

Rotational Symmetry Breaking in a Trigonal Superconductor Nb-doped Bi₂Se₃

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The search for unconventional superconductivity has been focused on materials with strong spin-orbit coupling and unique crystal lattices. Doped bismuth selenide (Bi₂Se₃) is a strong candidate, given the topological insulator nature of the parent compound and its triangular lattice. The coupling between the physical properties in the superconducting state and its underlying crystal symmetry is a crucial test for unconventional superconductivity. In this paper, we report direct evidence that the superconducting magnetic response couples strongly to the underlying trigonal crystal symmetry in the recently discovered superconductor with trigonal crystal structure, niobium (Nb)-doped Bi₂Se₃. As a result, the in-plane magnetic torque signal vanishes every 60°. More importantly, the superconducting hysteresis loop amplitude is enhanced along one preferred direction, spontaneously breaking the rotational symmetry. This observation indicates the presence of nematic order in the superconducting ground state of Nb-doped Bi₂Se₃.

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I. INTRODUCTION

Unconventional superconductors are characterized by superconducting order parameters that are noninvariant under crystal symmetry operations. When the order parameter is a single component, this noninvariance is manifested solely in the phase of the superconducting wave function and can only be detected by phase-sensitive measurements. On the other hand, when the order parameter is multi-component, the magnitude of the superconducting gap can be different along symmetry-related crystallographic directions. The gap anisotropy leads directly to a thermodynamic property of the superconducting state that spontaneously breaks the crystal rotational symmetry of the normal state. Prior to this work, no direct thermodynamic signature of rotational symmetry breaking due to superconductivity has been observed in any crystal.

Bismuth selenide (Bi₂Se₃) is one of the most promising materials to explore for unconventional superconductivity. Strong spin-orbit coupling in the triangular lattice produces a topologically insulating ground state [1,2]. Doping with a metallic element such as copper (Cu), strontium (Sr), or niobium (Nb) makes it superconducting [3–11]. We report

here the first direct observation of rotational symmetry breaking in the superconducting state of Nb-doped Bi₂Se₃ [12], a new member of the superconducting doped topological insulators. Possible odd-parity pairing symmetries in doped Bi₂Se₃, favored by strong spin-orbit interactions, have been theoretically proposed and classified according to the representations of the D_{3d} point group [5]. Among them, only the odd-parity pairing in the two-dimensional E_u representation gives rise to a nematic superconductor with broken rotational symmetry [13]. A recent nuclear magnetic resonance experiment on Cu_xBi₂Se₃ reveals an in-plane anisotropy in the spin susceptibility of the superconducting state [14], providing spectroscopic evidence for the E_u pairing. An electrical transport study on Sr-doped Bi₂Se₃ reveals the anisotropy of upper critical field H_{c2} [15]. Heat capacity measurements also show the anisotropy of H_{c2} [16]. Yet, there is not clear evidence showing the anisotropy in the superconducting properties deep in the superconducting state at H much smaller than H_{c2} . To solve this problem, we chose a unique method, torque magnetometry, to resolve the anisotropy of the superconducting critical current in these materials.

Our torque magnetometry approach is a new and powerful tool to investigate the nematicity. In general, rotational symmetry-breaking measurements require noncontact methods such as heat capacity, magnetization, or NMR since contact itself may generate a preferred axis. However, the combination of field rotation and thermal measurements or NMR requires special effort, while torque magnetometry can be performed in a rather standard and direct setup. In addition, we focus on the symmetry of the hysteresis loop as well as magnetic susceptibility in the superconducting

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state. As far as we know, this is the first time torque magnetometry has been used to investigate nematic order in the superconducting state. By contrast, torque magnetometry has been used to detect nematicity only in the normal state in superconductors URu₂Si₂ or BaFe₂(As_{1-x}P_x)₂ [17,18]. Thus, our new approach paves the way for further studies on nematicity in the superconducting ground state.

