure the intrinsic flux from the galaxies close to the Lyman edge (the range 1300–1800 Å is typical), since the stars that produce the ionizing radiation are the same as those dominating the detected light of the galaxies (Madau *et al.*, 1999). Even then, however, uncertainties in the spectra of the massive stars that dominate the radiation at early times introduce a comparable level of uncertainty into the estimate of the combined ionizing emissivity from the galaxy population (Bruzual and Charlot, 2003). Estimates for the conversion between the measured flux at 1500 Å (rest frame) and the predicted flux shortward of the Lyman discontinuity are provided in Table VI assuming a Salpeter initial mass function with $M_{\text{lower}} = 1M_{\odot}$ and $M_{\text{upper}} = 100M_{\odot}$ and either solar ($Z=0.02$) or 1/20 solar ($Z=0.001$) metal abundances, based on the STARBURST99 models of Leitherer *et al.* (1999).¹⁵ A similar value of $f_{\nu}(1500)/f_{\nu}(912^-) \approx 6$ is quoted by Madau *et al.* (1999). The values for the ratio $f_{\nu}(1350)/f_{\nu}(912^-)$ are about 5–10 % larger, and for $f_{\nu}(1700)/f_{\nu}(912^-)$ about 5–10 % smaller, than the values in Table VI. The lower mass cutoff $M_{\text{lower}} = 1M_{\odot}$ appears appropriate for some starbursts; in any case, choosing a lower value only alters the normalization to the total star formation rate as the lower-mass stars contribute negligibly to the spectra except at very late times (Leitherer and Heckman, 1995).

Another major uncertainty is the escape fraction $f_{\text{esc}}(\nu)$ of ionizing radiation, as this must multiply the emissivity based on galaxy counts and finally governs the contribution of the star-forming galaxies to the UV background. There are few direct measurements of the escape fraction, and virtually all are upper limits. Putman *et al.* (2003) inferred a global escape fraction from the Milky Way of 1–2 % from H α spectroscopic measurements of nearby high-velocity clouds. Based on a detection of Lyman continuum flux from FUSE observations of a local starburst galaxy, Bergvall *et al.* (2006) suggested an escape fraction of 0.04–0.1, subject to spectral modeling uncertainties. Fernández-Soto *et al.* (2003) placed an upper limit of 4% for galaxies in the redshift range $1.9 < z < 3.5$. Similar upper limits based on FUSE observations were obtained by Deharveng *et al.* (2001) and Heckman *et al.* (2001). Shapley *et al.* (2006) reported the detection of UV radiation shortward of the Lyman edge in a sample of Lyman break galaxies at $z \approx 3$ with a corresponding escape fraction of 14%, although the estimate is sensitive to the assumed calibrating population synthesis models and corrections for the IGM optical depth, and it may also apply only to the more luminous galaxies.

In addition to direct observational constraints, several attempts have been made to estimate the escape fraction from theoretical models, allowing for inhomogeneities in the interstellar medium of galaxies, the influence of su-

pernovae, and the flow of ionizing radiation through chimneys produced by large-scale outflows (Dove and Shull, 1994; Dove *et al.*, 2000; Wood and Loeb, 2000; Ciardi *et al.*, 2002; Clarke and Oey, 2002; and Fujita *et al.*, 2003). Escape fraction values ranging from less than 1% for quiescent disks to more than half in an inhomogeneous IGM are obtained. The models suggest that high star formation rates, such as in Lyman break galaxies, may sufficiently fragment the interstellar medium of the galaxies and/or create sufficient channels through supernova-driven superbubbles that escape fractions in excess of 10% may be achieved, particularly if star-forming regions are distributed throughout the disk of a galaxy.

A composite luminosity function of star-forming galaxies detected by the Lyman break method¹⁶ at $z \approx 3$ was derived by Dickinson (1998). Madau *et al.* (1999) combined this with determinations of the Lyman break population at $2.75 < z < 4$ by Madau *et al.* (1996, 1998) to estimate the emissivity of star-forming galaxies and their contribution to the metagalactic UV background.

Establishing the star-formation history of the Universe is currently an area of intense activity. A revised UV luminosity function of Lyman break galaxies was provided by Steidel *et al.* (1999). Giavalisco *et al.* (2004) measured the luminosity density of Lyman break galaxies in the redshift interval $3.5 < z < 6.5$, while Steidel *et al.* (2004) estimated the star-formation history of galaxies in the redshift interval $1.4 < z < 2.5$. Yoshida *et al.* (2006) measured the luminosity function of Lyman break galaxies in the SUBARU deep field at $z \approx 4$ and 5. Bouwens *et al.* (2006) provided a comprehensive analysis of the UV luminosity function of galaxies at $z \approx 6$ and the evolution of the luminosity function to $z \approx 3$.

Despite the heroic efforts to establish the UV luminosity density and cosmic star-formation rates at high redshifts, the contribution of the galaxies to the metagalactic UV background is still uncertain due to several factors. In addition to the ionizing radiation escape fraction and UV-to-Lyman limit conversion factor, the effects of internal galactic extinction, uncertainty in the amount of intergalactic extinction by the IGM (Meiksin 2006a), and the minimum source luminosity on the UV luminosity density and its evolution create further uncertainty in the net contribution of the galaxies.

The error budget may be illustrated using the results for $3 < z < 6$ (Giavalisco *et al.*, 2004; Bouwens *et al.*, 2006). The uncertainty in the measured luminosity density of the sources is 20% or larger. Another factor of 3 uncertainty results from the uncertain extinction correction to the number counts (Bouwens *et al.*, 2006). The uncertain lower-luminosity limit of the sources introduces a factor of 2 uncertainty to the integrated contribution of the sources to the UV background (Bouwens

¹⁵The code and model results are available at <http://www.stsci.edu/science/starburst99/>

¹⁶The Lyman edge moves into the optical range at $z \approx 3$, permitting the identification of galaxies with large Lyman breaks, as is expected for galaxies with high star-formation rates (Leitherer *et al.*, 1999).

et al., 2006). The conversion of the flux from the measured bands to shortward of the Lyman edge (see Table VI) introduces at least another 20% uncertainty. The attenuation length r_0 is uncertain by about 30% (Meiksin and White, 2004), and the uncertain evolution rate and birth time of the sources introduces another 10% uncertainty in the effective length scale to use in Eq. (73). Since these uncertainties are primarily systematic, the factors must be multiplied. Altogether, if middle values of the expected ranges are taken, a combined uncertainty of about a factor of 4 is still left for the contribution of the galaxies to Γ_{HI} , excluding the uncertainty of the escape fraction.

Gialalisco *et al.* (2004) obtained, for the comoving luminosity of sources at 1500 \AA , $\log_{10} \rho_{1500} \approx 19.25 \pm 0.05$ (in units of $\text{W Hz}^{-1} \text{Mpc}^{-3}$) at $3.4 < z < 4.1$ and $\log_{10} \rho_{1500} \approx 19.0 \pm 0.1$ at $4.6 < z < 5.2$. Applying the conversion factors in Table VI gives for the corresponding emissivities shortward of the Lyman edge $\log_{10} \rho_{912} \approx 18.4 \pm 0.06$ at $3.4 < z < 4.1$ and $\log_{10} \rho_{912} \approx 18.2 \pm 0.1$ at $4.6 < z < 5.2$. Use of these values in Eq. (73), combined with the attenuation length estimates of Meiksin and White (2004) (see Sec. VI.C.1), gives $\Gamma_{\text{HI},-12} \approx 2.7 f_{\text{esc}}$ at $3.4 < z < 4.1$ and $\Gamma_{\text{HI},-12} \approx 2.1 f_{\text{esc}}$ at $4.6 < z < 5.2$. Comparison with the required values for $\Gamma_{\text{HI},-12}$ in Table V (see Sec. VI.C.1), allowing for the contribution from QSOs in the PLE model of Meiksin (2005) (the PDE model estimates are even smaller) and for a factor 4 uncertainty in the galaxy contribution, imposes the restrictions on the escape fractions of $0.004 < f_{\text{esc}} < 0.9$ at $3.4 < z < 4.1$ and $0.02 < f_{\text{esc}} < 0.6$ at $4.6 < z < 5.2$. Similar escape fractions are inferred by Inoue *et al.* (2006). Galaxies thus plausibly make up the missing ionizing radiation, but the uncertainties are still too great to preclude additional sources, which may actually dominate. Since re-radiation by the IGM itself may contribute some 20–40 % of the total emissivity (Meiksin and Madau 1993; Haardt and Madau 1996), these restrictions on f_{esc} may be further eased. The emissivities are based on source counts uncorrected for the effects of internal extinction on color. Corrections may increase the emissivities by as much as a factor of 3–4 (Bouwens *et al.*, 2006), corresponding to a similar reduction factor in the required escape fractions.

At $5.5 < z < 6.5$, Bouwens *et al.* (2006) obtained a comoving integrated UV emissivity at $\lambda = 1350 \text{ \AA}$ of $\log_{10} \rho_{1350} \approx 19.0 \pm 0.25$ at $5.5 < z < 6.5$, with the error range covering the uncertainty in the lowest luminosity of the contributing sources. Using the same procedure as above, this translates into the large ionization rate of $\Gamma_{\text{HI},-12} \approx 20 f_{\text{esc}}$. Correcting the colors for internal extinction increases this value by about another 50%. Consistency with the residual ionization rate at $z \approx 5.5$, after subtracting the QSO contribution (which is small), gives $0.004 < f_{\text{esc}} < 0.09$ (or somewhat less, allowing for extinction corrections), a very plausible range, suggesting that these sources may in fact dominate the UV-ionizing background at high redshifts.

B. Fluctuations in the UV background

The discreteness of the sources of radiation will produce local fluctuations in the UV background. Several physical effects contribute to the fluctuations. Any single source will dominate the radiation field sufficiently nearby. The result is a region of enhanced photoionization around the source and a reduction in the local opacity of the IGM. Known as the “proximity effect,” the diminished strength of absorption by the Ly- α forest near an ionizing source like a QSO may be used to constrain the intensity of the UV background, as is discussed in the next section. If the opacity of the IGM to ionizing photons is sufficiently small that a large number of sources distributed over large spatial scales contribute to the radiation field, the fluctuations will be small. If the attenuation length, which is the characteristic distance over which the radiation from sources is diminished by IGM absorption, is smaller than the characteristic clustering scale of the sources, then the radiation field will be modulated by the large-scale spatial distribution of the sources. In the limit of such a short attenuation length that the number of sources contributing to the radiation field in any given region is subject to large Poisson fluctuations, the radiation field will exhibit substantial fluctuations (Zuo 1992a; Meiksin and White 2003). This will become a particularly appreciable effect near the reionization epochs of H I and He II, but may be an important effect well after the reionization epochs as well if the IGM opacity is sufficiently large at high redshifts.

The magnitude of the fluctuations may be estimated by considering the effect of Poisson fluctuations in the source numbers on the integrated intensity. The attenuation length r_0 is equivalent to the mean free path of an ionizing photon, the distance over which the mean number of absorbers encountered is unity. The probability that a photon survives a journey of a distance r is then $\exp(-r/r_0)$. In general the distance will depend on frequency, but most of the absorption takes place near the photoelectric edge at frequency ν_T . Provided the distances are sufficiently small that cosmological effects may be neglected, the generation of the radiation field may be considered in the Euclidean limit. Any individual source of luminosity L_ν a distance r from a given location will then contribute a flux $L_\nu \exp(-r/r_0)/4\pi r^2$ for $\nu > \nu_T$. Allowing for a luminosity distribution function $\Phi(L_\nu)$ per unit luminosity per unit volume with mean spatial density of sources between minimum and maximum luminosities L_{min} and L_{max} of $\bar{n} = \int dL_\nu \Phi(L_\nu)$, and defining $\bar{N}_0 = (4\pi/3)r_0^3 \bar{n}$ to be the mean number of sources within an attenuation volume, the distribution of the dimensionless energy density $u = u_\nu/u^*$, where $u^* \equiv (L^*/c)/4\pi r_0^2$ for a characteristic luminosity L^* , becomes (Meiksin and White, 2003)

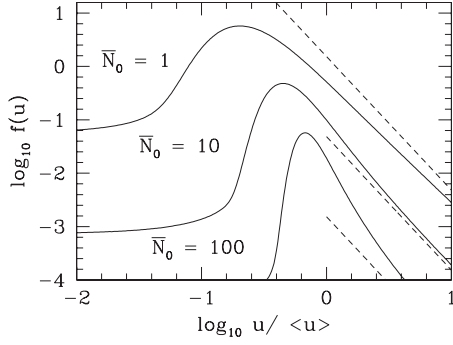


FIG. 10. The probability density $f(u)$ for the fluctuations in the energy density u of the UV background for a mean number of sources within the attenuation volume of $\bar{N}_0=1, 10$, and 100 for a QSO luminosity function (solid lines). The corresponding asymptotic limits for $u/\langle u \rangle \gg 1$ are also shown (dashed lines). The peak in the distributions shifts to lower $u/\langle u \rangle$ as \bar{N}_0 decreases. Adapted from Meiksin and White, 2003. Figure reproduced by permission of the Royal Astronomical Society (RAS) and Blackwell Publishing.

$$f(u) = \frac{1}{\pi} \int_0^\infty ds \cos\left(s \bar{N}_0 \int_{x_{\min}}^{x_{\max}} dx x \phi(x) \operatorname{Re} G(sx) - su\right) \times \exp\left(-s \bar{N}_0 \int_{x_{\min}}^{x_{\max}} dx x \phi(x) \operatorname{Im} G(sx)\right), \quad (75)$$

where $x=L_\nu/L^*$ and $\phi(x)$ is the normalized luminosity function of the sources

$$\phi(x) = \frac{\Phi(xL^*)L^*}{\int_{L_{\min}}^{L_{\max}} dL_\nu \Phi(L_\nu)}, \quad (76)$$

$x_{\min}=L_{\min}/L^*$, and $x_{\max}=L_{\max}/L^*$. The function $G(sx)$ is given by

$$G(sx) \equiv \int_0^\infty d\rho e^{isx\rho} \tau^3(\rho), \quad (77)$$

with $\tau(\rho)$ defined implicitly through $\rho(\tau) \equiv \tau^2 e^{-\tau}$. For large u , the distribution takes the asymptotic form $f(u) \sim (3/4)\bar{N}_0 \langle x^{3/2} \rangle u^{-5/2}$, where $x^{3/2}$ is averaged over $\phi(x)$. It follows that the variance $\langle u^2 \rangle - \langle u \rangle^2$ of the radiation energy density is undefined, diverging like $u_{\max}^{1/2}$ for $u_{\max} \gg 1$.

Examples of the resulting distribution function are shown in Fig. 10. A QSO luminosity function of the form Eq. (72) was used with parameters given by the maximum likelihood pure luminosity evolution fit (Meiksin, 2005) at $z=3$ (renormalized to $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$): $\beta_1=1.24$, $\beta_2=2.70$, $\phi_{\text{proper}}^* = 2.6 \times 10^{-5} \text{ Mpc}^{-3} \text{ mag}^{-1}$, and $M^* = -27.2$ at rest frame $\lambda = 1450 \text{ \AA}$. In anticipation of the upcoming discussion of helium reionization (see Sec. IVC.2), the attenuation lengths were fixed at 7, 15, and 33 (proper) Mpc, corresponding to averages of 1, 10, and 100 sources per attenuation volume. When the average is small, the distri-

bution becomes quite skewed towards low values, corresponding to few or no sources within an attenuation volume.

The Poisson fluctuations of sources within an attenuation volume will also give rise to spatial correlations in the radiation field. The correlation function is (Zuo, 1992b)

$$\xi_f(r) = \frac{1}{3\bar{N}_0} \frac{\langle x^2 \rangle r_0}{\langle x \rangle^2 r} \int_{r/r_0}^\infty du \frac{1}{u} \ln\left(\frac{u+r/r_0}{u-r/r_0}\right) e^{-u}, \quad (78)$$

where the averages $\langle \dots \rangle$ are performed over the dimensionless QSO luminosity function $\phi(x)$ [Eq. (76)]. For the luminosity function above at $z=3$, the coefficient $\langle x^2 \rangle / 3\langle x \rangle^2 \approx 2.6 \times 10^4$ so that substantial correlations are expected on scales $r < r_0$.

C. Observational constraints on the UV background

1. The proximity effect

The number of Ly- α forest systems decreases systematically near bright QSOs (Murdoch *et al.*, 1986; Tytler, 1987b; Lu *et al.*, 1991). The decrease, known as the ‘‘proximity effect,’’ is expected sufficiently near a QSO where its ionizing flux dominates the UV background (Carswell *et al.*, 1987). Bajtlik *et al.* (1988) quantified the effect in terms of the statistical properties of the Ly- α forest to obtain an estimate of the UV background.

The factor by which the H I column density in an absorption system will be reduced is $1 + \omega$, where ω is the ratio of the ionization rate $\Gamma_{\text{HI}}^{\text{Q}}$ due to the QSO at a luminosity distance r_L between the QSO and the absorber to the metagalactic ionization rate Γ_{HI} . The ionization rate due to the QSO is

$$\begin{aligned} \Gamma_{\text{HI}}^{\text{Q}} &= \int \frac{d\nu}{h\rho\nu} \frac{L_\nu^{\text{Q}}}{4\pi r_L^2} a_{\text{HI}}(\nu) \\ &= \frac{1}{1+z_{\text{Q}}} \frac{d_L^2}{r_L^2} \int d\nu \frac{f_\nu^{\text{Q}}}{h\rho\nu} a_{\text{HI}}(\nu), \end{aligned} \quad (79)$$

where f_ν^{Q} is the observed flux from the QSO at frequency $\nu' = \nu/(1+z_{\text{Q}})$ and $d_L = (1+z_{\text{Q}})c \int_0^{z_{\text{Q}}} dz/H(z)$ is the luminosity distance to the QSO at redshift z_{Q} for a flat universe ($\Omega_K=0$) (Peebles, 1993). For a power-law H I column density distribution $dN/dN_{\text{HI}} \propto N_{\text{HI}}^{-\beta}$, the increase in intensity will decrease the number of absorption systems above a given threshold $N_{\text{HI}}^{\text{thresh}}$ by the factor $(N_{\text{HI}}^{\text{thresh}})^{1-\beta} / [N_{\text{HI}}^{\text{thresh}}/(1+\omega)]^{1-\beta} = (1+\omega)^{-(\beta-1)}$. A mean line density $dN/dz = N_0(1+z)^\gamma$ would then become

$$dN/dz = N_0(1+z)^\gamma [1 + \omega(z)]^{-(\beta-1)}. \quad (80)$$

Measurements of ω as a function of distance r_L from the QSO as inferred from the depression in line density dN/dz permits a determination of the metagalactic Γ_{HI} .

Since Bajtlik *et al.* (1988), several estimates of the metagalactic ionization rate have been made using the proximity effect. Scott *et al.* (2000) performed a uniform analysis of the spectra of 99 QSOs at moderate resolution ($\sim 1 \text{ \AA}$) over the redshift range $0 < z < 5$ to obtain

an estimate of $\Gamma_{\text{H I}} = 1.9_{-1.0}^{+1.2} \times 10^{-12} \text{ s}^{-1}$ over $1.7 < z < 3.8$. (They also provided references to much of the previous literature.) The rates have generally exceeded the estimates of the contribution from quasars. Several systematic effects could account for some of the discrepancy. Redshifts for the quasars measured from low-ionization permitted lines such as the Balmer lines or Mg II or from forbidden lines such as [O III] $\lambda\lambda 4959, 5007 \text{ \AA}$ are redshifted compared with Ly- α and C IV by a few to several hundred km s^{-1} (Boroson and Green, 1992; Laor *et al.*, 1995; Vanden Berk *et al.*, 2001). If the higher redshifts reflect the true distances to the QSOs, then the QSO flux producing the proximity effect will be overestimated using QSO redshifts based on Ly- α or C IV, which in turn would result in an overestimate of the metagalactic ionization rate by as much as a factor of 2 (Scott *et al.*, 2000). Numerical simulations suggest that enhanced large-scale structure in the vicinity of a QSO will partly compensate for the photoionizing influence of the QSO, again resulting in an overestimate of the metagalactic rate by as much as a factor of 2–3 (Faucher-Giguère, Lidz, *et al.*, 2008).

Quasar variability will introduce scatter in the estimates for $\Gamma_{\text{H I}}$ and degrade the fit of ω vs r_L for a model assuming a constant quasar flux (Bajtlik *et al.*, 1988). Episodic behavior of QSO luminosities could introduce a further systematic in the estimates of the metagalactic ionization rate. If a QSO satisfies a survey magnitude threshold as a result of entering a bright phase, the neutral fraction will lag behind, resulting in an overestimate of the metagalactic rate. From Eq. (45) for $\phi \gg 1$, it follows that the actual metagalactic rate is a factor $1 - (1 + \omega) / \exp(-\Gamma_{\text{H I}}^{\text{tot}} t)$ smaller than the estimate assuming equilibrium, where ω is measured from the deficit in Ly- α forest absorption lines near the QSO and $\Gamma_{\text{H I}}^{\text{tot}} = \Gamma_{\text{H I}} + \Gamma_{\text{H I}}^{\text{Q}}$. Time averaging over a period t_Q during which the QSO is sufficiently bright to enter the survey produces the average factor $1 - (\Gamma_{\text{H I}} t_Q)^{-1} [1 - \exp(-\Gamma_{\text{H I}}^{\text{tot}} t_Q)]$. For $t_Q \approx 10^{12} - 10^{13} \text{ s}$, this would result in too low a value for ω , and so too little suppression of the Ly- α forest line density over a distance ct_Q from the QSO, as is frequently found (Scott *et al.*, 2000). An overestimate of the metagalactic photoionization rate by several percent could result.

