Robust and Clean Majorana Zero Mode in the Vortex Core of High-Temperature Superconductor (Li_{0.84}Fe_{0.16})OHFeSe

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The Majorana fermion, which is its own antiparticle and obeys non-Abelian statistics, plays a critical role in topological quantum computing. It can be realized as a bound state at zero energy, called a Majorana zero mode (MZM), in the vortex core of a topological superconductor, or at the ends of a nanowire when both superconductivity and strong spin orbital coupling are present. A MZM can be detected as a zero-bias conductance peak (ZBCP) in tunneling spectroscopy. However, in practice, clean and robust MZMs have not been realized in the vortices of a superconductor because of contamination from impurity states or other closely packed Caroli–de Gennes-Matricon (CdGM) states, which hampers further manipulations of MZMs. Here, using scanning tunneling spectroscopy, we show that a ZBCP well separated from the other discrete CdGM states exists ubiquitously in the cores of free vortices in the defect-free regions of $(Li_{0.84}Fe_{0.16})OHFeSe$, which has a superconducting transition temperature of 42 K. Moreover, a Diraccone-type surface state is observed by angle-resolved photoemission spectroscopy, and its topological nature is confirmed by band calculations. The observed ZBCP can naturally be attributed to a MZM arising from the chiral topological surface state of a bulk superconductor. Thus, $(Li_{0.84}Fe_{0.16})OHFeSe$ provides an ideal platform for studying MZMs and topological quantum computing.

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I. INTRODUCTION

In recent years, many recipes have been proposed for realizing MZMs [1–3], as a critical step towards topological quantum computation [4,5]. For example, MZMs are predicted to exist at the ends of a semiconductor nanowire with strong spin-orbital coupling (SOC) when it is in

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proximity to a superconductor and under a sufficiently large Zeeman field [2,3,6–8]. A quantized ZBCP has been observed in the tunneling spectrum of a hybrid device between superconducting aluminum and an InSb nanowire [9], providing compelling evidence for a MZM. However, fundamental quantum computing operations, such as braiding of MZMs in nanowires [10], are challenging and yet to be realized after a tremendous amount of ingenious technical endeavors [11,12].

Topological systems with additional dimensions provide a broader hunting ground in the search of MZM, e.g., in the vortex cores of a topological superconductor or superconducting heterostructures [1–3]. For conventional *s*-wave superconductors, confined quasiparticles in the vortex core give rise to CdGM bound states with $E = \mu \Delta^2 / E_F$, where μ is a half integer $(\pm 1/2, \pm 3/2...)$ [13].

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However, for a chiral *p*-wave superconductor, bound states still exist but with integer μ (0, ± 1 , $\pm 2...$)—the E = 0 state, or zero-energy mode, is a MZM [14]. Chiral p-wave superconductors are extremely scarce, but Fu and Kane have proposed that proximity effects from an s-wave superconductor on topological surface states would produce a two-dimensional system whose Hamiltonian effectively resembles a spinless $p \pm ip$ superconductor, and thus it can host Majorana bound states in its vortices [15] (the spinless nature is due to the fact that the topological surface state is spin nondegenerate). Based on this scenario, ZBCPs that may potentially correspond to MZMs have been found in the vortex cores of topological insulator-superconductor heterostructures (e.g., $Bi_2Te_3/NbSe_2$ and $Bi_2Te_3/FeTe_xSe_{1-x}$) [16-18], and topological surface states of bulk superconductors (e.g., $Cu_x Bi_2 Se_3$ and $FeTe_x Se_{1-x}$) [19–22]. However, an unambiguous identification or isolation of a MZM is still lacking in these systems. For materials with a large Fermi energy (E_F) , such as Bi₂Se₃/NbSe₂, Cu_xBi₂Se₃, and $Bi_2Te_3/FeTe_xSe_{1-x}$, a mode at zero energy is buried under many densely packed CdGM states in the vortex core, their energies separated by only a few μeV . Here, $FeTe_xSe_{1-x}$ has a small E_F , so its ZBCP can be readily distinguished from the CdGM states. However, there are intrinsic impurity effects of interstitial Fe and heavy Te doping [23,24]. A zero-bias impurity state was observed on interstitial Fe, which is insensitive to the magnetic field [23], but whether this is related to a MZM is yet to be confirmed. A ZBCP can be observed in a fraction of vortices in certain $FeTe_xSe_{1-x}$ samples [21], while it cannot be observed in samples annealed to reduce impurities [24]. Therefore, to study the largely unknown properties of MZMs, one needs to find a system that can host MZMs in a clean and robust manner, with weak pinning and scattering from impurities, which would lay the foundation for further operations such as braiding of MZMs.