More importantly, observing nematicity in the superconducting state itself is an exciting result. As mentioned above, observing nematicity in URu₂Si₂ and BaFe₂(As_{1-x}P_x)₂ has had a huge impact on the field since it significantly helps us understand the unconventional and complicated behaviors of those superconductors. Similarly, rotational symmetry breaking in the superconducting state suggests spin-triplet pairing and topological superconductivity. Thus, our approach and results greatly impact future research on topological superconductivity.

II. EXPERIMENTAL DETAILS

The detailed growth method of Nb-doped Bi₂Se₃ single crystals is described in Ref. [12]. Crystal orientation is determined by x-ray diffraction on single crystals. The x-ray diffraction pattern is known to be almost identical to Bi₂Se₃ [19]. The crystal orientation was determined from a $2\theta = 43.7^\circ$ peak corresponding to the (110) plane.

We used torque magnetometry to measure the superconducting hysteresis loop and magnetization of Nb-doped Bi₂Se₃. Since the free energy with respect to the external field H is given by $\mathcal{F} = \mu_0 V \vec{M} \times \vec{H}$, magnetic torque is given by the derivative of \mathcal{F} with respect to the magnetic field tilt angle ϕ : $\vec{\tau} = \mu_0 V \vec{M} \times \vec{H}$. Here, V is the volume of the sample, \vec{H} is the external magnetic field, and \vec{M} is the magnetization of the sample. Torque magnetometry is thus a thermodynamic probe that measures the free energy directly.

The torque is measured by mounting the sample standing on its edge in order to keep the external field in the sample's ab plane [see Fig. 1(a)]. We then rotate the cantilever. This measures the in-plane anisotropy of the sample's magnetic properties in the superconducting state. In the general case, the dominating term of paramagnetic torque is a periodic function of double the azimuthal angle ϕ :

$$\tau_{2\phi} = \frac{1}{2} \mu_0 V M H^2 \{ (\chi_{aa} - \chi_{bb}) \sin 2\phi - 2\chi_{ab} \cos 2\phi \}. \quad (1)$$

Here, $M_i = \sum_j \chi_{ij} H_j$. In a system with high symmetry (e.g., tetragonal or hexagonal), $\tau_{2\phi}$ becomes 0 because $\chi_{aa} = \chi_{bb}$ and $\chi_{ab} = 0$. In such a case, the leading torque term becomes

$$\tau_{2n\phi} = A_{2n\phi} \sin 2n(\phi - \phi_0), \quad (2)$$

where n is determined by the crystalline symmetry: e.g., $n = 2$ for the tetragonal lattice or $n = 3$ for the hexagonal