2. Constraints from helium ionization

The ratio of He II to H I column densities places a constraint on the ratio of the metagalactic UV background at the He II and H I photoelectric edges. From Eq. (42) and the corresponding equation for He II, assuming helium (like hydrogen) is highly ionized and so almost entirely in the form of He III,

$$\eta \equiv \frac{N_{\text{He II}}}{N_{\text{H I}}} = \frac{\Gamma_{\text{H I}} n_{\text{He}} \alpha_{\text{He III}}(T)}{\Gamma_{\text{He II}} n_{\text{H}} \alpha_{\text{H II}}(T)}, \quad (81)$$

where $\Gamma_{\text{H I}}$ and $\Gamma_{\text{He II}}$ are the photoionization rates per atom of H I and He II, respectively. For an approximate temperature dependence of $\alpha_{\text{H II}} \propto T^{-0.72}$ near $T = 10^4 \text{ K}$

(and similarly for He II) and a hydrogen-to-helium number density ratio of 12.9, it follows from Eq. (81), Eq. (40), and the analogous equation for $\Gamma_{\text{He II}}$ that

$$\eta \approx 1.68 \frac{3 + \alpha_{\text{L,He II}}}{3 + \alpha_{\text{L,H I}}} S_L = 0.42 \frac{\Gamma_{\text{H I}}}{\Gamma_{\text{He II}}}, \quad (82)$$

where the “softness parameter” $S_L = u_{\text{L,H I}} / u_{\text{L,He II}}$ is the ratio of the metagalactic UV energy density at the H I and He II Lyman edges (Madau and Meiksin, 1994), and $\alpha_{\text{L,H I}}$ and $\alpha_{\text{L,He II}}$ are the spectral indices just shortward of the respective edges. (Allowing for the full temperature dependences of the H II and He II radiative recombination rates introduces a weak temperature dependence of $\eta \propto T^{0.055}$; Shull *et al.*, 2004.) Because of the steepness of u_ν at energies just above 4 Ry (Fig. 9), instead of the softness parameter, it is usually more convenient to introduce the ionization rate ratio $\Psi = \Gamma_{\text{H I}} / \Gamma_{\text{He II}}$, as it is this ratio that governs η directly.

It follows from Eq. (18) that the ratio of the He II to H I optical depths at line center is given by

$$\frac{\tau_{0,\text{He II}}}{\tau_{0,\text{H I}}} = \frac{1}{4} \frac{b_{\text{H I}}}{b_{\text{He II}}} \eta \approx 0.10 \frac{b_{\text{H I}}}{b_{\text{He II}}} \Psi. \quad (83)$$

The value of Ψ is predicted to be large for a UV background dominated by QSOs (Fig. 9). For an intrinsic spectral index of $\alpha_Q = 1.5$, $\Psi \approx 100$ at $z \approx 3$, corresponding to $\eta \approx 40$ (Madau and Meiksin, 1994; Haardt and Madau, 1996), while for $\alpha_Q = 2$, $\Psi \approx 340$, corresponding to $\eta \approx 140$ (Madau and Meiksin, 1994). Interpolation to $\alpha_Q = 1.8$ gives $\Psi \approx 220$ and $\eta \approx 90$. Additional photoionizing sources, like galaxies, will increase Ψ and η further. The ratio of optical depths is thus expected to be large, so that a strong He II Ly- α signature is expected from the IGM. The ratio also depends on the ratio of the Doppler parameters. For pure thermal broadening, it follows from Eq. (10) that $b_{\text{H I}} / b_{\text{He II}} = 2$, and $\tau_{0,\text{He II}} / \tau_{0,\text{H I}} \approx 0.2\Psi$ will be quite large. But if velocity broadening dominates [see Eq. (11)], then $b_{\text{H I}} / b_{\text{He II}} \approx 1$ and $\tau_{0,\text{He II}} / \tau_{0,\text{H I}} \approx 0.1\Psi$. Systems optically thin in H I Ly- α with $\tau_{0,\text{H I}}$ as low as 0.1 will form saturated He II Ly- α lines.

Because of line blanketing, the measured optical depths will scale according to Eq. (31). A large effective optical depth due to blanketing is expected (Miralda-Escudé, 1993; Madau and Meiksin, 1994; Giroux *et al.*, 1995). This has been confirmed by observations (see Sec. II.B.5). The estimate of Madau and Meiksin (1994) required $\Psi > 200$ for the 95% lower limit $\tau_{\text{He II}} > 1.5$ at $z = 3.2$ of Hogan *et al.* (1997) if the absorbers are thermally broadened, but $\Psi > 1000$ to reach the 95% upper limit of $\tau_{\text{He II}} < 3.0$. For velocity-broadened absorbers, however, for which Zheng, Kriss, *et al.* (2004) found evidence, the upper limit may be satisfied by $\Psi < 500$. If the lower limit $\tau_{\text{He II}} > 4.8$ found by Heap *et al.* (2000) applies, however, then $\Psi > 1000$ is required even for velocity-broadened absorbers.

There is additional reason to believe values of $\Psi > 1000$ occur at $z > 3$. While the detection of a high He II

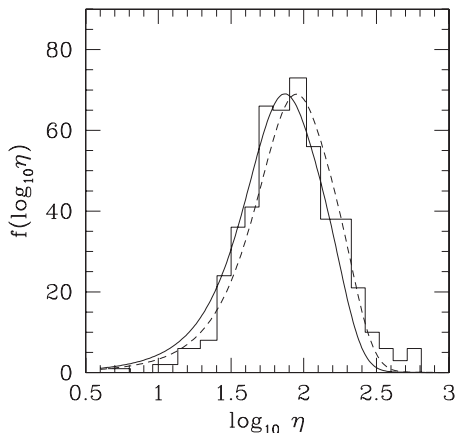


FIG. 11. Distribution of column density ratio $\eta = N_{\text{He II}}/N_{\text{H I}}$, for $N_{\text{He II}}$ measured from FUSE observations and corresponding $N_{\text{H I}}$ from Keck observations for absorption features over the redshift range $2.30 < z < 2.75$ (from Fechner *et al.*, 2006). Systems detected in spectral bins affected by metal line absorption have been excluded. The systems are further restricted to lie in the range $0.01 < \tau_{0,\text{H I}} < 0.1$ to assure completeness and reliable fits. Without this latter restriction, the full distribution ranges over $-0.2 < \log_{10} \eta < 3$. The solid curve shows the expected η distribution allowing for fluctuations in the He II-ionizing background for an average of ten QSOs per attenuation volume. The dashed line allows for a small increase in the mean η values within the measurement errors.

Ly- α optical depth was expected, the wide range in fluctuations in η came as a surprise. Some of the systems indicate values as large as $\eta > 1000$ at $z \leq 3$ based on follow-up optical observations of the H I Ly- α systems corresponding to the He II systems detected (Zheng, Kriss, *et al.*, 2004; Reimers *et al.*, 2005; Fechner *et al.*, 2006). Combining $N_{\text{He II}}$ measurements from FUSE observations over the redshift range $2.30 < z < 2.75$ with measurements of $N_{\text{H I}}$ for the corresponding H I systems using Keck observation, Fechner *et al.* (2006) obtained a very broad distribution for η , as shown in Fig. 11. Systems detected in spectral bins affected by metal line absorption have been excluded. The systems are further restricted to those with line-center optical depths in the range $0.01 < \tau_{0,\text{H I}} < 0.1$ to assure completeness and reliable fits. Without this latter restriction, the full distribution ranges over $-0.2 < \log_{10} \eta < 3$. A trend of decreasing η with decreasing redshift has also been found (Zheng, Kriss, *et al.*, 2004; Fechner *et al.*, 2006). Only fluctuations producing an extremely soft spectrum with $\Psi > 2000$ could account for the largest- η excursions. Such high values could arise from strong local H I-ionizing sources, or from a broad distribution in the He II-ionizing background with occasional low excursions. Higher values of η are found in H I voids, regions with $\tau_{\text{H I}} < 0.05$ (Shull *et al.*, 2004; Fechner *et al.*, 2006), again consistent with a local overdensity of hydrogen-ionizing sources compared with He II-ionizing sources producing the H I voids. The trend is also consistent with an increase in the relative attenuation length of hydrogen-ionizing photons compared with

He II-ionizing photons so that more distant hydrogen-ionizing (but not He II-ionizing) sources are able to add to the radiation field in the H I voids.

Monte Carlo realizations of the expected fluctuations in $\tau_{\text{He II}}$ were performed by Fardal *et al.* (1998), allowing for the discreteness of absorption systems and quasars. At $z=3$, they found a range of values $1.3 \lesssim \tau_{\text{He II}} \lesssim 2.3$, peaking at $\tau_{\text{He II}} \approx 1.9$. Since the He II column density scales inversely with the local intensity of the UV background (provided most of the helium is ionized to He III), the contribution of source discreteness to the distribution in the He II to H I column density ratio η may be predicted from Eq. (75) as $f(\eta) = f(u) |du/d\eta| = f(u) u^2 / \eta \langle u \rangle \langle u \rangle$, where $\eta = \eta \langle u \rangle \langle u \rangle / u$.¹⁷ The flattening of $f(u)$ for $u \ll 1$ shows that the average of $\eta \propto 1/u$ is undefined, diverging logarithmically at the upper end due to regions of low ionization.¹⁸

Using the distribution shown in Fig. 10 for an average of $N_0=10$ QSO sources per attenuation volume, the resulting distribution for η is shown in Fig. 11. The distribution function shown by the solid line is computed as the average of two distributions matched to the measured distributions with mean and spread of $\log_{10} \eta = 1.70 \pm 0.32$ at $z \approx 2.33$ and $\log_{10} \eta = 1.98 \pm 0.32$ at $z \approx 2.68$ (Fechner *et al.*, 2006). The dashed line uses means increased by 0.25σ to $\log_{10} \eta = 1.78$ and 2.06 . The measured values are well described by the model, except for a small tail at $\log_{10} \eta \approx 2.6$. These values may be produced by patches of only partially ionized helium, as would remain during the epoch of He II reionization before its completion (Zheng, Kriss, *et al.*, 2004; Reimers *et al.*, 2005). Alternatively, they may result from local H I-ionizing sources reducing the H I column density, but not He II. Effects of large-scale structure and radiative transfer on the fluctuations were explored using numerical simulations by Maselli and Ferrara (2005), Bolton *et al.* (2006), and Tittley and Meiksin (2007) (see Sec. VI.C.3).

The measured values for η may be compared with the expectation for a UV background dominated by QSOs. Using Eq. (82), the mean values for η correspond to $140 < \Psi < 270$. From Eq. (73), $\Psi \approx (\epsilon_L^{\text{H I}} / \epsilon_L^{\text{He II}}) (a_T^{\text{H I}} / a_T^{\text{He II}}) r_{\text{eff}}^{\text{H I}} / r_{\text{eff}}^{\text{He II}}$. Approximating the emissivity as $\epsilon_r \propto \nu^{-\alpha_S}$, taking $r_{\text{eff}}^{\text{H I}} \approx 70$ Mpc from Eq. (105) and $r_{\text{eff}}^{\text{He II}} \approx 15$ Mpc for ten QSOs in an attenuation volume at the He II Lyman edge (Sec. IV.B), gives Ψ

¹⁷Because the H I-ionizing radiation field will be more narrowly distributed, its fluctuations will contribute much less to the fluctuations in η and so may be neglected, except for large values due to the proximity effect. The joint H I and He II proximity effect would need to be modeled separately, including the effect on changing the attenuation length, which may be important for He II-ionizing photons when the attenuation length and range of the proximity effect are comparable.

¹⁸The presence of diffuse radiation will limit the maximum values of η , as will the approach to near full recombination to He II. The maximum value, however, will still be so large that no average will be well determined.

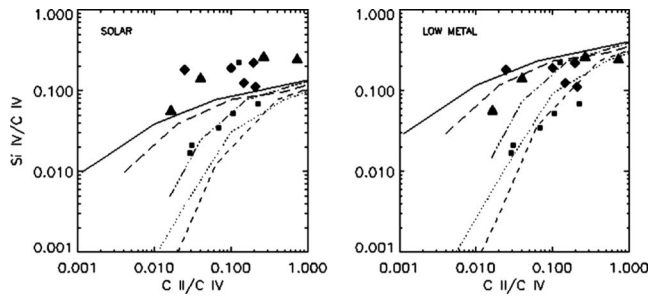


FIG. 12. Comparison of the observed values of Si IV/C IV vs C II/C IV with model predictions using CLOUDY with an input $\nu^{-1.5}$ power-law spectrum. Various breaks are allowed across the He II Lyman edge: dashed line, no break; dotted line, factor of 2; dash-dotted line, factor of 10; long-dashed line, factor of 100; solid line factor of 1000. The left panel shows results for a solar abundance ratio of Si/C; the right panel uses a ratio of Si/C three times solar. The differently shaped points indicate different lines of sight. Small points indicate $z < 3.1$ absorbers, while large indicate $z > 3.1$. From Songaila and Cowie, 1996. Figure reproduced by permission of the AAS.

$\approx 150\text{--}300$ for $1.5 < \alpha_S < 2.0$, producing a good match to the required average value of Ψ for a plausible emissivity spectral shape due to QSO sources.

3. Constraints from metal ionization

The presence of metal absorption systems permits further constraints on the shape of the UV metagalactic background. The ionization edges for several transitions of measured metal ions, primarily carbon, nitrogen, oxygen, and silicon, lie in the energy range 1–10 Ry, as shown in Fig. 9. The measured column density ratios of ionized states of these elements have been used to distinguish a UV background dominated by hard sources such as QSOs or active galactic nuclei (AGN) from a background dominated by galaxies and/or stars (Madau, 1991). The inferred ionization fractions may also be used to convert the measured column densities of the detected ions compared with the H I column density into physical densities, sizes, and total metallicities (Bergeron and Stasinska, 1986; Donahue and Shull, 1991; Bergeron et al., 1994). The findings suggest that Ly- α forest systems have metallicities less than 0.01 solar, while Lyman limit systems have metallicities from less than 0.01 solar up to 0.1 solar. Some systems show evidence for multiple phases with densities different by at least a factor of 10 (Bergeron et al., 1994). Sizes of typically tens of kiloparsecs are found, with total hydrogen densities of roughly $10^3\text{--}10^5\text{ m}^{-3}$.

Based on a comparison of Si IV to C IV vs C II to C IV, Songaila and Cowie (1996) found systematically different behaviors for systems at $z < 3.1$ compared with $z > 3.1$, as shown in Fig. 12. The Si IV to C IV ratio for a given C IV to C II ratio cannot be satisfied for any softness parameter without enhancing the Si/C ratio to about 3. In this case, the high-redshift systems require a break by a factor of 10–100 at the He II Lyman edge, while little or no break is required by the lower-redshift

systems. The large break at $z > 3$ is similar to the finding based on the He II to H I ratios found at $z \approx 3$ discussed above. Refined estimates of the UV background, including a plausible contribution from starburst galaxies, suggest the Si/C ratio need not exceed twice solar (Giroux and Shull, 1997). Based on observations of metal systems at $z > 3$, Savaglio et al. (1997) and D’Odorico et al. (1998a) similarly found a much larger ratio of Si IV to C IV column densities compared with the expectation for a QSO- or AGN-dominated UV background. They found a large softness parameter between the He II and H I Lyman edges of $S_L > 1000$ is required to bring the overabundance of silicon over carbon to below a factor of 10 over solar.

Using 19 high-quality QSO spectra over the redshift range $1.5 < z < 4.5$, Schaye et al. (2003) and Aguirre et al. (2004) performed a pixel optical depth analysis of C IV, Si IV, and H I in conjunction with simulated spectra. They found evidence for a highly inhomogeneous distribution of carbon with a cosmic mean of $[C/H] = -2.80 \pm 0.13$ at $z \approx 3$ and no evidence for evolution over the redshift range $1.8 < z < 4.1$, adopting the galaxy-QSO metagalactic spectrum of Haardt and Madau (2001), rescaled to reproduce the measured mean Ly- α transmitted flux. Introducing a large break in the metagalactic background at energies above 4 Ry, the He II photoelectric threshold for all redshifts indicates a decrease in metallicity with time, which could only be physical if large quantities of metal-poor gas were accreting onto the metal-enriched absorption systems or replacing them in the surveys as they accreted onto galaxy halos, possibilities that perhaps should not be discounted. Introduction of the large break only at $z > 3.2$, as would occur if He II were ionized late, however, yields a near constant (at most weakly increasing with time) carbon abundance. They find no redshift evolution in the ratio $\tau_{\text{Si IV}}/\tau_{\text{C IV}}$, and the silicon and carbon data require no sharp spectral change in the UV background at $z \approx 3$. They found a strong correlation between $\tau_{\text{Si IV}}/\tau_{\text{C IV}}$ and $\tau_{\text{C IV}}$, and argued the redshift effect reported by Songaila and Cowie (1996) may result from a different range in $\tau_{\text{C IV}}$ probed as a function of redshift, possibly due to different quality spectra for samples at $z < 3$ versus $z > 3$. They also inferred a Si/C ratio of $[\text{Si}/\text{C}] = 0.77 \pm 0.05$, with no indication for evolution in the ratio.

In a study of metal absorption systems in the spectra of $z \approx 2.5$ QSOs with intervening C IV and O VI detections, Simcoe et al. (2004) found roughly 30% of the Ly- α forest is enriched to abundances below $[C, O/H] \leq -3.5$. The systems are adequately modeled using a UV background dominated by QSOs or AGN having a power-law source spectrum $\nu^{-1.8}$, assuming a solar abundance ratio of carbon to oxygen. If instead the absorption systems are overabundant in oxygen by $[C/O] = -0.5$, as found for metal-poor galactic halo stars, then it is necessary to include a galactic radiation component.

Modeling metal absorption systems at $z \approx 2$ using CLOUDY and an assumed UV metagalactic background with contributions from both QSO sources and galaxies,

Simcoe *et al.* (2006) inferred a trend of decreasing sizes and increasing densities from high- to low-ionization states. The largest and lowest-density systems, with sizes of 0.1–10 kpc and densities of $2.5 \leq \log_{10} n_{\text{H}} \leq 3.5$ (in units of m^{-3}), are seen exclusively in C IV or Si IV. These sizes are comparable to the minimum inferred sizes based on coincident absorption systems along neighboring lines of sight (Sec. II.B.6). The lower-ionization species C II and Si II have sizes of 0.1–1 kpc and densities of $n \approx 10^4 \text{ m}^{-3}$, while Mg II and Al II systems have inferred sizes of about 100 pc and densities of $n_{\text{H}} \approx 10^5 \text{ m}^{-3}$. The smallest and densest structures are Fe II absorbers, with sizes of about 1 pc and densities of $n_{\text{H}} \approx 10^5 \text{ m}^{-3}$.

Comprehensive analyses of metal absorption systems in the range $1.4 < z < 3$ that are optically thin at the H I Lyman edge were carried out by Agafonova *et al.* (2005), Reimers *et al.* (2006), and Agafonova *et al.* (2007). They employed a Monte Carlo inversion procedure which allows for a random distribution of gas density and velocity along the line of sight. The procedure assumes a constant metallicity for each system, that the gas is optically thin to the ionizing UV radiation, assumed uniform, and that the gas is in thermal and ionization equilibrium. The ionizing UV background is expressed in parametric form. All parameters of the model are then varied to obtain the best fit to the metal absorption features, using CLOUDY to compute the ionization states and temperatures. The method is described by Levshakov *et al.* (2000), Agafonova *et al.* (2005), and references therein. Applied to individual systems, a range in He II to H I column densities is inferred from the data (Agafonova *et al.*, 2005), suggestive of a variable UV radiation field. Since the variability is generally based on systems optically thick to He II-ionizing radiation, the method does not distinguish between a UV radiation field that is variable on the metagalactic scale external to the absorbers and a radiation field that differs between the absorbers as a consequence of internal absorption.

They found a range of hydrogen densities from the analyses, with values as low as $n_{\text{H}} < 10^2 \text{ m}^{-3}$ to as high as $n_{\text{H}} > 10^4 \text{ m}^{-3}$, similar to the findings of Simcoe *et al.* (2006). The line-of-sight sizes of the metal absorbers range from a few parsecs to over 100 kpc. Systems at $z \leq 3$ are best fitted by imposing a strong reduction in flux between 3 and 4 Ry, as shown in Fig. 9. Such a reduction could be accounted for by strong He II Ly- α absorption. At $z < 1.8$, a much shallower break at 4 Ry is required compared with the model of Haardt and Madau (1996), suggesting that there may be fewer high-column-density systems filtering the He II-ionizing radiation than assumed by the model. The radiation field at $z < 3$ is dominated by sources with QSO or AGN spectra. Only a very small soft spectrum component from galaxies may contribute, suggesting an escape fraction of $f_{\text{esc}} < 0.05$. Large fluctuations in the UV background are also required. At $z \leq 3$, these are likely produced predominantly by the effects of radiative transfer through an IGM optically thick to He II-ionizing photons. The optical depth of He II-ionizing photons is dominated by

systems with $15 < \log_{10} N_{\text{H I}} < 16$, while much rarer systems with $\log_{10} N_{\text{H I}} > 17.2$ dominate the H I-ionizing photon optical depth. As a result, the mean free path of He II-ionizing photons is much shorter than for H I-ionizing photons, and relatively fewer sources contribute to the He II-ionizing radiation background in any given region. By $z \leq 2$, however, $\log_{10} N_{\text{H I}} < 16$ systems are sufficiently sparse that the IGM should become optically thin to He II-ionizing radiation to large distances, and the fluctuations are instead likely produced predominantly by the spread in the spectral indices of quasars. Fluctuations in $\eta = N_{\text{He II}}/N_{\text{H I}}$ and an anticorrelation between η and $N_{\text{H I}}$ may be accounted for by the filtering through the IGM of radiation from QSO sources with a variety of spectral shapes and by differences in the mean densities of the absorbing clouds. The progressive hardening of the UV background toward lower z would also account for the decrease in the median values for η as z decreases (Zheng, Kriss, *et al.*, 2004; Fechner *et al.*, 2006).

The modeling has some limitations, especially for systems with large values of η . A system with $\log_{10} N_{\text{H I}} < 17.2$ is optically thin to H I-ionizing radiation but thick to He II-ionizing radiation, so that a break at 3–4 Ry must be introduced to account for the radiative transfer internal to the system. The assumption of thermal equilibrium assumes adiabatic cooling or heating are negligible. The time scales are also long for the more rarefied systems. For a temperature of $T \approx 20\,000 \text{ K}$, the cooling time due to radiative recombination to H I exceeds 10^9 yr for $n_{\text{H I}} < 200 \text{ m}^{-3}$, which is becoming long, particularly if flows occur on shorter time scales so that adiabatic gains or losses are not negligible. Simcoe *et al.* (2004) also pointed out that the O VI abundances are sensitive to the poorly determined soft x-ray background. Still, the studies have lent considerable insight to the physical nature of the metal absorption systems and the background UV radiation field that ionizes them.

