

Low energy dissipation readout of single-molecule ferroelectric states by a spin-Seebeck signal

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Single-molecule magnets (SMMs) possessing bistable states have been considered as promising candidates to realize zero-dimensional (0D) ferroelectrics (FE) and multiferroics (MF) with high storage density. However, how to read or manipulate the FE states with low-energy-dissipation strategy is still a hard challenge. Here, we intercalated a magnetic metal porphyrin molecule, such as TiP with switchable vertical electric polarization, within the MoS₂ bilayer to realize 0D FE states. First-principles calculations show that the MoS₂ monolayer contacted by SMMs is spin polarized to provide two spin-dependent transport tunnels. As a temperature gradient is applied along the transport channels, a well-defined spin-Seebeck effect (SSE) occurs in the spin-polarized MoS₂ layer, helping to generate a pure thermal spin current. More importantly, the spin-Seebeck signal is associated tightly with the FE state in the same layer, and both of them can be switched simultaneously to another layer by an external electric field. The theoretical results not only put forwards a low-energy-dissipation strategy to read the SMM-based FE states, but also develop a new research field of spin-ferroelectro-caloritronics, which focuses on the interplay of electrons' spin and FE states in the presence of a temperature gradient.

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I. INTRODUCTION

Ferroelectrics and multiferroics have long been attractive for researchers in materials science and condensed matter physics because they provide new physical mechanisms for realizing information storage and processing with low-energy dissipation [1–10]. To develop the ferroelectric (FE) materials towards realistic device applications, two challenging issues need to be addressed—one is how to increase the data-storage density with FE domains and the other is how to improve the flexibility of FE materials for the easy control [11–13]. One of the feasible ways is to reduce the dimensionality of FE materials [14]. On the other hand, single-molecule magnets (SMMs) are currently subject of active interdisciplinary of research, owing to their peculiar quantum spin states and slow magnetic relaxation, which are potentially suitable for quantum computing and sensing applications [15–17]. Recently, zero-dimensional (0D) multiferroic (MF) materials have been integrated with SMMs constructed on polar metal porphyrin (MP) molecules such as TiP, VP, and TiP, which have buckled structures with switchable vertical electric polarizations to realize two opposite FE states [18–22]. This design is useful to obtain 0D quantum materials, which are characterized by their peculiar couplings between spin states and FE states. To obtain stable and controllable 0D FE states, we may

intercalate the SMMs within the bilayer structures constructed on two-dimensional (2D) materials such as MoS₂, MoSe₂, and MoTe₂ [19]. One of the advantages of this design is that the FE states induced by 0D multiferroics can be switched and manipulated easily by multiple feasible ways including an external electric field, and the other is that the information storing density can be enhanced remarkably, because every molecule in the SMMs can store even up to 1 bit data.

The material candidates to construct 0D FE states are usually semiconducting or insulating, which brings us a challenge how to realize the readout and manipulation of FE states with low-energy-dissipation strategies. To achieve feasible routes to read and detect the FE states, here we focus on the geometric structures of the aforementioned SMM-based 0D FE materials [19], and choose a SMM such as TiP molecule and a 2D material such as the MoS₂ monolayer as examples to construct 0D MF states. Here, TiP molecules, i.e., Ti porphyrin molecules, are widely present in many biochemical molecules, such as iron porphyrin in hemoglobin for oxygen transport in the blood. As illustrated in Figs. 1(a) and 1(b), a single TiP molecule is absorbed by a MoS₂ monolayer, and Ti atom in the SMM is coupled with the S atom in the MoS₂ monolayer. The single TiP molecule is a polar one characterized by two typical bistable states, in which the central Ti atom can shift upwards and downwards perpendicular to the molecule surface to realize two opposite electric polarizations. To ensure the stability of FE states, the TiP molecule is absorbed by the MoS₂ monolayer to form the Ti-S bond with an effective coupling, as described in Fig. 1(b). The first-principles calculations show that the spin splitting occurs in the MoS₂ monolayer due to the spin coupling with the TiP SMM. To illustrate this point, one can refer to their spin distributions in every repeated unit drawn in Fig. 1(c), and the

