

Orbital Ingredients and Persistent Dirac Surface State for the Topological Band Structure in $\text{FeTe}_{0.55}\text{Se}_{0.45}$

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$\text{FeTe}_{0.55}\text{Se}_{0.45}$ (FTS) occupies a special spot in modern condensed matter physics at the intersections of electron correlation, topology, and unconventional superconductivity. The bulk electronic structure of FTS is predicted to be topologically nontrivial due to the band inversion between the d_{xz} and p_z bands along Γ -Z. However, there remain debates in both the authenticity of the Dirac surface states (DSSs) and the experimental deviations of band structure from the theoretical band inversion picture. Here we resolve these debates through a comprehensive angle-resolved photoemission spectroscopy investigation. We first observe a persistent DSS independent of k_z . Then, by comparing FTS with FeSe, which has no band inversion along Γ -Z, we identify the spectral weight fingerprint of both the presence of the p_z band and the inversion between the d_{xz} and p_z bands. Furthermore, we propose a renormalization scheme for the band structure under the framework of a tight-binding model preserving crystal symmetry. Our results highlight the significant influence of correlation on modifying the band structure and make a strong case for the existence of topological band structure in this unconventional superconductor.

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The iron-based superconductors (IBSs) have substantially contributed to our understanding of electron correlation and unconventional superconductivity [1–10]. More recently, this material system has also emerged as one of the leading

platforms for the possible realization of topological superconductivity [11–19]. Among all proposed topological superconductors in IBSs, $\text{FeTe}_{0.55}\text{Se}_{0.45}$ (FTS) is the most investigated system. From density functional theory (DFT) calculations, the topological nature of FTS is predicted to arise from the inversion between the bulk p_z and d_{xz} bands along Γ -Z [20]. However, unlike weakly correlated topological materials such as Bi_2Te_3 , where theoretical predictions are usually reliable [21,22], experimental inputs are indispensable for a comprehensive understanding of FTS because of its strong electron correlation. Scanning tunneling spectroscopy experiments pioneered in identifying the possible topological superconductivity by observing zero-energy peaks at the vortex centers, which can be interpreted as Majorana zero-energy modes [23–28]. However, the

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absence of zero-energy peaks in some of the vortex cores requires further investigation [26]. In angle-resolved photoemission spectroscopy (ARPES) experiments, Zhang *et al.* first observed a Dirac-cone-like feature at a single photon energy and interpreted it as the Dirac surface state (DSS) [29]. Nevertheless, a later experiment reported that this feature exists only at certain photon energies, and speculated that it might originate from a bulk band instead of the DSS [30]. More importantly, the measured k_z dispersions [31–33] differ significantly from DFT predictions [12,20,29], with no direct evidence for either the p_z orbital or the band inversion in the bulk-band structure. These observations

challenge the claimed topological superconductivity in FTS. To resolve these conflicts, we perform systematic ARPES measurements.

We start by assigning the observed features near the Brillouin zone (BZ) center in FTS to the corresponding electronic states. According to band structure calculations [20], the states close to Fermi level are Fe d_{xz} , d_{yz} , d_{xy} , and Se/Te p_z . The intensities of the three Fe t_{2g} orbitals are strongly affected by matrix element effects near the BZ center [5,34–38]. Along the Γ - M direction under p (s) polarization, only the d_{yz} (d_{xz}) orbital is enhanced while the other t_{2g} orbitals are suppressed [see Supplemental Material