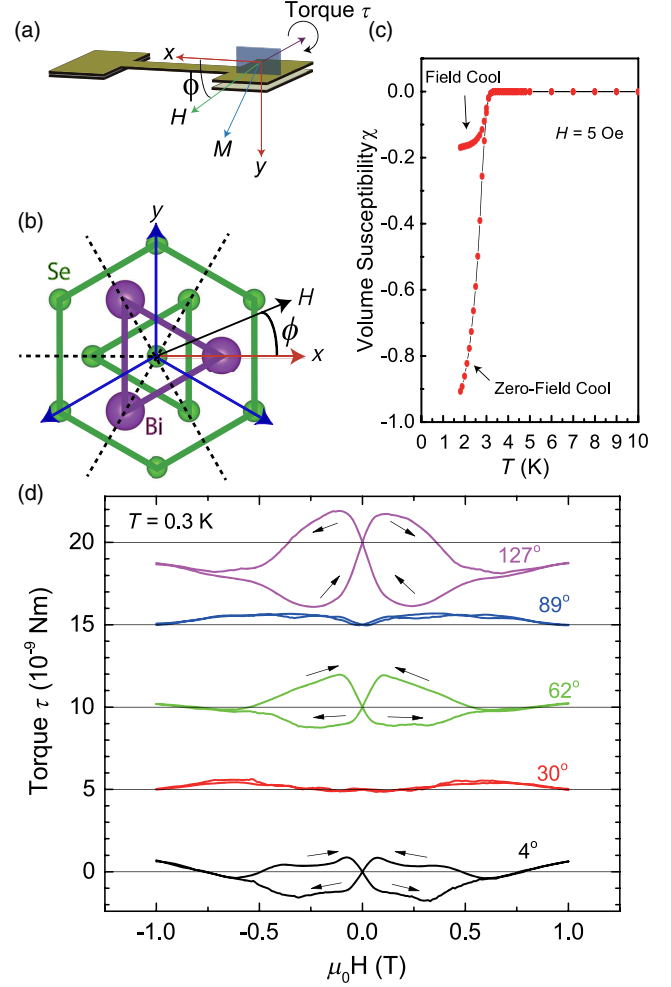


FIG. 1. Experimental setup, sample orientation, and torque curves of Nb_xBi₂Se₃. (a) Schematic sketch of torque magnetometry under in-plane field rotation. The magnetic field is applied in plane. The azimuthal angle ϕ is defined as the angle between the external magnetic field and the cantilever arm (x axis). Torque $\vec{\tau} = \mu_0 V \vec{M} \times \vec{H}$ is tracked by measuring the capacitance between the cantilever and the gold film beneath it. (b) Crystal structure of Nb_xBi₂Se₃ viewed down the crystalline \hat{c} axis. The dashed lines are the mirror planes of the crystal, and the blue arrows are the crystal axes. These crystal axes are shown to be the directions where the torque loop vanishes. (c) Meissner effect from the sample. The volume magnetic susceptibility reaches close to -1 , indicating a fully superconducting volume. (d) Selected torque curves at 0.3 K with external magnetic fields between -1 and 1 T. The magnitude of the hysteresis loop is at a maximum at around 120° and is nearly zero at 30° and 90° .

lattice. For tetragonal URu₂Si₂ or BaFe₂(As_{1-x}P_x)₂ [17,18], $\sin 4\phi$ is dominant at high temperatures, while $\sin 2\phi$ becomes pronounced at low temperatures, indicating the emergence of nematic order at low temperatures. In our case, Fig. 1(b) shows the crystal structure of Nb-doped Bi₂Se₃ looking down the hexagonal axis. As shown in the figure, the external field is in the hexagonal plane. Thus, in a paramagnetic normal state, a $\sin 6\phi$ torque response is

