Direct Visualization of the Nematic Superconductivity in $Cu_rBi₂Se₃$

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(Received 16 May 2018; revised manuscript received 25 September 2018; published 12 November 2018)

 $Cu_xB₁Se₃$ hosts both topological surface states and bulk superconductivity. It has been identified recently as a topological superconductor (TSC) with an extraordinary nematic, i.e., C_2 -symmetric superconducting state and odd-parity pairing. Here, using scanning tunneling microscopy, we directly examine the response of the superconductivity of $Cu_xB₁Se₃$ to magnetic field. Under out-of-plane fields $(B_⊥)$, we discover elongated magnetic vortices hosting zero-bias conductance peaks consistent with the Majorana bound states expected in a TSC. Under in-plane fields $(B_{//})$, the average superconducting gap exhibits twofold symmetry with field orientation; the long C_2 symmetry axes are pinned to the dihedral mirror planes under $B_{\ell} = 0.5$ T but rotate slightly under $B_{\ell} = 1.0$ T. Moreover, a nodeless Δ_{4x} gap structure is semiquantitatively determined for the first time. Our data paint a microscopic picture of the nematic superconductivity in $Cu_xBi₂Se₃$ and pose strong constraints on theory.

DOI: [10.1103/PhysRevX.8.041024](https://doi.org/10.1103/PhysRevX.8.041024) Subject Areas: Condensed Matter Physics, Superconductivity, Topological Insulators

I. INTRODUCTION

Topological superconductors, as host of Majorana fermions and Majorana zero modes (MZMs) [\[1\]](#page-7-0), may facilitate topological quantum computing. However, in practice, topological superconductors (TSCs) are rare. Among the various recipes for making a TSC [\[1,2\],](#page-7-0) bulk superconductors that host topological surface states are the most natural candidates. However, unlike the theoretical triumph in predicting topological insulators [\[1,3\]](#page-7-0), metals, and semimetals, theory and experiment diverge when it comes to TSCs. Consequently, there is a large gap in our understanding of TSCs, and in particular, details of the microscopic behavior of TSCs are in urgent demand for improving theory.

 $Cu_xBi₂Se₃$ is a prototypical example of the difficulties encountered. Since it hosts both topologically nontrivial surface states and bulk superconductivity [\[4,5\],](#page-7-1) it has been proposed to be a TSC, likely with an odd-parity pairing symmetry [\[6\].](#page-7-2) However, experimental results on $Cu_xBi₂Se₃$ present challenges for this interpretation. The absence of Pauli limiting behavior in the upper critical field suggests spin-triplet superconductivity or an anisotropic spin-singlet state [\[7\],](#page-7-3) and point-contact spectroscopy found a zero-bias conductance peak (ZBCP) on a cleaved surface [\[8\],](#page-7-4) which was attributed to MZMs. However, Andreev reflection spectroscopy on $Cu_xBi₂Se₃$ shows that the existence of the ZBCP depends on the barrier strength; its absence under finite barrier strength implies the absence of zero-energy Majorana fermions [\[9\]](#page-7-5). Furthermore, a low-temperature STM study observed a full superconducting gap without ingap states or any ZBCP in the vortex core, discrediting $Cu_xBi₂Se₃$ as a TSC [\[10\]](#page-7-6).

Recently, a nematic superconducting state was discovered in a NMR study of $Cu_xBi₂Se₃$ (Ref. [\[11\]](#page-7-7)). The spin susceptibility in the superconducting state exhibits twofold symmetry when rotating the in-plane magnetic field, which is surprising considering the threefold symmetry

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of the lattice. This symmetry breaking, together with the invariance of the Knight shift upon crossing T_c under an out-of-plane field, indicates the Cooper pairs are in a pseudo-spin-triplet state with a pinned d-vector direction [\[11\]](#page-7-7). Subsequently, measurements on Cu-, Sr-, and Nb -doped $Bi₂Se₃$ superconductors all revealed twofold symmetry in the in-plane field angular dependence of the specific heat, upper critical field, critical current, and magnetoresistance below T_c (Refs. [12–[15\]](#page-7-8)). These remarkable observations in $Cu_xBi₂Se₃$ have established it as an odd-parity TSC state $[16–18]$ $[16–18]$, with the d vector pinned to a specific lattice axis by strong spin-orbit coupling. However, contradictions still exist, especially in the gap symmetry and the pinning directions of the d vectors among the reported bulk and/or macroscopic measurements $[11-15]$. The d vector is reported to be pinned along the Se─Se bond direction in a NMR study by Matano et al. [\[11\],](#page-7-7) but it lies along the dihedral mirror plane of the Se lattice in specific heat measurements by Yonezawa et al. [\[13\]](#page-7-10) and magnetoresistance measurements by Pan *et al.* [\[12\]](#page-7-8). Thus, to reach a comprehensive microscopic understanding of this unique state and to reconcile the previous contradicting reports, we investigate the superconducting properties of $Cu_xBi₂Se₃$ by STM at ultralow temperature under magnetic fields with variable direction.