To reach these goals, we need a superconducting system that has a large superconducting gap, a small E_F , a stoichiometric lattice (at least in the sublattice responsible for superconductivity) with few defects, a short superconducting coherence length (ξ) to potentially reduce vortex pinning, and a topologically nontrivial electronic structure. The large gap usually also means high superconducting transition temperature (T_c) and large separations between bound states in vortices, which will make the operation temperature easier to reach in practice. As topological nontrivial band structures have been predicted to exist in many iron-based superconductors [25–27], $(Li_{1-x}Fe_x)$ OHFeSe with a T_c as high as 42 K appears to be a promising candidate. It belongs to the heavily electrondoped family of iron selenide that only has electron Fermi pockets, and its E_F is merely 50–60 meV [28,29]. Unlike $FeTe_xSe_{1-x}$, the superconducting FeSe layers in $(Li_{1-x}Fe_x)OHFeSe$ are stoichiometric [Fig. 1(a)]. The remaining questions are whether it could exhibit topologically nontrivial behavior and if it hosts MZMs. To address these questions, we conduct density functional theory (DFT) and dynamical mean field theory (DMFT) calculations and ARPES measurements on $(Li_{0.84}Fe_{0.16})$ OHFeSe, and we find nontrivial band inversion and topological surface states. We study the vortex states of $(Li_{0.84}Fe_{0.16})$ OHFeSe by lowtemperature scanning tunneling microscopy (STM). In the core of impurity-free vortices, we indeed discover discrete CdGM states, which are clearly separated from a unique state located exactly at zero bias. Such a *clean and robust* zero-energy mode exists in all the free vortex cores of $(Li_{0.84}Fe_{0.16})$ OHFeSe and matches all expectations of Fu and Kane's theory, providing an ideal platform to further explore the properties and applications of MZMs.

II. RESULTS

A. Electronic structure calculations and ARPES measurements

In Fig. 1(b), we present our DFT combined with DMFT calculations of the electronic structure of $(Li_{0.75}Fe_{0.25})OHFeSe$ (details of the calculation are described in the Appendix and Sec. S1 of Ref. [30]). Along the Γ -Z direction, the three flat bands around the Fermi level are dominated by the Fe $3d_{xy}$, $3d_{xz}$, and $3d_{yz}$ orbitals, whereas the dispersive band is composed of the Se $4p_z$ orbital and the $3d_z^2$ orbital of Fe in the (Li_{1-x}Fe_x)OH layer. This dispersive Se $4p_z$ band has odd parity at the Γ and Z points. It crosses the Fermi level and the Fe 3d bands along $\Gamma - Z$, giving rise to a nontrivial band inversion and band topology. Here, Fe atoms in the $(Li_{1-x}Fe_x)OH$ layer play an important role as they hybridize strongly with the Se $4p_z$ orbital and change the dispersion and position of the Se $4p_z$ band. Without the Fe atom in the $(Li_{1-x}Fe_x)OH$ layer, the band inversion along the Γ -Z direction would not exist and the band topology would be trivial [as demonstrated in Fig. S1(b)]. The spin-orbital coupling (SOC) also plays an important role. Without SOC, the Fe $3d_{xz}$ and $3d_{yz}$ bands are degenerate at the Γ point and are in the Γ_5^+ states, whereas the dispersive Se $4p_z$ band is in the odd Γ_2^- state at the Γ point. With SOC, the doubly degenerate Γ_5^+ states are separated into a singlet low-lying Γ_6^+ state and an upper Γ_7^+ state, and the Γ_2^- state changes to the Γ_6^- state [26]. Under the C_{4v} symmetry inherent in the tetragonal crystal structure, the two Γ_6^+ and Γ_6^- state-derived Λ_6 bands with dominating Fe $3d_{xz}$ and Se $4p_z$ orbital characters hybridize with each other along the Γ -Z direction and open a gap close to 2.5 meV around their crossing point [marked by the circle in Fig. 1(b)]. The Z_2 invariant is calculated to be 1 after this SOC gap opens [26], which suggests $(Li_{0.75}Fe_{0.25})$ OHFeSe is in a topologically nontrivial phase. Since one cannot make a transition between two states with different topologies without closing the band gap-namely, here between a topological nontrivial bulk with band inversion and the topological trivial "insulating" vacuum-the transition region, i.e., surface, would host gapless topological surface



FIG. 1. Band structure and topological surface states of $(Li_{1-x}Fe_x)OHFeSe$. (a) Crystal structure (left), surface Brillouin zone (upper right), and schematic of the projection from the 3D to 2D Brillouin zone on the (001) surface (lower right) of $(Li_{1-x}Fe_x)OHFeSe$. (b) Band structure of $(Li_{0.75}Fe_{0.25})$ OHFeSe along the M- Γ -Z-(R) direction, represented by spectral functions calculated by DFT combined with DMFT methods [more extended band structure is shown in Fig. S1(a)]. The dashed circle indicates the small SOC gap at the crossing point of Se $4p_z$ and Fe $3d_{xz}$ bands. The dashed rectangle corresponds to the left half of the energy-momentum range of panel (c). (c) Calculated bulk and surface states on the (001) surface along the $\overline{\Gamma} - \overline{M}$ direction, illustrated by the spectral function. Dirac-cone-like topological surface states (TSS) centered at $\overline{\Gamma}$ connect the bulk valence band (BVB) and conduction band (BCB). The BVB and BCB are mainly composed of $3d_{xz}$ and $3d_{yz}$ orbitals along this direction, respectively. (d) Photoemission intensity of $(Li_{0.84}Fe_{0.16})$ OHFeSe measured across $\overline{\Gamma}$ along cut #1 in panel (a). The dashed curves show the bulk band structure determined by second derivatives. The green dashed rectangle corresponds to the energy-momentum range of panel (e). (e) An enlargement of data in panel (d) near E_F at the $\overline{\Gamma}$ point. Finite spectral weight can be clearly observed within the bulk band gap. (f) Second derivative of the photoemission intensity in the marked region of panel (e), where a Dirac-cone-like dispersion can be seen. (g) Momentum distribution curves (MDCs) of the data in panel (e) in the energy range of -28 meV-2 meV (normalized by the intensity near $k_{\parallel} = 0$). Red markers indicate the Dirac-cone-like dispersion extracted from the two-Lorentzian-peak fitting (blue and dashed curves). (h) The FWHM obtained from the one-peak fit [shown in Fig. S2(a)], as a function of energy. Error bars represent 95% confidence bounds. (i) E-kdispersion extracted from the two-peak fit in panel (g), and the linear fit around the crossing point. Error bars represent 95% confidence bounds of the fitted peak position. (j) Photoemission intensity taken along cut #2 across \overline{M} in panel (a). The dashed curve shows the dispersion of the bulk electron band. (k) The energy distribution curves (EDCs) of the data in panel (j) after dividing by Fermi-Dirac distribution. (1) Symmetrized EDC near the Fermi crossing of the M pocket, where a superconducting gap of around 10 meV is observed (indicated by red arrows). All the data were measured at 5.6 K using 21.2-eV photons.