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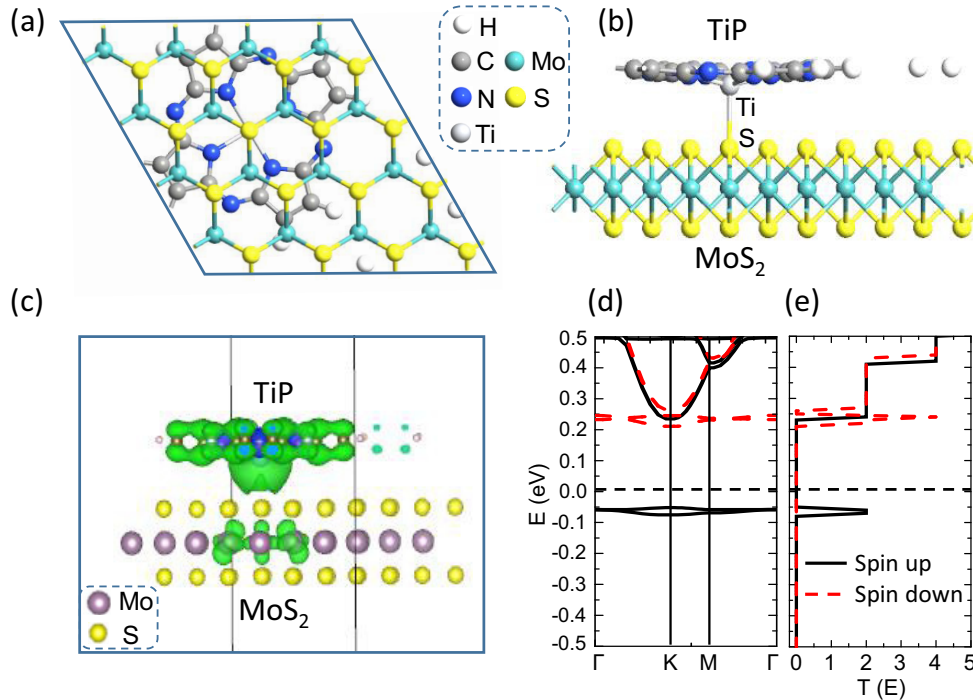


FIG. 1. (a, b) Top and side views of MoS₂ monolayer adsorbed by a single magnetic TiP molecule, where Ti atom in the single molecule is coupled with the S atom in MoS₂. (c) Spin distributions in the MoS₂ monolayer and the TiP molecule. (d) Band structure of MoS₂ monolayer coupled with single TiP molecules and (e) spin-dependent transmission of the MoS₂ monolayer coupled with a list of TiP molecules, in which the length of Ti-S bond and the distance between two neighboring SMMs are adopted as the same as those in (b).

spin polarized band structures in MoS₂ monolayer drawn in Fig. 1(d). We find that the highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO) bands are constructed only by the spin-up and spin-down electrons, respectively, and divided by an energy gap about 0.3 eV. Moreover, these spin-splitting bands around the Fermi level are contributed to mainly by the S atoms in MoS₂ monolayer, indicating that two spin transmission channels, one for the spin-up electrons and the other for the spin-down ones, appear in the MoS₂ monolayer, as illustrated in Fig. 1(e).

In this work, we constructed spin caloritronic devices based on the MoS₂ monolayer or bilayer intercalated by TiP SMMs. The theoretical calculations reveal that as a temperature gradient is applied in the TiP-MoS₂-bilayer device, and by adjusting the direction of an external electric field, the spin-Seebeck currents are driven in the different MoS₂ layer, which is associated tightly with the different FE states in TiP SMMs, meaning that the spin-Seebeck signals connect with the related FE states in the TiP-MoS₂-bilayer-based device. These properties not only indicate that we obtain a new low-energy-dissipation strategy, i.e., by detecting the spin-Seebeck signal in the different MoS₂ layer, to read the corresponding FE state in the SMM, but also develop a new interdisciplinary research field of spin-ferroelectro-caloritronics, which focuses on the interplay of electrons' spin and FE states in the presence of temperature gradient.