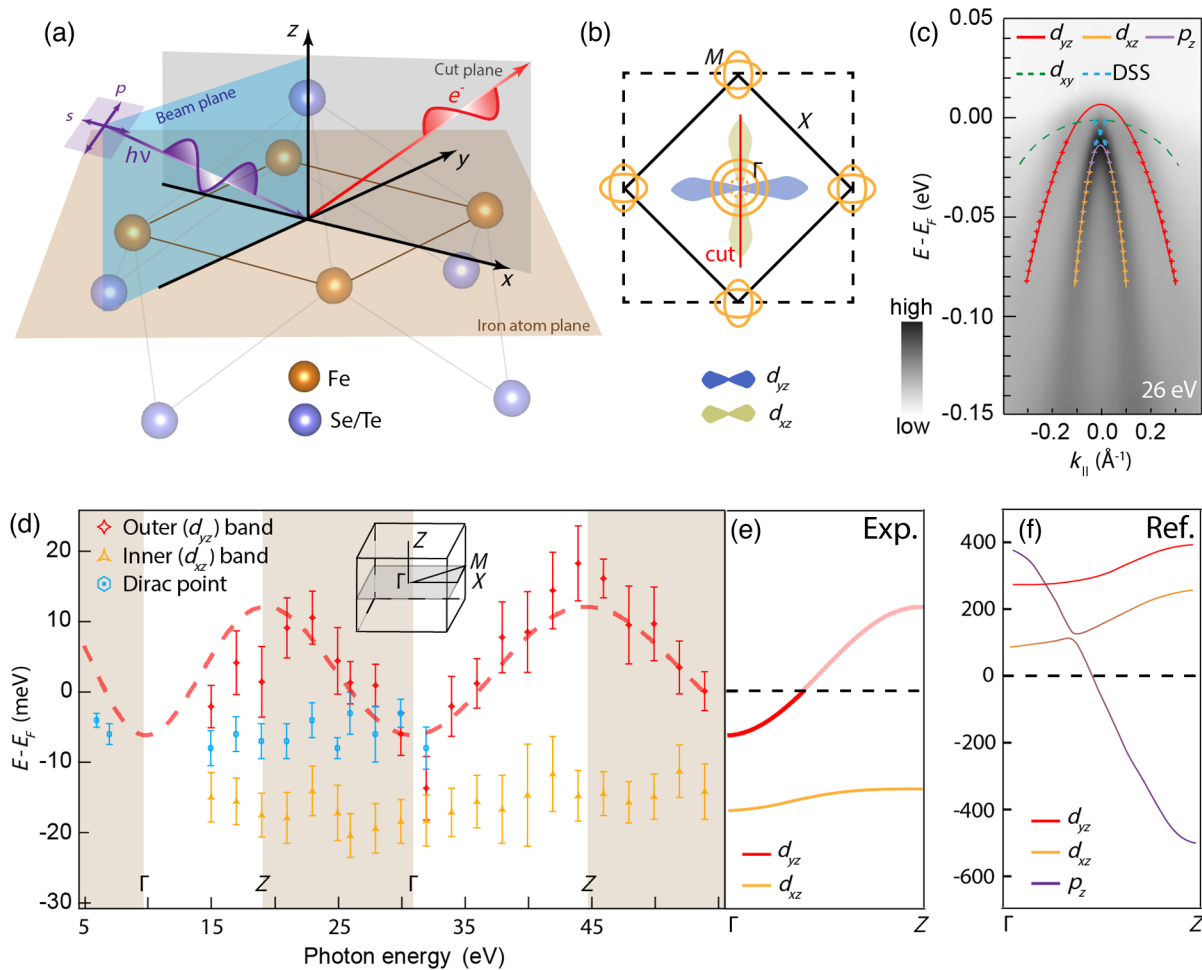


FIG. 1. ARPES experimental geometry and band dispersions along Γ - Z . (a) Schematic of the ARPES experimental geometry. The electric field of s and p polarization are normal and parallel to the beam plane, respectively. (b) Schematic of the cut geometry along Γ - M . Black solid and dashed lines show 2-Fe and 1-Fe Brillouin zones (BZ), respectively. Orange solid lines mark two holelike pockets near the zone center (d_{yz} and d_{xz} bands) and two electron pockets at M . The orange dashed line marks one holelike band closely below E_F (d_{xy} band). Green and blue patterns show the shapes of d_{xz} and d_{yz} orbitals projected on the xy plane, respectively. (c) A representative ARPES spectra along Γ - M at $h\nu = 26$ eV with p polarization. Crosses show the band dispersion extracted from momentum distribution curve (MDC) analysis. Red and purple-orange solid lines are parabolic fits to the d_{yz} and p_z - d_{xz} bands, respectively. Green and blue dashed lines are guides to the eye for the d_{xy} band and Dirac surface state (DSS), respectively. (d) Photon energy dependence of low energy electronic states. The red dashed guide to the eye indicates the periodicity of the outer band top along Γ - Z . Inset shows the 3D BZ and high symmetry points. (e),(f) Schematic of the bulk band dispersion along Γ - Z . The dispersion extracted from (d) and adapted from Ref. [20] are shown in (e) and (f), respectively.