V. EARLY MODELS

Several models have been suggested for describing the physical structure of the Ly- α forest absorption systems. All of the early models have been supplanted by numerical cosmological simulations, which provide a largely successful description of the Ly- α forest and associated absorption systems within the broader context of cosmological structure formation. Vestiges of the early models, however, survive. In this section, elements of those models are discussed that continue to provide physical insight into the findings of the simulations, or which may still offer viable alternative descriptions of some absorption systems.

A. Pressure-confined clouds

The earliest physical model for the absorbers was one in which the absorption features arise from distinct

clouds pressure confined by a hot IGM (Sargent *et al.*, 1980). Denoting the cloud temperature and hydrogen number density by T_c and n_c , and those of the IGM by T_{IGM} and n_{IGM} , the condition of pressure equilibrium is $n_c T_c = n_{\text{IGM}} T_{\text{IGM}}$. Allowing for clouds photoionized by a QSO- (or) AGN-dominated UV background, small enough to be Jeans stable and able to withstand thermal evaporation by the hot confining medium, while requiring the IGM to meet the Gunn-Peterson constraint, Sargent *et al.* (1980) found for the cloud parameters at $z \approx 2.4$, $n_c = 100 \text{ m}^{-3}$, $T_c = 3 \times 10^4 \text{ K}$, $n_{\text{IGM}} = 10 \text{ m}^{-3}$, and $T_{\text{IGM}} = 3 \times 10^5 \text{ K}$. These values were somewhat modified by Ostriker and Ikeuchi (1983) and others.

The pressure-confined models suffered from a serious shortcoming: a wide range of sizes was required to reproduce the range in observed H I column densities. The higher column density systems would need to be so large that they would become unstable under their own gravity. Jeans stability limits the size of a self-gravitating cloud of density n_c and temperature T_c to be sufficiently small that a sound wave can cross it in less than the time for it to gravitationally collapse. This requirement is necessary to ensure that the internal gas pressure gradient of the cloud is able to balance its weight. For an isothermal gas, this corresponds to a maximum size of

$$\lambda_J = \left(\frac{\pi k_B T}{\bar{m}} \right)^{1/2} \frac{1}{(G\rho_0)^{1/2}} \approx 5.2 \times 10^{21} \left(\frac{n_{\text{IGM}} T_{\text{IGM}}}{10^6 \text{ K m}^{-3}} \right)^{1/2} \left(\frac{100 \text{ m}^{-3}}{n_c} \right) \text{ m}. \quad (84)$$

In ionization equilibrium with an ionization rate $\Gamma_{\text{H I}} \approx 10^{-12} \text{ s}^{-1}$, Eq. (44) gives a neutral hydrogen density for a cloud at $T_c = 3 \times 10^4 \text{ K}$ of $n_{\text{H I}} \approx 0.002 \text{ m}^{-3}$. This gives a maximum column density for a Jeans-stable cloud of $N_{\text{H I, max}} \approx 10^{15} \text{ cm}^{-2}$. The observed distribution extends to values two orders of magnitude larger before the absorbers become Lyman limit systems. A further failure of the model is that a system with a column density of $N_{\text{H I}} = 10^{14} \text{ cm}^{-2}$ would have a typical size of 17 kpc. This conflicts with the sizes inferred from coincident absorbers along neighboring lines of sight to lensed QSO images, which give cloud sizes in excess of 70 kpc for systems with $N_{\text{H I}} < 10^{14} \text{ cm}^{-2}$ (Sec. II.B.3).

Elements of the pressure-confined model, however, may still describe some absorption systems. The clouds could, for example, be confined by a wide range of pressures in different environments, which are themselves gravitationally confined (Baron *et al.*, 1989). The association of metal absorption systems with galaxies suggests they may be pressure-confined systems within galactic halos, as may be Lyman limit systems (Mo and Miralda-Escudé, 1996).

B. Dark matter minihalos

A more viable physical model for the absorbers is gravitational confinement by a dark matter halo. Rees (1986) recognized that the Ly- α forest is a necessary con-

sequence of the cold dark matter (CDM) scenario for structure formation. The same normalization of the CDM primordial matter power spectrum that recovers the clustering of galaxies predicts an abundance of low-mass minihalos with virial velocities comparable to the sound speed of photoionized gas. The gas trapped in these halos will produce absorption features with H I column densities and line widths comparable to those observed (Ikeuchi, 1986; Rees, 1986).

To fix parameters, consider the formation of a minihalo through gravitational collapse. The formation of a dark matter halo may be approximated by the spherical collapse model. The evolution of the radius $r(t)$ of a spherical shell of mass M in an Einstein-de Sitter universe, which provides a good description at high redshifts, is given by the parametric solution (Peebles, 1980)

$$r = r_V(1 - \cos \theta), \quad t = (r_V/v_{\text{circ}})(\theta - \sin \theta), \quad (85)$$

where r_V is the virial radius of the shell and $v_{\text{circ}} = (GM/r_V)^{1/2}$ is the circular velocity of the shell at the time of virialization. For a top hat initial spherical perturbation, the central dark matter density at the time of virialization is $\rho_{\text{DM}} = (9/8)(3\pi + 2)^2 \rho_{\text{crit}}(z_V)$, where $\rho_{\text{crit}}(z_V)$ is the critical Einstein-de Sitter density at the virialization epoch at redshift z_V . Since the gas is dissipative, its core radius will be smaller than the virial radius of the dark matter halo. Approximating the gas as being in hydrostatic equilibrium within a uniform density dark matter halo, the gas will have a Gaussian profile $\rho(r) = \rho(0) \exp(-r^2/r_c^2)$ with core radius

$$r_c = \left(\frac{k_B T / \bar{m}}{2\pi G \rho_{\text{DM}} / 3} \right)^{1/2} \approx 13(1 + z_V)^{-3/2} T_4^{1/2} h^{-1} \text{ kpc}, \quad (86)$$

where T_4 is the gas temperature in units of 10^4 K . A minihalo virialized at $z_V = 3$ will be only a few kiloparsecs in size. A minihalo of mass $10^9 M_\odot$ would have an adequate circular velocity to confine the gas. The H I column densities produced will range over $13 < \log_{10} N_{\text{H I}} < 16$. Higher-column-density systems become self-gravitating and Jeans unstable (Meiksin, 1994), and will likely produce stars.

Bond *et al.* (1988) pointed out that the gas will in general be in a dynamical state, either collapsing with an increasing core density or expanding after photoionization. The observational signatures and thermal properties of minihalos were explored by Meiksin (1994). Gas associated with the minihalos gives rise to absorption features with $N_{\text{H I}} \lesssim 10^{13} \text{ cm}^{-2}$ on scales of 100 kpc at $z = 3$. Even though the gas is in motion, the line profiles are found to remain nearly Doppler in shape, although broadened by the gas motion. In the idealized case of an isothermal gas in free expansion, so that the gas profile is Gaussian with a linear velocity profile $v = v_c(r/r_c)$, the Voigt profile is exactly preserved for lines of sight passing through the cloud, but with the Doppler parameter broadened to $b = (2k_B T / m_{\text{H}} + v_c^2)^{1/2}$. Typical temperatures in the inner region of minihalos with circular ve-

locities of $v_c \approx 40 \text{ km s}^{-1}$, which give rise to systems with $N_{\text{HI}} > 10^{15} \text{ cm}^{-2}$, are $(30\text{--}40) \times 10^4 \text{ K}$, consistent with the measurements of [Rauch *et al.* \(1996\)](#) for metal absorption systems expected to be associated with comparable H I column densities (see Sec. [II.B.6](#)). In the inner 10–30 kpc, temperatures of $T \approx (30\text{--}60) \times 10^4 \text{ K}$ are predicted, with substantial deviations from thermal equilibrium due to adiabatic heating of the infalling gas. In the outer 10–100 kpc, the gas is significantly adiabatically cooled by Hubble expansion. Temperatures half these values are expected in smaller halos of $v_c \approx 20 \text{ km s}^{-1}$.

Further consequences of the minihalo model, including number counts, effects of photoionization, and ablation due to ram pressure on minihalos moving relative to their environments, have been explored by [Ikeuchi *et al.* \(1989a, 1989b\)](#), [Murakami and Ikeuchi \(1990\)](#), [Miralda-Escudé and Rees \(1993\)](#), and [Murakami and Ikeuchi \(1993, 1994\)](#).

C. Caustics and sheets

A gravitational perturbation will generically form sheets since the enhanced density along a given direction will accelerate the collapse along that direction. Once a growing density fluctuation becomes nonlinear, it will produce a caustic. The caustic formation is well described by the Zel’dovich approximation ([Zel’dovich, 1970](#))

$$\mathbf{x}(\mathbf{q}, t) = \mathbf{q} - D(t) \nabla \Psi(\mathbf{q}), \quad \mathbf{v}(\mathbf{q}, t) = -a\dot{D}(t) \nabla \Psi(\mathbf{q}), \quad (87)$$

where \mathbf{x} is the comoving position of a particle with initial comoving position \mathbf{q} , $\mathbf{v} = a\dot{\mathbf{x}}$ is the peculiar velocity, $\Psi(\mathbf{q})$ describes the initial deformation of the density field, the gradient is with respect to \mathbf{q} , and $D(t)$ is the growth factor for linear perturbations $D(t) = (\dot{a}/a) \int^t da / \dot{a}^3$ ([Peebles, 1993](#)). The physical radius is related to the comoving radius through $\mathbf{r} = a(t)\mathbf{x}$, where $a(t) = 1/(1+z)$ is the expansion factor of the Universe at the epoch corresponding to redshift z . Conservation of mass gives for the density, up until the time of caustic formation, $\rho(\mathbf{x}, t) = \rho(\mathbf{q}) / |d^3\mathbf{x}/d^3\mathbf{q}|$, where the denominator is the determinant of the Jacobian of the coordinate transformation. For 1D collapse, the density prior to caustic formation grows as $\rho(x, t) = \rho_0 a(t)^{-3} / [1 - D(t)d^2\Psi/dq^2]$, which is exact for the 1D collapse of a slab. Gravitational instability ensures that a uniform density ellipsoidal density perturbation will collapse most rapidly along its shortest axis, forming a “Zel’dovich pancake.”

Baryons infalling along with the dark matter will produce Ly- α forest absorption features. The line profiles will become distorted at the time the caustic forms before the baryons come into dynamical equilibrium ([McGill, 1990](#); [Miralda-Escudé and Rees, 1993](#); [Meiksin, 1994](#)). The H I column densities produced will range over $13 < \log_{10} N_{\text{HI}} < 15$, with postshock temperatures peaking at $(50\text{--}60) \times 10^4 \text{ K}$ ([Meiksin, 1994](#)).

D. Galactic models

Since the earliest papers on the Ly- α forest it was recognized that galaxies should give rise to intervening absorption systems. Their characteristics and frequency, however, are unclear. The interstellar medium of disk galaxies is expected to produce damped Ly- α forest absorbers, although relatively few DLAs have been shown to arise from disks (see Sec. [VIII.A.1](#)). Other suggestions include condensates in cooling outflows from dwarf galaxies ([Wang, 1995](#)), the gas-rich dwarf galaxies themselves ([York *et al.*, 1986](#)), debris from satellite galaxies lost through tidal stripping by a central galaxy or expelled by supernovae ([Wang, 1993](#); [Morris and van den Bergh, 1994](#)), or pressure-confined clouds in a two-phase gaseous galactic halo medium ([Mo and Miralda-Escudé, 1996](#)). The outflow model in particular may give rise to distorted absorption line features if a line of sight intercepts the outflowing diffuse gas.

Another suggestion is that the absorption lines arise from gas in extended disks with too low surface density to produce many stars, the “vanishing cheshire cat” model of [Salpeter \(1993\)](#). In this model, an inner disk gravitationally confined region of radius about 15 kpc is surrounded by an extended pressure-confined disk of radius about 250 kpc. The inner region has a low gas surface density compared with most disk galaxies, but sufficiently large to produce a DLA feature in any line of sight passing through it. The outer region has such a low surface density that the hydrogen is photoionized by the metagalactic UV background. The outer region will give rise to Ly- α forest features. A transition region will produce Lyman limit systems. The relative abundances of the various H I column densities is accounted for by the progressively diminishing geometric cross section for increasing column densities. The transition between gravitational and pressure confinement may be adjusted to account for deviations from a perfect power law in the column density distribution. The Cheshire cat nature of the galaxy arises once star formation begins, producing a starburst galaxy. Metal-enriched gas ejected by the stars will accelerate the cooling and strengthen the burst, resulting in the expulsion of the gas in the central region and quenching further star formation. The result will be an outer “smiling” gaseous disk, possibly enriched in gas and metals by a galactic fountain if material from the starburst falls onto the disk, and a very low surface brightness “invisible” galaxy in the center.

Aspects of the model, and the balance of gravitational and pressure forces in slab models generally, have been explored by [Charlton *et al.* \(1993, 1994\)](#) and [Salpeter and Hoffman \(1995\)](#).

VI. NUMERICAL SIMULATION

A. Cosmological structure formation

1. Dynamical evolution of the dark matter and baryons

The successful description of the large-scale distribution of galaxies by the cold-dark-matter-dominated sce-

nario of cosmological structure formation (Davis *et al.*, 1985) led to attempts to account for the Ly- α forest within the same scenario. Using a combined hydrodynamics and gravity code, Cen *et al.* (1994) demonstrated that the baryons will trace similar small-scale structure as does the dark matter due to gravitational instability in the cold dark matter scenario. Several other groups soon followed with similar results (Zhang *et al.*, 1995, 1997; Hernquist *et al.*, 1996; Miralda-Escudé *et al.*, 1996; Wadley and Bond, 1997).

In the gravitational instability scenario of structure formation, cosmological structures grow from smaller structures through gravity. The growth of structures is governed by the coupled gravity-fluid equations describing both the collisionless gravitating matter component and the collisional baryonic component. Because of the enormous change in spatial scales as the Universe expands, it is convenient to solve the equations in a frame comoving with the expansion (Peebles, 1993). The physical position \mathbf{r} and velocity \mathbf{u} are then expressed in terms of the comoving position \mathbf{x} and peculiar velocity \mathbf{v} according to

$$\mathbf{r} = a(t)\mathbf{x}, \quad \mathbf{u} = \dot{\mathbf{r}} = \dot{a}\mathbf{x} + \mathbf{v}, \quad (88)$$

where $\mathbf{v} = a\dot{\mathbf{x}}$ and $a(t) = 1/(1+z)$ is the cosmological expansion factor corresponding to the cosmological epoch at the redshift z .

The dynamical equations for the dark matter component are

$$d\mathbf{x}_d/dt = \mathbf{v}_d(\mathbf{x}, t)/a, \quad (89)$$

$$\frac{d\mathbf{v}_d(\mathbf{x}, t)}{dt} + \frac{\dot{a}}{a}\mathbf{v}_d = -\frac{1}{a}\nabla\phi(\mathbf{x}, t), \quad (90)$$

where $\phi(\mathbf{x}, t)$ is the gravitational potential, and the gradient is with respect to the comoving coordinate system. The fluid equations expressing mass and momentum conservation are

$$\frac{\partial\rho(\mathbf{x}, t)}{\partial t} + 3\frac{\dot{a}}{a}\rho + \frac{1}{a}\nabla\cdot[\rho(\mathbf{x}, t)\mathbf{v}(\mathbf{x}, t)] = 0, \quad (91)$$

$$\begin{aligned} \frac{\partial\mathbf{v}(\mathbf{x}, t)}{\partial t} + \frac{\dot{a}}{a}\mathbf{v}(\mathbf{x}, t) + \frac{1}{a}[\mathbf{v}(\mathbf{x}, t)\cdot\nabla]\mathbf{v}(\mathbf{x}, t) \\ = -\frac{1}{\rho a}\nabla p(\mathbf{x}, t) - \frac{1}{a}\nabla\phi(\mathbf{x}, t), \end{aligned} \quad (92)$$

where $\rho(\mathbf{x}, t)$ and $p(\mathbf{x}, t)$ are the gas density and pressure at \mathbf{x} at cosmological time t . Because the evolution equation for the entropy, Eq. (51), is already in the comoving frame, it remains the same with the understanding that d/dt is replaced by $\partial/\partial t + (1/a)\mathbf{v}(\mathbf{x}, t)\cdot\nabla$ (Peebles, 1993). The heating and cooling terms include the physical processes discussed in Sec. III.B. The evolution of the ionization state of a mixture of hydrogen and helium is given by Eqs. (46). The inclusion of ionization assumes a given set of H I, He I, and He II, photoionization rates and photoheating rates. These must be computed from the ambient radiation field. The initial ionization state of

the gas is set during the passage of ionization fronts produced by radiation sources that photoionized the gas during the epochs of hydrogen and helium reionization. This is discussed in Sec. VII.

The dark matter and fluid are coupled through Poisson's equation for the gravitational potential

$$\nabla^2\phi = 4\pi G a^2[\rho_{\text{tot}}(\mathbf{x}, t) - \langle\rho_{\text{tot}}\rangle], \quad (93)$$

where $\rho_{\text{tot}} = \rho_d + \rho$ is the total mass density of the dark matter and fluid combined, $\langle\rho_{\text{tot}}\rangle$ is the spatial average of ρ_{tot} over the Universe, and $p \ll (\rho_{\text{tot}} - \langle\rho_{\text{tot}}\rangle)c^2$ has been assumed. In terms of the present-day matter closure parameter Ω_m , $\langle\rho_{\text{tot}}\rangle = 3H_0^2\Omega_m/8\pi G a^3$. Equations (89)–(93) are valid for any Friedmann-Robertson-Walker universe, including those with nonzero vacuum energy (such as an effective cosmological constant).

These are the same equations that describe the mix of dark matter, baryons, and radiation that gives rise to the cosmic microwave background, except for the addition of the radiation energy density and pressure. The principal difference is that while the density fluctuations are linear for the CMB up to the time the baryons begin to recombine and decouple from the radiation, the description of the growth of cosmological structures extends the computation of the fluctuations into the nonlinear regime. Numerical solutions to Eqs. (89)–(93) generally begin at a sufficiently high redshift that the primordial density fluctuations are still linear on the scales of interest, but after the matter and radiation have decoupled. The most convenient set of boundary conditions for solving the partial differential equations (PDEs) for the coupled dark matter and gas on cosmological scales is to assume that all variables are periodic over the simulation volume. It is, therefore, important that the simulation volume be sufficiently large to represent a fair sample of the Universe.

No structures will form unless the matter is initially inhomogeneous. The inhomogeneity is usually specified in terms of a primordial power spectrum of matter fluctuations, which is the ensemble average of the squared modulus of the Fourier modes of the density field. The mass density expanded in Fourier modes within a periodic Cartesian volume V_{box} may be expressed as

$$\rho(\mathbf{x}, t) = \langle\rho\rangle\left(1 + \sum_{\mathbf{k}\neq 0} \delta_{\mathbf{k}}(t)\exp(-i\mathbf{k}\cdot\mathbf{x})\right), \quad (94)$$

where the Fourier amplitudes $\delta_{\mathbf{k}}(t)$ are assumed to have random phases and to be distributed according to a Gaussian random process. The power spectrum, which quantifies the amplitude of the density fluctuations, may be defined as $P(k) = V_{\text{box}}\langle|\delta_{\mathbf{k}}|^2\rangle$, where the average is over independent statistical realizations of the Fourier amplitudes.

The real-space analog of the power spectrum is the spatial correlation function $\xi(r)$ of the density field,

$$\langle \rho(\mathbf{x}' + \mathbf{x})\rho(\mathbf{x}') \rangle = \langle \rho \rangle^2 [1 + \xi(\mathbf{x})], \quad (95)$$

where the average is carried out over all spatial locations \mathbf{x}' . The correlation function is related to the power spectrum through a Fourier transform

$$\xi(\mathbf{x}) = \frac{1}{(2\pi)^3} \int d^3k \left(P(k) - \frac{1}{n_p} \right) \exp(-i\mathbf{k} \cdot \mathbf{x}), \quad (96)$$

where n_p is the mean spatial density of the particles, and the Poisson noise contribution due to an average number of $n_p V_{\text{box}}$ particles per simulation volume has been subtracted.

It is convenient to define the amplitude of density fluctuations

$$\Delta^2(k) = (k^3/2\pi^2)P(k). \quad (97)$$

The amplitude of mass fluctuations $(\delta M/M)^2$ in a sphere of radius r_f is then given by

$$\sigma_{r_f}^2 = \int_0^\infty \frac{dk}{k} \Delta^2(k) \left(\frac{3j_1(kr_f)}{kr_f} \right)^2, \quad (98)$$

where $j_1(x) = (\sin x)/x^2 - (\cos x)/x$ is a spherical Bessel function. A common fiducial normalization measure is the mass fluctuation σ_8 filtered on a scale of $r_f = 8h^{-1}$ Mpc, where $h = H_0/100$ km s $^{-1}$ Mpc $^{-1}$. The spectrum of matter fluctuations may be expressed in the form

$$\Delta^2(k, z) = \delta_H^2 \left(\frac{ck}{H_0} \right)^{3+n} \frac{D^2(z)}{D^2(0)} T^2(k), \quad (99)$$

where $T(k)$ is the transfer function describing the evolution of density perturbations as they cross the present-day horizon scale with amplitude δ_H , n is the spectral index, and $D(z)$ is the growth factor for the density perturbations (see Sec. V.C). The transfer function for a cold-dark-matter-dominated universe was first computed by Peebles (1981). A fast numerical code for computing the transfer function to high accuracy is provided by Eisenstein and Hu (1999).

2. Methods of numerical simulations

Several numerical methods have been developed for solving the combined gravity-fluid equations. The most common methods for solving the dark matter evolution equations sample the distribution function of the dark matter using massive pseudoparticles and solve for their evolution either on a mesh or using a hierarchical tree. The most common mesh codes use either the particle-mesh (PM) or particle-particle particle-mesh (P³M) techniques. Tree algorithms instead arrange the particles into a hierarchy of groups and approximate the forces exerted by distant groups on a given particle by their lowest multiple moments. The fluid equations are frequently solved using a finite-difference representation of the fluid equations, handling shocks either with artificial viscosity or through shock capturing. An alternative scheme, smoothed particle hydrodynamics (SPH), smooths the fluid equations and samples the smoothed

fluid variables using pseudoparticles. The algorithm is intrinsically Lagrangian in nature. A comparison of two publicly available codes using these methods, ENZO and GADGET, is provided by O'Shea *et al.* (2005). The paper also serves as a good entry point to the vast literature on the subject. A more general overview of N -body methods is provided by Bertschinger (1998).