The remainder of this paper is organized as follows. The spin caloritronic devices based on the MoS₂ monolayer or bilayer intercalated by TiP SMMs are designed, and the theoretical methods are introduced in details in Sec. II, then the numerical results for the thermally driven charge and spin

currents to confirm the occurrence of the spin-Seebeck effect (SSE) are presented and how the spin-Seebeck signals are associated with the corresponding FE states is explained in Sec. III. In the last section, the main conclusions are summarized.

II. DEVICE MODELS AND THEORETICAL METHOD

Considering the unique spin-splitting band structures of TiP-coupled MoS₂ monolayer, and the fact that occurrence of spin splitting in MoS₂ monolayer is tightly associated with the FE state in the TiP SMM, we may explore new routes to read and manipulate these 0D FE states. To realize this idea, we try to design a spintronic device based on the above-mentioned TiP-coupled MoS₂ monolayer, as drawn in Fig. 2(a), where three typical device regions, i.e., the left lead, the central scattering region, and the right lead, are constructed. To perform the structural optimization on the TiP-coupled-MoS₂-monolayer-based devices, we first performed the theoretical calculations based on density functional theory (DFT) methods implemented in the Vienna *ab initio* Simulation Package codes (VASP) [23,24]. The exchange-correlation effect is described within the generalized gradient approximation (GGA) in the Perdew-Burke-Ernzerhof (PBE) functional [25], together with the projector augmented wave method [26]. The Brillouin zone integration of the supercell in 2D materials is sampled with a $5 \times 5 \times 1$ Monkhorst-Pack [27] grid, the kinetic energy cutoff is set to be 400 eV, and a vacuum space of 40 Å is set in the vertical direction. PBE-D2 functional of Grimme [28] is used to account for weak van der Waals interactions. For TiP-coupled-MoS₂-monolayer-based device,