states (TSS) in the band gap. More specifically, the hybridization gap between the Γ_6^+ and Γ_6^- states at the surface is removed by the discontinuity of the surface. Indeed, our calculations show that Dirac-cone-like surface

states centered at $\overline{\Gamma}$ appear on the (001) surface as shown in Fig. 1(c). The topological surface states have helical spin texture and can produce the MZM when it is in close proximity to *s*-wave superconductivity [15,26,27].

Guided by these calculations, we have conducted further ARPES measurements on high-quality $(Li_{0.84}Fe_{0.16})$ OHFeSe films grown on LaAlO₃ by hydrothermal epitaxy $(T_c \sim 42 \text{ K})$ [31,32] (see the Appendix for details). Figure 1(d) shows the ARPES spectrum of a cleaved film across the Brillouin zone (BZ) center as shown in Fig. 1(a). Multiple parabolic bands can be clearly resolved below the Fermi surface, and there is one flat band around -300 meV. Moreover, an electron band with its band bottom at about -50 meV is observed at M [Figs. 1(j) and 1(k)]. These observed bands and the ones calculated in Fig. 1(b) have one-to-one correspondence, although qualitatively. The relative positions and bandwidths may differ due to correlation effects. We also note that certain bands, such as the other electronlike band at M, were not observed here due to known matrix element effects. A precise band calculation for heavily electron-doped iron selenides is still challenging; however, qualitative features of the measured bands are reproduced by the calculation in Fig. 1(b), and the generic features here resemble several iron chalcogenide superconductors [33].

Intriguingly, in the region near the Fermi energy as plotted in Fig. 1(e), some finite spectral weight within the bulk band gap can be clearly observed. The second derivative of the region containing this spectral weight [Fig. 1(f)] displays an X-shaped band structure. Figure 1(g) shows the momentum distribution curves (MDCs) of the data in Fig. 1(e) near E_F . Through a one-Lorentzianpeak fit [shown in Fig. S2(a)], we found that the width of the spectral peak near $k_{//} = 0$ has a minimum at E =-20 meV [Fig. 1(h)]. This would indicate the position of the band crossing point. Then, we apply a two-peak fit to MDCs, assuming each peak has a constant FWHM like that of the single peak at E = -20 meV (the scattering rate variations are expected to be negligible in such a small energy window). The results display a nearly linear, Diraccone-like band dispersion, as shown in Fig. 1(g), and its overall fitting quality is better than that of the one-peak fit [see Fig. S2(c) for comparison]. In Fig. 1(i), we plot the E-k relations extracted from the two-peak fit; a linear fit is found to be plausible near the crossing point, which gives $v_F = 5.5(\pm 1.5) \times 10^4$ m/s and $E_D = 20(\pm 2)$ meV [see Fig. S2(d) for more details]. The k_F is determined to be about 0.028 Å⁻¹ through the MDC near E_F .

We note that the existence of topological surface states is determined by the band topology. The qualitative agreement between the measured and calculated band structures throughout BZ would suggest that they have the same topology. Therefore, the predicted topological surface states provide the most natural explanation for such a nearly linear, Dirac-cone-like band dispersion at Γ . Nevertheless, one should examine whether it is related to any other known electron pockets in the $(\text{Li}_{1-x}\text{Fe}_x)\text{OH}$ and FeSe surface layers exposed by cleavage. On the FeSe surface layer, an electronlike pocket would only appear around Γ after heavily doping electrons through potassium dosing, and thus it is well above the Fermi energy in the case considered here [34]. There is possibly an electron pocket around Γ in the (Li_{1-x}Fe_x)OH surface layer, based on our previous quasiparticle interference (QPI) measurements of (Li_{0.8}Fe_{0.2})OHFeSe bulk crystal [35]. However, its band bottom is at about 50 meV below E_F with a much larger Fermi velocity, so it cannot be the Dirac cone observed here. Therefore, we conclude that the observed Dirac band dispersion can only be attributed to the topological surface state predicted in our calculations.

The FeSe surface of $(\text{Li}_{1-x}\text{Fe}_x)$ OHFeSe is fully gapped [35,36], as shown in Fig. 2 below. If this topological surface state is on the FeSe surface, it should be gapped. A superconducting gap of about 10 meV can be observed on the electronlike band around \overline{M} , as shown in Figs. 1(j) and 1(k), and further illustrated in Fig. 1(l) (details are described in the caption). The absence of a gap in our data for the topological surface state around $\overline{\Gamma}$ may be attributed to the fact that this gap is small, while the resolution of ARPES is about 6 meV. Moreover, ARPES collects data over a millimeter-sized region and thus contains a large contribution from the nonsuperconducting and disordered $(\text{Li}_{1-x}\text{Fe}_x)\text{OH}$ surface, which has low-energy spectral weight near $\overline{\Gamma}$.