All of the techniques share a common method for initiating the density fluctuations and associated peculiar velocity field based on the Zel'dovich approximation (Efstathiou *et al.*, 1985). Substituting $\mathbf{v}_d = a\dot{\mathbf{q}}_d = -a\dot{D}(t)\nabla\Psi(\mathbf{q}_d)$, using Eq. (87) for the dark matter, into the equation for peculiar velocity from Eq. (90) gives

$$\Psi(\mathbf{q}_d) = \phi(\mathbf{q}_d, t)/4\pi G\langle\rho_{\text{tot}}\rangle a^2 D + \text{const}, \quad (100)$$

after noting that $a\ddot{D} + 2\dot{a}\dot{D} = 4\pi G\langle\rho_{\text{tot}}\rangle aD$, which follows from Eq. (91) applied to the combined dark matter and gas density. The initial deformation is, therefore, proportional to the gravitational potential ϕ (up to an arbitrary integration constant). This offers a straightforward prescription for specifying the initial conditions. First, choose the $\delta_{\mathbf{k}}$'s according to a Gaussian random process: $\delta_{\mathbf{k}} = \sqrt{P(k)}g \exp(i\theta)$, where g is a Rayleigh random deviate in the range $0 < g < \infty$ with unit mean and unit variance, and θ is a random phase uniformly distributed over $0 < \theta < 2\pi$. In Fourier space, the gravitational potential is $\phi_{\mathbf{k}} = -4\pi G a^2 \langle\rho_{\text{tot}}\rangle \delta_{\mathbf{k}} k^{-2}$ since the Fourier transform of $\nabla^2\phi$ is $-k^2\phi_{\mathbf{k}}$, where $\phi_{\mathbf{k}}(t)$ is the Fourier transform of $\phi(\mathbf{q}, t)$. The gravitational potential may then be constructed from

$$\begin{aligned} \phi(\mathbf{q}, t) &= \sum \phi_{\mathbf{k}} \exp(-i\mathbf{k} \cdot \mathbf{q}) \\ &= -4\pi G a^2 \langle\rho_{\text{tot}}\rangle \sum \frac{\delta_{\mathbf{k}}}{k^2} \exp(-i\mathbf{k} \cdot \mathbf{q}). \end{aligned} \quad (101)$$

The deformation function $\Psi(\mathbf{q}_d)$ then follows from Eq. (100). The displacements and velocities of the particles then follow from Eqs. (87),

$$\mathbf{x} = \mathbf{q} - \sum \frac{i\mathbf{k}}{k^2} \delta_{\mathbf{k}} \exp(-i\mathbf{k} \cdot \mathbf{q}), \quad (102)$$

$$\mathbf{v} = -a \frac{\dot{D}}{D} \sum \frac{i\mathbf{k}}{k^2} \delta_{\mathbf{k}} \exp(-i\mathbf{k} \cdot \mathbf{q}). \quad (103)$$

The optimal form of these equations allows for convolution with the differencing operator used to evaluate the gradient of the gravitational potential (Efstathiou *et al.*, 1985). Once initiated, any of the various numerical methods described above may be used to evolve forward the dark matter and baryon fluctuations into the nonlinear regime.

The resolution requirements of the simulations depend on the statistical quantity for which convergence is sought. While the demands for convergence on the HI column density distribution over the range $13 < N_{\text{HI}} < 15$ are not very severe, the early simulations tended to overestimate the width of the absorption features. It is now recognized that good convergence on the Doppler

parameter distribution and of the pixel flux distribution requires at the minimum good resolution of the Jeans length (Theuns *et al.*, 1998; Bryan *et al.*, 1999). A resolution of $9h^{-1}$ kpc (comoving) is about the right level at $z=2$, but still inadequate by $z \geq 3$ (Bryan *et al.*, 1999), although the rate of convergence is sensitive to the gas temperature and assumed cosmology. Slightly coarser resolution is adequate for converging on the pixel flux distribution. A large simulation volume is required to ensure that the full contribution of long-wavelength modes is included (Wadsley and Bond, 1997; Theuns *et al.*, 1998; Bryan *et al.*, 1999), requiring a box size of at least $5h^{-1}$ Mpc (comoving). Similar demands are found using pure dark matter pseudohydrodynamics simulations, for which sequences of large high-resolution simulations have been performed to test convergence (Meiksin and White, 2001). Matching both the resolution and box-size requirements demands simulations of minimally 512^3 zones, and preferably 1024^3 zones for grid-based codes to achieve good convergence on the properties of low H I column density systems. Similar numbers of particles are required for SPH computations. Even with these parameters, converging on the extremes in the temperature distribution proves difficult. Such large hydrodynamics simulations are only now becoming feasible.

The simulations show that the baryons closely trace the distribution of dark matter down to the Jeans length scale, when pressure forces prevent further collapse of the baryons. This has prompted an alternative approach to IGM simulations based solely on the evolution of the dark matter (Petitjean *et al.*, 1995; Croft *et al.*, 1998; Meiksin and White, 2001). The gas overdensity is either set equal to the dark matter overdensity or found by allowing for a pressure by treating it as a modification to the gravitational potential in the hydrodynamics particle mesh (HPM) approach (Gnedin and Hui, 1998). The gas temperature is solved for either by allowing for photoelectric heating and radiative cooling (Petitjean *et al.*, 1995) or through a polytropic equation of state $T = T_0(\rho/\langle\rho\rangle)^\gamma$. This alternative is based on the recognition by Hui and Gnedin (1997) that the temperatures found in numerical hydrodynamics simulations are determined largely through a balance between photoelectric heating and adiabatic cooling losses for structures with overdensities $\rho/\langle\rho\rangle < 5$. Comparisons with full hydrodynamical computations show that using a PM code or HPM code with a polytropic equation of state gives a reasonably good description of the properties of the IGM properties, including its absorption statistics (Meiksin and White, 2001; Viel *et al.*, 2002, 2006), although full hydrodynamics simulations should still be used for detailed comparisons to the data.

Yet another approach altogether is to generate the density fluctuations stochastically from a log-normal distribution (Bi *et al.*, 1992; Bi, 1993; Bi and Davidsen, 1997). This approach captures many of the qualitative features of the structure of the IGM and provided an early argument that the Ly- α forest itself may be accounted for by density fluctuations in a diffuse IGM.

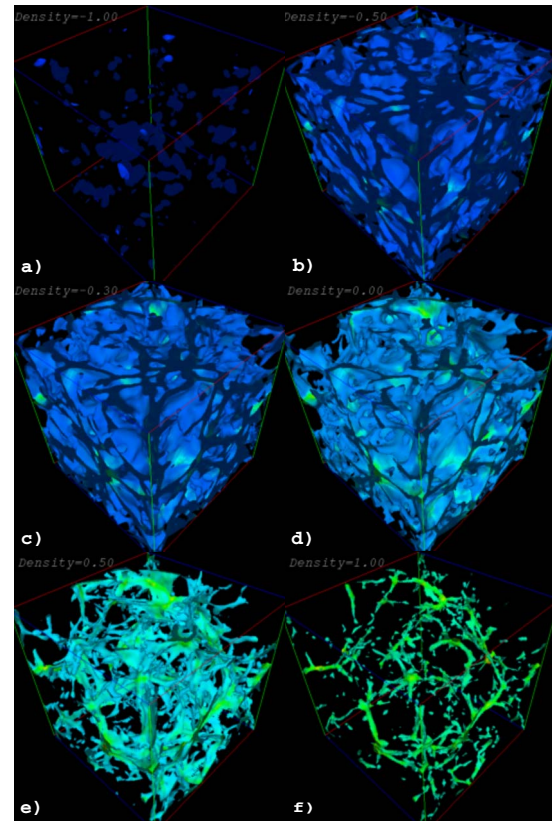


FIG. 13. (Color online) Isodensity contour surfaces of \log (baryon overdensity) at $z=3$ for a flat cold-dark-matter-dominated universe. The contour levels are $\log_{10}(\rho/\langle\rho\rangle) = -1.0, -0.5, -0.3, 0.0, 0.5, \text{ and } 1.0$. Low-density regions are amorphous structures filling sheets at the mean density which intersect at overdense filaments. The filaments intersect at highly overdense collapsed halos. From Zhang *et al.*, 1998. Figure reproduced by permission of the AAS.

B. Physical properties of the intergalactic medium

The results of structure formation simulations show that the IGM fragments into an interconnected network of sheets, filaments, and halos (Cen *et al.*, 1994; Zhang *et al.*, 1995; Katz *et al.*, 1996; Miralda-Escudé *et al.*, 1996; Wadsley and Bond, 1997). The various morphologies correspond to different physical densities and different H I column density absorption systems. These dependences are illustrated in Figs. 13 and 14, taken from the simulation of Zhang *et al.* (1998) of a cold-dark-matter-dominated Einstein-de Sitter universe with the radiation field from Haardt and Madau (1996) based on QSO sources. The simulation volume was 9.6 Mpc (comoving) on a side, and the power spectrum was normalized to $\sigma_8=0.7$ with $h=0.5$. At $z=3$, systems with $N_{\text{HI}} \leq 10^{13} \text{ cm}^{-2}$ arise from the amorphous underdense regions enclosed by the sheets. The underdense regions have characteristic diameters of a few comoving Mpc, and occupy most of the volume of the Universe. The sheets have densities comparable to the mean baryon density, and give rise to absorption systems with $10^{13} \leq N_{\text{HI}} \leq 10^{14} \text{ cm}^{-2}$. Systems with $10^{14} \leq N_{\text{HI}} \leq 10^{15} \text{ cm}^{-2}$

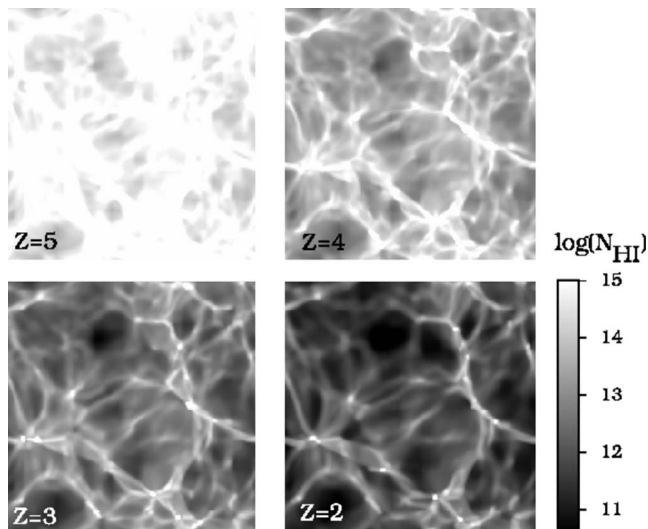


FIG. 14. Evolution of the H I column density. The filamentary structure of the IGM is nearly stationary in the comoving frame. By contrast, the decline in the physical gas density results in rapid evolution of the H I column density, and the IGM becomes increasingly transparent with time. From Zhang *et al.*, 1998. Figure reproduced by permission of the AAS.

originate in the filaments, which are moderately overdense structures ($1 \leq \rho/\langle\rho\rangle \leq 5$). Higher-column-density systems, with $N_{\text{HI}} \geq 10^{15} \text{ cm}^{-2}$, arise in spheroidal nodes with overdensities of several to over 100 embedded within the filaments.

The mean temperatures of overdense systems range over $10^4 - 3 \times 10^4 \text{ K}$ (Cen *et al.*, 1994; Theuns *et al.*, 1998; Zhang *et al.*, 1998), while Miralda-Escudé *et al.* (1996) found mean temperatures up to $6 \times 10^4 \text{ K}$. These larger values may be due to the hard UV background assumed. Much higher temperatures are also found, extending up to $10^6 - 10^7 \text{ K}$, for gas associated with collapsed halos (Theuns *et al.*, 1998). There is less agreement on the temperatures in the underdense regions. The time to achieve thermal equilibrium exceeds a Hubble time for underdense gas (Meiksin, 1994; Miralda-Escudé and Rees, 1994). The gas temperature will, therefore, reflect the thermal history of the gas following reionization, and so is sensitive to the particular reionization model. The Ly- α forest simulations also did not take into account the heating effects of reionization itself (Tittley and Meiksin, 2007).

The thicknesses of the filaments are approximately 100 kpc (proper), with coherence lengths of about 1 Mpc. The scales are consistent with the observational constraints based on neighboring line-of-sight statistics discussed in Sec. II.B.3. This is comparable to the isothermal Jeans length. For a characteristic hydrogen number density of 55 m^{-3} , corresponding to five times the mean baryon density at $z=3$, and a characteristic temperature of $2 \times 10^4 \text{ K}$, the pressure is 10^6 K m^{-3} , and the Jeans length from Eq. (84) is 320 kpc.

The baryonic overdensity at $z=3$ is found to scale as $\rho/\langle\rho\rangle \approx 3(N_{\text{HI}}/10^{14} \text{ cm}^{-2})^{1/2}$, with the neutral fraction

scaling as $x_{\text{HI}} \approx 1.3 \times 10^{-5} (N_{\text{HI}}/10^{14} \text{ cm}^{-2})^{1/2} T_4^{-0.75} \Gamma_{\text{HI},-12}^{-1/2}$ (Zhang *et al.*, 1998). The neutral fraction dependency is comparable to the estimate in Sec. II.B.3, and results in virtually all baryons' residing in the Ly- α forest at $z > 1$.

The structure of the IGM at $z \ll 1$ differs somewhat from its structure at $z > 2$. Davé *et al.* (1999) obtained the relation between overdensity and H I column density of $\rho/\langle\rho\rangle \approx 20(N_{\text{HI}}/10^{14} \text{ cm}^{-2})^{0.7} e^{-0.4z}$, similar to the finding of Zhang *et al.* (1998) at $z=3$. A given overdensity results in H I column densities smaller by a factor of 10–50 at $z \ll 1$ than at $z > 2$. Most absorption systems at low redshift arise in systems with hydrogen densities of $n_{\text{H}} \approx 0.1 - 10 \text{ m}^{-3}$ for H I column densities of $N_{\text{HI}} \approx 10^{13} - 10^{15} \text{ cm}^{-2}$. Structures retain coherence over scales of several hundred kiloparsecs. The gas temperatures for structures with $\rho/\langle\rho\rangle < 10$ are about a factor of 2 smaller at $z \ll 1$ than at $z > 2$. A hot intermediate-density gas phase also arises from shocks in filaments and in galaxy, galaxy group, and galaxy cluster halos, reaching temperatures of over 10^7 K .

C. Statistical properties of the absorption systems

1. Mean metagalactic ionization rates

Almost all that is directly known about the structure of the IGM is derived from spectra. The simulation results must, therefore, be translated into spectra for comparison against observational data to test the validity of the models. The spectra, normalized to a unit continuum level, may be expressed as $\exp(-\tau_\nu)$, where τ_ν , the IGM optical depth as a function of frequency, is given by Eq. (14). Allowing for a peculiar velocity v varying along the line of sight,

$$\tau_\nu = \int dz' \frac{dl_p}{dz'} n(z') \sigma \left[\nu(1+z') - \nu_{lu} \left(1 - \frac{v}{c} \right) \right]. \quad (104)$$

Setting $n = \langle n \rangle (1 + \delta)$, where δ is the local density contrast, Eq. (104) is identical to Eq. (15) for the Gunn-Peterson effect in the absence of perturbations ($v = \delta = 0$). For this reason, the varying optical depth of the IGM is sometimes referred to as giving rise to a “fluctuating Gunn-Peterson effect” (Miralda-Escudé and Rees, 1993; Cen *et al.*, 1994).

An example of a spectrum generated from the Λ CDM simulation of Cen *et al.* (1994) with $\Omega_v = 0.6$, $\Omega_m = 0.4$, $h = 0.65$, and normalization $\sigma_8 = 0.79$ is shown in Fig. 15. The temperature variations closely trace the baryon density fluctuations. The absorption features are slightly offset from the density features due to the peculiar motion of the gas. Mild overdensities produce weak features while large overdensities produce stronger features. The apparently isolated absorption features arise not from distinct clouds but from modulations in the density field produced by the gravitational instability of primordial density fluctuations.

Any comparison between the simulated and measured spectra requires normalization by the uncertain ioniza-

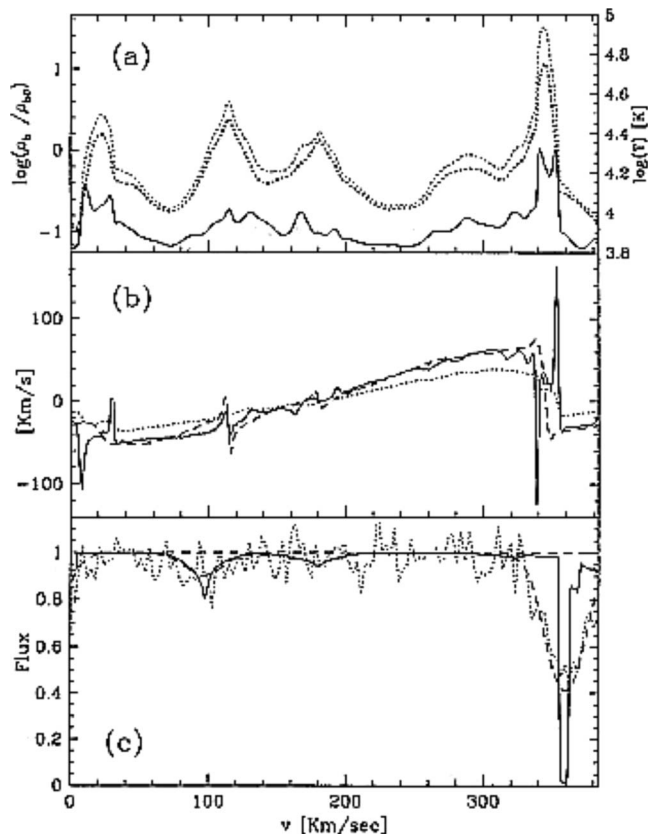


FIG. 15. A line-of-sight cut through a Λ CDM simulation of the Ly- α forest at $z=3$. The top panel shows the gas temperature (solid line), gas density (thick dotted line), and gas pressure, in arbitrary units (thin dotted line). All are shown as a function of the spatial coordinate r expressed in velocity units through $v=Hr$, for $H=512h \text{ km s}^{-1} \text{ Mpc}^{-1}$. The gas temperature and density are closely correlated. The middle panel shows the peculiar velocity (dotted line), the gravitational acceleration divided by the Hubble constant (dashed line), and the total hydrostatic and gravitational acceleration divided by the Hubble constant (solid line). An infalling peculiar velocity pattern forms around a collapsing structure near $v \approx 360 \text{ km s}^{-1}$. The bottom panel shows the transmission factor $\exp(-\tau_\nu)$ before convolving with a Doppler profile (solid line), after convolution with a Doppler profile (dashed line), and after adding the effects of instrumental resolution and noise (dotted line). From Cen *et al.*, 1994. Figure reproduced by permission of the AAS.

tion rates for H I and He II. The uncertainty in the normalization rate for He II is compounded by the unknown epoch of He II reionization, which may have been as late as $z \approx 3$. Late He II reionization will also affect the gas temperatures, particularly for underdense gas. This in turn affects the optical depth through the gas. Much of the uncertainty on global flux properties may be removed by normalizing to the measured mean Ly- α transmission $\langle \exp(-\tau_\nu) \rangle$ of the IGM. Although an error in the temperature of the gas will result in a small offset in the inferred ionization rate [see Eq. (42)], once normalized, the probability distribution of the emissivity is only slightly affected. Altering the temperature of the gas as required by the line widths, either directly or by

boosting the heating rate, can further improve the fits.

Various groups have provided estimates for the H I ionization rate Γ_{HI} based on matching their simulation results to measurements of the mean Ly- α transmissivity. Results from Meiksin and White (2004), Bolton *et al.* (2005), and Bolton and Haehnelt (2007) are shown in Table V. All predicted rates are in reasonably good agreement. Bolton and Haehnelt (2007) provided an additional estimate at $z=2$ of $\Gamma_{\text{HI},-12} = 1.29^{+0.80}_{-0.46}$, which agrees well with the estimate from Tytler, Kirkman, *et al.* (2004) of $\Gamma_{\text{HI},-12} = 1.44 \pm 0.11$. An additional uncertainty of a few to several percent may result from fluctuations in the ionizing background (Gnedin and Hamilton, 2002; Croft, 2004; Meiksin and White, 2004). A comparison of the required ionization rates with the predictions from QSO sources shows that unless there is a large population of low-luminosity AGN so far undetected at high redshifts, QSOs alone are unable to provide the required ionization rates at $z \gtrsim 3$.

Specifying Γ_{HI} fixes the entire equilibrium ionization structure of the gas (except in isolated optically thick regions). This permits the contribution of the IGM to the attenuation length of ionizing photons to be determined directly from a simulation. In principle, a self-consistent solution for the equilibrium structure of the IGM may then be obtained, including the magnitude of the required emissivity for any given spectral shape using Eq. (73). Meiksin and White (2004) found for a Λ CDM cosmology the (proper) attenuation length is approximated to 10% accuracy by

$$r_0 \approx 1.7 \times 10^4 (1+z)^{-4.2} h^{-1} \text{ Mpc} \quad (105)$$

for $2.75 < z < 5.5$. Because the simulation underpredicts the number of Lyman limit systems by a large factor, these are added using the results of Stengler-Larrea *et al.* (1995). It is found that the diffuse gas comprising the Ly- α forest and the Lyman limit systems contribute about equally to the attenuation length, consistent with models based on direct line counts (Meiksin and Madau, 1993). The implied (comoving) metagalactic emissivity at the Lyman edge required to recover the H I ionization rates is (Meiksin 2005)

$$\epsilon_L \approx A_{\text{MG}} \left(\frac{3 + \alpha_{\text{MG}}}{3} \right) (1+z)^\gamma h \text{ W Mpc}^{-3}, \quad (106)$$

where $A_{\text{MG}} = 8.4^{+9.7,31}_{-4.5,6.5} \times 10^{18}$, $\gamma = -1.6 - 0.6 \ln(A_{\text{MG}}/8.4 \times 10^{18})$, and α_{MG} is the spectral index of the metagalactic emissivity, $\epsilon_\nu = \epsilon_L (\nu/\nu_L)^{-\alpha_{\text{MG}}}$. The errors on A_{MG} are the 1σ and 2σ limits.