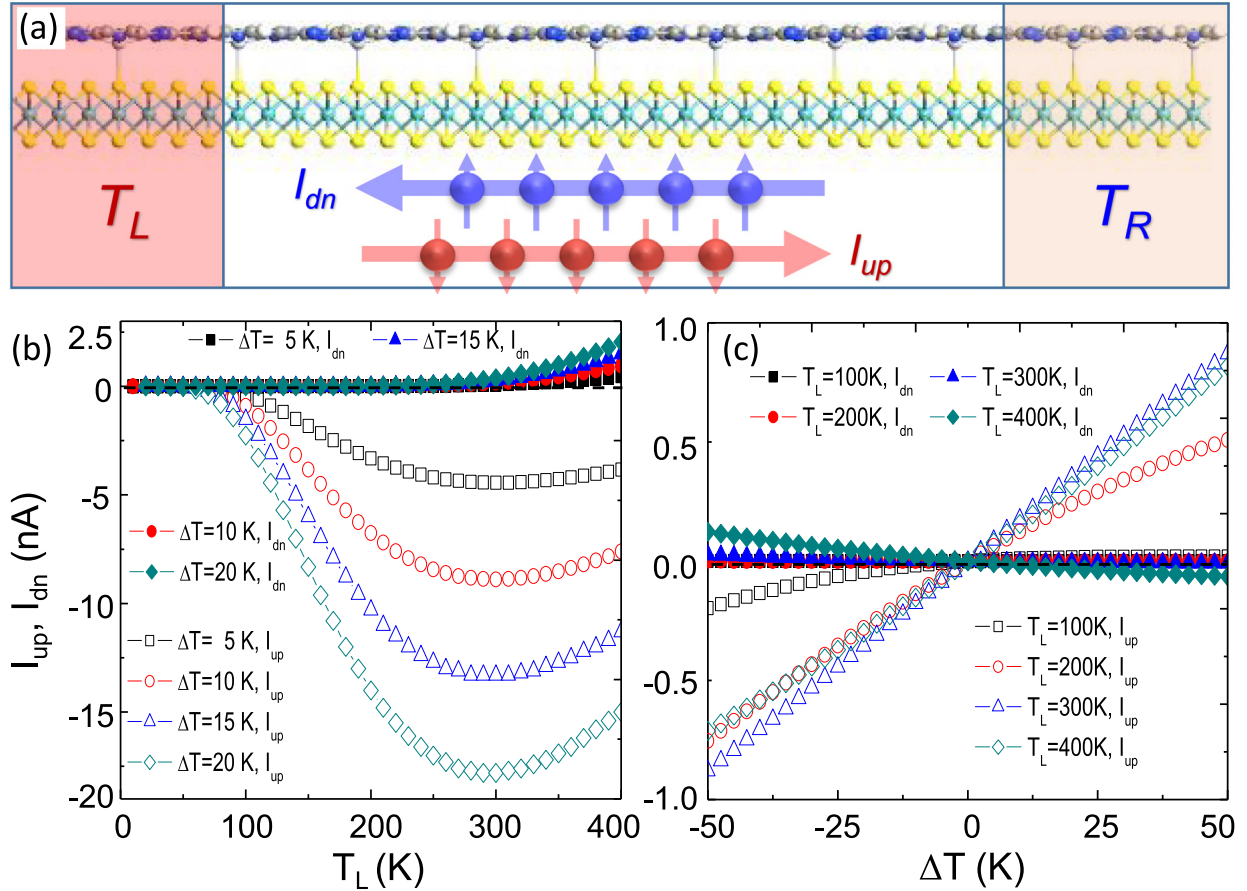


FIG. 2. (a) Schematic of the TiP-coupled-MoS₂-based spin-caloritronic device, where the semi-infinite left and right leads are composed of the same MoS₂ monolayer with the temperature T_L and T_R , respectively. The spin currents I_{up} and I_{dn} and their flow directions are denoted by the arrows with different colors. (b) The thermally driven spin currents I_{up} and I_{dn} versus the temperature T_L at the different temperature gradient ΔT . (c) The spin-dependent currents I_{up} and I_{dn} versus ΔT at the different temperature T_L .

to eliminate the interaction between adjacent molecules, a 2×2 supercell of MoS₂ monolayer is adopted so that the distances between the hydrogen atoms on the edges of two adjacent molecules are greater than 3.7 Å, and thus the interaction between them might be negligible. Furthermore, to derive the electrons to transport in the MoS₂ monolayer, the temperatures in the left and right leads are set as T_L and T_R , respectively, and a temperature gradient ΔT ($= T_L - T_R$) is adopted. Owing to two spin-dependent transmission channels distributed nearly symmetrically above and below the Fermi level, two spin-dependent currents, i.e., the spin-up current I_{up} and the spin-down one I_{dn} , may be driven by the temperature gradient to flow in the opposite directions, as displayed in Fig. 2(a). The appearance of thermally driven spin-dependent currents characterized by the above two typical features indicates that the conduction electron-based SSE [29–36] occurs in the present spintronic device based on the TiP-coupled MoS₂ monolayer.

To confirm the occurrence of SSE in the present TiP-absorbed-MoS₂-based spintronic device, we may numerically calculate the thermally driven spin current I_{up} and I_{dn} by using the DFT [37,38] combined with the nonequilibrium Green's function (NEGF) approach [39–42], as implemented in the SIESTA and the TRANSAMPA codes [43]. In the Landauer-Büttiker formalism [44], the spin-dependent currents are given

by [45]

$$I_{\sigma} = \frac{e}{h} \int_{-\infty}^{+\infty} \{T_{\sigma}(E)[f_L(E, T_L) - f_R(E, T_R)]\} dE, \quad (1)$$