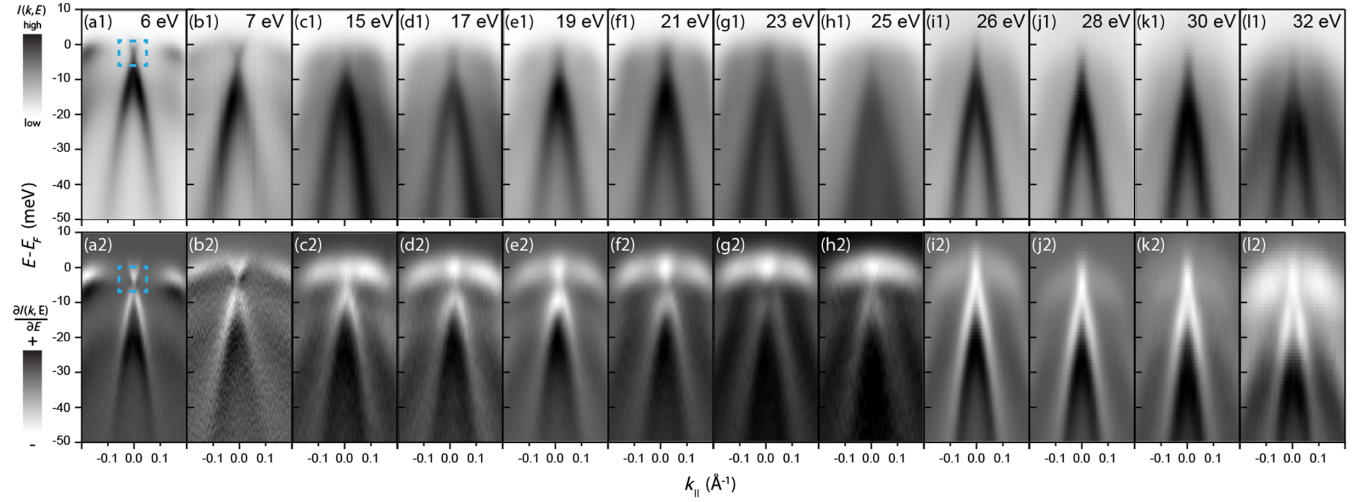


FIG. 2. Dirac surface state at different photon energies. (a1)–(l1) ARPES spectra over a wide range of photon energies. (a2)–(l2) The first-energy-derivative spectra in (a1)–(l1). Blue dashed boxes indicate the energy-momentum window containing the DSS signal. 6–7 eV spectra are taken with lasers. 15–25 and 26–32 eV spectra are taken with synchrotron light source at two complementary beam lines. All cuts go through BZ center. Detailed analysis on DSS is presented in Supplemental Material Fig. S2 and S3 [39].

(SM) Secs. 1 and 6 for details [39]. Figure 1(c) shows a representative ARPES spectrum along Γ - M in-plane direction under p polarization at photon energy $h\nu = 26$ eV [the corresponding data under s polarization are shown in Fig. S1(b) in SM [39]]. Similar to the other IBSs in the 11 family [5,35–37], we observe three hole bands near E_F . The outer band [Fig. 1(c), red line] is of d_{yz} character and is observed only under p polarization. The d_{xy} orbital produces a flat holelike band [Fig. 1(c), green line] with weak intensity, which can be more clearly identified in the second-energy-derivative spectra [Fig. S1(c), green dashed line]. The inner band is typically identified with the d_{xz} orbital in 11-family compounds and has weak (strong) intensity under p (s) polarizations. Surprisingly, the inner band here [Fig. 1(c), orange-purple line] has strong intensity under both p and s polarizations, which we will explain later.

We perform parabolic fits to the in-plane dispersions of bulk bands obtained from momentum distribution curve (MDC) analysis (see SM Sec. II for details [39]). The extracted band top positions are plotted in Fig. 1(d) as a function of photon energy (or k_z , with fitted inner potential $V_0 \approx 11.3$ eV; see SM Sec. III for details). The outer band top shows periodic oscillations spanning a ~ 20 meV range [red guideline in Fig. 1(d)], while the inner band shows almost no k_z dispersion within measurement uncertainties, consistent with previous reports [31–33]. Figures 1(e) and 1(f) show the schematic band k_z dispersion extracted from experiments and the DFT calculations in Ref. [20], respectively. Contrary to the DFT calculations, first glance revealed neither a k_z -dispersive p_z band nor band inversion, with an additional inconsistency in fermiology. Indeed, the k_z dispersion of the inner band is almost identical to those in other 11-family compounds without band inversion [40], raising questions on the predicted topological nature in FTS.