II. EXPERIMENTAL METHODS

The Cu_xBi₂Se₃ ($x = 0.31$) single crystals are prepared via an electrochemical intercalation method as described in Ref. [\[19\]](#page-7-11). Magnetic susceptibility measurement shows a superconducting transition temperature (T_c) of about 3 K and shielding fraction of about 17% at 1.8 K (see Part 1A of Ref. [\[20\]\)](#page-7-12). STM measurements are conducted in a millikelvin STM system with vector magnetic field at the base temperature of 20 mK. The effective electron temperature (T_{eff}) of the system is calibrated to be 310 mK (see Part 2 of Ref. [\[20\]](#page-7-12)). The $Cu_xBi₂Se₃$ samples are cleaved in vacuum at 77 K and immediately transferred into the STM module. PtIr STM tips are used after being treated on an Au (111) surface. The dI/dV spectra are collected using a standard lock-in technique with modulation frequency $f = 787$ Hz and typical modulation amplitude $\Delta V = 30-50 \mu V$.

 $Cu_xBi₂Se₃$ crystals are thin-bar shaped with sizes of about $1.7 \times 1.3 \times 0.30$ mm³ for sample 1 and $2.5 \times 1.7 \times$ 0.14 mm^3 for sample 2. The demagnetization effect due to the irregular sample shape is very weak, as discussed in Part 1B of Ref. [\[20\]](#page-7-12); thus, it is neglected in our experiments under magnetic fields. For the measurements under $B_{//}$, the possible residual out-of-plane field component is carefully eliminated via vortex mapping (see Part 3 of Ref. [\[20\]](#page-7-12)). Moreover, the influence of the in-plane magnetic vortex and spatially inhomogeneity of superconducting gap under $B_{//}$ are considered and discussed in detail in Part 4 of Ref. [\[20\].](#page-7-12)

III. RESULTS AND DISCUSSION

The cleaved $Cu_xBi_2Se_3$ surface exhibits three types of regions (Fig. [1\)](#page-2-0), two superconducting (SC-I, SC-II) and one nonsuperconducting (NSC). The statistics on how often these regions are observed in different samples are summarized in Table I of Ref. [\[20\].](#page-7-12) The probability of SC regions being found is unexpectedly low, indicative of the intrinsically inhomogeneous superconductivity of $Cu_xBi₂Se₃$ [\[21\].](#page-7-13)

Figures [1\(a\)](#page-2-0) and [1\(b\)](#page-2-0) show the surface morphology of the NSC region. Large, flat terraces are observed, whose heights are integer multiples of 0.95 nm, as shown in Fig. [1\(e\).](#page-2-0) This height corresponds to the spacing between adjacent $Bi₂Se₃$ quintuple layers based on previous x-ray diffraction of $Cu_xBi_2Se_3$ (Ref. [\[4\]\)](#page-7-1). The terraces are atomically flat with two kinds of intrinsic defects [Fig. [1\(b\)](#page-2-0)]. Bright dots are most likely intercalated Cu atoms as seen in previous STM studies [\[10,22\],](#page-7-6) while trefoil defects, commonly observed on $Bi₂Se₃$ surfaces, arise from the substitution of Se atoms by Bi (Ref. [\[23\]](#page-8-0)). The inset of Fig. [1\(b\)](#page-2-0) shows the undistorted hexagonal Se atomic lattice with the lattice constant of about 0.41 nm. Here we define the x axis as one of the Se—Se bond directions and the y axis as perpendicular to x within the same Se plane, as indicated in the inset of Fig. [1\(b\)](#page-2-0). As for the electronic structure, a Dirac-conelike feature is suggested by linearly dispersing density of states (DOS) observed in the dI/dV spectra shown in Fig. [1\(d\)](#page-2-0) [\[23,24\]](#page-8-0), as well as the quasiparticle interference patterns along a step edge shown in Part 5 of Ref. [\[20\].](#page-7-12) The extracted Dirac point is located at about 370 meV below the Fermi energy (E_F) . This is consistent with angleresolved photoemission spectroscopy measurements on bulk $Cu_xBi₂Se₃$ crystals [\[5\],](#page-7-14) indicating the existence of topologically nontrivial surface states in NSC regions. A nearly flat DOS is observed around E_F [Fig. [1\(c\)](#page-2-0)], precluding the existence of a superconducting gap.