where e is the electronic charge, h is the Plank constant, and the equilibrium Fermi-Dirac distribution of the left (right) lead at temperature $T_{L(R)}$ is given by the equation $f_{L(R)}(E, T_{L(R)}) = [1 + \exp(E - \mu_{L(R)})/k_B T_{L(R)}]^{-1}$. $\mu_{L(R)}$ is the chemical potential in the left (right) lead. $T_{\sigma}(E)$ is the spin-resolved transmittance function, which is defined as $T_{\sigma}(E) = \text{Tr}[\Gamma_L^{\sigma} G_{\sigma}^R(E) \Gamma_R^{\sigma} G_{\sigma}^A(E)]$ [25], where σ ($= \uparrow, \downarrow$ or up, dn) denotes the spin index, and $\Gamma_{L/R}^{\sigma} = i|\Sigma_{L/R}^{\sigma} - \Sigma_{L/R}^{\sigma \dagger}|$ indicates the interaction between a central scattering region and the left (right) lead, whose self-energy is $\Sigma_{L/R}^{\sigma}$. $G_{\sigma}^{R/A}(E)$ represents the retarded (advanced) Green's function of the central scattering region, $G_{\sigma}^R(E) = [H_{\sigma}^c - (E + i\eta) + \Sigma_L^{\sigma} + \Sigma_R^{\sigma}]^{-1}$ and $G_{\sigma}^A(E) = [G_{\sigma}^R(E)]^{\dagger}$, here H_{σ}^c is the Hamiltonian in the central scattering region. Considering that the SMM-coupled MoS₂ monolayer designed here are structurally perfect, thermally driven electrons can move freely in the MoS₂ monolayer. The above expressions will help us to obtain the thermal spin-dependent currents transport through the TiP-coupled MoS₂ monolayer.

In addition, to examine further the features of SSE, we also calculate the spin-dependent Seebeck coefficients, which measure the spin voltage induced by temperature gradient in the TiP-coupled-MoS₂-based devices. In the linear response regime, if ΔT approaches zero, we get $T = T_L \approx T_R$ and $\mu = \mu_L \approx \mu_R$ in the spin caloritronic device constructed here. Thus, the spin-dependent Seebeck coefficients (S_σ) can be calculated by [46]

$$S_\sigma(\mu, T) = -\frac{1}{eT} \frac{K_{\sigma,1}(\mu, T)}{K_{\sigma,0}(\mu, T)}, \quad (2)$$

where, $K_{\sigma,n}(\mu, T)$ is given by

$$K_{\sigma,n}(\mu, T) = -\int_{-\infty}^{+\infty} (E - \mu)^n \frac{\partial f(E, \mu, T)}{\partial E} T_\sigma(E) dE. \quad (3)$$

$S_{ch} = (S_{up} + S_{dn})/2$ and $S_{sp} = S_{up} - S_{dn}$ are the charge-Seebeck and spin-Seebeck coefficient. Note that in the theoretical calculations, the electron-phonon interaction (EPI) is ignored here since the electron-phonon mean free paths in the MoS₂ monolayer are short to about 9 nm at room temperature as demonstrated in a previous literature [47], indicating that much weak EPI exists in the MoS₂-monolayer-based devices.

III. RESULTS AND DISCUSSION

Now, we turn to elucidate how to readout the two opposite FE states by the related spin-Seebeck signals in TiP-coupled-MoS₂-based devices. When a temperature gradient ΔT is applied between two leads, $f_L(T_L) - f_R(T_L - \Delta T)$ is no longer equal to zero and displays inverse symmetric behaviors around the Fermi level [48,49]. Since $f_L - f_R$ is an odd function, the sign of I_σ is determined by the slope of the transmission coefficient T_σ near to the Fermi level, according to the aforementioned expressions of spin-dependent currents [34]. Considering that the spin-up and spin-down transmission spectra are located below and above the Fermi level, respectively, I_{up} and I_{dn} should have the opposite signs, indicating the occurrence of conduction electron-based SSE in the device [50]. This property is confirmed further by their numerical results as illustrated in Figs. 2(b) and 2(c), where I_{up} and I_{dn} versus T_L and ΔT are plotted, respectively. Indeed, one can see that $I_{up} < 0$ while $I_{dn} > 0$ from the DFT calculations combined with the NEGF method. Moreover, I_{up} and I_{dn} possess different threshold temperatures due to their different spin-dependent band gaps. This is to say that, in the low-temperature region of T_L , both I_{up} and I_{dn} are forbidden, indicating that there is no any carrier transport to denote the related FE state. In the intermediate-temperature region, only I_{up} appears, indicating that the carrier transport is dominated by the absolute spin-polarized currents, and only as T_L increases to larger values, the SSE occurs, which is helpful to reduce the charge current $I_c (= I_{up} + I_{dn})$ while to enhance the net spin current $I_s [= \frac{\hbar}{2e}(I_{up} - I_{dn})]$.

