Extended regime of metastable metallic and insulating phases in a two-orbital electronic system

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We investigate the metal-to-insulator phase transition driven by the density-density electronic interaction in the quarter-filled model on a cubic lattice with two orbitals split by a crystal field. We show that a systematic consideration of the nonlocal collective electronic fluctuations strongly affects the picture of the phase transition provided by the dynamical mean-field theory. Our calculations reveal the appearance of metallic and Mott insulating states characterized by the same density but different values of the chemical potential, which is missing in the local approximation to electronic correlations. We find that the region of concomitant metastability of these two solutions is remarkably broad in terms of the interaction strength. It starts at a critical value of the interaction slightly larger than the bandwidth and extends to more than twice the bandwidth, where the two solutions merge into a Mott insulating phase. Our results illustrate that nonlocal correlations can have crucial consequences on the electronic properties in the strongly correlated regime of the simplest multiorbital systems.

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There are two main mechanisms responsible for the formation of an insulating phase in electronic materials: a gap at the Fermi energy in the noninteracting band structure and the many-body localization induced by strong electronic interactions, as for instance the Mott scenario [1,2]. The interplay between these different mechanisms can strongly affect the degree of electronic correlations and therefore the phase diagram of the material [3]. Both these effects are especially important when a subset of doubly or triply degenerate localized orbitals appears in the electronic spectrum at Fermi energy. Usually, the charge distribution on neighboring atoms lifts this degeneracy, which results in a local splitting of the orbitals called crystal field splitting. Strong electronic correlations may greatly renormalize the electronic spectral distribution, thus affecting the orbital splitting [4–7]. The crystal field splitting also has a strong influence on the Mott transition in several materials, as it favors orbital polarization and orbital selective phenomena [8–21].

The dynamical mean-field theory (DMFT) [22] is currently the most widely used theoretical method for describing the Mott transition in realistic materials [23,24]. For instance, this method captures the coexistence of metallic and insulating phases that accompanies the Mott transition in both single-

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band [25–31] and multiorbital [32–36] systems. However, in some cases DMFT is insufficient, because this theory accounts only for local correlation effects. Considering even shortrange correlations beyond DMFT significantly modifies the coexistence region and drastically reduces the critical value of the interaction [30]. Long-range correlations can have even more dramatic consequences [37]. Therefore, an important leap towards an accurate theoretical description of correlated materials would be to understand the effect of nonlocal collective electronic fluctuations on the spectral function. Unfortunately, most of the available theoretical methods for multiorbital systems are either limited to a weakly correlated regime [38-44], or do not take into account all the desired physical ingredients, such as long-range correlations [45–48] or spatial magnetic fluctuations [49-58]. Attempts to go beyond these assumptions using diagrammatic methods lead to expensive numerical calculations [59–66], while unbiased quantum Monte Carlo methods are so far limited to specific parameter regimes or symmetries due to the fermionic sign problem [67–72].

In this Letter, we investigate the effect of nonlocal correlations on the Mott transition in a two-orbital model with the crystal field splitting and the density-density approximation for the interaction. This model is relevant for investigating the low-energy physics of some transition metal oxides [9] and of fulleride molecular crystals [73–77]. More importantly, this model is one of the simplest multiorbital systems that allows for studying the influence of the orbital splitting on the Mott transition. So far this simple model has not been studied beyond the local DMFT approximation [6] due to computational difficulties associated with incorporating nonlocal correlations in the multiorbital framework. We challenge this solution

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of the problem by utilizing a relatively inexpensive diagrammatic extension of DMFT [78]—the dual triply irreducible local expansion (D-TRILEX) method [79–82]. This approach accounts for the effect of the nonlocal collective electronic fluctuations on the spectral function in a self-consistent manner [80,83,84]. We find that, despite the apparent simplicity, the considered model displays a nontrivial behavior around the Mott transition. In particular, considering the nonlocal correlations beyond DMFT reveals a broad coexistence region of metastable metallic and Mott insulating phases that extends from approximately the bandwidth to more than twice the bandwidth in the value of the interaction. Our results might guide the understanding of the memristive effects experimentally observed in VO₂ thin-film samples [85,86].