At $z > 4$, Eq. (106) is well above the predictions from QSO counts. As discussed in Sec. IV.A.2, Eq. (106) may be matched by the emissivity of galaxies at the Lyman edge for plausible escape fractions of the ionizing radiation.

2. Spectral properties of the IGM

The predicted spectral properties of the Ly- α forest are sensitive to the cosmological parameters used

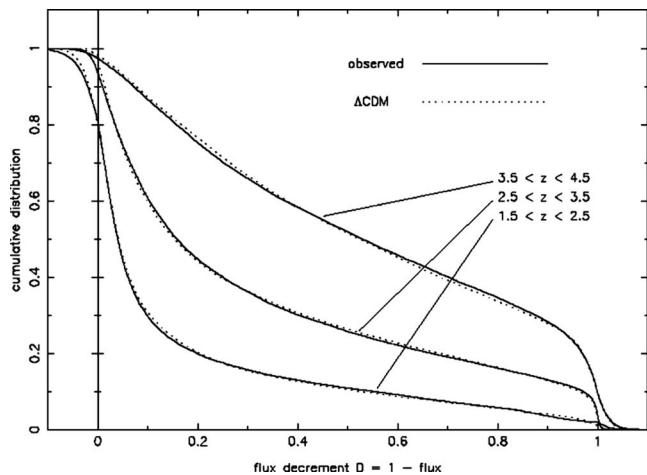


FIG. 16. Comparison of the cumulative flux per pixel distribution from a Λ CDM simulation with data based on high-resolution Keck spectra of seven QSOs. The data have been grouped into three redshift intervals and the observations corrected to take into account evolution in the mean transmission within each interval. Noise has been added to the simulated data to match the noise properties of the measured spectra. From Rauch, Miralda-Escudé, *et al.*, 1997. Figure reproduced by permission of the AAS.

(Rauch, Miralda-Escudé, *et al.*, 1997; Wadsley and Bond, 1997; Theuns *et al.*, 1999; Machacek *et al.*, 2000; Jena *et al.*, 2005). Comparisons with the spectral properties of the Ly- α forest have shown agreement for plausible cosmological models. Machacek *et al.* (2000) showed that the distribution of optical depth per pixel in the models is well fitted by a log-normal distribution for values in the range $0.02 < \tau < 4$, roughly the measurable range. This prediction is confirmed by the observations of Becker *et al.* (2007), who found that the flux distributions in 55 high-resolution QSOs are well reproduced by log-normal distributions for the underlying optical depths. Detailed comparisons show that the predicted cumulative distributions of pixel fluxes agree to a precision of a few percent with measurements in individual QSO spectra (Meiksin *et al.*, 2001).

These results suggest that the Ly- α forest may be used as an effective tool for selecting between rival cosmological models of structure formation. An example of a comparison between the Λ CDM simulation discussed above and high-signal-to-noise-ratio high-resolution Keck spectra of seven QSOs is shown in Fig. 16 (Rauch, Miralda-Escudé, *et al.*, 1997). Machacek *et al.* (2000) and Meiksin *et al.* (2001) found that the shape of the pixel flux distribution and the magnitude of the Doppler parameters vary systematically with the normalization on small scales, like σ_J filtered on the Jeans scale, as defined by Eq. (98) with filter scale $r_J = \lambda_J$ from Eq. (84). A detailed comparison between the predicted flux distributions for several cosmological models and measurements from several high resolution Keck spectra constrains σ_J , defined for an isothermal gas at $T = 2 \times 10^4$ K, in the range $1.3 \lesssim \sigma_J \lesssim 1.7$ at $z = 3$ (Meiksin *et al.*, 2001), although this is somewhat subject to the uncertain thermal

properties of the gas. The closest agreement is found for the larger values of σ_J . A range of Λ CDM models, however, shows that agreement with σ_8 inferred from WMAP measurements of CMB fluctuations prefers lower values (Meiksin and White, 2004), so that there is some tension between the higher normalization preferred by the Ly- α forest simulations and the lower normalization preferred by the CMB measurements.

Voigt profile fitting to the spectra permits comparison between the predicted and measured H I column density and Doppler parameter distributions. Here the models fare somewhat less well compared with the pixel flux distribution. The models successfully reproduce the H I column density distributions to good accuracy over a wide range of values of $14 \lesssim \log_{10} N_{\text{HI}} \lesssim 16$ at high redshifts ($2 < z < 4$) (Cen *et al.*, 1994; Zhang *et al.*, 1995, 1997; Hernquist *et al.*, 1996; Wadsley and Bond, 1997; Meiksin *et al.*, 2001) and at moderate to low redshifts ($0 < z < 2$) (Davé *et al.*, 1999; Paschos *et al.*, 2008). A discrepancy is found at higher column densities, with simulations generally finding fewer systems with $\log_{10} N_{\text{HI}} > 16$ than measured. This is particularly true for Lyman limit systems (Katz *et al.*, 1996; Meiksin and White, 2004), although extrapolation of the simulation results to smaller mass halos suggests that agreement is possible, depending on the appropriate minimum circular velocity of halos able to produce high H I column density systems in the metagalactic photoionizing background (Gardner *et al.*, 2001). A smaller discrepancy is found for DLAs. The simulations of Nagamine *et al.* (2007) suggest that the incidence of DLAs may be met if they are associated with halos having masses as low as $10^{8.5} h^{-1} M_{\odot}$.

It is less clear that all Lyman limit systems arise from collapsed halos. Allowing for radiative transfer effects, Kohler and Gnedin (2007) found their simulations produce Lyman limit systems from material bound to and falling onto galaxies rather than from minihalos. It is possible the systems have more than a single origin.

Because the detailed distribution of the absorption line parameters is sensitive to the method of line finding and fitting (see Sec. II.B.1), a definitive comparison between the simulations and the measured absorption line properties requires identical line analysis methods. Automation of the line analysis is necessary for processing the large number of lines of sight from simulations to build up reliable statistics. A few codes are publicly available. An industry standard is VPFIT,¹⁹ a sophisticated code that handles in addition to H I features a wide range of metal lines. A simpler alternative well adapted to automated fitting of H I features is AUTOVP (Davé *et al.*, 1997). Based on fits with AUTOVP, Davé *et al.* (1997) found that the simulations predict a greater fraction of lower-Doppler-parameter systems than measured. Similar discrepancies were found by Bryan *et al.* (1999) and Theuns *et al.* (1999).

¹⁹<http://www.ast.cam.ac.uk/~rfc/vpfit.html>

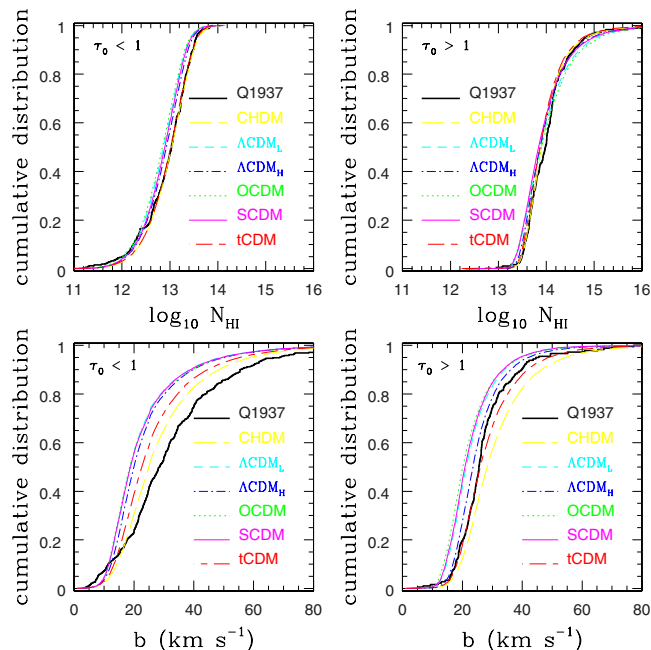


FIG. 17. (Color online) Comparison of the cumulative H I column density (upper panels) and Doppler parameter (lower panels) distributions for the Ly- α forest measured along the line of sight to the QSO Q1937-1009 with predictions for six cosmological models: a standard CDM model (SCDM), two Λ CDM models with high (Λ CDM_H) and low (Λ CDM_L) baryon densities, an open CDM model (OCDM), a tilted CDM model (tCDM), and a mixed hot dark matter and cold dark matter model (CHDM). Much better agreement is found for absorption line systems with line center optical depths $\tau_0 > 1$ (right panels) than for $\tau_0 < 1$ (left panels). From Meiksin *et al.*, 2001. Figure reproduced by permission of the RAS and Blackwell Publishing.

A detailed comparison between several high-resolution QSO spectra and numerical simulations for a variety of models, analyzed using AUTOVP and a similar code, SPECFIT, by Meiksin *et al.* (2001) showed that it is not possible to match simultaneously the pixel flux distributions, column density distributions, and Doppler parameter distributions using simulations with optically thin reionization. While adjusting σ_j may help to match the Doppler parameters, it destroys agreement with the pixel flux distribution. In Fig. 17, a comparison is shown between the predicted and measured line parameter distributions for the Ly- α forest detected in the spectrum of the $z=3.8$ QSO Q1937-1009. The systems have been isolated by their line center optical depths. The comparisons show that the discrepancies are due primarily to the low-optical-depth systems, with line center optical depths $\tau_0 < 1$.

The origin of the discrepancies is most likely the temperature of the gas. Artificial broadening of the absorption features gives good agreement between the measurements and predictions of the Λ CDM_L model for the pixel flux and column density distributions, and good agreement between the Doppler parameter distributions. Since the optically thin absorbers arise in under-

dense regions, the temperature of the gas will retain a memory of its heating history. Since the underdense gas occupies most of the volume of the Universe, whatever heated the gas must have been ubiquitous. The best candidate is late reionization of He II, in the redshift interval $3 < z < 4$. This would boost the gas temperature, possibly by the required amount. The effects of heating by late He II reionization may be mimicked to some extent by boosting the He II heating rate (Bryan and Machacek, 2000; Tytler, Kirkman *et al.*, 2004), but the only fully satisfactory solution requires incorporating radiative transfer (Tittley and Meiksin, 2007).

With the goal of developing a physical description for the origin of the Doppler parameter distribution, Hui and Rutledge (1999) introduced a semianalytic approach based on the growth of the density perturbations to derive a Doppler parameter distribution of the form

$$dN/db = (4b_\sigma^4/b^5)\exp(-b_\sigma^4/b^4), \quad (107)$$

where b_σ is a fit parameter. Restricting their analysis to systems with column densities $12.5 \leq \log_{10} N_{\text{HI}} \leq 14$, corresponding to the physical conditions of the IGM for which their analysis best applies, Hui and Rutledge (1999) found that the distribution provides statistically acceptable matches to the Doppler parameter distributions of the Ly- α forest along the lines of sight to four QSOs with high resolution Keck spectra (Hu *et al.*, 1995). Adequate matches, however, were not found for Q0000-26 (Lu, Sargent, Womble, and Takada-Hidai, 1996) or HS 1946+7658 (Kirkman and Tytler, 1997a). The Doppler parameter distributions measured in the spectra of all six of the QSOs, without any restriction on the column density range applied, are well fitted by log-normal distributions (see Table II). Ricotti *et al.* (2000) generalized Eq. (107) to

$$\partial^2 \mathcal{N} / \partial N_{\text{HI}} \partial b \propto N_{\text{HI}}^{-\alpha} (b_*/b)^\varphi \exp[-(b_*/b)^\Phi], \quad (108)$$

where α is a fit constant, and φ , Φ , and b_* are allowed mild dependences on the column density. The best fits obtained for absorbers in several lines of sight over the redshift range $2.5 \leq z \leq 4$ have $1.6 < \alpha < 2.1$, $2.6 < \varphi < 5.9$, and $2.0 < \Phi < 7.2$, with values almost independent of column density.

Several attempts have been made to infer the temperature of the IGM directly from the Doppler parameter distribution. One approach is to normalize the distributions using simulations, invoking additional sources of heat input to allow for a range in temperatures (Bryan and Machacek, 2000). Another exploits a polytropic relation between the gas density and temperature (Hui and Gnedin, 1997; Schaye *et al.*, 1999), calibrated using numerical simulations. Both methods rely on numerical simulations that neglect the effect of reionization on the temperature of the underdense gas, which may be substantial (Abel and Haehnelt, 1999; Bolton *et al.*, 2004; Tittley and Meiksin, 2007). Modeling the Doppler parameter distributions according to Eqs. (107) and (108) to obtain lower cutoff values, Ricotti *et al.* (2000) and Schaye, Theuns, *et al.* (2000) found evidence for a

temperature jump and reduction in the polytropic index toward isothermality near $z=3.0$. Both groups attributed their results to late He II reionization. He II reionization simulations predict a more gradual change (McQuinn *et al.*, 2009). No significant change in the temperature or polytropic index over the redshift range $2.4 < z < 3.9$ is found by McDonald *et al.* (2001, 2003). Although any conclusion using these methods is subject to the accuracy of the modeling assumptions made, the possibility of measuring an unambiguous temperature jump in this redshift range merits further investigation.

3. Intergalactic helium absorption

As for the H I absorption features, the numerical simulations predict the properties of He II absorption as well. The systems that dominate the measured He II optical depths arise from the diffuse structures in underdense regions (Zhang *et al.*, 1995; Croft *et al.*, 1997). This makes predictions for the He II optical depths difficult for two reasons: (1) high spatial resolution is required to accurately compute the structures in the underdense regions, and (2) the gas temperature is sensitive to the history of reionization since the time for the temperature to reach equilibrium is comparable to or longer than a Hubble time. The latter affects both the ionization fraction of He II because of the temperature dependence of the radiative recombination rate and the Doppler widths of the absorption features. Another uncertainty is the epoch of full helium reionization. The results of Zhang *et al.* (1995, 1998) suggest that matching to both the H I and He II Ly- α mean optical depth measurements at $2.5 \leq z \leq 3.3$ requires an ionization rate ratio of $\Psi \approx 250\text{--}400$, comparable to the inferred values from line statistics (Sec. IV.C.2) and corresponding to an intrinsic QSO spectral index of 1.8–2.0, allowing for filtering through the IGM (Haardt and Madau, 1996). A similar estimate is obtained from high-resolution numerical simulations by Bolton *et al.* (2006), who found values for Ψ rising from 139_{-67}^{+99} at $z=2.1$ to 301_{-151}^{+576} at $z=2.8$, assuming a spatially uniform UV background. Most of the uncertainty stems from the uncertainties in the measurements of the He II Ly- α mean optical depths. Allowing for spatial fluctuations in the QSO contribution lowers the inferred values for Ψ by about a factor of 2. Allowing for fluctuations also reproduces much of the observed scatter in the He II to H I column density ratio η (Sec. IV.C.2), except for the extreme excursions at $\eta < 10$ and $\eta > 200$.

4. Metal absorption systems

By providing the physical scales of density structures and their associated temperatures, the simulations permit estimates of the ionization states of metals for any assumed UV radiation field. Several observed features are reproduced by the models. The metal absorption features arise within the substructure of systems that give rise to the H I Ly- α features, and may result in multiple features corresponding to a single H I system

(Haehnelt *et al.*, 1996; Hellsten *et al.*, 1997; Rauch, Haehnelt, and Steinmetz, 1997; Zhang *et al.*, 1997). The frequencies of C II, C IV, Si IV, and N V systems are comparable to those observed at $z \approx 3$ assuming a QSO- or AGN-dominated UV background and metallicities of $[C/H] \approx -2.5$ (Hellsten *et al.*, 1997). The C IV to H I column density ratio decreases with increasing H I column density since higher column densities correspond to systems with higher densities and so lower ionization parameters (Hellsten *et al.*, 1997).

Hellsten, Hernquist, *et al.* (1998) ranked a variety of metal ions by their degree of detectability. The strongest absorption lines are the O VI $\lambda\lambda 1032, 1038$ Å doublet for low-column-density systems, with $N_{\text{H I}} < 10^{15} \text{ cm}^{-2}$. These lines unfortunately are very difficult to extricate from the Ly- α forest. The measured levels of O VI associated with C IV systems at $z \approx 3$ require an overabundance of $[O/C] \approx 0.5$, assuming a QSO- or AGN-dominated UV background, suggestive of enrichment by type II supernovae (Davé *et al.*, 1998). If helium was not fully ionized by $z \approx 3$, the resulting break between the H I and He II Lyman edges would require a much higher overabundance of oxygen. At least half the IGM must have helium fully reionized to keep $[O/C] < 10$.

Longward of the H I Ly- α line, the strongest lines are the C IV $\lambda\lambda 1548, 1551$ Å doublet for all systems with $N_{\text{H I}} < 10^{17} \text{ cm}^{-2}$. In high-column-density systems, the regions giving rise to C II absorption sometimes do not coincide with those giving the strongest C IV absorption, resulting in velocity offsets between the two.

At low redshift, the formation of galaxy groups and clusters will produce an outer region of high density $\rho/\langle\rho\rangle \approx 100$ and temperatures of $T \approx 10^5\text{--}10^7$ K, which will give rise to strong absorption lines of O VI (for temperatures $5.3 \leq \log_{10} T \leq 6.3$), O VII ($5.3 \leq \log_{10} T \leq 6.7$), and O VIII ($6 \leq \log_{10} T \leq 7.3$) in a warm-hot intergalactic medium (WHIM), detectable in the extreme ultraviolet and x ray (Hellsten, Gnedin, and Miralda-Escudé, 1998; Perna and Loeb, 1998; Cen and Ostriker, 1999; Davé *et al.*, 2001; Chen *et al.*, 2003; Viel, Branchini, *et al.*, 2003; Yoshida *et al.*, 2005). Especially of interest is the O VI $\lambda\lambda 1032, 1038$ Å doublet, which has already been detected in numerous systems at low redshifts (Danforth and Shull, 2005, 2008; Tripp *et al.*, 2008). For relatively high metallicities (at least 0.1 of solar), a few higher ionization species features may be detected by Chandra and XMM-Newton (Chen *et al.*, 2003). These, along with lines of carbon, nitrogen, and possibly neon and iron, may be detectable by the proposed x-ray satellites XEUS²⁰ (Chen *et al.*, 2003; Viel, Branchini, *et al.*, 2003) and Constellation-X²¹ (Petre *et al.*, 2007). The interpretation of the abundances, however, may be complicated by imperfect equilibration between the electron and ion temperatures in hot regions with $T \approx 10^7$ K (Yoshida *et al.*, 2005), unless collective plasma processes, such as scattering off Alfvén waves, are adequate for driving the

²⁰<http://www.rssd.esa.int/index.php?project=XEUS>

²¹<http://constellationx.nasa.gov>

electrons and ions into thermal equilibrium.

Predictions for low-ionization species are much more difficult. Observations suggest sizes for C II, Si II, Mg II, and Al II systems of typically below a kiloparsec, down to sizes of only about 1 parsec (Simcoe *et al.*, 2006). It is a challenge for any cosmological numerical simulation to produce such small, dense clumps.

5. The flux power spectrum

In addition to the direct flux and line parameter measurements, the models may also be tested by appealing to higher-order moments of the flux distribution. The one that has received the most attention is the flux power spectrum, as a vehicle for using the Ly- α forest to constrain cosmological models. Two broad approaches have been pursued. In the first, measurements of the flux power spectrum are inverted to obtain a measurement of the underlying dark matter power spectrum (Croft *et al.*, 1998, 1999; Hui, 1999; Nusser and Haehnelt, 1999). In the second, the flux power spectrum itself is used directly as a statistic to be matched by models (McDonald *et al.*, 2000, 2005; Mandelbaum *et al.*, 2003).

The basis of the inversion methods is the relation between the 1D and 3D matter power spectra (Lumsden *et al.*, 1989)

$$\Delta_{1D}^2(k) = k \int_k^\infty dy \frac{\Delta^2(y)}{y^2} \quad (109)$$

and

$$\Delta^2(k) = -k^2 \frac{d}{dk} \left(\frac{\Delta_{1D}^2(k)}{k} \right), \quad (110)$$

where $\Delta_{1D}^2(k)$ is the 1D mass fluctuation spectrum, related to the matter spatial correlation function $\xi(x)$ by

$$\xi(x) = \int_0^\infty \frac{dk_x}{k_x} \Delta_{1D}^2(k_x) \cos(k_x x). \quad (111)$$

Equation (109) shows that Δ_{1D}^2 depends on all small scales, well into the nonlinear range of density fluctuations. Because the flux along the line of sight to a QSO probes the 1D density field of the IGM, it might appear that any predictions require computation of the full nonlinear extent of the power spectrum to all small scales. Even the highest resolution simulations are unable to achieve convergence on Δ_{1D}^2 even at small k (Meiksin and White, 2004). The statistics of the 1D power spectrum are also notoriously non-Gaussian.

Such stringent demands for interpreting the flux power spectrum are avoided for two reasons: (1) the width of the absorption features acts to filter the 3D density field, erasing the smallest scale, nonlinear contributions to the 1D flux power spectrum; and (2) the inversion Eq. (110) at low k depends only on the behavior of the 1D flux power spectrum at low k . Numerical convergence on the 1D flux power spectrum $\Delta_F^2(k)$ at small k is achievable with sufficiently fine spatial resolution and a sufficiently large box size. A comoving box size of

$25h^{-1}$ Mpc with a force resolution of $30\text{--}60h^{-1}$ kpc (comoving) gives a flux power spectrum convergent to 10% on scales $k < 0.01 \text{ km}^{-1} \text{ s}$ at $z > 3$, with more severe requirements at lower redshifts (Meiksin and White, 2004). The greater ease of convergence for the flux power spectrum, however, pays the price of insensitivity to the underlying matter power spectrum. As a result, a large number of spectra are required to measure the matter power spectrum to high accuracy. A precision of 5% requires some 10^4 lines of sight (Zhan *et al.*, 2005).

Inversion methods have been further developed and applied by McDonald *et al.* (2000) and Croft, Weinberg, *et al.* (2002), who assumed the 1D flux power spectrum is proportional to the 1D matter spectrum up to a scale-dependent bias factor, $\Delta_F^2(k) = b^2(k) \Delta_{1D}^2(k)$, and by Nusser and Haehnelt (1999, 2000) and Zaroubi *et al.* (2006), who converted local optical depth measurements to local density estimates, assuming a power-law relation between the two.