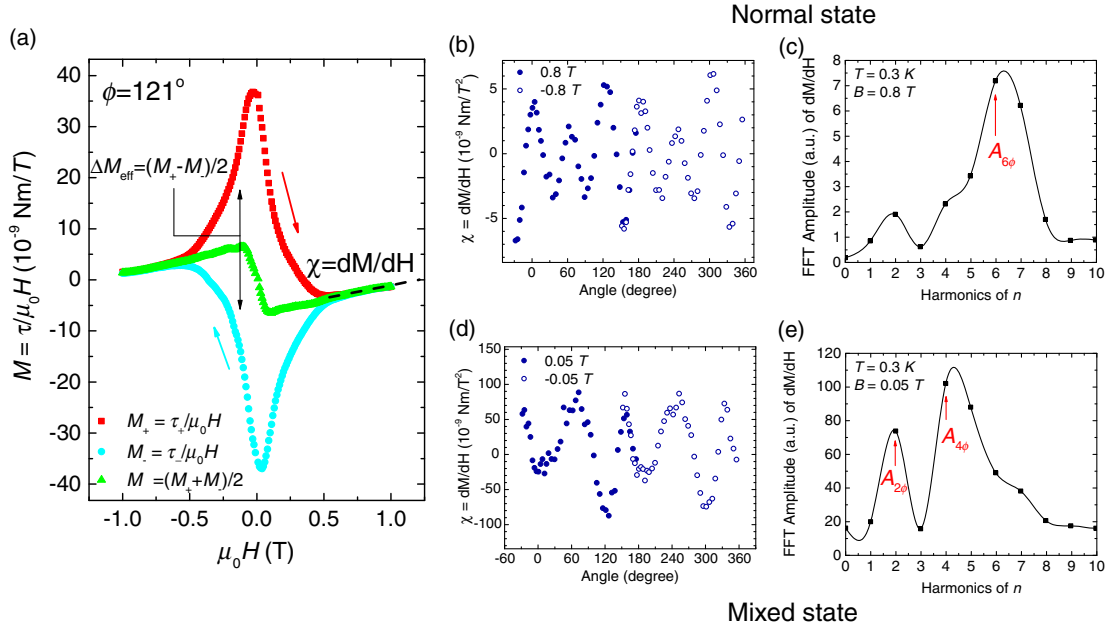


FIG. 2. The angular dependence of susceptibility of $\text{Nb}_x\text{Bi}_2\text{Se}_3$ in a normal state and superconducting state. (a) Examples of the hysteretic M - H curves demonstrate the definition of M , ΔM , and χ . Note that $M_{\pm} = \tau_{\pm}/\mu_0 H$, $M = (M_+ + M_-)/2$, $\Delta M = (M_+ - M_-)/2$, and $\chi = dM/\mu_0 dH$, where τ_+ is the torque signal from the up-sweep of the magnetic field, and τ_- is the torque signal from the down sweep of the magnetic field. (b) Angular dependence of effective susceptibility χ in a normal state at 0.3 K. A magnetic field of 0.8 T was applied to suppress the superconductivity. The angle ϕ is defined as the tilt angle between the positive x axis and the magnetic field direction. Reversing the sign of the magnetic field is equivalent to rotating the cantilever 180° . We thus used the negative field values to complete the 360° angular dependence (open circles). It is clearly shown that $\sin 6\phi$ is dominant. This indicates that the crystal has hexagonal symmetry. (c) The FFT plot of the data shown in (b). Here, $A_{6\phi}$ is dominant, while $A_{2\phi}$ and $A_{4\phi}$ are very small. (d) Angular dependence of effective susceptibility χ in a superconducting state at 0.3 K. The crystal symmetry is lower than the normal state, resulting in a lower n periodic function of ϕ . (e) FFT plot of the data shown in (d). Note that $A_{2\phi}$ and $A_{4\phi}$ are dominant, while $A_{6\phi}$ is very small. The contrast between the pattern in the normal state and the superconducting state demonstrates the breaking of the rotational symmetry in the superconducting state.

expected from the crystal structure. In this case, anisotropy in the magnetic susceptibility would bring the magnetic torque to zero along the in-plane mirror lines and the normal axis of the mirror lines of the crystal. The azimuthal angle ϕ is the angle between the external magnetic field and the x axis defined by the cantilever arm. Based on the x-ray diffraction pattern of this particular sample, we find that $\phi = 0^\circ$, 60° , and 120° correspond to the in-plane mirror line of the crystal, as shown by the dashed lines in Fig. 1(b). In the same crystal structure diagram, the blue axes are the in-plane crystal axes, which are 30° away from the mirror lines.

The Nb-doped Bi_2Se_3 sample used in our experiment has a superconducting volume close to 100%, as shown by the volume magnetic susceptibility which approaches -1 in the zero-field cooled run [see Fig. 1(c)]. This is much higher than that of Cu-doped Bi_2Se_3 [8,9].

The measured torque shows a strong superconducting signal. Figure 1(d) shows some examples of the magnetic torque on the cantilever from the sample. The torque τ is plotted as a function of the external magnetic field at temperature $T = 0.3 \text{ K}$. We swept the field up and down from -1 T to 1 T to measure the entire superconducting

hysteresis loop. Arrows along the curve show the field sweep direction. The τ - H loop is a signature of the strong flux pinning characteristic of type-II superconductors. The pinned flux lines form a vortex solid, and the flux density inside the superconductor always resists the change in the applied magnetic field. A simple analysis based on the Bean model shows that the hysteresis of the magnetization gives a direct measurement of the superconducting critical current density in the mixed state of type-II superconductors (see Supplemental Material Ref. [20]).