B. STM characterization of the sample surface and superconducting gap

STM measurement was conducted in a cryogenic STM with a base temperature of 0.4 K and had an energy resolution of 0.36 meV (see the Appendix and Ref. [30], Sec. S3). Figure 2(a) shows typical topography of a cleaved (Li_{0.84}Fe_{0.16})OHFeSe film. We observed both FeSe-terminated (left) and $(Li_{1-x}Fe_x)OH$ -terminated (right) surfaces. The inset of Fig. 2(a) shows the atomically resolved FeSe lattice with $a_0 = 3.8$ Å. Dimerlike defects at the Fe site were frequently observed (dashed circle) and are likely substitutional impurities. The typical tunneling spectrum (dI/dV) of the FeSe surface is shown in Fig. 2(b) (blue curve). It displays a full superconducting gap with two pairs of coherence peaks (referred to as Δ_1 and Δ_2) and a flat bottom, as observed in bulk crystals [35,36]. Since our band calculations and ARPES measurements reveal surface states at $\overline{\Gamma}$, it is possible that the double gaps actually originate from the bulk and the surface band, as discussed below. For the $(Li_{1-r}Fe_r)OH$ surface, the tunneling spectrum typically shows metallic behavior with a weak dip off the Fermi level [green curve in Fig. 2(b)].

To determine the gap of the FeSe surface more precisely, we fit the tunneling spectrum with a Dynes function (see Sec. S4 of Ref. [30] for details). The observed gaps are broader than an isotropic gap with a similar size [grey curve in Fig. 2(c)]. However, the line shape of the smaller gap (Δ_1) can be well fitted by an empirical anisotropic gap function: $\Delta_1(k) = \Delta_1^{\min} + (\Delta_1^{\max} - \Delta_1^{\min}) |\cos 2\theta|$ [red curve



FIG. 2. Topography, superconducting gap, QPI, and vortex mapping of $(\text{Li}_{0.84}\text{Fe}_{0.16})$ OHFeSe film. (a) Topographic image of a cleaved film ($V_b = 1 \text{ V}, I = 5 \text{ pA}$). Inset: The lattice of the FeSe surface ($V_b = 50 \text{ mV}, I = 20 \text{ pA}$). A dimerlike defect is marked by the circle. (b) Typical dI/dV spectra taken on the FeSe surface at 0.4 K ($V_b = -20 \text{ mV}, I = 60 \text{ pA}$) and on the ($\text{Li}_{0.84}\text{Fe}_{0.16}$)OH surface at 4.2 K ($V_b = -20 \text{ mV}, I = 60 \text{ pA}$). Note that Δ_1 and Δ_2 refer to the smaller and larger gaps, respectively. (c) Fits of the superconducting gap (blue dots) to a single isotropic gap function (gray dashed curve), a single anisotropic gap function (red curve), and a double anisotropic gap function (green dashed curve). Details are described in Ref. [30]. (d) Symmetrized FFT-QPI pattern of an FeSe surface taken at $V_b = 5 \text{ mV}$ (mapping size: $36 \times 36 \text{ mm}^2$). (e) Color plot of FFT line cuts through $q = (\pi, \pi)$ [azimuth averaged along the dashed circle in panel (d)]. The dashed curve is a parabolic fit to the electronlike dispersion. (f) Topographic image of an FeSe surface $(V_b = -30 \text{ mV}, I = 40 \text{ pA}; \text{size: } 36 \times 36 \text{ nm}^2$); green arrows highlight dimerlike defects. (g) ZBC map of the area in panel (f), under B = 10 T. Pinned vortices are indicated by arrows. The dashed circle encloses a free vortex. If we assume that each vortex carries a flux quantum $\Phi_0 = h/2e$, this area should contain $(B \times S)/\Phi_0 = 6.3$ vortices, consistent with the observed number of 7.

in Fig. 2(c)] after subtracting a sloping background. The fit yields $\Delta_1^{\text{max}} = 8.2 \text{ meV}, \ \Delta_1^{\text{min}} = 5.7 \text{ meV}, \text{ and a small}$ Dynes term Γ of 0.1 meV. Note that such a Δ_1^{max} value can also be estimated as half the distance between the two corresponding coherence peaks, as can Δ_2^{max} . However, the larger gap Δ_2 has additional broadening, which makes the determination of gap anisotropy difficult. The green curve in Fig. 2(c) gives a simulated spectrum with $\Delta_2^{\text{max}} =$ 14.5 meV (see Ref. [30] for details). We note that the size of Δ_1 (even Δ_1^{max}) is obviously smaller than the ARPES measured gap (~10 meV) on the \overline{M} pocket; thus, Δ_1 is unlikely from the \overline{M} pocket, and it can only be attributed to the gap of the topological surface state obtained through proximity from the bulk. On the other hand, Δ_2^{max} is larger than 10 meV, and thus Δ_2 should correspond to the bulk gap on the \overline{M} pocket. As will be shown below, the gap size measured by ARPES reflects the average size of Δ_2 .