Figures $1(f)$ and $1(g)$ display the surface morphologies of one kind of superconducting region (SC-I) observed in sample 1. Large terraces are observed here as well, but their heights are integer multiples of 1.56 nm [Fig. [1\(j\)](#page-2-0)], much larger than in the NSC regions. Moreover, as shown in Fig. $1(g)$, the terraces are rough, with many Cu clusters distributed on them. It appears that the spacing between $Bi₂Se₃$ quintuple layers in this region is expanded considerably by Cu intercalation, which will lead to a more twodimensional structure. The SC-I region is adjacent to the NSC region shown in Figs. [1\(a\)](#page-2-0) and [1\(b\).](#page-2-0) Although the surface lattice cannot be directly seen in the SC-I region, the orientation of atomic step edges suggests it has the same lattice orientation with the nearby NSC region (see Part 1D of Ref. [\[20\]](#page-7-12) for details). The dI/dV spectrum obtained in the SC-I regions $[Fig. 1(i)]$ $[Fig. 1(i)]$ exhibits a similar Diracconelike feature, but the Dirac point is now 650 meV below E_F . This significant shift to lower energy compared to the

FIG. 1. The three types of Cu_xBi₂Se₃ surfaces and corresponding dI/dV spectra. (a),(b) Typical topographic images of the NSC region: (a) $V_b = 3$ V, $I = 20$ pA; (b) $V_b = 1$ V, $I = 20$ pA. Two kinds of typical defects are marked by green circles. The inset of (b) shows an atomically resolved image (V_b = 30 mV, I = 70 pA). (c),(d) Typical dI/dV spectra of the NSC region: (c) V_b = 2 mV, $I = 150 \text{ pA}, \Delta V = 30 \mu\text{V};$ (d) $V_b = 1 \text{ V}, I = 100 \text{ pA}, \Delta V = 10 \text{ mV}$. (e) Terrace heights in the NSC region along linecut 1 in (a). (f), (g) Typical topographic images of the SC-I region: (f) $V_b = 3 \text{ V}$, $I = 10 \text{ pA}$; (g) $V_b = 3 \text{ V}$, $I = 10 \text{ pA}$. (h),(i) Typical dI/dV spectra of the SC-I region: (h) $V_b = 2$ mV, $I = 100$ pA, $\Delta V = 50 \mu$ V; (i) $V_b = 1$ V, $I = 100$ pA, $\Delta V = 10$ mV. The orange lines in (d) and (i) show the linear dispersion of the DOS; the energies of Dirac points (DP) are indicated. (j) Terrace heights in the SC-I region along linecut 2 in (f). (k) Superconducting spectra collected across a step edge along linecut 3 in (f). (l),(m) Typical topographic images of the SC-II region: (1) differential image, $V_b = 3$ V, $I = 20$ pA; (m) $V_b = 2$ V, $I = 20$ pA. The inset of (m) shows an atomically resolved image $(V_b = 5 \text{ mV}, I = 100 \text{ pA})$. (n),(o) Typical dI/dV spectra of the SC-II region: (n) $V_b = 2 \text{ mV}, I = 200 \text{ pA}, \Delta V = 30 \mu\text{V};$ (o) $V_b = 1$ V, $I = 150$ pA, $\Delta V = 10$ mV.

NSC region indicates that the SC-I region is heavily doped with electrons. As shown in Fig. [1\(h\)](#page-2-0), a fully developed superconducting gap with pronounced coherence peaks is observed at E_F , which is consistent with previous reports [\[10,19\]](#page-7-6). We note that the heavy-electron-doping effect may be critical for the origin of superconductivity here. Such a U-shaped gap is spatially homogeneous in the SC-I region, and it is insensitive to Cu clusters and step edges,as shown in Fig. [1\(k\)](#page-2-0) and Fig. S6 in Ref. [\[20\]](#page-7-12). Usually for spin-triplet superconductors, such as $Sr₂RuO₄$, the superconductivity is very sensitive to impurities [\[25\]](#page-8-1). However, two theoretical studies suggest a different impurityscattering behavior for the unconventional superconductivity resided in a topological insulator, where the pair decoherence introduced by impurity scattering is strongly suppressed by spin-orbital coupling and spin helical nature in intercalated $Bi₂Se₃$ [\[26,27\]](#page-8-2).