To resolve the discrepancies, in the following, we will report three observations unique to FTS to support a topological band structure: (i) the k_z -independent DSS, (ii) the presence of p_z orbital character in the inner band, and (iii) the orbital character crossover hinted by the spectral weight variations.

We first demonstrate the k_z -independent DSS. Figures 2(a1)–2(l1) show the enlarged spectra near E_F over a wide range of photon energies, taken with 6 and 7 eV lasers and synchrotron photons between 15 and 32 eV. Our result is consistent with the first report of the DSS at $h\nu = 7$ eV [29], but contains data covering the entire Γ - Z trajectory. Contrary to the previous photon-energy-dependence study [30], we find that the DSS feature persists throughout the photon energy range in Figs. 2(a1)–2(l1) in the energy-momentum window indicated by the blue dashed box [Figs. 2(a1) and 2(a2)]. The first-energy-derivative plots in Figs. 2(a2)–2(l2) better highlight the DSS at some photon energies. We note that the DSS feature exists in a very narrow momentum and energy window, and consequently requires careful measurements with optimized measurement alignment, small beam spot size, and high instrument resolution. Following an earlier study [33], we further perform a quantitative analysis to confirm the k_z -independent DSS signal. We fit MDCs between -14 meV and E_F , and extract the widths of the MDC peaks associated with the DSS as a function of energy (see SM Sec. IV for details [39]). The MDC widths are expected to reach minimum at the binding energy of the Dirac point. In Fig. 1(d), we show that the binding energy of the Dirac point stays fixed as a function of photon energy, despite the ~ 20 meV k_z dispersion of the d_{yz} band. The 2D nature of the Dirac-cone-type feature confirms its surface state origin and rules out the interpretation of the p_z

band bottom in an earlier study [41]. Above 32 eV, the DSS signal becomes hard to identify because of the deteriorated in-plane momentum resolution and a potential matrix element suppression of the p_z atomic orbital component (to be discussed below) [42]. Nevertheless, the photon energy range presented here is large enough to cover the entire Γ -Z range [Fig. 1(d)]. Therefore, our data support the DSS interpretation and exclude the possibility that the Dirac-cone-like dispersion comes from the subtle bulk-band crossing at specific k_z [30].

Having confirmed the existence of DSS, we now look for its bulk correspondence by first searching for the evidence of the p_z orbital that participates in the band inversion with the d_{xz} . In Fig. 3, we compare the spectra of FTS with those of FeSe, a closely related compound predicted to have no band inversion along Γ -Z [20]. Figures 3(a)–3(e) and 3(g)–3(i) show spectra of FTS and FeSe along the Γ -M direction at different photon energies, respectively. We first compare the band intensity as a function of in-plane

momentum (k_{\parallel}). Along the Γ -M direction under p polarization, the matrix element of the d_{xz} is suppressed near $k_{\parallel} = 0$, while the matrix elements of d_{yz} and p_z orbitals remain large (Figs. S10 and S12 [39]). Experimentally, we indeed find that the inner band of FeSe, whose orbital character is dominantly d_{xz} without considering the spin-orbit coupling (SOC) [40], has suppressed intensity near the inner band top ($k_{\parallel} = 0$) [Figs. 3(g)–3(i)]. In contrast, the inner band of FTS shows maximal intensity at $k_{\parallel} = 0$ [Figs. 3(a)–3(e)]. This indicates the presence of either the d_{yz} or the p_z orbital component near the inner band top.