To probe the symmetry of the superconducting sample, we focused on both the symmetry of magnetic susceptibility and the hysteresis loop. We simply define $M_{\pm} = \tau_{\pm}/\mu_0 H$, $M = (M_+ + M_-)/2$, and $\Delta M_{\text{eff}} = (M_+ - M_-)/2$, as well as the effective magnetic susceptibility $\chi = [dM/(\mu_0 dH)]$, where τ_+ (τ_-) is the sample's magnetic torque from the H -increasing (decreasing) sweeps, respectively [Fig. 2(a)]. Since the critical field H_{c2} is about 0.6 T, above 0.6 T the sample enters the normal state and τ_+ and τ_- (also M_+ and M_-) overlap with each other. Below the critical field, $M = (M_+ + M_-)/2$ is the average magnetization from the mixed state. From the Bean model, supercurrents induced by field sweeping up and field sweeping down contribute

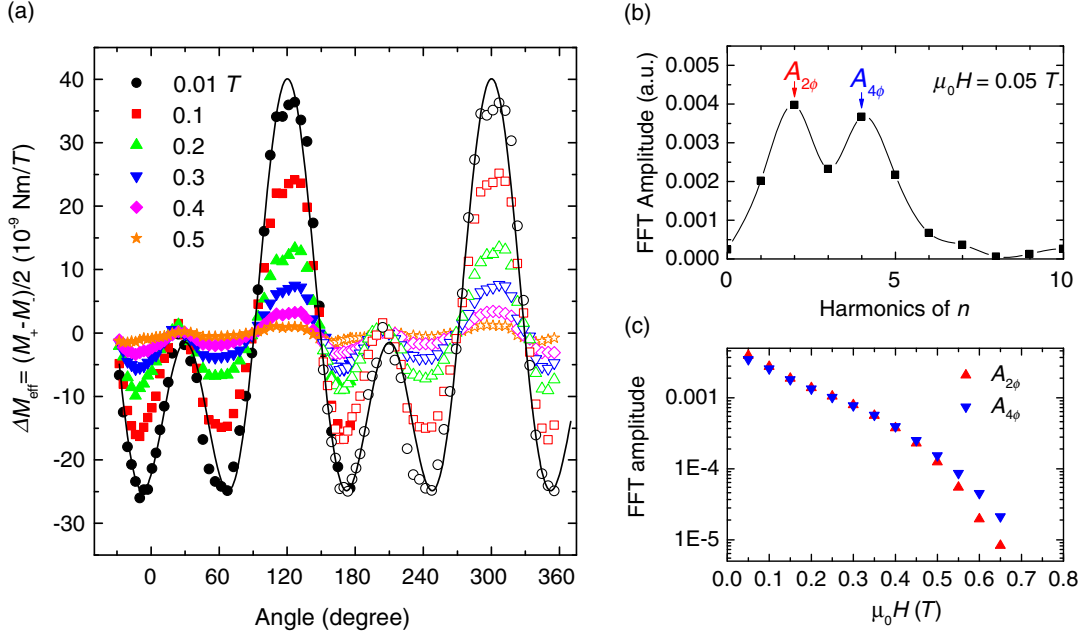


FIG. 3. The angular dependence of spontaneous effective magnetization. (a) The angular dependence of spontaneous effective magnetization $\Delta M - \phi$. The data were taken at 0.3 K at a few selected H fields. Data taken from the positive field sweep are plotted as filled symbols, and data from the negative field sweep are plotted as open symbols. The solid lines show $f(\phi) = 2A_{2\phi} \sin(\phi - 30^\circ) \cos 3\phi$. (b) FFT of $\Delta M - \phi$ at $\mu_0 H = 0.05$ T. The first peak, $A_{2\phi}$, is the amplitude of the nematic order term. The second peak, $A_{4\phi}$, represents the $\sin 4\phi$ term originating from the product fit function $f(\phi) = 2A_{2\phi} \sin(\phi - 30^\circ) \cos 3\phi$. (c) The magnetic field dependence of the FFT amplitudes $A_{2\phi}$ and $A_{4\phi}$ in the superconducting state of Nb-doped Bi_2Se_3 . The FFT amplitude is plotted in logarithmic scale for clarity. Above 0.6 T, the superconducting hysteresis loop quickly vanishes as H approaches the upper critical field.