In addition to the SC-I regions, we observe another type of superconducting region (referred to here as SC-II) in sample 2, on islands with steep topographic variations as shown in Figs. [1\(l\)](#page-2-0) and [1\(m\).](#page-2-0) While the NSC and SC-I regions often exhibit large flat terraces with uniform terrace height, the SC-II regions exhibit many irregular terraces of several to tens of nanometers width; the terrace height is nonuniform, even with fractional values observed, whose origins are discussed in Part 1E of Ref. [\[20\]](#page-7-12). However, the terraces are atomically flat with the atomic lattice shown in the inset of Fig. $1(m)$, which is the same as that of the NSC region. No clear Dirac-conelike feature is observed in this region, while a sharp U-shaped superconducting gap

appears at E_F , as shown in Figs. [1\(o\)](#page-2-0) and [1\(n\)](#page-2-0), respectively. Why superconductivity occurs in these islands is unclear, and we provide a discussion in Part 1E of Ref. [\[20\]](#page-7-12).

The U-shaped spectrum suggests the superconducting gap is fully opened at the Fermi surface; however, we find that it still has significant broadening beyond thermal effects, which can be reasonably accounted for by k -space anisotropy of the gap size $[11–15]$. We fitted the superconducting spectra by the Dynes formula [\[28\]](#page-8-3) with a twofold anisotropic gap function: $\Delta_k = \Delta_0 + \Delta_1 |\cos \theta|$ and $T_{\text{eff}} = 310 \text{ mK}$ (see Part 6 of Ref. [\[20\]\)](#page-7-12). A small Dynes term Γ is used to account for finite quasiparticle lifetime broadening [\[28\]](#page-8-3). The fit to the gap in the SC-I region shown in Fig. [1\(h\)](#page-2-0) yields $\Delta_0 = 0.256$ meV, $\Delta_1 = 0.206$ meV, and $\Gamma = 0.004$ meV; the fit to a typical superconducting spec-trum in the SC-II region [Fig. [1\(n\)\]](#page-2-0) yields $\Delta_0 = 0.477$ meV, $\Delta_1 = 0.103$ meV, and $\Gamma = 0.001$ meV. Evidently, these regions differ greatly in gap size and gap anisotropy ratio. Significant anisotropy of the superconducting gap is expected for the reported nematic superconducting state of $Cu_xBi₂Se₃$ (Refs. [11–[15\]\)](#page-7-7).

To further examine the superconducting state, we apply an out-of-plane magnetic field and measure the SC-I regions. Figure [2\(a\)](#page-3-0) and Fig. S9 in Ref. [\[20\]](#page-7-12) show zerobias conductance (ZBC) mappings under various B_{\perp} , where typical vortex lattices are revealed. It is notable that the vortices are significantly elongated along the y axis and exhibit an elliptical shape. Meanwhile, the vortex lattices are also stretched along this direction. Exponential fits to the profiles along the long and short axes of a vortex under $B_{\perp} = 0.2$ T are shown in Fig. [2\(b\)](#page-3-0), which give Ginzburg-Landau coherence lengths (ξ) of 30.83 and 19.70 nm, respectively, a ratio of 1∶0.64. Since the shape of the vortex is related to the superconducting gap structure [\[29\]](#page-8-4), the elongated vortices observed here are consistent with the highly anisotropic superconducting gap (Δ_k) suggested by the fit in Fig. [1\(h\)](#page-2-0), where the ratio between the gap maximum and gap minimum in the SC-I region is estimated to be $(\Delta_0 + \Delta_1)$: $\Delta_0 = 1$: 0.55. Moreover, upon increasing B_{\perp} , as the vortex density increases, the vortex size and ξ decrease noticeably [Fig. [2\(c\)](#page-3-0) and Figs. S9(a)–S9(c) in Ref. [\[20\]](#page-7-12)). Such a significant field dependence of the vortex

FIG. 2. Vortex state in the SC-I region of Cu_xBi₂Se₃. (a) Vortex mapping in the SC-I region (225 × 225 nm²) at $V_b = 0$ mV under $B_{\perp} = 0.2$ T. The profile of one vortex core is indicated by the green ellipse. (b) Exponential fits to line profiles of a single vortex along its long and short axes. (c) Field dependence of the coherence lengths along the long and short axes of the vortex. (d),(e) Evolution of the dI/dV spectra (V_b = 2 mV, I = 100 pA, $\Delta V = 50 \mu$ V) taken along the two orthogonal linecuts in (a) as indicated. The green numbers indicate the distances of the spectra from the vortex core center. (f) dI/dV spectra as a function of field strength, comparing the vortex core center (red curve) with the bulk tens of nanometers away.

size may suggest multiband effects [30–[33\];](#page-8-5) e.g., the ξ of the surface and bulk states of $Cu_xBi₂Se₃$ could be different. We note that a field-dependent coherence length was also observed in $Bi₂Te₃$ films grown on a NbSe₂ substrate [\[34\]](#page-8-6).