Method. The Hamiltonian of the considered two-orbital model on a cubic lattice

$$H = \sum_{jj',l,\sigma} c^{\dagger}_{jl\sigma} (t^l_{jj'} + \Delta_l \, \delta_{jj'}) c_{j'l\sigma} + \frac{U}{2} \sum_{j,ll'} n_{jl} \, n_{jl'}$$

contains three contributions. We restrict the hopping to the nearest-neighbor lattice sites and set it to $t_{(ii')}^l = 1/6$ for each of the two orbitals $l \in \{1, 2\}$. Hereinafter, the energy is expressed in units of the half bandwidth of the cubic dispersion W/2 = 6t = 1. The interaction U between electronic densities $n_{jl} = \sum_{\sigma} c^{\dagger}_{jl\sigma} c_{jl\sigma}$ describes both the intra- and interorbital Coulomb repulsion. Calculations are performed at quarter filling, which corresponds to the average density of $\langle n \rangle = 1$ electron per two orbitals. In order to induce an orbital polarization $\delta n = (\langle n_2 \rangle - \langle n_1 \rangle)/\langle n \rangle$, we take a relatively large value for the crystal field splitting $\Delta = 2\Delta_1 = -2\Delta_2 = 0.3$. This case was studied in detail in Ref. [6] using DMFT. It was demonstrated, that local electronic correlations enlarge the orbital splitting, resulting in a high degree of orbital polarization. Consequently, the single electron mostly populates the lower orbital (l = 2) that undergoes the Mott transition at a critical value of the electronic interaction. A similar interplay between the orbital polarization and Mott physics is also found in actual materials such as V₂O₃ [9] and SrVO₃ [87–89], where it is important for the Mott transition.

In order to investigate how nonlocal correlations affect the DMFT scenario of the Mott transition, we employ the D-TRILEX method [79,80,82], where collective electronic fluctuations are treated diagrammatically beyond DMFT. This method was derived as an approximation to the dual boson theory [90–99], one of the most commonly used diagrammatic extensions of DMFT (cf. Refs. [61,66,100–113]). The D-TRILEX method stands out for its lowered complexity, which allows one to address multiband problems [81,82,84] (cf. Refs. [61,62]), and its capability of correctly reproducing the results of more elaborate theories. The reduction of the critical interaction for the Mott transition compared to DMFT [79] is very similar to cluster DMFT [30]. Additionally, it shows a precise agreement with exact benchmarks for some single- and multiband systems [80,82].

If the system exhibits strong magnetic fluctuations, as frequently happens at half filling, the Mott transition usually lies inside the antiferromagnetic (AFM) phase. In this case, addressing the Mott transition requires to perform calculations in a symmetry broken phase, which is problematic. Going

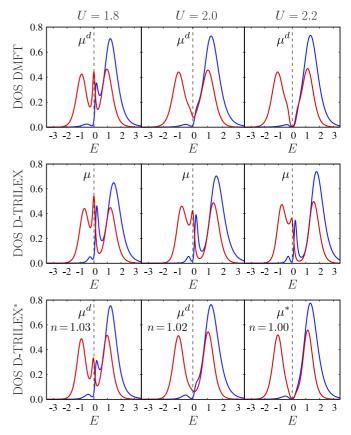


FIG. 1. DOS for the upper (l=1, blue line) and lower (l=2, red line) orbitals calculated for different interactions U=1.8 (left column), U=2.0 (middle column), and U=2.2 (right column). Top row: DMFT solution at quarter filling that corresponds to the chemical potential μ^d . Middle row: Quarter-filled metallic D-TRILEX solution for the chemical potential μ . Bottom row: A further D-TRILEX* calculation based on the DMFT solution. Calculations for U=1.8 and U=2.0 are performed for μ^d . The resulting $\langle n \rangle > 1$ is specified in panels. At U=2.2 the quarter-filled D-TRILEX* solution appears at $\mu^* \simeq \mu^d$ and corresponds to the Mott insulating state.

away from half filling suppresses the magnetic fluctuations and allows one to access the Mott transition from the paramagnetic phase. According to our calculations, the highest critical temperature for the Néel transition for the considered quarter-filled model lies below T=0.06. For this reason, we set the inverse temperature to $T^{-1}=15$, which ensures that the system is located outside the AFM phase but close to its boundary to observe strong magnetic fluctuations. We perform DMFT calculations using the W2DYNAMICS package [114]. The D-TRILEX solution is based on the numerical implementation described in Ref. [82]. The local density of states (DOS) is obtained from the corresponding local Green's functions via analytical continuation using the ana_cont package [115].