equally, so $M = (M_+ + M_-)/2$ corresponds to the intrinsic magnetic susceptibility of the sample. The sample was measured at $T = 0.3$ K over an angular range of 200° . Reversing the sign of the magnetic field is equivalent to rotating the cantilever 180° , so we extend the negative field sweep data to complete the 360° angular dependence.

We first check the crystalline symmetry in the normal state at high fields. In the normal state, the effective magnetic susceptibility χ shows a periodic pattern with a period of 60° . Note that, while the actual anisotropic susceptibility is constant, the effective susceptibility $\chi = (dM/[\mu_0 dH])$ is multiplied by the angular factor $\sin 2n\phi$, resulting in zero or negative χ . As stated above in Eq. (2), this 60° period is expected from the hexagonal lattice of the samples. Figure 2(b) shows the angular dependence of the susceptibility χ at 0.8 T, well above the critical field. The normal state torque clearly follows a periodic function of 6ϕ . The fast Fourier transformation (FFT) of the data in Fig. 2(b) is shown in Fig. 2(c). As shown, the Fourier component of 6ϕ is dominant in the normal state. If the sample symmetry is broken, the contribution from the 2ϕ component should be orders of magnitude larger. Therefore, a small 2ϕ component would be from the higher-order term of the geometric factors. Thus, we conclude that the sample is hexagonal in the normal state.

Now, we focus on the symmetry of the superconducting state. In a superconducting state, the torque curve cannot be explained by the formula for a paramagnetic system. However, in analogy with the torque response of a hexagonal ferromagnetic material, $\tau = A_{6\phi} \sin 6\phi$, the torque curve from the hexagonal superconducting material should follow the $\sin 6\phi$ dependence as well.

In contrast, the angular dependence of our data clearly breaks the $\sin 6\phi$ pattern. Figure 2(d) shows the angular dependence of the magnetic susceptibility at 0.05 T, well below the critical field. It is clearly shown that the angular dependence of the susceptibility is different from the normal state. Figure 2(e) shows the FFT of the data in Fig. 2(d). Notice that the 2ϕ and 4ϕ components are dominant rather than the vanished 6ϕ component. This implies that the superconducting state breaks the rotational symmetry required by the crystalline lattice.

Finally, the symmetry breaking in the superconducting state is even more pronounced in the hysteresis loop. Figure 3(a) shows the magnitude of the hysteresis of the magnetization $\Delta M_{\text{eff}} = (M_+ - M_-)/2$. The hysteresis loop size, ΔM_{eff} , goes to zero every 60° . We also note that for a broad field range, the absolute amplitudes of $A_{2\phi}$ and $A_{4\phi}$ are equal, as shown in the FFT data [Figs. 3(b) and 3(c)]. Under this condition, ΔM_{eff} follows the function $f(\phi) = 2A_{2\phi} \sin(\phi - 30^\circ) \cos 3\phi$, as shown by the solid

line in Fig. 3(a). This fitting reveals a possible origin of the observed rotational symmetry breaking. The effective superconducting magnetic moment follows the *product* of $\sin(\phi - 30^\circ)$ and $\cos 3\phi$, rather than the *sum* of two ordering functions. Therefore, there is a strong coupling between the crystalline symmetry and a nematic ordering in the triangular superconductor Nb-doped Bi_2Se_3 . The phases between these two sinusoidal functions are locked in the measurement. This suggests that while nematic order is a spontaneous symmetry breaking in the superconducting state, the order seems to be stabilized by the crystalline symmetry. The coupling makes sure that the nematic ordering direction is locked to one of the mirror planes of the triangular lattice. As pointed out in Ref. [13], the nematic order verifies the two-component nature of the superconducting order parameter. Thus, an odd-parity superconducting order is very likely to exist in the ground state, which creates promise for topological superconductivity in Nb-doped Bi_2Se_3 .