Figures [2\(d\)](#page-3-0) and [2\(e\)](#page-3-0) show the evolution of dI/dV spectra taken along the short and long axes, respectively, of a vortex under $B_{\perp} = 0.2$ T. Far from the vortex, the superconducting gap is only slightly affected [blue curves in Figs. [2\(d\)](#page-3-0) and [2\(e\)\]](#page-3-0), and it is gradually suppressed upon approaching the vortex core. Within a few nanometers of one vortex core center, weak ZBCPs are observed with a full width at half maximum of about 0.29 meV [red curves in Figs. [2\(d\)](#page-3-0) and [2\(e\)](#page-3-0)]. This ZBCP is observed for the first time in vortices of $Cu_xBi_2Se_3$ (Refs. [\[10,22\]](#page-7-6)). It could be composed of both conventional Caroli–de Gennes– Matricon bound states and the long-predicted Majorana bound state expected at zero energy in 2D TSC. These are hard to distinguish because the energy separation of the bound states $\delta E = \Delta^2/E_F$ (Ref. [\[35\]](#page-8-7)) is about 0.4 μ eV here, assuming $\Delta_k = 0.5$ meV and $E_F = 650$ meV. Nevertheless, our observation of a ZBCP is consistent with the prediction of TSC in $Cu_xBi₂Se₃$. As shown in Fig. [2\(f\)](#page-3-0) and Figs. S9(d), S9(e), and S10 in Ref. [\[20\]](#page-7-12), ZBCPs have also been observed in some vortex cores under $B_{\perp} = 0.3$ T, but their intensities are slightly weaker than under $B_{\perp} = 0.2$ T. The spectrum near zero bias is distorted for $B_{\perp} = 0.4$ T, and the ZBCP is clearly absent for $B_{\perp} = 0.6$ T, as shown in Fig. [2\(f\)](#page-3-0) and Fig. S9 in Ref. [\[20\].](#page-7-12) This behavior resembles the evolution of the Majorana zero-energy mode observed in $5-QL$ Bi₂Te₃ films grown on $NbSe₂$ (Ref. [\[36\]](#page-8-8)). The weakening and disappearance of a ZBCP in the vortex core under high field is interpreted as a result of the coupling between states in adjacent vortices [\[36\].](#page-8-8) When the field is small, the distance between vortices is large compared to the vortex core size, so the interaction between the vortex bound states can be neglected. Upon increasing field, the intervortex distance shortens, enhancing these interactions and eventually destroying the Majorana zero mode [\[36\]](#page-8-8).

To further illustrate the nematic superconductivity in $Cu_xBi₂Se₃$, we apply an in-plane magnetic field and study the superconducting spectra within the same area of the SC-I region as a function of θ defined as the azimuthal angle of $B_{//}$ with respect to the x axis of the Se lattice [see inset of Fig. [3\(a\)](#page-4-0)]. Under various $B_{//}$, no obvious in-plane vortices are observed on the surface, and the superconducting spectra are spatially homogeneous (see Part 4 of Ref. [\[20\]](#page-7-12) for more details). This phenomenon is possible because the superconductivity on the surface (likely resides in topological surface state) is more robust to the orbital depairing of an in-plane field so that the bulk vortex lines are pushed away from the surface, as shown theoretically in Ref. [\[37\].](#page-8-9) Consequently, the in-plane field does not generate noticeable spatial inhomogeneity on the superconducting spectrum. However, we observe obvious variation of the superconducting spectrum with the direction of B_{\perp} .

FIG. 3. The average superconducting gap as a function of θ in the SC-I region. (a) Typical dI/dV spectra measured under $B_{\perp}=0.5$ T with different field orientations. The definition of θ is indicated in the inset, where the purple spheres represent Se atoms. The definitions of Δ_{CP}^* and Δ_{LE}^* are indicated by the double-arrowed lines. (b) Angular dependence of Δ_{CP}^* and Δ_{LE}^* under $B_{//} = 0.5$ T. The sinusoidal fit highlights the clear twofold symmetry. (c),(d) Same as (a) and (b) except that $B_{//}$ is increased to 1.0 T. (e) In-plane magnetic field dependence of Δ_{LE}^* for $\theta = 85^\circ$, 40°, and 0°. (f) Field dependence of the oscillation amplitudes of Δ_{CP}^* and Δ_{LE}^* . The oscillation amplitude is defined here as the ratio of the peak-to-peak amplitude of the oscillation to the maximal gap size at that field.