QPI measurements were carried out on the FeSe surface. Figure 2(d) presents a typical fast-Fourier-transformed (FFT) QPI image taken at E = 5 meV and T = 4.2 K—more data are presented in Sec. S5 of Ref. [30]. The dominant features are the ringlike patterns centered at (0, 0), (π, π) , and $(0, 2\pi)$, which arise from the scattering between electron pockets at \overline{M} [35,36]. Figure 2(e) summarizes the averaged FFT line cuts through $q = (\pi, \pi)$, which displays an electronlike dispersion. Using q = 2k, a parabolic fit yields a band bottom at $-57(\pm 7)$ meV and $k_F = 0.21(\pm 0.02)$ Å⁻¹, consistent with the reported band structure at \overline{M} of $(\text{Li}_{1-x}\text{Fe}_x)$ OHFeSe [28,29]. In relation to the topological surface states at $\overline{\Gamma}$, we note that a spin-helical structure with spin-momentum locking would strongly suppress backscattering, causing them to be invisible to QPI.

Under a magnetic field of 10 T perpendicular to the surface, a zero-bias-conductance (ZBC) map is taken on a 36×36 nm² area of FeSe surface [Fig. 2(f)], as shown in Fig. 2(g). Vortex cores are visible as bright circular regions. We find that many of the vortices are pinned by dimerlike defects, as indicated by the corresponding arrows in Figs. 2(f) and 2(g). The pinned vortices all have "dark-spot"-like features near their centers, which are induced by impurity states. However, we can still find unpinned or "free" vortices



FIG. 3. Bound states in the free vortex cores. (a,b) dI/dV spectra taken across the free vortices 1 and 2, shown in the inset images, respectively (set point: $V_b = -17$ mV, I = 60 pA). (c,d) Color plots of the spatial dependence of the dI/dV spectra shown in panels (a) and (b), respectively. Dashed lines indicate the zero bias, and arrows indicate the positions of discrete low-energy states. (e,f) Topographic image and vortex mapping (B = 10 T) of an FeSe surface, respectively. Two free vortices (3 and 4) are observed in this region. (g) dI/dV spectra taken along the blue arrow in panel (e), at T = 4.2 K and B = 0 T. Red dashed lines trace the position of inner coherence peaks. (h,i) dI/dV spectra taken along the red arrows in panel (f) across the center of vortices 3 and 4, respectively (set point: $V_b = -5$ mV, I = 60 pA). Dashed lines indicate peak positions at the vortex center.

that emerge in defect-free areas, such as the one marked by a dashed circle in Fig. 2(g).

C. Discrete bound states in the free (unpinned) vortex cores

The tunneling data of four different free vortices are presented in Fig. 3. Figure 3(a) plots the dI/dV line cut taken across vortex 1 (inset image, along the arrow); the red curve is measured at the vortex center. It is remarkable that multiple (five) discrete peaks are observed near the core center. There is one peak located exactly at zero bias (a ZBCP), with the other peaks distributed symmetrically around it. The energy spacing between these 5 peaks is close to 1.5 meV. Figure 3(c) presents the spatial evolution of the spectra in a color plot. On leaving the core center, the intensities of these discrete peaks (marked by -2, -1, 0, 1, 2 here, also referred to as E_{-2} , E_{-1} , E_0 , E_1 , E_2 hereafter) decrease and vanish at about 2 nm away. Intriguingly, when the discrete peaks fade out, a pair of much broader peaks [shaded regions in Fig. 3(a)] show up at higher energies. Those peaks keep shifting to higher energies on moving

away from the core, giving an X-shaped pattern in Fig. 3(c). Figures 3(b) and 3(d) present similar data taken on another free vortex (vortex 2). Multiple low-energy core states including a ZBCP were also observed, albeit with a slightly smaller energy spacing (1 meV), and there are also "shifting" high-energy states away from the core center. The behavior of these states, except the one at zero bias, are expected for the CdGM vortex states in the quantum limit [13,37].

Such a ZBCP accompanied by discrete CdGM states was repeatedly observed in free vortices. In regions with few defects, such as the one shown in Fig. 3(e), more than one free vortex (vortices 3 and 4) could be found [Fig. 3(f)]. At zero field, a clean superconducting gap is observed over this region, which could vary by about 2 meV along the long cut [Fig. 3(g)]. Figures 3(h) and 3(i) show the dI/dV line cuts of vortices 3 and 4, respectively, focusing on the region close to the vortex center (±1.4 nm) and low energies (±5 meV). There are five discrete peaks with a ZBCP in most spectra, with the energy spacing of 0.8–1.0 meV, well above our energy resolution (0.36 meV).



FIG. 4. Quantitative characterization of the vortex core states. (a)–(d) Summed low-energy dI/dV spectra taken near the centers of vortices 1–4. Black dots are experimental data. Red solid curves are the fits to multiple Gaussian peaks (dashed curves are the individual peaks). (e) Peak energy position (marked by red vertical rods) and FWHM (represented by the length of colored bars) of the core states of vortices 1–4, obtained from Gaussian peak fitting. The black error bars represent the ranges of peak energy fluctuations (see Sec. S8 of Ref. [30] for more details). (f) Plots of $|E_2|$ (red circles) as a function of $(\overline{\Delta_1})^2$ and $|E_1|$ (blue circles) as a function of $(\Delta_2^{\max})^2$. Dashed lines are the linear fitting (see legend). (g) Spatial dependence of the intensity of the core states. Here, I_2 , I_1 , I_0 , I_{-1} , and I_{-2} represent the intensity (dI/dV values at the peak energy) of the five core states E_2 , E_1 , E_0 , E_{-1} , and E_{-2} of vortex 1. The red solid curve is the exponential fit to the decay of E_0 .