To better understand this orbital component, we further look into the spectral weight contrast between the inner and outer bands. We quantify the contrast by defining the spectral weight ratio (SWR) as the ratio between the average intensities in region 2 [orange bar in Fig. 3(a) sampling the inner band] and region 1 [red bars in Fig. 3(a)

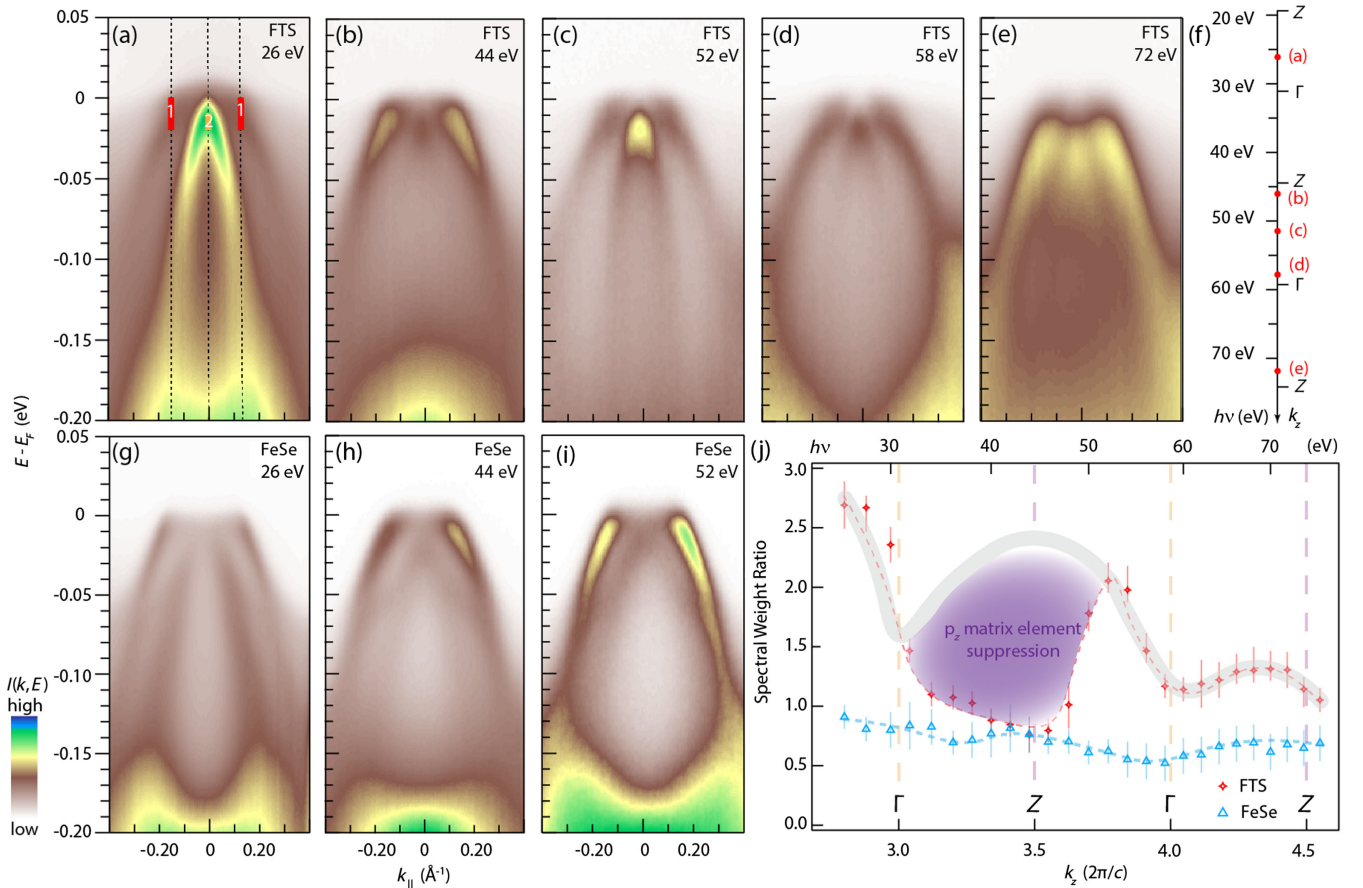


FIG. 3. Spectral weight modulation in FTS. (a)–(e) FTS spectra cut along Γ -M taken at $h\nu =$ (a) 26 eV, (b) 44 eV, (c) 52 eV, (d) 58 eV, and (e) 70 eV, respectively. The red and orange bars in (a) indicate region 1 and region 2 in spectral weight analysis, respectively. (f) Correspondence between photon energy and k_z for FTS. Red dots mark photon energies in (a)–(e). (g)–(i) FeSe spectra cut along Γ -M taken at (g) 26 eV, (h) 44 eV, and (i) 52 eV, respectively. (j) The spectral weight ratio (SWR) as a function of photon energy for FTS and FeSe. The k_z values apply to FTS only. Orange and purple dashed lines indicate Γ and Z points in FTS, respectively. The gray line is a guide to the eye for the expected oscillatory behavior. The purple shaded area marks the anomalous matrix element depression. All cuts are along Γ -M taken under p polarization.