Figure [3\(a\)](#page-4-0) shows typical superconducting spectra when applying a $B_{//}$ of 0.5 T at $\theta = 90^{\circ}, 40^{\circ}$, and 10°. Clearly, the superconducting gap, as estimated from both the leading edge (Δ_{LE}^*) and coherence peaks (Δ_{CP}^*), varies with θ . We use asterisks (*) here to emphasize that these actually constitute weighted averages of Δ_k under $B_{//}$. The angular dependence of Δ_{CP}^* and Δ_{LE}^* based on an extensive data set is summarized in Fig. [3\(b\)](#page-4-0) and exhibits clear twofold symmetry, with maxima around $\theta = 90^{\circ}$ and 270° (coinciding with the y axis) and minima near $\theta = 0^{\circ}$ and 180° (coinciding with the x axis). Figures $3(c)$ and $3(d)$ show similar twofold symmetry for $B_{//} = 1.0$ T. In addition, Δ_{LE}^* along $\theta = 85^{\circ}$, 40°, and 0° decrease monotonically with increasing $B_{//}$, and no crossover is observed between them, as shown in Fig. [3\(e\)](#page-4-0) and Fig. S11 in Ref. [\[20\]](#page-7-12). Our detailed experiments indicate that the superconducting gap (Δ_{CP}^*) and Δ_{LE}^*) of Cu_xBi₂Se₃ exhibits twofold symmetry throughout the studied $B_{//}$ range from 0.25 to 1.5 T. The suppression of the superconducting gap by B_{\perp} is much faster along the x axis ($\theta = 0^{\circ}$) than nearly along the y axis $(\theta = 85^{\circ})$, suggesting a smaller upper critical field B_{c2} along the x axis. Thus, a larger ξ_y is evaluated than ξ_x from the Ginzburg-Landau relations $B_{c2}^x = [(\Phi_0)/(2\pi \xi_c \xi_y)]$ and $B_{c2}^{y} = [(\Phi_0)/(2\pi \xi_c \xi_x)]$, which is consistent with our observations that the vortex is elongated along the y axis of the lattice shown in Fig. [2\(a\).](#page-3-0) Figure [3\(f\)](#page-4-0) displays the oscillation amplitudes of $\Delta_{\rm CP}^*$ and $\Delta_{\rm LE}^*$ under various $B_{//}$. The ratios are different for Δ_{CP}^* and Δ_{LE}^* , but the trend is the same—both increase gradually as $\overline{B}_{//}$ increases. For Δ_{LE}^* , the oscillation amplitude increases from 8.7% under B_{\perp} = 0.25 T to 28.9% under $B_{//} = 1.5$ T, while for Δ_{CP}^{*} it changes from 5.1% to 8.1%. The gradual smearing of the gap edge (Δ_{LE}^*) of the DOS under $B_{//}$ is consistent with the Volovik effect; the quasiparticle energy spectrum is Doppler shifted in the mixed state due to a supercurrent flow running around the vortices, which leads to a broadening of the gap edge even for a nodeless superconductor at finite temperature [\[38](#page-8-10)–42].

Our main results are summarized in Fig. [4.](#page-5-0) The data are plotted in polar coordinates and with respect to the underlying Se lattice. Figure [4\(a\)](#page-5-0) shows the profile of an elongated vortex core and the twofold symmetry of Δ_{LE}^* measured under $B_{//} = 0.5$ T for the SC-I region. The long axis of Δ_{LE}^* is shown by the red dashed line, which actually nearly coincides with the long axis of the vortex, as well as the dihedral mirror plane (dash-dot lines) of the Se lattice. Figure [4\(b\)](#page-5-0) shows the angular distribution of Δ_{LE}^* under $B_{1/} = 1.0$ T—its long axis is rotated by about 17.5° off the dihedral mirror plane. This rotation can also be readily seen by comparing the data in Figs. [3\(b\)](#page-4-0) and [3\(d\)](#page-4-0) directly, as shown in Fig. $S14(a)$ in Ref. [\[20\]](#page-7-12).

One can retrieve information on the angular distribution of Δ_k based on the angular dependence of Δ_{LE}^* . Since the