The positions of E_{-2} , E_{-1} , E_1 , and E_2 peaks vary in different vortices, and they even vary at different locations in the same vortex. As shown in Figs. 3(h) and 3(i), upon leaving the center, the positions of E_{-2} , E_{-1} , E_1 , and E_2 peaks shift away from the dashed lines that represent the peak positions at the center. This is because the CdGM states are spaced by $\delta E = \Delta^2 / E_F$, and the superconducting gap varies in space [Fig. 3(g)]. In contrast, the energy position of the E_0 peak is always at zero bias, independent of the local gap, which suggests that it is most likely protected by some global properties, such as topology. In addition, since conventional CdGM states are not located at zero energy, but at *half-integer* multiples of Δ^2 / E_F , the origin of the E_0 peak is highly nontrivial.

The high-level core states are closely packed and form the broad "shifting" peaks. In theory, the spacing between high-level states will decrease and make them undistinguishable, while the maximum intensity of core states will shift to high energy on leaving the core center [37–39], resulting in two "splitting" peaks. This behavior has been widely observed, such as in NbSe₂ (Ref. [38]); however, individual core states are rarely seen due to the small $\delta E = \Delta^2/E_F$ for most conventional superconductors. Here, we clearly observe both discrete low-level core states and the quasicontinuous high-level states, benefitting from the relatively large δE of $(\text{Li}_{1-x}\text{Fe}_x)$ OHFeSe (as shown below) and sufficiently high resolution at 0.4 K (for comparison, see Ref. [30], Sec. S6, for the T = 4.2 K data).

The well-separated low-level core states enable quantitative analysis. We first apply multiple-Gaussian-peak fitting to the summed low-energy spectra taken near the vortex center (over a range of about ± 0.7 nm to reduce the uncertainty from peak fluctuations). The results are shown in Figs. 4(a)–4(d) for vortices 1–4, respectively. Here, each core-state peak corresponds to one Gaussian peak. The fitted peak energies are directly labeled in Figs. 4(a)–4(d) and are also illustrated in Fig. 4(e) with error bars that represent the energy *range* of peak fluctuation. The full widths at half maximum (FWHM) of the Gaussian peaks are illustrated in Fig. 4(e) by colored bars. The detailed values of all the fit parameters are listed in Table SI in Ref. [30]. From the fitting, we can reveal several important facts.

First, the fitted energy of E_0 for all the vortices is negligibly small, typically 1 order of magnitude smaller than the energy resolution (0.36 meV). The fluctuation range of E_0 [error bars in Fig. 4(e)] always covers zero. Meanwhile, the FWHM of the E_0 peak is in the range of 0.59–0.80 meV, larger than the energy resolution. However, one cannot attribute such an additional broadening (0.23–0.44 meV) to two unresolved conventional CdGM states sitting close to zero bias, assuming they have the energy of $\pm \frac{1}{2}\Delta^2/E_F$, because it would require a superconducting gap with a mean size of 3.6–5.0 meV (assuming $E_F = 57$ meV), and the observed local gap size near these vortices is well above that value [see Fig. S6 and Table SII; the size of $\overline{\Delta_1} = (\Delta_1^{max} + \Delta_1^{min})/2$ is around 7 meV]. In addition, the FWHM of E_0 is obviously narrower than the FWHM of other CdGM states. As discussed below, the gap anisotropy may induce additional broadening but cannot account well for the finite width of E_0 . Therefore, within our experimental resolution, E_0 is a zero-energy state with finite width, whose origin is yet to be explored.

Second, the energies of the $E_{\pm 2}$ and $E_{\pm 1}$ states are nearly symmetric with respect to the Fermi level (with different values for different vortices). However, the spacing between E_2 and E_1 is always slightly larger than that between E_1 and E_0 . The ratio of $(E_2 - E_{-2})/(E_1 - E_{-1})$ falls between 2.1 and 2.5 for vortices 1–4 (see Table SII). This is unexpected if we assume all five states are from one single electronic component since the spacing between neighboring states will decrease when going to higher energy [37,39]. Therefore, these may actually arise from two bands with different gap size and/or band bottom position, as we observe a double gap dI/dV spectrum and a topological surface state. Meanwhile, the local gap inhomogeneity and anisotropy should also affect the energy of the core state for different vortices. Taking into account these effects, we measure the local gap size (Δ_1^{max} , Δ_1^{min} , and Δ_2^{max}) of the region where these vortices emerge (see Fig. S6 and Table SII for details). As Δ_1 is attributed to the topological surface state, and its approximate mean size is $\overline{\Delta_1} = (\Delta_1^{\text{max}} + \Delta_1^{\text{min}})/2$, considering the Dirac point is at 20 meV below the Fermi level (defined as E_D), then it could reasonably account for the E_0 and $E_{\pm 2}$ states for most free vortices through the general formula $E = \mu \Delta^2 / E_D$ and $\mu = 0, \pm 1$. In Fig. 4(f), we plot $|E_2| = (E_2 - E_{-2})/2$ vs $(\overline{\Delta_1})^2$ for different vortices (red spots); a linear fit gives $|E_2| = (0.97\overline{\Delta_1})^2 / E_D$. We note that there is a more specific calculation on the vortex states of proximity-induced superconductivity in the topological surface state [40], which gives $E = \pm 0.83 \Delta^2 / (\Delta^2 + E_D^2)^{1/2}$ for the two second-lowest states. This formula can estimate $E_{\pm 2}$ states by taking $\Delta \sim 1.06\overline{\Delta_1}$, which is also in between Δ_1^{\min} and Δ_1^{\max} (see Table SII).