sampling the outer band; see SM Sec. V for details [39]). The SWRs for the Γ - M cut are plotted in Fig. 3(j) as a function of photon energy (see Figs. S6 and S8 for the raw spectra [39]). For FeSe, the SWR remains almost constant with tiny modulations. This behavior is expected because the dominant orbital components for the inner and outer bands in FeSe are d_{xz} and d_{yz} , respectively [40], and the matrix element ratio between these two orbital components is roughly photon-energy independent (Fig. S10 [39]). In contrast, the SWR for FTS shows strong and intricate modulations, echoing the in-plane intensity distribution anomaly and consistent with the k_z -dependent mixing of either the d_{yz} or the p_z orbital components in the inner d_{xz} band. In the case of d_{yz} mixing with d_{xz} , the SWR modulation is only expected in the data collected along the Γ - M but not the Γ - X direction, because these two orbitals have the similar matrix elements along Γ - X as required by symmetry [Fig. S5(d); also see SM Sec. 5 for details [39]]. However, we also observe a similar SWR modulation in data taken along Γ - X (see SM Sec. V for details). Therefore, the SWR modulations can only arise from the hybridization between the d_{xz} and p_z orbitals near the inner band top. The contrasting behaviors in FeSe and FTS highlight the importance of the Te $5p_z$ orbital: It introduces strong interlayer hopping and brings the p_z dispersion across the Fe t_{2g} bands [20], eventually leading to a significant mixing of the p_z orbital character into the inner Fe d_{xz} band.

Having established the p_z orbital component, we now further look for evidence of d_{xz} - p_z orbital character crossover near the inner band top as a function of k_z —a natural consequence of the bulk-band inversion. The SWR in FTS in Fig. 3(j) can be understood as a product of two effects: an oscillatory behavior by the orbital character change (gray guide to the eye) and an anomalous depression of the photoemission matrix element near 40 eV (purple shaded area). The overall oscillatory behavior suggests that the spectral weight of the inner band reaches the maximum at Z and the minimum at Γ . This implies a d_{xz} - p_z crossover of the orbital character going from Γ to Z at the inner band top since the p_z orbital has a much larger photoemission matrix element than that of the d_{xz} orbital under p polarization. On the other hand, the anomalous suppression can be attributed to the matrix element effect. To show this, we calculate the photoemission dipole matrix element approximately using free-electron plane-wave states as final states and hydrogenlike wave functions as initial states (see SM Sec. VI. 1 for details [39]) [43–45]. The calculated matrix elements of the d_{xz} and p_z orbitals are further normalized by that of the d_{yz} orbitals for direct comparison with SWR (Fig. S11 [39]). We observe a strong atomic photoemission matrix element suppression of the p_z orbital around 40 eV, consistent with the experimental data. However, we cautiously note that such matrix element suppression is sensitive to the approximations of wave functions for the initial and final states (see SM Sec. VI for detailed

discussion). Nevertheless, the novel spectral weight in FTS highlights the existence of p_z orbital, and furthermore, serves as a strong hint for the d_{xz} - p_z orbital character crossover.

We remark that a related spectral weight modulation of the d_{xz} orbital in the inner band under the s polarization has been reported in Ref. [33] with a similar k_z periodicity in support of band inversion. However, our comprehensive data here reveal the more critical and unconventional elements in FeSCs, the p_z orbital component under the p polarization, and present a complete picture with more convincing experimental evidence indicating the inversion between the p_z and d_{xz} bands by (i) the identification of the p_z orbital and exclusion of other mixing possibilities in FTS, (ii) the expected absence of such p_z orbital in the control experiment of FeSe, (iii) the observation of SWR modulation further supporting the d_{xz} and p_z band crossing along the Γ - Z direction, and (iv) the persistent DSS required by a nontrivial topological band structure.