FIG. 4. Nematicity of the superconducting gap in different domains. (a) Comparison of the profile of elliptical vortex and twofold symmetry of Δ_{LE}^* under $B_{//} = 0.5$ T in the SC-I region, with respect to the Se lattice (the purple spheres represent Se atoms, gray solid lines and dash-dot lines indicate the Se─Se bond directions and the dihedral mirror planes, respectively). (b) Twofold symmetry of Δ_{LE}^* under $B_{//} = 1.0$ T in the SC-I region. (c),(d) Twofold symmetry of Δ_{LE}^* in the SC-II region observed in domain A under $B_{//} = 0.5$ T and domain B under $B_{11} = 1.0$ T, respectively. Red squares are the experimental data, while the magenta symbols in (d) denote the symmetric data obtained by shifting the experimental data by 180°. Red dashed lines show the long axis of Δ_{LE}^* through its two gap maxima. Polar coordinates are plotted out by gray dashed circles on a scale that differs among the panels; the sinusoidal fit functions describing the twofold symmetry of Δ_{LE}^* are also listed to show the oscillation amplitudes and the directions of the C_2 axes. The rotation of the long C_2 axis of Δ_{LE}^* under $B_{//} = 1.0$ T is marked in (b) and (d). The angular distribution of Δ_k in various superconducting regions is sketched by thick blue curves, whose anisotropies are extracted from the fitted gap anisotropy in Figs. $1(h)$ and $1(n)$, and Fig. S8 in Ref. [\[20\]](#page-7-12). The fitting functions for Δ_k are also listed. (e) Schematics of the in-plane-field angular-dependent quasiparticle excitation (red dots) in the low-temperature and low-field condition [\[39\]](#page-8-11).

orbital depairing effect of $B_{//}$ (in-plane vortex) is not obvious here, the influence of $B_{//}$ on superconductivity mainly includes two effects: the Volovik [38–[42\]](#page-8-10) and Zeeman effects. The former effect has been extensively studied in nodal superconductors theoretically and exper-imentally [38–[40\]](#page-8-10) and leads to a DOS under $B_{1/2}$ that exhibits characteristic oscillatory behavior with field orientation. At low temperature and low field, as illustrated in Fig. [4\(e\)](#page-5-0), more quasiparticles are excited when the field is perpendicular to the gap minimal direction of Δ_k than along other directions because the field-induced supercurrents (which run perpendicular to the field) can lead to the strongest Doppler shift of the quasiparticle energy around the gap minimal region. Thus, the short axis of Δ_{LE}^* is actually perpendicular to the gap minimal direction, since this field orientation produces the most quasiparticle excitations. Meanwhile, the application of $B_{//}$ will induce Zeeman effect, whose energy scale is about 0.1 meV for $B_{//} = 1.0$ T, comparable to the minimal gap magnitude (0.256 meV) in the SC-I region. For E_u -symmetry pairing, the d vector is expected to be parallel to the maximal gap direction of Δ_k , and it is normal to the plane in which the spins of the equal-spin-paired electrons are aligned [\[16\]](#page-7-9). The Zeeman depairing effect is the strongest when $B_{//}$ is parallel to the d vector because the electron spins may deviate from the original plane under sufficient $B_{//}$ [\[25\]](#page-8-1). Therefore, both the Volovik effect and Zeeman effect will suppress Δ_{LE}^* much more strongly when $B_{//}$ lies along the maximal gap direction of Δ_k . Consequently, the distribution of Δ_k for the SC-I region can be qualitatively determined; as illustrated by the thick blue curve in Fig. [4\(a\),](#page-5-0) the gap maxima are along a Se─Se bond direction, which is rotated 90 $^{\circ}$ from the long axis of Δ_{LE}^{*} . The tunneling spectra here and the specific heat measured by Yonezawa et al. [\[13\]](#page-7-10) reflect the integrated DOS over the Fermi surface under the influence of $B_{//}$, and they thus exhibit weaker anisotropy than Δ_k , whose anisotropy can be more precisely estimated by fitting the tunneling spectra or via the vortex anisotropy. The blue curve thus gives the first semiquantitative sketch of an anisotropic nodeless gap structure in $Cu_xBi₂Se₃$. This angular distribution of the Δ_k is consistent with the orientation of the observed elongated vortices as, empirically, a vortex will extend out in the direction of a gap minimum (assuming only weak Fermi velocity anisotropy) [\[29\].](#page-8-4)

For the SC-II region, qualitatively similar data are measured on two domains (see Figs. S12 and S13 in Ref. [\[20\]\)](#page-7-12). Δ_{LE}^* and Δ_{CP}^* in this region also vary noticeably with field orientation θ , exhibiting twofold symmetry, although the Δ_k here are larger than those of the SC-I regions. Figure [4\(c\)](#page-5-0) gives the angular dependence of Δ_{LE}^* in domain A of the SC-II region under $B_{//} = 0.5$ T; the long axis of Δ_{LE}^* lies along the dihedral mirror plane of the Se lattice. According to above analysis, the angular distribution of Δ_k in domain A is illustrated by the blue curve, with its maxima again along a Se─Se bond direction. Similar to the case of the SC-I region, in domain B of the SC-II region, which has the same lattice orientation as domain A, the long axis of Δ_{LE}^* under $B_{//} = 1.0$ T is rotated to an intermediate angle, about 20.7° off another dihedral mirror plane, as shown in Fig. [4\(d\)](#page-5-0) and Fig. S14(b) in Ref. [\[20\].](#page-7-12) The origin of such a rotation under $B_{1/2}$ 1.0 T is unclear and merits future investigation. Our data show that gap nematicity is ubiquitous in all the superconducting domains of $Cu_xBi₂Se₃$, the long $C₂$ axis of Δ_k is pinned along one of the three equivalent Se─Se bond directions, which may vary for different SC domains (see more discussion in Part 9 of Ref. [\[20\]\)](#page-7-12).