For the topologically trivial bulk state around M with $E_F = 57 \text{ meV}$, its gap is Δ_2 . Its lowest-order core states should be at $\pm \frac{1}{2} \Delta_2^2 / E_F$. The mean value of Δ_2 is difficult to determine, but Δ_2^{max} can be estimated by the coherence peaks. We find that a linear fit of $|E_1| = (E_1 - E_{-1})/2$ vs $(\Delta_2^{\text{max}})^2$ yields $|E_1| = \frac{1}{2} (0.72 \Delta_2^{\text{max}})^2 / E_F$ [blue dashed line in Fig. 4(f)]. The value of $0.72 \Delta_2^{\text{max}} \approx 10$ meV is consistent

with the ARPES gap size on the band around the M point [Figs. 1(j) and 1(k)], which should be close to $\overline{\Delta_2}$. Although the two data points marked by dashed circles deviate from the fits, they still show a monotonic relation with the gap. We speculate that this could be due to some local variation of carrier concentration, which is difficult to determine precisely for each vortex. Despite this uncertainty, the most self-consistent understanding is that the E_0 and $E_{\pm 2}$ are from the topological surface state, while $E_{\pm 1}$ are from the trivial bulk band.

Third, the fitted FWHMs of the E_{+2} and E_{+1} states vary between 0.8 and 2 meV. We expect that this is at least partially due to the sizable anisotropy of Δ_1 and Δ_2 . The broadening of $E_{\pm 2}$ caused by gap anisotropy of Δ_1 [defined by $\alpha = (\Delta_1^{\text{max}} - \Delta_1^{\text{min}})/(\Delta_1^{\text{max}} + \Delta_1^{\text{min}})]$ can be estimated by $\delta(\Delta_1^2/E_{\rm D}) = 2\alpha(\overline{\Delta_1})^2/E_D$, yielding an additional broadening in the range of 0.7-1.5 meV for vortices 1-4. Meanwhile, although the gap anisotropy of Δ_2 is unknown, if we take the same value with α and assume $\overline{\Delta_2} = 0.72 \Delta_2^{\text{max}}$, its contribution to the FWHM of $E_{\pm 1}$ is in the range of 0.3–0.6 meV. Then, the resulting total broadenings are compatible with the fitted FWHMs. However, the estimated total broadening of E_{+2} (1.1–1.9 meV) is significantly larger than the FWHM of E_0 , indicative of the special properties of the latter. It is also worth noting that the core states have different but comparable weight, as reflected by the peak area summarized in Table SI. Moreover, the intensities of $E_{\pm 2}$ and $E_{\pm 1}$ are asymmetric. This is consistent with the particle-hole asymmetry expected for a superconductor with small E_F [37,41,42].

Figure 4(g) shows the spatial dependence of the intensity of the core states $\left[\frac{dI}{dV}\right]$ values at the peak energies, extracted from Fig. 3(c) for vortex 1]. The E_0 state is more concentrated at the vortex center (especially compared to E_{+2}), consistent with the calculated behavior of the vortex state of a p + ip superconductor [43,44]. An exponential fit (red solid curve) gives a decay length of 1.4 nm, which is an estimation of coherence length. Theoretically, the lowlevel core states should have an additional oscillation with a period of $\lambda_F = 2\pi/k_F$ (characterized by Bessel functions [43,44]) besides the exponential decay. Here, k_F is 0.21 Å⁻¹ for the bulk band and about 0.03 Å⁻¹ for the surface band (from QPI and ARPES measurements), which gives $\lambda_F^B = 3.0$ nm and $\lambda_F^S = 21.0$ nm. These values are both significantly larger than ξ ; thus, the λ_F oscillation cannot be observed here.

D. Core states of impurity-pinned vortices

A large number of vortices are pinned by dimerlike defects [Figs. 2(f)–2(g)], as the dimerlike defects at the Fe site can locally suppress superconductivity by inducing impurity states. Figures 5(a) and 5(b) show the tunneling spectra measured at T = 0.4 K on two typical dimerlike defects under B = 0 T and 10 T (or 11 T). Multiple, sharp,



FIG. 5. Bound states in the impurity pinned vortex cores. (a,b) dI/dV spectra measured on two dimerlike defects at B = 0 T and B = 10(11) T ($V_b = -17$ mV, I = 60 pA). Insets in panels (a) and (b): ZBC maps of the pinned vortex. (c,d) dI/dV spectra measured along the arrows in the inset image, respectively.

impurity-state peaks can be observed at B = 0 T (blue curves), and the peak positions can vary for different defects (see Fig. S8 for additional data). In some cases, a zero-bias peak can show up at the defect site in zero field [Fig. 5(b)]. At a high field, vortices pinned by these two defects are observed in the ZBC map [the insets of Figs. 5(a) and 5(b)]. The spectra on the defect sites now display signatures of split impurity states, such as the double peaks marked by arrows in Fig. 5(a) (see also Fig. S8). The zero-bias peak in Fig. 5(b) is also split away from zero bias. This result suggests that the dimerlike defects are mostly *magnetic* [45]. Figures 5(c) and 5(d) show the tunneling spectra along the arrows in the insets of Figs. 5(a) and 5(b), respectively. There is no zero-bias peak at the vortex center. Upon moving away from the defect site, the impurity states decay, while the broad high-energy core-state peaks appear [shaded regions in Figs. 5(c)-5(d)]. These observations apparently suggest a competition between CdGM and impurity states. We note that the pinned vortices always have a "hole" in their center in the ZBC map, which also indicates that the low-energy core states are strongly suppressed by the magnetic impurity (see also Figs. S5(d)–S5(f)]. Nevertheless, we note that, in some cases, the zerobias vortex state recovers a certain distance away from the defect site, as highlighted by the green curve in Fig. 5(d).