In principle, the flux autocorrelation function may also be used to test models. Simulations, however, are found to converge even more slowly on this statistic, with convergence to better than 10% problematic for separations exceeding 3% of the box size (Meiksin and White, 2004).

Methods that rely on direct comparisons between the measured and predicted flux power spectra require a large grid of simulations to cover the range in expected cosmological model parameters. Because of the considerable computational expense involved in running full hydrodynamical simulations, McDonald *et al.* (2005) relied instead on a large grid of HPM pseudohydrodynamics simulations (see Sec. VI.A.2), calibrated by a few full hydrodynamics runs. These are computed using 256^3 cells in box sizes of $10h^{-1}$ Mpc (comoving) or smaller. This is well below the box size recommended by Meiksin and White (2004), who also found that the prediction for $\Delta_F^2(k)$ is sensitive to the method of smoothing at the several percent level near the peak and beyond (towards smaller values of k). In a comparison of full hydrodynamics simulations with HPM simulations in $30h^{-1}$ Mpc (comoving) boxes, Viel *et al.* (2006) found HPM simulations with many more grid zones (1200^3) than particles (2×200^3 for gas and dark matter) are required to converge to within 5% of the full hydrodynamics derived flux power spectrum on scales $k < 0.03 \text{ km}^{-1} \text{ s}$ at $z=3$ and 4. For 400^3 grid zones, the discrepancy is several percent and scale dependent. At $z=2$, convergence is even poorer, with disagreement as large as 20–30%, as shocks play an increasingly important role in heating the gas, an effect which an HPM simulation cannot account for.

A large number of physical systematic effects may also affect the flux power spectrum. The impact of galactic winds (Croft, Hernquist, *et al.*, 2002; McDonald, Seljak, *et al.*, 2005) and ionization radiation fluctuations (Croft *et al.*, 1999; Croft, 2004; Meiksin and White, 2004; McDonald, Seljak, *et al.*, 2005) are generally found not to have much effect on the inferred matter power spec-

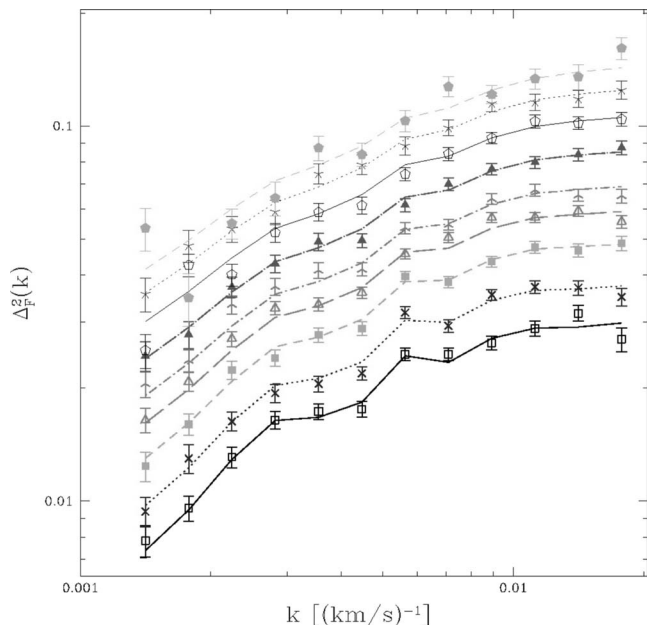


FIG. 18. Comparison of the best-fitting model (lines) and the mean power spectrum measured from the Ly- α forest in 3035 SDSS QSO spectra (points with error bars). The model includes the effect of Si III absorption. The curves show a sequence in redshifts, increasing from $z=2.2$ at the bottom to $z=3.8$ at the top, in steps of $\Delta z=0.2$. From McDonald *et al.*, 2006. Figure reproduced by permission of the AAS.

trum, except possibly at $z=5-6$ when the attenuation length to ionizing photons becomes so short few sources contribute to the local UV background.

More of a concern are known systematics that affect measurements of the Ly- α forest power spectrum. The effect of the wings of damped Ly- α absorbers and absorption by intervening metal absorption systems (Croft *et al.*, 1999; Croft, Weinberg, *et al.*, 2002) must be corrected for to obtain high-precision measurements of the flux power spectrum (McDonald, Seljak, *et al.*, 2005). McDonald *et al.* (2006) provided an estimate for the influence of the damping wings from DLAs. They also corrected for metal absorption, uncertainties in sky subtraction, and calibration errors. They found clear evidence for contamination by Si III absorption, and devised a method for removing its influence.

Any measurement of the flux power spectrum and comparison with models also require a careful estimate of the QSO continuum. An optimal method for estimating the QSO continuum in the context of flux power spectra measurements is formulated by Hui *et al.* (2001). The flux power spectrum was measured from high-resolution spectra of 27 QSOs by Kim *et al.* (2004a, 2004b). The largest and most precise set of measurements by far is that made using a sample of 3035 QSO spectra from the Sloan digital sky survey (McDonald *et al.*, 2006). The evolution of the measured flux power spectrum is shown in Fig. 18.

Despite their differences, the various approaches have yielded reasonably good agreement on the inferred constraints of cosmological parameters. Using the inversion

method, Zaroubi *et al.* (2006), assuming $n=1$ for the matter power spectrum, obtained $\sigma_8=0.92(\Omega_m/0.3)^{-0.3}$. A joint analysis with the WMAP CMB data and a prior on the Hubble constant yields $\sigma_8=0.92\pm 0.04$ and $\Omega_m=0.30\pm 0.05$. Combining the Ly- α flux power spectrum measurements from the SDSS (McDonald *et al.*, 2005, 2006) with CMB, supernovae and galaxy clustering constraints, Seljak *et al.* (2006) found the Ly- α flux power spectrum increases from $\sigma_8=0.80\pm 0.03$ to 0.85 ± 0.02 . They obtained an index of $n=0.965\pm 0.012$ with no evidence for a running spectral index, $dn/d\ln k = -0.020\pm 0.012$. In a separate analysis of the measured SDSS flux power spectra, Viel and Haehnelt (2006) obtained $\sigma_8=0.91\pm 0.07$, $\Omega_m=0.28\pm 0.03$, and $n=0.95\pm 0.04$. Using pure dark matter simulations, Desjacques and Nusser (2005) obtained $\sigma_8=0.7-0.9$.

The flux power spectra measurements tend to pull the normalization of the matter power spectrum to larger values compared with estimates based on other methods. This is consistent with the larger values of $\sigma_8=0.9-1$ preferred by cosmological models that match measurements of the pixel flux distribution function and WMAP constraints (Meiksin *et al.*, 2001; Meiksin and White, 2004). On the other hand, the model comparisons all neglect radiative transfer effects. Allowing for an inverted equation of state over the redshift range $2 < z < 3$, in which underdense regions are warmer than overdense ones, lowers the allowed range for σ_8 (Bolton *et al.*, 2008). There is growing evidence that the equation of state is inverted, or at least not as monotonic as the power spectra and pixel flux distribution analyses have assumed (Becker *et al.*, 2007; Bolton *et al.*, 2008). Simulations including radiative transfer show a broad spectrum of temperatures at a given density, including hot underdense regions, in scenarios with late He II reionization (Tittley and Meiksin, 2007).

VII. REIONIZATION

A. The epoch of reionization

The reionization of the IGM is one of the principal unsolved problems of cosmological structure formation. Three epochs of reionization of the IGM may be identified, one for hydrogen and two for helium. Because the same radiation sources capable of photoionizing hydrogen would likely also photoionize He I to He II, only the epochs of hydrogen reionization and full helium reionization to He III are likely to be distinct. As discussed in Secs. II.B.5 and IV.C.2, there is strong evidence full helium reionization occurred at $z\approx 3.5$. The most likely He II reionization sources are QSOs. The epoch of hydrogen reionization is much less certain. The topic attracted considerable attention following measurements of the IGM Ly- α optical depth in high-redshift QSOs and CMB measurements of intergalactic Thomson scattering. Unlike full helium reionization, the sources of hydrogen reionization may well be the first sources of radiation to turn on in the Universe, ending the dark

ages that followed the recombination of the primordial hydrogen and helium plasma. Because of the numerous recent reionization reviews (see Sec. I), I concentrate here only on some of the most salient aspects.

The Ly- α optical depth of the IGM measured in the spectra of several $z > 5.8$ QSOs discovered by the Sloan digital sky survey has shown that the IGM was reionized by $z \approx 5.7$ (Fan *et al.*, 2000, 2001a), but the Ly- α optical depth rises rapidly toward higher redshifts (Becker *et al.*, 2001, 2007; Djorgovski *et al.*, 2001; Pentericci *et al.*, 2002; Fan *et al.*, 2004; Fan, Strauss, *et al.*, 2006). By $z \approx 6$, the spectra become so black shortward of Ly- α that usually only lower limits to the optical depth can be obtained, even using the higher-order Lyman resonance transitions. The rapid rise is suggestive of an approach to the EOR. This interpretation is not unique, as only a small neutral fraction is adequate for providing a large Ly- α optical depth by Eq. (15). A QSO at $z \approx 6.4$, moreover, shows transmitted flux at $z \approx 6.1$ (White *et al.*, 2003, 2005). Gaps, however, are expected as H II regions develop and evolve prior to their complete overlap (Furlanetto *et al.*, 2004; Wyithe and Loeb, 2006).

The interpretation of the IGM transmission measurements at $z > 6$ as evidence for the approach to the EOR is further confounded by WMAP measurements of the intergalactic Thomson optical depth

$$\begin{aligned} \tau_e &= \int_{z_l}^{z_u} dz n_e c \sigma_T \left| \frac{dt}{dz} \right| \\ &\approx 0.004 [(\Omega_m(1+z_u)^3 + \Omega_b)^{1/2} - (\Omega_m(1+z_l)^3 + \Omega_b)^{1/2}], \end{aligned} \quad (112)$$

where σ_T is the Thomson cross section, $n_e(0)$ is the comoving electron density (assumed constant and without full helium reionization), and a flat universe is assumed. The five-year WMAP polarization data yield a marginalized optical depth of $\tau_e = 0.087 \pm 0.017$ (Dunkley *et al.*, 2009) up to the EOR, corresponding to an EOR redshift of $z_u = 11.0 \pm 1.4$, assuming reionization was a single, instantaneous event throughout the Universe. The 2σ and 3σ lower limits are $z_u > 8.2$ and $z_u > 6.7$, respectively (Dunkley *et al.*, 2009). These values are lowered slightly to $\tau_e = 0.084 \pm 0.016$ and $z_u = 10.8 \pm 1.4$, allowing for additional astrophysical constraints on the preferred cosmological model from Type Ia supernovae and baryonic acoustic oscillations (Hinshaw *et al.*, 2009).

It is worth noting that a non-negligible contribution to the total Thomson optical depth will arise from the IGM prior to the EOR because of the residual electron density frozen out after the recombination era. A residual fraction of as little as $(2-4) \times 10^{-4}$ over the redshift range $7 < z < 500$ (Page *et al.*, 2007) will produce an additional optical depth of $\Delta\tau_e = 0.005-0.01$, using Eq. (112). Careful modeling of the contribution to the polarization signal from residual electrons between the recombination era and the Epoch of Reionization is required to estimate the contribution due to reionization sources alone.

B. The growth of cosmological H II regions

The reionization of the Universe occurs as a consequence of the overlap of H II regions driven into the IGM by discrete radiation sources.²² Unlike the H II region around a star in a galaxy, the growth of cosmological H II regions will generally not terminate in a Strömgren sphere, defined as the surface within which the rate of radiative recombinations balances the rate of production of ionizing photons by the source. As the ionization front (I front) of the H II region advances, the expansion of the Universe reduces the density of the gas into which the I front moves. Unless the I front encounters a large density inhomogeneity, it will travel unimpeded, lagging further and further behind the Strömgren radius (Shapiro, 1986), until either the source dies or the I front overlaps with another I front, produced by another source or sources.

The advance of the I front of an isotropic cosmological H II region into a multicomponent IGM is described by (Shapiro, 1986; Donahue and Shull, 1987; Shapiro and Giroux, 1987; Meiksin and Madau, 1993)

$$4\pi r_I^2 n_H \left(\frac{dr_I}{dt} - H r_I \right) = S(0) - \frac{4}{3} \pi r_I^3 n_H^2 \sum_i c_i f_{eH,i} \alpha_B(T_i), \quad (113)$$

where r_I is the proper radius of the I front, $n_H = \sum_i f_i n_{H,i}$ is the mean hydrogen density of the IGM averaged over the various components with volume filling factors f_i , H is the Hubble parameter, $S(0)$ is the emission rate of ionizing photons from the central sources, $c_i = f_i n_{H,i}^2 / n_H^2$ is the partial recombination clumping factor of the gas from component i , $f_{eH,i}$ is the number of electrons per hydrogen atom in component i (which will contain helium and possibly metals), and $\alpha_B(T_i)$ is the case B radiative recombination rate to the $n=2$ level of hydrogen, allowing for ionizations from the ground state by the diffuse radiation emitted following recombinations to the ground state (see Sec. IV.A.1). If the diffuse radiation is treated separately, then case A recombination should be used, and a second set of partial ionization clumping factors must be introduced to represent the volume-averaged product of the local ionization rate and H I density in each subcomponent i (Kohler *et al.*, 2007). If the electron fractions $f_{eH,i}$ and temperatures of the various components are approximately the same, then $f_{eH,i} \alpha_B(T_i)$ may be approximated as $f_{eH} \alpha_B(T)$ and it is convenient to introduce a total recombination clumping factor over all subcomponents, $\mathcal{C}(z) = \sum_i c_i(z)$. The recombination term in Eq. (113) is then $(4\pi/3) r_I^3 n_H^2 \mathcal{C} f_{eH} \alpha_B(T)$. (If the diffuse radiation is treated

²²Excepted are scenarios invoking reionization by decaying or annihilating dark matter particles (Sciama 1982, 1998; Scott *et al.*, 1991; Mapelli *et al.*, 2006). Mapelli *et al.* (2006) found that, while some popular dark matter candidates may cause partial reionization, none are able to fully reionize the IGM prior to $z=6$.

separately, then a similar total ionization clumping factor may be similarly defined.)

Equation (113) is an approximation for which it is assumed that the I front, within which the gas transforms from neutral to highly ionized, is narrow compared with the radius of the H II region. It also assumes that the I front propagates rapidly compared with the sound speed so that the effects of gas motion induced by the pressure within the H II region may be neglected. It assumes as well that the I front propagates slowly compared with the speed of light, which formally breaks down in the early stages. Near-luminal expansion may be approximately described by replacing $4\pi r_I^2 n_{\text{H}}$ on the left-hand side (LHS) of Eq. (113) by $4\pi r_I^2 n_{\text{H}} + S'/c$, where S' is the right-hand side (RHS) of Eq. (113) (White *et al.*, 2003; Wyithe and Loeb, 2004; Shapiro *et al.*, 2006). This will ensure that $dr_I/dt < c$.

A key uncertainty in the rate at which an H II region expands is the recombination clumping factor. Because the clumping factor may be dominated by rare very dense structures, establishing its value from numerical simulations is not straightforward. In particular, systems that produce ionizing photons should be excluded. The dynamical response of clumped structures to an impinging I front must also be computed, which requires radiative transfer and high spatial resolution. The degree to which a dense cold clump bound by a minihalo impedes the propagation of an I front in general depends on the mass of the clump and the intensity and spectral shape of the incident radiation field (Shapiro *et al.*, 2004; Iliev *et al.*, 2005). A wide range of values for the clumping factor are available in the literature. On the basis of high-resolution simulations, Iliev *et al.* (2007) found the recombination clumping factor is well fitted over the redshift range $6 < z < 30$ by

$$\mathcal{C}(z) \approx 26.2917 \exp(-0.1822z + 0.003505z^2) \quad (114)$$

for models using the preferred WMAP three-year cosmological parameters (Spergel *et al.*, 2007).

The evolution in the filling factor of ionized gas as the H II regions grow may be quantified by the porosity parameter $Q_{\text{H II}}$, which is the product of the volume ionized per source of a given ionizing photon luminosity, integrated over the luminosity function of the sources (Donahue and Shull, 1987; Meiksin and Madau, 1993). For $Q_{\text{H II}} > 1$, the IGM becomes completely ionized. Its growth is governed by (Madau *et al.*, 1999; Meiksin, 2005)

$$\frac{dQ_{\text{H II}}}{dz} = \left(\frac{\dot{n}_S(z)}{n_{\text{H}}(0)} - \frac{\mathcal{C}(z)Q_{\text{H II}}}{t_{\text{rec}}(z)} \right) \left(-\frac{1}{H(z)(1+z)} \right), \quad (115)$$

where $n_{\text{H}}(0)$ is the comoving number density of hydrogen, $\dot{n}_S(z)$ is the production rate of ionizing photons per comoving volume, and $t_{\text{rec}}(z) = 1/n_{\text{H}}(z)f_{\text{eH}}\alpha_{\text{B}}(T)$ is the recombination time at the mean electron density at redshift z . If the comoving emissivity of the sources is given

as $\epsilon_{\nu}^S(z) = \epsilon_L^S(\nu/\nu_L)^{-\alpha_S}(1+z)^{\gamma_S}$, the ionizing photon production rate is

$$\dot{n}_S = \int_{\nu_L}^{\infty} d\nu \frac{\epsilon_{\nu}^S(z)}{h\nu} = \frac{\epsilon_L^S}{h\nu\alpha_S}(1+z)^{\gamma_S}. \quad (116)$$

To solve Eq. (115), it is convenient to define $\tau_{\text{H,H I}}(z) = \mathcal{C}(z)t_{\text{H}}(z)/t_{\text{rec}} \approx 0.02\mathcal{C}(z)(1+z)^{3/2}$, which is the Hubble time $t_{\text{H}} = 2/3H(z)$ measured in units of the recombination time, normalized here at $T = 10^4$ K and including the recombination clumping factor. It is equivalent to the mean number of recombinations per hydrogen atom over a Hubble time. Similar definitions may be introduced for the reionization of He I, $\tau_{\text{H,He I}} \approx 0.03\mathcal{C}(z)(1+z)^{3/2}$ (assuming all ionized He I is in the form of He II), and of He II, $\tau_{\text{H,He II}} \approx 0.2\mathcal{C}(z)(1+z)^{3/2}$. Adopting the clumping factor from Eq. (114) gives nearly constant values for the various τ_{H} over $6 < z < 8$ of $\tau_{\text{H,H I}} \approx 4.7$, $\tau_{\text{H,He I}} \approx 5.3$, and $\tau_{\text{H,He II}} \approx 32$. For constant $\tau_{\text{H,H I}}$, Eq. (115) may be directly integrated, yielding

$$\begin{aligned} Q_{\text{H II}}(z) &\approx \frac{1}{1 + \tau_{\text{H,H I}} - 2\gamma/3} \left[\frac{\dot{n}_S(z)t_{\text{H}}(z)}{n_{\text{H}}(0)} \right. \\ &\quad \left. - \frac{\dot{n}_S(z_i)t_{\text{H}}(z_i)}{n_{\text{H}}(0)} \left(\frac{1+z}{1+z_i} \right)^{3\tau_{\text{H,H I}}/2} \right] \\ &\approx \frac{1}{1 + \tau_{\text{H,H I}} - 2\gamma/3} \frac{\dot{n}_S(z)t_{\text{H}}(z)}{n_{\text{H}}(0)}, \end{aligned} \quad (117)$$

where z_i is the turn-on redshift of the ionizing sources, and the assumption $z_i \gg z$ has been made to obtain the final expression. Similar expressions apply for He I and He II reionization, on replacing $\tau_{\text{H,H I}}$ by the appropriate form for He I or He II, using the production rate of ionizing photons for He I or He II for \dot{n}_S , and replacing $n_{\text{H}}(0)$ by $n_{\text{He}}(0)$. In principle, a recombination clumping factor appropriate to each species must be used since the depth of self-shielding in clumps will differ for different species. To date, simulations have focused on the clumping of ionized hydrogen gas only.

The (comoving) production rate of ionizing photons from the UV background emissivity estimate of Eq. (106) follows from Eq. (116),

$$\dot{n}_S \approx A_S[(3 + \alpha_{\text{MG}})/3\alpha_S](1+z)^{\gamma} h \text{ ph s}^{-1} \text{ Mpc}^{-3}, \quad (118)$$

where $A_S = 1.3_{-(0.7,1.0)}^{+(1.5,4.6)} \times 10^{52}$, $\gamma = -1.6 - 0.6 \ln(A_S/1.3 \times 10^{52})$, and α_S is the spectral index at frequencies above the Lyman edge (Meiksin, 2005). (This neglects any contribution to the required emissivity from the diffuse recombination radiation from the IGM. If the IGM contributes 30% of the emissivity, A_S should be reduced by a factor of 1.3.) Substitution into Eq. (117) and extrapolation of Eq. (118) to high redshifts show that the Universe would be reionized by $z_{\text{ri}} \approx 5.5$ for $\alpha_{\text{MG}} = \alpha_S = 0.5$, but as late as $z_{\text{ri}} \approx 3.8$ for $\alpha_{\text{MG}} = \alpha_S = 1.8$. Reionization by $z_{\text{ri}} \geq 6$, as suggested by observations, requires either a hard spectrum for the sources or an increase over the evolution rate of Eq. (106) in the comoving emissivity at $z > 6$ (Miralda-Escudé, 2003; Meiksin, 2005; Bolton and Haehnelt, 2007).

C. Sources of reionization

1. Galaxies

High-redshift galaxies are generally considered the most likely candidates for the reionization of the Universe. The discovery of high-redshift galaxies in deep surveys has sparked much debate over whether the population of galaxies that reionized the Universe has now been identified (Bouwens *et al.*, 2004, 2006; Bunker *et al.*, 2004, 2006; Stiavelli *et al.*, 2004; Yan and Windhorst, 2004). The uncertainties involved preclude any definite decision.