Results. To illustrate the effect of nonlocal correlations on the Mott transition, we compare the DOS predicted by DMFT and D-TRILEX methods. The result of these calculations is shown in Fig. 1 for three different values of the interaction U = 1.8, U = 2.0, and U = 2.2. First, let us focus on the quarter-filled calculations presented in the two upper

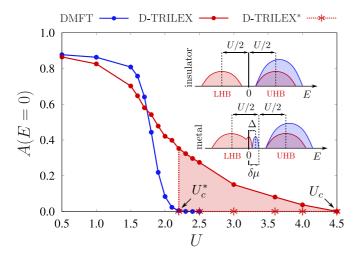


FIG. 2. Electronic density at Fermi energy A(E=0) for the lower orbital (l=2) as a function of the interaction U. The result is obtained from DMFT (blue dots), metallic D-TRILEX (red dots), and insulating D-TRILEX* (red asterisks) solutions. The red shaded area highlights the simultaneous existence of the metallic and the Mott insulating solutions. The inset sketches the difference in the DOS between the insulating (top) and metallic (bottom) D-TRILEX solutions. In the insulating case, the Fermi energy lies between the LHB and UHB that are split approximately by U. In the metallic case, the difference in the chemical potential $\delta \mu = \mu^* - \mu$ brings the upper part of the LHB to the Fermi energy, which results in the formation of the quasiparticle peak at E=0. The splitting between the quasiparticle peaks coincides with the value of the crystal field splitting $\simeq \Delta$.

rows of this figure. We find that the results of the DMFT and D-TRILEX methods are different already at U = 1.8. In both cases, the DOS is metallic. The lower orbital (l = 2,red line) displays a three-peak structure consisting of the quasiparticle peak at Fermi energy E = 0 and two side peaks that correspond to lower and upper Hubbard bands (LHB and UHB). The upper orbital (l = 1, blue line) also exhibits the quasiparticle peak in the DOS that appears close to the Fermi energy at $E \simeq \Delta$. However, the three-peak structure predicted by DMFT possesses a high degree of electron-hole symmetry. Instead, the DOS of obtained for the same orbital (l = 1)using the D-TRILEX approach resembles the DOS of a holedoped Mott insulator with the quasiparticle peak being shifted closer to the LHB [22]. The quasiparticle peaks in the DOS of DMFT vanish simultaneously between U = 1.8 and U = 2.0, which signals the tendency towards a Mott insulating state in a multiorbital system at finite temperature. A further increase of the interaction decreases the electronic density at Fermi energy A(E=0). The latter reaches zero at $U_c^* \simeq 2.2$ (blue line in Fig. 2), and the DMFT solution enters the Mott insulating phase. On the contrary, the D-TRILEX solution remains metallic for the discussed values of the interaction (middle row in Fig. 1). Thus, even at U_c^* it reveals pronounced quasiparticle peaks in the DOS for both orbitals. Figure 2 shows that A(E = 0) in the metallic D-TRILEX solution also decreases upon increasing the interaction. However, this solution turns into a Mott insulator only at a very strong critical interaction $U_c \simeq 4.5$, which is larger than twice the bandwidth.

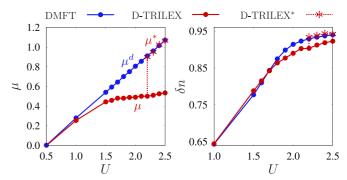


FIG. 3. Chemical potential (left panel) and orbital polarization (right panel) for the quarter-filled DMFT (blue dots), metallic D-TRILEX (red dots), and insulating D-TRILEX (red asterisks) solutions. The result is obtained for different values of the interaction U. Chemical potentials for the insulating D-TRILEX (μ^*) and DMFT (μ^d) solutions nearly coincide. For $1.0 \leq U < 2.2$ no quarter-filled D-TRILEX solution exists near μ^d . The chemical potential μ for the metallic D-TRILEX solution strongly deviates from μ^d at $U \geqslant 1.5$.

This result seems surprising, since in the single-orbital case the nonlocal correlations lead to a more insulating electronic behavior [30], as correctly captured by the D-TRILEX method [79]

To explain the observed effect, we note that quarter filling in DMFT and D-TRILEX corresponds to different values of the chemical potential. The left panel of Fig. 3 shows that at $U \ge 1.5$ the chemical potential μ of D-TRILEX (red dots) significantly deviates from μ^d of DMFT (blue dots), and this difference increases with increasing the interaction. We point out that D-TRILEX calculations are based on the DMFT solution of the local impurity problem that plays a role of the reference system [79,80]. We find that the quarter-filled metallic D-TRILEX solution originates from the metallic reference system that has smaller average density. Figure 4 shows that due to $\langle n \rangle < 1$ the reference system (dashed lines) remains metallic even at U_c^* . At the same time, the DOS predicted by

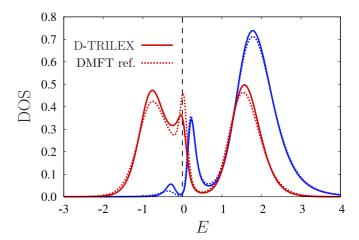


FIG. 4. DOS for the metallic D-TRILEX solution (solid lines) and its DMFT reference system (dashed lines) obtained for the same value of the chemical potential μ at the critical interaction U_c^* . The reference system is a doped Mott insulator with $\langle n \rangle = 0.96$.