III. DISCUSSION

We first discuss the advantages and disadvantages of our approach. As mentioned above, torque magnetometry does not require special instruments, except for an *in situ* rotator. This method has been used for observing the normal state symmetry breaking of strongly correlated materials [17,18] since it is very sensitive to crystal symmetry breaking. In our study, we show that the amplitude of the hysteresis loop originating from the supercurrent reflects the symmetry of the magnetic susceptibility in the superconducting state. Generally, the hysteresis signal is much larger than the signal from magnetic torque in the superconducting state, so focusing on the symmetry of the hysteresis loop is a good way to detect symmetry breaking in small samples.

There are disadvantages as well in using torque magnetometry to detect symmetry breaking. First, torque magnetometry does not directly measure the superconducting gap symmetry. Thus, even though nematic order is observed by torque, further experiments such as STM are required to understand exactly the origin of the nematicity. Second, since the anisotropy of magnetic susceptibility between in-plane and out-of-plane is one order of magnitude larger than within the plane, a small angle misalignment of the sample could affect the measurement. As shown in Ref. [20], when the sample is misaligned by a few degrees, it shows an extra contribution of the $A_{2\phi}$ component. Thus, extra attention has to be given to exclude the possibility that $A_{2\phi}$ is purely from the sample misalignment. However, note that even with the additional contribution, the measurement still reveals two key nematic features: (a) a large $A_{4\phi}$ component and (b) a vanishing $A_{2\phi}$ component with high fields.

Next, our study of the magnetic torque demonstrates a symmetric vanishing of the superconducting hysteresis. Magnetic torque is sensitive to the magnetic anisotropy of

the superconducting signal, and the hysteretic M - H loops arise from the flux pinning of the vortex solids in the superconducting state. Therefore, the superconducting diamagnetic signal, which comes from the vortex solid, prefers to align along the crystalline axis planes of the triangular lattice. As shown by the crystal structure plot in Fig. 1, the crystalline axis planes exist at every 60° . The diamagnetic signal is maximum when the magnetic field aligns with these preferred directions. The magnetic torque $\vec{\tau} = \mu_0 \vec{M} \times \vec{H}$ vanishes at these preferred directions when the M vector is exactly collinear (parallel or antiparallel) to the applied field H .

A question arises as to why the diamagnetic response is preferred on these particular axes. As pointed out in Ref. [13], the multicomponent superconducting order parameter leads to a nematic superconducting state that spontaneously breaks rotational symmetry of the crystal and exhibits uniaxial anisotropy in the ab plane. As a result, it is expected that the superconducting diamagnetic signal sticks to these preferred axes.

The hysteresis loop is greatly enhanced along one direction. To explore possible explanations for the rotational symmetry breaking, we first consider extrinsic factors that can induce symmetry breaking. First, if this was an electrical or heat transport measurement, it could be from the measurement current or the heat flow itself. However, torque magnetometry is a noncontact measurement, and it does not break the symmetry of the bulk sample. Indeed, this is one of the big advantages of our method, as torque measurement can be easily combined with field rotation. Second, structural phase transition is not likely the origin of the observed rotational symmetry breaking. We observed the smooth heat capacity and resistivity as a function of temperature (see Ref. [20]). The symmetry of the torque measurement in the normal state also shows $\sin 6\phi$ dependence as expected from the crystalline symmetry, which indicates that the rotational symmetry breaking originates from the superconducting state.