Consider the (comoving) luminosity density at $5.5 < z < 6.5$ from Bouwens *et al.* (2006), corrected upward by 50% to allow for internal extinction, of $\rho_{1350} \approx 10^{19.4} \text{ W Hz}^{-1} \text{ Mpc}^{-3}$. The conversion rates between $L_\nu(1350 \text{ \AA})$ (in W Hz^{-1}) and the production rate of ionizing photons for a Salpeter initial mass function with $M_{\text{lower}}=1M_\odot$ and $M_{\text{upper}}=100M_\odot$ and solar metallicity are

$$\begin{aligned} \dot{N}_{\text{S,H I}} &= 10^{32.0} \text{ ph s}^{-1} L_\nu(1350 \text{ \AA}), & \text{H I}, \\ \dot{N}_{\text{S,He I}} &= 10^{31.3} \text{ ph s}^{-1} L_\nu(1350 \text{ \AA}), & \text{He I}, \\ \dot{N}_{\text{S,He II}} &= 10^{29.6} \text{ ph s}^{-1} L_\nu(1350 \text{ \AA}), & \text{He II} \end{aligned} \quad (119)$$

(Leitherer *et al.*, 1999). For a metallicity of 1/20 solar, the rates are about 0.1 dex higher for H I, 0.2 dex higher for He I, and 0.4 dex smaller for He II. A similar conversion for H I is inferred from Madau *et al.* (1998, 1999) for an alternative Salpeter model with $M_{\text{lower}}=0.1M_\odot$ and $M_{\text{upper}}=125M_\odot$. Assuming that all ionizing photons escape, applying these rates to the luminosity density at $5.5 < z < 6.5$, Eq. (117) (and its variants for He I and He II reionization, assuming the same recombination clumping factors, which may in fact differ) shows that the galaxies are able to reionize H I by $z_{\text{ri}}=12$ and He I by $z_{\text{ri}}=21$, while they are unable to reionize He II even by the present epoch. The results for H I and He I, however, are very sensitive to the uncertainty in the counts and the escape fractions. If only 10% of the ionizing radiation escapes, then the reionization epochs for H I and He I are reduced dramatically to $z_{\text{ri}}=1.8$ and 3.7, respectively. Reionization of H I by $z=6$ requires $f_{\text{esc}} > 0.6$, while for He I, $f_{\text{esc}} > 0.3$ is needed. Allowing for the upper limits on the counts eases these constraints, as would lower metallicities for the stars (Tumlinson and Shull, 2000) or an initial mass function heavily tilted to very massive ($\sim 300M_\odot$) stars (Bromm *et al.*, 2001). On the other hand, a decline in the comoving luminosity density of the sources at $z > 6$ would make the case that these sources reionized the Universe less secure. While the population of sources that reionized the Universe may have been discovered in high-redshift surveys, a definite conclusion is still premature. There is some evidence for a population of low-luminosity star-forming galaxies at redshifts as high as $z \approx 8-10$ that may con-

tribute substantially to the total budget of reionizing photons (Stark, Ellis, *et al.*, 2007).

Several semianalytic estimates for the expected contribution of galaxies to the reionization of both hydrogen and helium have been made (Haiman and Holder, 2003; Venkatesan *et al.*, 2003; Haiman and Bryan, 2006; Shull and Venkatesan, 2008). The possible halo masses of the objects that dominate reionization cover a broad range, including systems as small as minihalos with masses $M_{\text{halo}} < 10^6 M_\odot$ and virial temperatures $T_{\text{vir}} < 1000 \text{ K}$ which would have so far evaded detection. Definitive predictions, however, are hampered by the need to incorporate several poorly determined quantities, including the fraction of baryons in a collapsed halo that are converted into stars, the number of ionizing photons produced by the stars, and the escape fraction of the ionizing radiation from the galaxies. Recent estimates suggest that the efficiency of ionization per galaxy cannot be too high, or a Thomson optical depth would be produced that is too large compared with CMB polarization measurements (Haiman and Bryan, 2006; Shull and Venkatesan, 2008).

2. QSOs

The emissivity of QSOs lies well below the requirements for reionization, unless there is a large population of very low-luminosity active galactic nuclei (AGN) (Meiksin, 2005; Bolton and Haehnelt, 2007; Srbinovsky and Wyithe, 2007). The estimated production rate of ionizing photons from accretion onto massive black holes in the Universe is comparable to the rate from nucleosynthesis in stars (Meiksin, 2006c): low-luminosity AGN may still await discovery at high redshifts. By contrast, QSOs likely fully ionized helium by $z \approx 3$, and possibly as early as $z \approx 5$ if they have hard spectra extending down to the He II photoelectric edge (Meiksin, 2005).

An interesting alternative class of reionization sources is a possible population of miniquasars, systems produced by intermediate mass black holes with masses $(200-1000)M_\odot$ growing by accretion onto seed black holes produced by the collapse of very massive Population III stars (Madau *et al.*, 2004). Such sources could plausibly reionize the Universe by $z \approx 15$.

3. Other sources

Various alternative sources have been proposed for the reionization of the IGM, including globular star clusters (Ricotti, 2004), massive Population III stars more generally, with their formation possibly triggered early by primordial magnetic fields (Tashiro and Sugiyama, 2006), and an early generation of black holes (Venkatesan *et al.*, 2001; Ricotti and Ostriker, 2004; Ricotti *et al.*, 2005). While these mechanisms are intriguing and have received a variety of theoretical investigations, observational evidence for any of them is as yet wanting. The possibility that sources other than galaxies reionized the IGM, however, should not be discounted: the Universe can surprise.

D. 21 cm signature of reionization

An altogether novel method for discovering the epoch of reionization is through the detection of the 21 cm signature from the neutral IGM before and during the reionization process. The emission or absorption of 21 cm radiation from a neutral IGM is governed by the spin temperature T_S of the hydrogen, defined by

$$n_1/n_0 = 3 \exp(-T_*/T_S), \quad (120)$$

where n_0 and n_1 are the singlet and triplet $n=1$ hyperfine levels and $T_* \equiv h_P \nu_{10}/k_B \approx 0.07$ K, where ν_{10} is the frequency of the 21 cm transition. In the presence of only the CMB radiation, the spin temperature will come into equilibrium with the CMB on a time scale of $T_*/T_{\text{CMB}} A_{10} \approx 3 \times 10^5 (1+z)^{-1}$ yr, where $A_{10} = 2.85 \times 10^{-15} \text{ s}^{-1}$ is the spontaneous decay rate of the transition. In this case, the spin temperature will be the same as the CMB temperature, and no emission or absorption relative to the CMB will be detectable. A mechanism is needed to decouple the two temperatures. Two mechanisms may couple the spin temperature to the kinetic temperature of the gas. One is the collisions between hydrogen atoms (Purcell and Field, 1956). The collision-induced coupling between the spin and kinetic temperatures is dominated by spin exchange between colliding hydrogen atoms, with possible significant contributions from electron-hydrogen collisions and proton-hydrogen collisions, depending on the ionization fraction and temperature (Smith, 1966; Dalgarno, 1967; Allison and Dalgarno, 1969; Zygelman, 2005; Furlanetto and Furlanetto, 2007; Hirata and Sigurdson, 2007). The second, less obvious, mechanism is scattering by Ly- α photons (Wouthuysen, 1952; Field, 1958). The Wouthuysen-Field effect mixes the hyperfine levels of neutral hydrogen in its ground state via an intermediate transition to the $2p$ state. An atom initially in the $n=1$ singlet state may absorb a Ly- α photon that puts it in an $n=2$ state, allowing it to return to the triplet $n=1$ state by a spontaneous decay. The combined atomic collision rates are generally too small at the average IGM densities at the redshifts of interest, although collisions may be important in overdense regions, $\delta\rho/\rho \gtrsim 30[(1+z)/10]^{-2}$ (Madau *et al.*, 1997). Instead the dominant mechanism at detectable redshifts for the near future is likely to be Ly- α scattering.

A patchwork of either 21 cm emission or absorption against the cosmic microwave background will result (Hogan and Rees, 1979). Large radio telescopes such as LOFAR, the MWA, PAPER, or the SKA offer the prospect of measuring this signature, and so detecting the transitional epoch from a dark universe to one with light. The spin temperature of the neutral hydrogen is

$$T_S = (T_{\text{CMB}} + y_\alpha T_\alpha + y_c T_K)/(1 + y_\alpha + y_c), \quad (121)$$

where

$$y_\alpha \equiv \frac{P_{10} T_*}{A_{10} T_\alpha} \quad \text{and} \quad y_c \equiv \frac{C_{10} T_*}{A_{10} T_K} \quad (122)$$

are the Ly- α and collisional pumping efficiencies, respectively. Here P_{10} is the indirect deexcitation rate of the triplet state via absorption of a Ly- α photon to the $n=2$ level, and $T_S \gg T_*$ is assumed. Consideration of the net transition rates between the various hyperfine $n=1$ and $n=2$ levels shows that the $1 \rightarrow 0$ transition rate via Ly- α scattering is related to the total rate

$$P_\alpha = c \int_0^\infty d\nu \sigma_\nu \frac{u_\nu}{h_P \nu}, \quad (123)$$

where σ_ν is the resonance line cross section given by Eq. (12), u_ν is the radiation energy density, and $P_{10} = 4P_\alpha/27$ (Field, 1958). The quantity T_α is the color temperature of the radiation field, given by the harmonic mean $T_\alpha = 1/\langle T_u^{-1}(\nu) \rangle$ of the frequency-specific temperature $T_u(\nu) = -(h_P/k_B)(d \ln u_\nu/d\nu)^{-1}$, weighted by $u_\nu \varphi_\nu(a, \nu)$ (Meiksin, 2006b). The factor C_{10} is the rate of collisional deexcitation of the triplet level. In the absence of collisions, there exists a critical value of P_α which, if greatly exceeded, would drive $T_S \rightarrow T_K$. This thermalization rate is (Madau *et al.*, 1997)

$$P_{\text{th}} \equiv \frac{27A_{10}T_{\text{CMB}}}{4T_*} \approx (5.3 \times 10^{-12} \text{ s}^{-1}) \left(\frac{1+z}{7} \right). \quad (124)$$

It corresponds to a Ly- α intensity of $J_\alpha \approx 0.6S_\alpha^{-1} \times 10^{-24} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1}$, where S_α is a suppression factor of order unity that takes into account the effect of recoils in an expanding medium on the shape of the intensity near the center of the line profile (Chen and Miralda-Escudé, 2004; Furlanetto *et al.*, 2006). The value of the intensity corresponds to a comparable number of Ly- α photons as hydrogen atoms at $z=8$, and so is comparable to the intensity expected from sources able to reionize the Universe (Madau *et al.*, 1997). This coincidence suggests that the Wouthuysen-Field mechanism may reveal the IGM prior to its complete reionization.

To illustrate the basic principle of the observations, consider a patch of neutral material with spin temperature $T_S \neq T_{\text{CMB}}$, having an angular size on the sky that is large compared with a beamwidth, and radial velocity extent that is larger than the bandwidth due to the Hubble expansion. Following an analysis similar to the derivation of the Gunn-Peterson optical depth [Eq. (15)], and taking into account the reduction in the absorption coefficient due to stimulated emission by the factor $1 - e^{-T_*/T_S} \approx T_*/T_S$ for $T_* \ll T_S$, the intergalactic optical depth at $21(1+z)$ cm along the line of sight is

$$\begin{aligned}
\tau(z) &= \frac{3}{32\pi} x_{\text{H I}} [1 + \delta(z)] \bar{n}_{\text{H I}} \lambda_{10}^3 \frac{A_{10}}{H(z)} \frac{T_*}{T_S} \\
&\approx 0.0032 h^{-1} [1 + \delta(z)] \left(\frac{x_{\text{H I}}(z)}{T_S} \right) \Omega_m^{-1/2} (1+z)^{3/2} \\
&\quad \times \left(1 + \frac{1 - \Omega_m}{\Omega_m (1+z)^3} \right)^{-1/2}, \quad (125)
\end{aligned}$$

which will typically be much less than unity. Here $x_{\text{H I}}$ is the neutral fraction, δ accounts for fluctuations about the mean hydrogen density, $n_{\text{H I}} = \bar{n}_{\text{H I}}(1 + \delta)$, and a factor of 1/4 is introduced since only hydrogen atoms in the singlet state will take part in the absorption. A flat universe is assumed for the second form in Eq. (125) and $\Omega_b h^2 = 0.022$. Field (1959a) applied Eq. (125) to a search for intergalactic emission or absorption against a background radio galaxy. No clear emission or absorption signature was detected, with an upper limit on the 21 cm optical depth of $\tau < 0.0075$. For $\Omega_m = 0.3$, $h = 0.7$, and $T_S = T_{\text{CMB}}$, this corresponds to $x_{\text{H I}}(1 + \delta) < 1.5$ along the line of sight. The values $\Omega_m = 1$ and $\delta = 0$ would correspond to an upper limit on the baryon density of $\Omega_b < 0.2$, assuming hydrogen was all neutral, showing that early measurements could already have ruled out a baryon-dominated universe closed by a neutral IGM.

In the context of the radio measurements of the IGM planned today, an alternative observational strategy consists of cross-correlating measurements of patches separated in either angle or frequency. Possible detections include large isolated H II regions, as would be produced by the first QSOS (Madau *et al.*, 1997) or, possibly more straightforwardly, a global statistically averaged fluctuation signal from the IGM (Tozzi *et al.*, 2000). Foreground contamination, particularly fluctuations in the ionosphere and discrete sources in the Galaxy, pose formidable challenges to detecting the 21 cm signature from the epoch of reionization. But the development of novel detection strategies suggests the challenges may not be insurmountable. Discussions on the feasibility of the measurements are provided by Wyithe *et al.* (2005), Bowman *et al.* (2006), Datta *et al.* (2007), and in the reviews by Fan, Carilli, and Keating (2006), Furlanetto *et al.* (2006), and Barkana and Loeb (2007), which also discuss specific reionization scenarios.

VIII. ABSORBER-GALAXY CONNECTION

Ever since their discovery, intervening absorption systems have held the promise of opening a new window on the evolution of galaxies by probing the gas in galaxies as it was converted into stars, and tracing the feedback of the stars on the gas as supernovae and stellar winds pollute their environment with metals. Despite searches, direct evidence relating intervening absorbers to galaxies has been scant until only the past few years. Today, the absorber-galaxy connection is fast becoming a growing area in IGM studies.

A. Galaxy-associated IGM absorption

1. Association of DLAs with galaxies

The motivation for the original systematic damped Ly- α absorber survey was the search for gaseous disks of galaxies at high redshifts (Wolfe *et al.*, 1986). A large number of surveys have been conducted since, summarized by Wolfe *et al.* (2005). There are several properties of DLAs suggestive of galactic disk material: (1) They are the dominant reservoir of neutral hydrogen at high redshifts ($z > 3$) (Prochaska *et al.*, 2005; Jorgenson *et al.*, 2006), (2) with the cosmic gas mass density Ω_g^{DLA} decreasing and metallicity increasing with cosmic time (Prochaska *et al.*, 2003). (3) There is evidence for depletion of Fe and Si onto dust grains similar in strength to that in cold gas in the Galaxy (Petitjean *et al.*, 2002). (4) There is photometric evidence for reddening by dust, with the amount of extinction increasing with iron column density similarly to the trend found for interstellar clouds within the Galaxy (Vladilo *et al.*, 2006). (5) Molecular hydrogen is present in about 15–20 % of the systems (Ledoux, Petitjean, and Srianand, 2006), with the metallicity and depletion factor increasing with the amount of H₂ (Ledoux *et al.*, 2003). (6) The metallicity of DLAs increases with the velocity width of the line profiles for low-ionization metals, which presumably trace the gravitational potentials of the systems, and is suggestive of a mass-metallicity correlation (Ledoux, Petitjean, *et al.*, 2006). (7) In addition to a cold low ionization phase, a warm phase is indicated by C IV and Si IV absorption systems, and a hot phase is indicated by O VI absorption detections (Fox *et al.*, 2007), demonstrating a complex interstellar medium in DLAs much as is found in disk galaxies. (8) Using a method that deduces the star-formation rate from the strength of C II* $\lambda 1335.7$ as a measure of the amount of gas heating by the photoelectric dust mechanism due to UV heating by massive stars, Wolfe, Prochaska, and Gawiser (2003) inferred star-formation rates in a presumed cold neutral medium in DLAs similar to that in the interstellar medium of the Galaxy. (9) The inferred global cosmic star formation rate in DLAs at $z \approx 3$ is comparable to that of Lyman break galaxies at the same redshift (Wolfe, Gawiser, and Prochaska, 2003). (10) A search for Lyman break galaxies at $z > 1$ associated with DLAs shows evidence for a significant spatial correlation between the two, with a cross-correlation length comparable to the autocorrelation length of Lyman break galaxies (Cooke *et al.*, 2006). (11) Optical counterparts to DLAs at $z < 1$ suggest that the DLAs arise as part of large (radii of $\sim 30h^{-1}$ kpc), rotating H I disks (Chen, Kennicutt, and Rauch, 2005). (12) The incidence rate and column density distribution of DLAs at $z < 1$ are comparable to those of low redshift galaxies directly measured in H I (Zwaan *et al.*, 2005).

Despite the circumstantial evidence favoring a galactic disk connection for DLAs, there is strong contrary evidence as well: (1) While they are the dominant reservoir of neutral gas, DLAs contain less than half the mass density of present-day stars. (2) The amount of neutral

gas in DLAs exceeds the stellar mass in present-day disks (Wolfe *et al.*, 2005), which suggests they trace the disk component of galaxies, but their metal depletion patterns most often resemble that of warm disk clouds in the Galaxy or halo clouds (Ledoux *et al.*, 2002). The difference in the UV metagalactic backgrounds at low and high redshifts may partially account for the apparent discrepancy. (3) The C_{II^*} inferred star-formation rates suggest that the mass in metals produced should have been a factor of 30 larger than that measured in DLAs (Wolfe, Gawiser, and Prochaska, 2003). (4) The C_{II^*} inferred star-formation rates somewhat exceed the prediction of the Kennicutt-Schmidt (Schmidt, 1959; Kennicutt, 1998) relation between the star-formation rate and gas mass in galaxies (Hopkins *et al.*, 2005). Possibly the principal source of heat powering the measured C_{II^*} cooling rates is star formation in centrally located compact Lyman break galaxies rather than in the bulk of a spatially extended DLA system (Wolfe and Chen, 2006). (5) DLAs are sufficiently abundant that if they obeyed the Kennicutt-Schmidt relation, then 3% of the sky should be lit up with star-forming DLAs at high redshifts, contrary to observations, which find a comoving star-formation density a factor 30–100 smaller than predicted (Wolfe and Chen, 2006). (6) Most puzzling is the rarity of successful follow-up optical identifications. While there is mounting circumstantial evidence that DLAs and Lyman break galaxies are associated with the same systems at $z > 1.6$, only a handful of DLAs show Ly- α in emission (Möller *et al.*, 2004). Galactic counterparts have been confirmed in the optical and near-infrared regions for about a dozen DLAs at $z < 1.6$ (Chen and Lanzetta, 2003; Rao *et al.*, 2003; Schulte-Ladbeck *et al.*, 2004; Chen, Kennicutt, and Rauch, 2005). The numbers are too few, however, to establish whether or not the galaxies represent a random sampling of the main population of galaxies (Wolfe *et al.*, 2005). The nature of DLAs and their relation to present-day galaxies remain an enigma.

Simulations set in a Λ CDM cosmology reasonably well reproduce the number of DLAs and their evolution at high redshifts when dissipation due to cooling, star formation, and subsequent supernovae feedback and galactic winds are included (Nagamine *et al.*, 2004a). The DLAs are found to arise in halos no smaller than those with total masses of about $10^8 h^{-1} M_{\odot}$ at high redshifts (Nagamine *et al.*, 2004a), and almost all in dark matter halos less than $10^{13} h^{-1} M_{\odot}$ (Nagamine *et al.*, 2007). Detailed comparisons between the simulated DLAs and observations, however, reveal some discrepancies. The predictions for the number of systems along a line of sight lie somewhat below the measured number. This may be due to overly compact DLAs in the simulations, which also show narrower velocity widths than measured. High-resolution simulations with radiative transfer suggest that gas in tidal tails and quasifilamentary structures also produce DLAs (Razoumov *et al.*, 2006), which may help to reconcile the predicted and measured numbers. The star-formation rate in the simulations is consistent with the observational estimates in DLAs;

however, an order of magnitude more metals are produced in the simulations than measured (Nagamine *et al.*, 2004b). Simulations with radiative transfer suggest that the UV radiation from stars produced in DLAs and the ambient UV metagalactic background may regulate the rate of star formation within DLAs (Iliev *et al.*, 2006). Detailed kinematic comparisons between the simulations and observations have yet to be made. While the simulations have gone a long way toward accounting for the DLAs within the framework of the Λ CDM model for structure formation, much work still remains to demonstrate that this model correctly describes the origin of most DLAs.

2. Association of metal absorbers with galaxies

Optical and infrared searches for counterparts to metal absorption systems, such as Mg II or C IV, have proven an effective means of discovering galaxies (Bergeron and Boissé, 1991; Steidel *et al.*, 1994, 1995, 1997; Bouché *et al.*, 2007). On the whole, the galaxies appear to sample the general population of galaxies in the field, although there occur fewer dim blue galaxies in the absorber-selected samples. The morphological and kinematic properties of galaxies associated with Mg II systems are reviewed by Churchill *et al.* (2005).

The spectra of QSOs proximate to galaxies on the sky probe galactic environments. Adelberger *et al.* (2005) found galaxies at $2 \lesssim z \lesssim 3$ generally show very strong C IV absorption, $N_{\text{C IV}} \gg 10^{14} \text{ cm}^{-2}$, within 40 kpc (proper) of the galaxy, and C IV absorbers with typical column densities of $N_{\text{C IV}} \approx 10^{14} \text{ cm}^{-2}$ are found as far out as 80 kpc. The key question is why metals are near the galaxies. Galaxies are known to be associated with large-scale baryonic overdensities, at least as probed by the Ly- α forest. In the nearby Universe, the stronger absorbers ($13.2 < \log_{10} N_{\text{H I}} < 15.4$) are spatially correlated with galaxies, although with mixed views over the strength of the cross correlation compared with the galaxy autocorrelation function (Penton *et al.*, 2002; Ryan-Weber, 2006; Wilman *et al.*, 2007). At higher redshifts, Adelberger *et al.* (2005) similarly found that galaxies are associated with enhanced amounts of Ly- α absorption. If the IGM is polluted by metals, then the proximity of metal absorption systems with galaxies may merely reflect the correlation of H I with galaxies. Alternatively, the metals associated with galaxies may have been ejected by the galaxies in a wind following an episode of intense star formation. Either alternative is intriguing. The possibility that galaxies polluted their environment with metals suggests that these metals may serve as tracers of the past star-formation history of stars in the galaxy, and so provide independent constraints on their formation. On the other hand, if metal pollution is widespread throughout the IGM, it raises the question of whether the pollution was *in situ*, produced by some ubiquitous undetected class of stellar systems like a population of high-redshift globular star clusters, or caused by the collective ejecta of galaxies that underwent a superwind phase. In the latter case, it may mean

that the evolution of the stellar population of galaxies was not isolated, but that galaxies “talked” with each other as their stars formed, entraining metal-enriched material produced by other galaxies. A galactic wind may also delay the onset of star formation in nearby low-mass halos by delivering turbulent kinetic support to the gas (Fujita *et al.*, 2004). In extreme cases, a wind may eradicate the gaseous content of nearby low-mass halos through evaporation or shock-driven stripping, suppressing star formation in these systems entirely (Scannapieco *et al.*, 2000).