III. DISCUSSION AND CONCLUSION

Our data represent the cleanest and most robust zero-bias mode observed in vortices so far. The robustness is manifested in the following aspects:

- (i) It is always present at zero bias in free vortex cores, regardless of variations in the underlying superconducting gap.
- (ii) It can survive to high magnetic field because of the short coherence length. The ξ of $(\text{Li}_{1-x}\text{Fe}_x)\text{OHFeSe}$ is significantly smaller than that of $\text{FeTe}_x\text{Se}_{1-x}$ (~3 nm) [21] and $\text{Bi}_2\text{Te}_3/\text{NbSe}_2$ (~30 nm) [16], which also means a higher probability to observe multiple free vortices and a lower probability of pinning by impurities during vortex motion. These points are critical for braiding and fabricating qubits.
- (iii) The large superconducting gap and high T_c make the system robust against temperature fluctuations and relatively easy to study in experiments.
- The cleanness is manifested in three aspects:
 - (i) The ZBCP is unambiguously separated from other low-lying CdGM states and free from impurity effects in free vortices.
 - (ii) The FeSe layer is intrinsically stoichiometric, so an improved sample quality will allow more free vortices in larger defect-free regions, enabling further manipulation of the MZMs.
 - (iii) The width of the ZBCP is the narrowest of all the core states.

The proximity effect of bulk superconductivity induces topological superconductivity in chiral topological surface states [1-3,15], which naturally generates a MZM in the vortex core and explains our observation. Nevertheless, in Sec. S10 of Ref. [30], we use a two-band model to simulate the vortex states with a variety of possible relevant pairing functions (fully gapped to be consistent with our experiment) of the bulk superconducting state, such as pure s-wave, d + id', and nodeless d-wave, in both the presence and absence of SOC. None of these scenarios would lead to a robust ZBCP. Other origins may lead to a ZBCP in the tunneling spectrum such as the Kondo effect; SIS tunneling can also be excluded since there is no impurity in the free vortex and the tip used here is nonsuperconducting. Therefore, so far MZM is the most likely origin of the observed clean and robust ZBCP.

To summarize, our experimental and theoretical findings compellingly demonstrate that $(Li_{0.84}Fe_{0.16})OHFeSe$, a heavily electron-doped FeSe-based superconductor, is topologically nontrivial. We present the cleanest and most

robust zero-energy modes in vortices so far, which enable us to obtain the important properties of MZMs with unprecedented accuracy and reliability, including their spatial distribution, scattering rate, response to magnetic impurities, and tunneling quantum efficiency as compared to conventional CdGM states, which would put strong constraints on theory. Our work thus presents an ideal and practical platform to further study the properties of MZMs, explore their manipulation such as braiding, and construct MZM-based qubits, which opens a new, clear route to rapid progress in both the fundamental understanding and potential applications.

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Q. L. and C. C. contributed equally.

APPENDIX: EXPERIMENTS AND METHODS

The high-quality single-crystalline superconducting films of $(Li_{0.84}Fe_{0.16})OHFeSe$ were grown on a LaAlO₃ substrate by a matrix-assisted hydrothermal epitaxial method, as described in Refs. [31,32]. The full widths at half maximum (FWHM) of their x-ray rocking curves are 0.1–0.12 degrees, indicative of their high quality. The thicknesses of different films vary from 100 to 400 nm.

STM measurements were conducted in a UNISOKU cryogenic STM at T = 0.4 K or 4.2 K. The sample was cleaved at 78 K in ultrahigh vacuum with a base pressure of 5×10^{-11} Torr and immediately transferred into the STM module. Pt-Ir tips were used after being treated on a clean Au (111) substrate. The dI/dV spectra were collected by a standard lock-in technique with a modulation frequency of 741 Hz and a typical modulation amplitude ΔV of 0.1 mV at 0.4 K and 1.0 mV at 4.2 K.

ARPES data were taken under an ultrahigh vacuum of 5×10^{-11} mbar, with a Fermi Instruments discharge lamp (21.2 eV He-I α light) and a Scienta DA30 electron

analyzer. The energy resolution is 6 meV, and the angular resolution is 0.3° .

We used fully charged, self-consistent, density functional theory combined with dynamical mean-field theory (DFT + DMFT) [46] to calculate the electronic structure of (Li, Fe)OHFeSe in the paramagnetic state. The DFT part is based on the linearized, augmented, plane-wave method as implemented in WIEN2K [47]. A Hubbard U of 5.0 eV and Hund's coupling J = 0.8 eV were used in the calculations, consistent with previous calculations [48]. The DMFT quantum impurity problem was solved using the continuous-time quantum Monte Carlo method [49] at temperature T = 116 K. We used the experimentally determined crystal structure including the internal atomic positions in our calculations [50]. The surface states were calculated through the iterative Green's function method [51], taking into account the renormalization and shifting of the DFT bands due to strong electronic correlation effects. More specific details of the calculation are described in Sec. S1 of Ref. [30].

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