D-TRILEX (solid lines) is not dramatically different from the one of the reference system. This fact suggests that for a given value of the chemical potential the effect of nonlocal collective electronic fluctuations in the metallic regime consists in moving the spectral weight from above to below the Fermi energy, which brings the filling of the system to $\langle n \rangle = 1$.

To confirm this statement, we perform D-TRILEX calculations for the chemical potential μ^d of the quarter-filled DMFT solution. The corresponding result is shown in the bottom row of Fig. 1 and is referred to as the D-TRILEX* calculation in order not to confuse it with the metallic solution. We observe that the obtained DOS is again practically identical to the one of DMFT (bottom versus top row in Fig. 1). However, the D-TRILEX* calculations performed in the regime $1.0 \le U < 2.2$, where the DMFT solution is metallic, correspond to $\langle n \rangle > 1$. Moreover, no quarter-filled D-TRILEX* solution is found near μ^d in this regime of interactions. This fact supports our previous finding that in the metallic regime nonlocal correlations increase the average density of the considered system.

This physical picture changes when the DMFT solution becomes Mott insulating. We find that the corresponding D-TRILEX* solution undergoes the Mott transition at the same critical interaction U_c^* as in DMFT (bottom right panel of Fig. 1). Moreover, at $U \geqslant U_c^*$ the average density for the D-TRILEX* solution becomes $\langle n \rangle = 1$ for $\mu^* \simeq \mu^d$ (bottom left panel of Fig. 1). The right panel of Fig. 3 shows that the insulating DMFT and D-TRILEX* solutions are almost fully polarized and have approximately the same value of δn , which results in electron-hole symmetric DOS for the lower orbital (top and bottom left panels of Fig. 3). Consequently, the upper orbital becomes nearly unoccupied and thus cannot strongly interact with the lower one. Therefore, no transfer of the spectral weight between the orbitals by means of the nonlocal fluctuations occurs in the insulating regime. Remarkably, the metallic D-TRILEX solution has a lower δn compared to

At $U \geqslant U_c^*$ the D-TRILEX* solution remains quarter filled and Mott insulating, which is confirmed by the zero electronic density at Fermi energy (red asterisks in Fig. 2). Therefore, both the DMFT and the D-TRILEX methods predict the Mott transition for the considered system at the same value of the critical interaction U_c^* . However, including nonlocal collective electronic fluctuations beyond DMFT allows one to additionally capture the metallic solution that coexists with the Mott insulating one up to the second critical interaction U_c . For $U > U_c$ any value of the chemical potential inside the Mott gap gives the same average density, and the two solutions corresponding to μ and μ^* can be considered equivalent. A more detailed discussion of the hysteresis curve appearing in Fig. 3 can be found in the Supplemental Material (SM) [116].

Coexisting solutions with the same average density but different values of the chemical potential have also been found in the DMFT solution of the Hubbard-Kanamori model for small doping around half filling [117–121], and for different parameters using a strong-coupling expansion [119]. Since the quarter-filled model considered in our work displays a strong orbital polarization, it can be expected that taking into account the Hund's rule coupling J, which is present in the Kanamori parametrization of the electronic interaction [24,122], should not qualitatively change the observed results. To confirm this point, we perform calculations for the case of J = U/6 and find that the metastability discussed above survives also in this case, as shown in SM [116].

Conclusions. We investigated the effect of nonlocal collective electronic fluctuations on the Mott transition in a two-orbital quarter-filled model with a density-density interaction by comparing the results of the D-TRILEX and DMFT methods. At the considered temperature, the DMFT solution of the problem remains metallic below the critical interaction $U_c^* = 2.2$, and at this value of the interaction undergoes the Mott transition. We find that the inclusion of nonlocal correlations by means of the D-TRILEX approach stabilizes the metallic phase up to the very large critical interaction $U_c = 4.5$. The D-TRILEX method also captures the appearance of Mott insulating phase at U_c^* as a second metastable solution. This leads to a remarkably broad coexistence region between the metallic and the Mott insulating phases that exist at the same filling, but with different values of the chemical potential between the U_c^* and the U_c critical interactions. Our results show that for a simple two-orbital model, DMFT cannot correctly interpolate between the moderately and strongly interacting regimes, in analogy with the single-orbital case. This fact brings further evidence that nonlocal correlations may lead to nontrivial effects due to the presence of additional channels for collective electronic fluctuations also in multiorbital systems.

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