Evidence that high-redshift galaxies do impact on the IGM is provided by Adelberger *et al.* (2005), who found that about a third of the galaxies in their sample at $2 \lesssim z \lesssim 3$ show clearings of weak or absent H I absorption out to distances of $1h^{-1}$ Mpc (comoving). Simulations suggest, however, that the clearings are consistent with random fluctuations (Desjacques *et al.*, 2006; Kawata and Rauch, 2007). The kinematic studies of Songaila (2006) showed that C IV systems at $2 < z < 3.5$ with $N_{\text{C IV}} > 2 \times 10^{13} \text{ cm}^{-2}$ lie in complexes having velocity widths of up to $300\text{--}400 \text{ km s}^{-1}$, suggestive of galactic outflows. Lower-column-density systems lie in complexes with substantially lower velocity widths of $\sim 50 \text{ km s}^{-1}$, suggesting they are not part of any galactic outflow, although they may be part of residual outflows that were initiated at much higher redshifts (Fujita *et al.*, 2004). The evidence for galactic outflows has prompted an increasing interest in the impact of galactic winds on the IGM, discussed next.

B. Galactic winds and the IGM

Galactic winds occur throughout the Universe, in a variety of environments, over a wide range of galactic masses, including starbursts in the local Universe (Heckman *et al.*, 1998) and Lyman break galaxies at $z \approx 3$ (Pettini *et al.*, 2002) and Ly- α emitting systems associated with them (Wilman *et al.*, 2005). A comprehensive review of galactic winds in the Universe is provided by Veilleux *et al.* (2005). Reviews specific to the IGM are provided by Aguirre and Schaye (2007) and Bertone *et al.* (2008).

A natural mechanism for enriching the gas near galaxies with metals is through winds. The possible enrichment by wind ejecta raises further questions: What sort of galaxies ejected the metals? When did they do it? How does the metal pollution relate to the star-formation history of the Universe?

Geometric estimates of the impact of galactic winds may be made based on the spatial correlations of the metals and galaxies. Porciani and Madau (2005) found that metal-enriched bubbles of comoving radius ~ 100 kpc expelled at $z=9$ by a biased population of dwarf galaxies with a halo mass of $10^9 M_{\odot}$, polluting the region around Lyman break galaxies, would account for both the metal abundances measured at $z=3$ and the measured spatial cross correlation between metals and Lyman break galaxies. Using high-resolution high-

signal-to-noise-ratio spectra, Scannapieco *et al.* (2006a, 2006b), studied the clustering properties of high (C IV and Si IV) and low (Mg II and Fe II)-ionization metal absorption systems. In conjunction with numerical simulations, they found that a uniform distribution of metals fails to reproduce the correlations measured. Modulating the metallicity by the density field similarly fails. They found, however, that the C IV correlation function is well reproduced by assigning the metals to clumps confined to bubbles of comoving radius 2 Mpc around systems with masses exceeding $10^{12} M_{\odot}$ at $z=3$. A similar model with a slightly larger bubble radius recovers the measured correlations of Mg II and Fe II at $z=0.5\text{--}2$. Both models are degenerate with a biased high-redshift enrichment model with the metals confined to 2.5 Mpc (comoving) radius bubbles around $3 \times 10^9 M_{\odot}$ systems at $z=7.5$. The results are consistent with two scenarios, metals deposited by winds from massive galaxies at $z \approx 3$, or by winds from dwarf galaxies at high redshifts, $z > 7$. An early wind model is also favored by the near constant mass density associated with C IV systems over the broad redshift range $2 < z < 6$ (Songaila, 2005; Ryan-Weber *et al.*, 2006). Whether any of these scenarios are viable depends on whether wind models that support them may be physically realized.

Correlations between low-redshift absorption systems and galaxies provide a potentially powerful means of inferring the origins of the metals. Tumlinson and Fang (2005) found that dwarf galaxies are able to reproduce the line-of-sight number density of O VI systems if they produce winds extending out to about 200 kpc, while luminous galaxies would need to produce winds extending to 0.5–1 Mpc. Similar results are obtained from the O VI survey analysis of Stocke, Penton, *et al.* (2006), who matched O VI systems at $z < 0.15$ with galaxies in the field. They found that the metal systems have median distances of 350–500 kpc (for $h=0.7$) from L_{*} galaxies, and 200–270 kpc around $0.1L_{*}$ galaxies. A contribution from $0.1L_{*}$ galaxies is required to reproduce the line-of-sight number density of O VI absorbers.

While these results are consistent with the ejection of metals from the galaxies detected, this is not the only possible picture. The metals may have arisen at earlier times in smaller systems that eventually merged into the galaxies seen. Alternatively, they may have been ejected from much smaller systems, perhaps as small as globular star clusters or very faint dwarf galaxies, that are spatially correlated with the visible galaxies. The metals may also have been deposited very early in the history of the Universe, perhaps by blowout from the progenitors of present-day galaxies in superwinds or possibly driven out by the impact of AGN that may have been active in the progenitors.

As a galactic wind expands into the IGM, it will drive a shock front that sweeps up the surrounding gas into a thin shell just behind the shock. In this limit, the thin-shell approximation may be used to describe the advance of the shock front. Denoting the distance of the shock front from the center of the galaxy by R_s , the mass

of the expanding gas interior to R_s by M_g , the mean interior pressure by P_b and enthalpy density by h_b , the external pressure and density by P_0 and ρ_0 , respectively, the velocity of the external gas relative to the galaxy by v_H , the gravitational potential energy of the wind gas by W , and assuming mass injection from the center at the rate \dot{M}_{in} with velocity v_{in} , the equations describing the evolution of the shock front radius and the interior thermal energy E_b of the bubble powered by energy injected at the rate $L_{in}(t)$ and cooling at the rate $L_{cool}(t)$ are, in the thin-shell approximation (Ostriker and McKee, 1988; Madau *et al.*, 2001),

$$d(M_g \dot{R}_s)/dt = 4\pi R_s^2(1 - f_{cl})[(P_b - P_0) + \rho_0 v_H(\dot{R}_s - v_H)] - M_g \dot{R}_s^2/\lambda_{cl} + W/R_s + \dot{M}_{in} v_{in}, \quad (126)$$

$$dE_b/dt = L_{in}(t) - 4\pi R_s^2 P_b \dot{R}_s + 4\pi R_s^2 h_b(\dot{R}_s - v_H) - P_b dV_{cl}/dt - L_{cool}(t), \quad (127)$$

where isothermal jump conditions across the shock front have been assumed for the energy equation, presuming the wind expands into a photoionized medium. A clumpy interior is allowed for due to the presence of clouds with a volume filling factor f_{cl} and a spatial density and cross section corresponding to a mean free path λ_{cl} , which enters as a drag term on the advance of the shock front in Eq. (126). The interior net cooling L_{cool} will be dominated by Compton cooling at high redshifts and two-body atomic processes, which in turn depend on the gas clumping factor, and radiative heating from the galaxy or UV metagalactic background at lower redshifts. The second and fourth terms on the RHS of Eq. (127) account for energy loss due to work done by the shock on the surrounding gas and on crushing interior clouds, respectively.

The factors in Eqs. (126) and (127) highlight the various uncertainties in any galactic wind calculation. The rate of mass and energy injection by the stars and supernovae depend on the rate of star formation and the initial mass function of the stars, which may have a lower upper-mass cutoff in starbursts compared with normal galaxies (Leitherer and Heckman, 1995), or may be dominated by massive stars if the metallicity is low (Bromm and Loeb, 2003). The cooling rate will depend on the metallicity of the bubble interior, its clumpiness, and on how well mixed the metals are. It will also depend on the temperature of the interior gas, which requires specifying the amount of interior mass even though it is negligible compared with the mass in the shell. Most of the interior mass results from evaporative losses from the contact surface between the hot interior and the cool shell (Madau *et al.*, 2001). The rate of evaporation depends on the degree to which thermal heat conduction may be suppressed by interior magnetic fields, although mechanical heat input balancing adiabatic expansion losses dominates the interior thermodynamics, so this may not be critical. The strength of the shock front may be substantially dissipated as the shock

overtakes small clouds and crushes them. Lastly, the progress of the shock front depends on the environment of the galaxy, which will differ in different directions, so that the winds will in general be anisotropic. The acceleration of dense gas by hot rarefied gas and the motion of surfaces past one another as the bubble penetrates the IGM will also generally be subject to Rayleigh-Taylor and Kelvin-Helmholtz instabilities, giving rise to the mixing of gas components with vastly contrasting densities and temperatures and the formation of eddies both at the surface of the bubble and in its interior as the shell fragments. Thermal instabilities may also play a role. Magnetic fields will generally also affect the fragmentation of the expanding shell, and may affect the crushing of interior clouds. No numerical simulation is able to contend with all these factors: the required spatial resolution, range in time scales, and number of physical processes involved are far too demanding. Instead, simulators must resort to the art of approximation.

Several estimates of the possible impact of galactic winds on the IGM have been made. An instantaneous stellar burst of $10^6 M_\odot$, typical of a dwarf galaxy with total halo mass $M_h \approx 10^9 M_\odot$ and allowing for a conversion efficiency $f_* \approx 0.01$ of gas mass into stars, produces a mechanical luminosity provided by supernovae and stellar winds of 5×10^{33} W (Leitherer *et al.*, 1999), assuming a Salpeter initial mass function in the range $(1-100)M_\odot$. The contribution of supernovae dies off after about 4×10^7 yr, and the mechanical luminosity plummets, having yielded a total mechanical energy input of 2×10^{48} J. If the wind is allowed to expand until it reaches pressure equilibrium with the surrounding IGM, then the maximum distance the wind travels may be estimated. For example, if a fraction ν_m of the mechanical energy is available to power the wind (taking into account losses internal to the galaxy and as the wind expands), balancing the mean internal pressure $P_b = (2/3)E_b/V_s = E_b/2\pi R_s^3$ (assuming $\gamma=5/3$ for the ionized interior gas), where V_s is the bubble volume, with the pressure of the external IGM $P_{IGM} \approx 5 \times 10^{-20} T_4(1+z)^3$ N m⁻², gives a maximum comoving bubble radius of $R_{s,c} \approx 300(\nu_m/0.1)^{1/3} T_4^{-1/3}$ kpc.

The maximum radius is comparable to the geometric estimates discussed above. If radiative losses are taken into account, however, the expansion stalls before it reaches the maximum value (Madau *et al.*, 2001). More massive galaxies driving stronger winds might be appealed to, but this is problematic on two grounds: they are much rarer than dwarf galaxies at high redshifts and the ram pressure of the surrounding infalling IGM can smother the expansion of the wind (Fujita *et al.*, 2004).

An estimate of the maximum mass halo able to produce an escaping wind may be made as follows. Galaxies have nearly flat rotation curves, corresponding to envelope density profiles slightly steeper than $\rho \sim 1/r^2$ (Peebles, 1993). The infall velocity of the gas is then $v_H \approx (2GM_V/r_V)^{1/2}$, where $M_V = (4\pi/3)\rho_V r_V^3$ is the mass of the virialized halo of mean density $\rho_V = 2[3(3\pi$

$+2)/4]^2 \rho_{\text{crit}}(0)(1+z_V)^3$ and radius r_V (Sec. V.B). Assuming the gaseous component follows the profile of the envelope of dark matter, the ram pressure at the surface of the bubble is $P_{\text{ram}} = \rho v_H^2 = (3/2\pi)(\Omega_b/\Omega_m)GM_V^2/r_V^2 R_s^2$ for $R_s \gg r_V$. If the ram pressure dominates the IGM pressure, then it will determine the stalling radius where it matches P_b , according to Eq. (126). The criterion $P_{\text{ram}} < P_b < E_b/(2\pi r_V R_s^2)$ (for $R_s > r_V$) imposes the upper limit on the virial mass of the galaxies able to produce escaping winds of

$$M_V < (5 \times 10^7 h^{-1} M_\odot) \left(\frac{v_{mf*}}{0.001} \right)^{3/2} \left(\frac{1+z_V}{10} \right)^{-3/2}, \quad (128)$$

in good agreement with hydrodynamical computations (Fujita *et al.*, 2004). For a more complete treatment, hydrodynamical simulations are required. Examples of recent wind simulations include Theuns, Viel, *et al.* (2002), Aguirre *et al.* (2005), Cen *et al.* (2005), Cen and Ostriker (2006), Oppenheimer and Davé (2006), Kawata and Rauch (2007), and Kobayashi *et al.* (2007).

IX. PROSPECTS FOR THE FUTURE

IGM studies are entering a new phase in both observations and computations that promises to settle a number of outstanding questions. Prominent among these are the circumstances that led to the reionization of the Universe. At the same time, the growing recognition of the relationship between the IGM and galaxies is likely to shift the subject increasingly toward a merger with the more embracing subject of galaxy formation. Perhaps most spectacularly, imminent and planned detectors and space missions may open up a new era in IGM science: direct imaging of the structure of the IGM in the infrared and radio regions.

Recent years have witnessed the detection of high-redshift Ly- α emitting galaxies, long sought as candidates for the first-forming galaxies (Partridge and Peebles, 1967). Measurements of the Ly- α emitter luminosity function and its evolution would in principle provide evidence for the reionization epoch, as the Ly- α radiative damping edge of neutral patches would increasingly erode the lines and produce a sharp decrease in the luminosity function. Evidence for such rapid evolution over the redshift range $5.7 < z < 7$ has been obtained from the Subaru deep field (Iye *et al.*, 2006; Kashikawa *et al.*, 2006). The interpretation of any decline, however, is complicated by systematics, such as the unknown evolution in the dust content, the structure of the local IGM that may produce a Ly- α radiative damping wing, and the mass of the systems producing star formation, as well as the possible infall of the IGM toward the source and the impact of winds produced by the source on the surrounding IGM, all of which could affect the intensity and shape of the Ly- α emission line and so the evolution of the Ly- α luminosity function (Santos, 2004; Haiman and Cen, 2005; Davé *et al.*, 2006; Nilsson *et al.*, 2007). McQuinn *et al.* (2007) suggested these uncertainties may be circumvented using the angular correlation

function of the Ly- α emitters. The angular correlations will be strongly modulated by H II regions during the EOR on large scales where dark matter fluctuations are weak, providing a distinctive signature of reionization. Much improved Ly- α emitter statistics are anticipated with current or upcoming narrowband surveys which may make it possible to realize these tests (Horton *et al.*, 2004; Gardner *et al.*, 2006; Stark, Loeb, and Ellis, 2007; Ouchi *et al.*, 2008).

Anticipated CMB polarization measurements are expected to further narrow the redshift range during which reionization occurred. Polarization anisotropy measurements on arcminute scales by the recently launched Planck satellite²³ may reveal the expected patchiness of reionization, which may be used to discriminate between competing reionization scenarios (Santos *et al.*, 2003; McQuinn *et al.*, 2005; Zahn *et al.*, 2005). The Atacama cosmology telescope²⁴ (ACT) and the south pole telescope²⁵ (SPT) have already embarked on such measurements.

The relationship between the IGM and galaxies will be further clarified by upcoming galaxy surveys, especially at low redshifts. UV spectroscopy with the cosmic origins spectrograph (COS),²⁶ recently installed on HST, will refine the measurements of low- to moderate-redshift metal absorption systems, and increase sample sizes by an order of magnitude, greatly improving the statistics on the correlations with galaxies. Currently detections of the WHIM have been confined almost entirely to O VI measurements. Detections of further high-ionization species would be possible using COS as well as the spectroscopic capabilities of the proposed x-ray satellite Constellation X or a possible smaller scale satellite with high-resolution x-ray spectroscopic capability (Nicastro, 2006), providing important diagnostics on the physical properties of the WHIM. LOFAR is expected to detect the synchrotron emission from 10^7 starburst galaxies, which with follow-up optical, UV, and submillimeter observations, will provide a wealth of data that may establish the impact of winds on the IGM over a wide range of redshifts, including the spreading of metals. Even greater numbers may be detected by a square kilometer array, with an expected detection rate of several thousand at $z > 5$ per square degree surveyed. Optical spectroscopy using a giant segmented mirror telescope (GSMT),²⁷ such as the thirty meter telescope²⁸ (TMT), the giant Magellan telescope (GMT),²⁹ and an extremely large telescope³⁰ (ELT) could measure the temperature of the moderate- and even low-density components of the IGM by measuring the velocity widths of multiple metal line absorption systems. Deep

²³<http://www.rssd.esa.int/Planck>

²⁴<http://www.physics.princeton.edu/act/>

²⁵<http://spt.uchicago.edu/>

²⁶<http://cos.colorado.edu>

²⁷<http://www.gsmt.noao.edu>

²⁸<http://www.tmt.org>

²⁹<http://www.gmto.org>

³⁰<http://www.eso.org/projects/e-elt/>

photometric surveys with such large telescopes could detect very low luminosity galaxies that may be associated with low redshift metal absorption systems. The ultra-deep survey of the James Webb space telescope,³¹ to be launched in 2014, will detect dwarf galaxies out to redshifts of $6 < z < 10$, and may positively identify the population of galaxies which reionized the IGM (Gardner *et al.*, 2006; Windhorst *et al.*, 2006). These multiband measurements, extending from radio waves through x rays, will help to establish the metal pollution patterns throughout the IGM and their relationship with star-forming galaxies.

These advances will enable simulations to provide a complete description of the evolution of the IGM. Such a prospect would open up new opportunities for other areas of astrophysics and cosmology to exploit the IGM as a tool for testing models of interest. For example, the abundances and distribution of metals as well as the linewidths of metal and hydrogen absorption features around galaxies could place stringent constraints on galaxy formation models and the winds young galaxies may produce, including the possible impact on the host galaxy and its surroundings of an embedded AGN (Sijacki *et al.*, 2007). The imaging of the IGM around QSO sources could directly reveal the opening angles of their emission cones and relative orientation to the observer, placing strong constraints on unification models of AGN.

Precise predictions for the absorption statistics of the IGM may provide valuable constraints on modifications of standard cosmological models such as those allowing for a “dark energy” equation of state. Dark energy will affect the growth rate of structures in the IGM, possibly at a detectable level in future surveys (Viel, Matarrese, *et al.*, 2003). The density fluctuations in the IGM along the line-of-sight and transverse directions will differ as a consequence of the difference between radial and angular distances at high redshifts (Alcock and Paczynski, 1979). With sufficient statistics, the difference may be detectable in the correlation function or power spectrum measurements of the transmitted Ly- α flux through the IGM (Hui *et al.*, 1999; McDonald and Miralda-Escudé, 1999; Marble, Eriksen, Impey, Bai, and Miller, 2008; Marble, Eriksen, Impey, Oppenheimer, and Davé, 2008). Even more ambitious would be the direct detection of the expansion of the Universe through the monitoring of absorption lines along fixed lines of sight over a period of several years through spectroscopy on extremely large telescopes (Corasanti *et al.*, 2007; Liske *et al.*, 2008). Since realizing such a measurement would require the development of an extraordinarily stable detection system and adequate taming of systematics associated with variations in the QSO brightness and spectral shape and their effects on the noise statistics, such a project may spur efforts to investigate the technical characteristics of large telescopes and the behavior of QSOs at unprecedented levels of accuracy.

The next few years may produce the first images of the IGM. Ionizing radiation reprocessed by the neutral gas in Lyman limit systems into Ly- α photons may soon be detectable by upcoming Ly- α narrowband detectors (Hogan and Weymann, 1987; Gould and Weinberg, 1996; Cantalupo *et al.*, 2005, 2007). It may even be possible to detect the Ly- α photons emitted by a central source like a QSO and scattered by the surrounding neutral IGM prior to reionization (Leob and Rybicki, 1999) or Ly- α photons produced by collisional excitation within the rapidly expanding ionization fronts during the EOR (Cantalupo *et al.*, 2008), providing Ly- α tomographic imaging of the neutral IGM. Such detections would complement the planned IGM imaging by the LOFAR, MWA, and SKA radio facilities using 21 cm tomography. Cross correlations between the Ly- α and radio images may help to establish statistically significant detections.

At even higher redshifts, 21 cm tomography prior to reionization may become possible through the production of a 21 cm signature via Ly- α and collisional decoupling of the spin temperature from the CMB. At $z > 30$, collisional decoupling alone is adequate, offering the opportunity to explore the redshift desert $30 < z < 200$ and examine the primordial density fluctuation power spectrum on scales smaller than can be reached by CMB measurements. Such measurements could probe the structure of an inflationary potential and induced non-gaussian fluctuations (Bharadwaj and Ali, 2004; Loeb and Zaldarriaga, 2004; Barkana and Loeb, 2005; McQuinn *et al.*, 2006; Pillepich *et al.*, 2007). Astrophysical and instrumental systematics and sources of radio-frequency interference, both manmade and natural, such as arises from the ionosphere, likely preclude such measurements using currently planned radio facilities (Bowman *et al.*, 2007). These limitations, however, may be circumvented by placing a radio telescope in space. Even more adventurous would be to build a much larger facility on the far side of the Moon, where it would be shielded from terrestrial radio-frequency interference (Carilli *et al.*, 2007). The exploration of long wavelengths unavailable to terrestrial radio astronomy would open up a new panorama on the Universe, introducing a new era of “astronomy on the far side.” While not all of these prospects may materialize, others not currently envisaged will surely arise, ensuring that IGM science will continue to flourish for many years to come.

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