

**Publisher's Note: Report of the American Physical Society Study Group
on Boost-Phase Intercept System for National Missile Defense:
Scientific and Technical Issues [Rev. Mod. Phys. 76, S1 (2004)]**

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This Report was published online on 5 October 2004 with an oversight in the Acknowledgments and an error in the pagination in the Tables of Contents (both the full-article Table of Contents on p. vii and the section Tables of Contents at the beginning of each section). There was also an error in the pagination of the Lists of Tables and Figures following the full-article Table of Contents. The second sentence in the first paragraph of the Acknowledgments should have read, "We express our deep appreciation to APS Presidents James Langer (2000), George Trilling (2001), William Brinkman (2002), Myriam Sarachick (2003), and Helen Quinn (2004) and especially to APS Executive Officer Judy Franz, who have all played essential roles in advising and encouraging the study and Study Group." The page associations in the Tables of Contents and the Lists of Tables and Figures were out of synchronization with the actual pages of the Report. The Report has been corrected as of 16 February 2005. The Report is incorrect in the printed version of the journal. The corrected full-article Table of Contents and Lists of Tables and Figures are reprinted in the back of this issue as an aid to the print readers.

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D.10	Variance correction factor vs. normalized variance for tilt mode	S405