In the theory of Fu [\[16\]](#page-7-9) describing the nematic superconductivity in $Cu_xBi₂Se₃$, two types of odd-parity pairing symmetries were proposed, Δ_{4y} and Δ_{4x} . Δ_{4y} is nodeless with its gap maxima along a dihedral mirror plane of the Se lattice (y axis), while Δ_{4x} has its gap maxima along a Se—Se bond direction $(x \text{ axis})$ with a pair of point nodes in the y-z plane that are protected by mirror symmetry. The Δ_{4y} gap distribution is supported by specific heat [\[13\]](#page-7-10) and magnetoresistance measurements [\[12\]](#page-7-8). However, our data suggest that the gap maxima of Δ_k are pinned along one of the three equivalent Se─Se bond directions, consistent with the NMR study [\[11\]](#page-7-7) and supporting a Δ_{4x} pairing symmetry without nodes. The differences among bulk measurements remind us that the summed responses from all domains with different gap amplitudes and orientations may give an average gap maximum rotated from the actual ones, as the multidomain effect is directly observed in our study of the SC-II region (Part 9 of Ref. [\[20\]\)](#page-7-12) and previously discussed by Yonezawa et al. in Fig. S8 of their paper [\[13\]](#page-7-10). Thus, our findings at the atomic scale facilitate an understanding of the complex phenomena reported in bulk measurements on doped $Bi₂Se₃$ materials [11–[15\]](#page-7-7) and provide more-direct constraints on theory.

IV. CONCLUSION

In summary, our data reveal a unique nematic superconducting state in $Cu_xBi_2Se_3$ and give a semiquantitative description of its anisotropic gap distribution, which is likely a nodeless Δ_{4x} pairing symmetry. On the one hand, we observe a Dirac-conelike surface DOS in the SC-I regions, a ZBCP in vortex cores under 0.2–0.3 T out-ofplane fields, and a nematic superconducting order parameter with an anisotropic gap and a preferential symmetry axis. A nematic superconducting state with an anisotropic gap has been predicted only for odd-parity superconduc-tivity [\[16](#page-7-9)–18], and the preferential direction of the C_2 symmetry axis of the gap and its highly nontrivial response to field strength indeed suggest a pseudospin triplet pairing [\[11\]](#page-7-7). The ZBCP might be the long-sought Majorana bound state, so our findings further support topologically nontrivial superconductivity in this material. On the other hand, many aspects of our data are not readily explained by current theories for TSC. For example, we neither observe in-gap states (Fig. $1(k)$ and Fig. S15 in Ref. [\[20\]\)](#page-7-12) at the step edge as would be expected for a two-dimensional TSC [\[8,16,43\]](#page-7-4), nor do we observe in-gap states corresponding to Majorana fermions on the surface as expected for a threedimensional TSC [\[16,18\].](#page-7-9) It is still mysterious why the predicted point nodes appear to be gapped out and why the long axis of Δ_{LE}^* rotates under high $B_{//}$. In short, our findings reveal the microscopic behavior of the nematic superconductivity in $Cu_xBi_2Se_3$, which will facilitate an understanding of its extraordinary properties and microscopic pairing mechanism, and more importantly, our data impose strong constraints for further improving theories of topological superconductivity.

ACKNOWLEDGMENTS

We thank Guoqing Zheng, Jiangping Hu, Fuchun Zhang, Liang Fu, Dunghai Lee, Jing Wang, and Darren Peets for helpful discussions. This work is supported by the National Natural Science Foundation of China, National Key R&D Program of the MOST of China (Grants No. 2016YFA0300200, No. 2017YFA0303004, and No. 2017YFA0303104), National Basic Research Program of China (973 Program) under Grant No. 2015CB921700, Science Challenge Project (Grant No. TZ2016004), and Shanghai Education Development Foundation and Shanghai Municipal Education Commission (Chenguang Program). The work at Cologne receives funding from the European Research Council under the European Union's Horizon 2020 research and innovation program (Grant Agreement No. 741121) and is also supported by DFG (CRC1238 "Control and Dynamics of Quantum Materials," Projects A04).

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