It is also possible that the spontaneous enhanced direction is locked to the strain or structure defects. The magnetization hysteresis loop measures the supercurrent. Thus, the hysteresis loop is determined by the domain structures. The domain pattern might be pinned to some directions by the crystalline defects. However, we note that the effective magnetic susceptibility χ also shows the rotational symmetry-breaking behavior in the superconducting state. Given that χ is averaged from the up and down sweeps, based on the Bean model, χ should not couple to the domain formation. Thus, the rotational symmetry breaking in χ suggests that the domain structures do not play a key role in rotational symmetry breaking. Furthermore, a periodic vanishing of the hysteresis loop requires unconventional ordering in the superconducting state. Early torque studies on high- T_c cuprates, untwinned

$\text{YBa}_2\text{Cu}_3\text{O}_7$ [21], and $\text{Tl}_2\text{Ba}_2\text{CuO}_{6+\delta}$ [22] show in-plane vanishing of the superconducting hysteresis along their crystal axes. In contrast, in classical s-wave superconductors NbN and NbSe₂, the torque signal with H in plane shows no anisotropy [22].

Therefore, we conclude that the symmetry breaking is an intrinsic behavior. There are several possible origins. The first one is odd-parity superconductivity with a nodeless superconducting gap. As shown in Ref. [20], our heat capacity measurement is consistent with a nodeless gap. However, since the superconducting volume is not 100%, there is a remaining density of states which may affect the shape of the heat capacity curve. The second possibility is a nodal even-parity superconducting gap with E_g order [13]. Recently, it has been reported that the penetration depth shows a power-law behavior at low temperatures, indicating point nodes [23]. Further experiments such as STM are required to determine whether there is a nodal gap structure in this material.

We would also like to point out a potential difference between our observations in Nb-doped Bi₂Se₃ and the similar early experimental observation in Cu-doped Bi₂Se₃ [14,16], Sr-doped Bi₂Se₃ [15], and the theoretical explanation [13] of nematic order in the spin susceptibility of Cu-doped Bi₂Se₃. In the Cu-doped material, quantum oscillations [7,9] and photoemission [6,11] reveal that there is only one bulk Fermi pocket. In contrast, the electronic state in Nb-doped Bi₂Se₃ shows at least two distinct Fermi surfaces [24]. Our work calls for further theoretical and experiential exploration of the impact of multi-orbitals in the search for unconventional superconductors. While in Sr-doped Bi₂Se₃ large H_{c2} anisotropy has been observed between fields parallel and perpendicular to the crystal axis [15], our torque shows a relatively isotropic critical field. This difference could be due to the measurement technology as torque magnetometry is a thermodynamic probe. Further study would be required to elucidate this question.

The unique sensitivity of our in-plane torque magnetometry leads to a promising new tool for probing the superconducting pairing symmetry of other unconventional superconductors. It can elucidate or confirm potential p-wave superconducting symmetry in materials such as Sr₂RuO₄ [25] and UPt₃ [26,27]. In contrast to those materials, the exponential decay in the heat capacity in Nb-doped Bi₂Se₃ suggests a superconducting gap without line nodes. It would be very interesting to investigate whether a nodal superconducting gap would enhance or diminish the nematic order in the superconducting state.

IV. MATERIALS AND METHODS

We performed torque magnetometry measurements with our home-built cantilever setup by gluing the Nb-doped Bi₂Se₃ single crystal to the end of a thin beryllium copper cantilever. We then placed the cantilever in an external

magnetic field H . We measured the torque on the cantilever by tracking the capacitance between the metallic cantilever and a fixed gold film underneath, using an AH2700A capacitance bridge with a 7-kHz drive frequency. We calibrated the spring constant of the cantilever by tracking the angular dependence of capacitance caused by the sample weight at zero magnetic field.

The tilt angle ϕ is defined as the angle between the direction of the magnetic field and the positive x axis, which is marked in Fig. 1(a) as the direction of the cantilever arm.

The sample heat capacity is measured in the Quantum Design Physical Properties Measurement System using the relaxation method.

The National High Magnetic Field Laboratory provided the magnet and He3 fridge. During the torque magnetometry measurement, samples were soaked in pumped liquid helium 3, and the magnetic field was swept at 0.25 T/min.

We performed the magnetization measurement with a Quantum Design Magnetic Properties Measurement System at $H = 5$ Oe.

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