With a confirmed topological band structure, we finally show a picture to reconcile the discrepancy between Figs. 1(e) and 1(f) under the framework of a tight-binding model preserving crystal symmetry (see SM Sec. VII for details [39]). Starting from the band structure calculated by the DFT [Fig. 4(a)], we make adjustments in two steps: (i) renormalize the d bands by a factor of 3 with respect to the experimental E_F in accordance with the in-plane dispersion [4,5,37,46] [Fig. 4(b)], and (ii) increase the d_{xz} - p_z SOC strength as a phenomenological factor to further capture the many-body interactions [Fig. 4(c)]. See SM Sec. VII for details [39]. It is worth noting that a quantitative reproduction of experimental observations further requires an E_F that locates in the gap between the d_{xz} and p_z bands [Fig. 4(d)] and a reduction of energy separation between the d_{yz} and d_{xz} bands. We note that the relative position of the holelike band with respect to the Fermi level also varies in literature [20,29]. The origin of

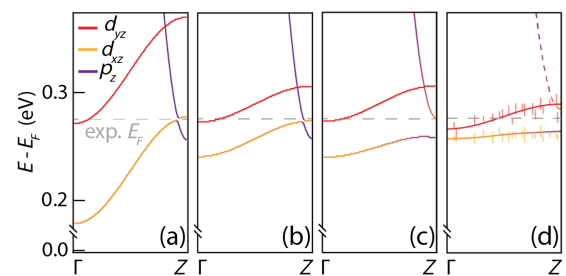


FIG. 4. Renormalization steps for the band structure. (a) DFT calculation results. (b) Renormalize the d bands by a factor of 3 with respect to the experimental E_F (gray dashed line). (c) A further increase of d_{xz} - p_z SOC strength as a phenomenological measure of many-body correlations. (d) Comparison with the experimental data. The vertical lines show the experimental band tops from Fig. 1(d) and the parameters are chosen to fit the experimental data.

this discrepancy remains an ongoing research topic, with strong correlations and Mott transition effects as potential candidates [47–49]. Nevertheless, our picture vividly highlights the critical role of strong correlation in the realization of an overall topologically nontrivial band character by dramatically renormalizing the DFT predictions. This greatly reduces the energy scale and ensures the proximity of the inverted band gap to the E_F for topological physics to be relevant.

In conclusion, we provide a strong case for a topological band structure in $\text{FeTe}_{0.55}\text{Se}_{0.45}$ by systematically analyzing the band dispersion and spectral weight. Our picture reconciles the discrepancy between the calculated band structure and experimental observations by necessary many-body renormalizations and provides a baseline for the further pursuit of topological physics in this system.

Experimental methods. FTS samples were grown by the flux method [50]. Magnetic susceptibility measurements show superconducting transition at 14 K, in agreement with the previous report [29]. The FTS data at 6 and 7 eV photon energies were collected using laser ARPES systems at Stanford University, with Scienta R4000 and R8000 analyzers, respectively. After taking each spectra on the sample, the E_F is calibrated using the Fermi edge of a polycrystalline gold electrically connected to the sample. The energy resolution was 5 meV (3 meV) and the measurement temperature was 20 K (16 K) for the 6 eV (7 eV) experiments. FTS data between 15 and 25 eV data were collected at the Stanford Synchrotron Radiation Lightsource (SSRL) beam line 5-4 using a Scienta R4000 analyzer, with energy resolution at 5 meV and temperature at 16 K. The FTS data between 26 and 76 eV were collected at SSRL beam line 5-2 using a Scienta DA 30 analyzer with energy resolution at 12 meV and temperature at 16 K. The FeSe data between 26 and 52 eV are collected at SSRL beam line 5-2, on a detwinned sample [51], with energy resolution at 12 meV and temperature at 12 K. The pressure was kept below 4×10^{-11} Torr throughout all ARPES measurements.

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Y.-F. L., D.-H. L., and Z.-X. S. designed the experimental plan. Y.-F. L., S.-D. C., H. P., and J. A. S. performed ARPES experiments and data analysis. Y.-F. L. and H. P. performed matrix element calculations. M. G.-D., M. I. I., and Y.-F. L. performed DFT calculations and tight-binding modeling. Y.-L. Z. and Z.-Q. M. synthesized high-quality FTS samples. T. C., M. Y., and P.-C. D. synthesized high-quality FeSe samples. Y.-F. L., S.-D. C., M. G.-D., M. G. V., D.-H. L., and Z.-X. S. wrote the manuscript with input from all authors. J. A. S., M. H., D.-H. L., and Z.-X. S. supervised the whole project.

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