Furthermore, to confirm further the occurrence of SSE in the device, we also calculated the spin-dependent Seebeck coefficients S_{up} , S_{dn} , S_{ch} , and S_{sp} versus the device temperature T and the potential μ in the TiP-coupled-MoS₂-based devices in Fig. S1 in the Supplemental Material [51]. One can find that changing trends of these coefficients versus the device

temperature T are much similar with those of I_{up} , I_{dn} , I_{ch} , and I_{sp} versus T_L . In particular, two spin-dependent Seebeck coefficients S_{up} and S_{dn} possess the opposite signs, for all device temperature settings [Fig. S1(a)] or around the Fermi level (Fig. S1(b)), which is a typical characteristic of conduction electron-based SSE. Besides, the spin-Seebeck coefficients at low temperatures are high to $10^4 \mu\text{V/K}$, supporting that the TiP-coupled MoS₂ monolayer has the potential to work as good thermoelectric-conversion devices.

To obtain a low-energy-dissipation strategy to realize the readout of FE states in the 0D MF materials by using the spin-Seebeck signals, two key issues should be addressed: (i) how to combine the thermally driven spin currents with the corresponding FE states and (ii) how to reduce the thermal charge current I_c and to enhance the spin current I_s since the charge current usually brings Joule heat, which is not beneficial to design low-energy-dissipation nanodevices. To construct two FE states with opposite electric polarizations, we intercalate the SMM within a bilayer of 2D materials, such as the MoS₂ bilayer adopted here. As illustrated in Figs. 3(a) and 3(b), the single TiP molecules are sandwiched between two MoS₂ monolayers. Since the TiP molecule is polar and its electric polarization appears along the vertical direction of the molecule surface, we can apply an external electric field \vec{E} to flip their polarization directions. If \vec{E} is applied in the upwards direction, the TiP molecules are absorbed by the upper MoS₂ monolayer, otherwise, the TiP molecules are absorbed by the lower monolayer. Thus, two opposite electric polarization states corresponding to two opposite FE states characterized by “0” and “1” are achieved. It should be pointed out that the previous first-principles calculations reveal that the potential barrier between these two opposite FE states is high to 0.73 eV [19], which ensures the thermal stability of these electric-polarized states even at room temperature.

On the other side, as the magnetic TiP molecules are absorbed by the upper MoS₂ monolayer, the later would be spin polarized to provide two spin-dependent transport channels as interpreted above, while the lower MoS₂ monolayer keeps insulating [see Figs. 3(c) and 3(d)]. Thus, we can construct the spin-caloritronic device based on the TiP-intercalated MoS₂ bilayers by using the similar way, as drawn in Figs. 3(e) and 3(f). In the present device geometrical structures, we can use the thermally driven spin currents to read or manipulate the corresponding FE state, thanks to the occurrence of the layer-dependent SSE in the system.

As for the second key issue, it is fortunate that we also obtain an effective way to reduce the thermal charge current, and even to get a nearly pure spin current without any charge accumulation to read the corresponding FE states. The *ab initio* calculations show that the spin-splitting band structures of TiP-intercalated MoS₂ bilayer can be adjusted effectively by controlling the Ti-S bond length $L_{\text{Ti-S}}$. It should be noted that as $L_{\text{Ti-S}}$ is adjusted, the spin distribution in the related MoS₂ monolayer will be changed. However, from the previous first-principles calculations [19], the vertical distance between Ti and porphyrin plane is long to 0.42 Å, and the binding energy of Ti in the TiP molecule is high to 12 eV per atom, much larger than the bulk cohesive energy of Ti, revealing that the system of TiP-intercalated MoS₂ bilayer is stable, and the electric-polarized state in TiP molecule is

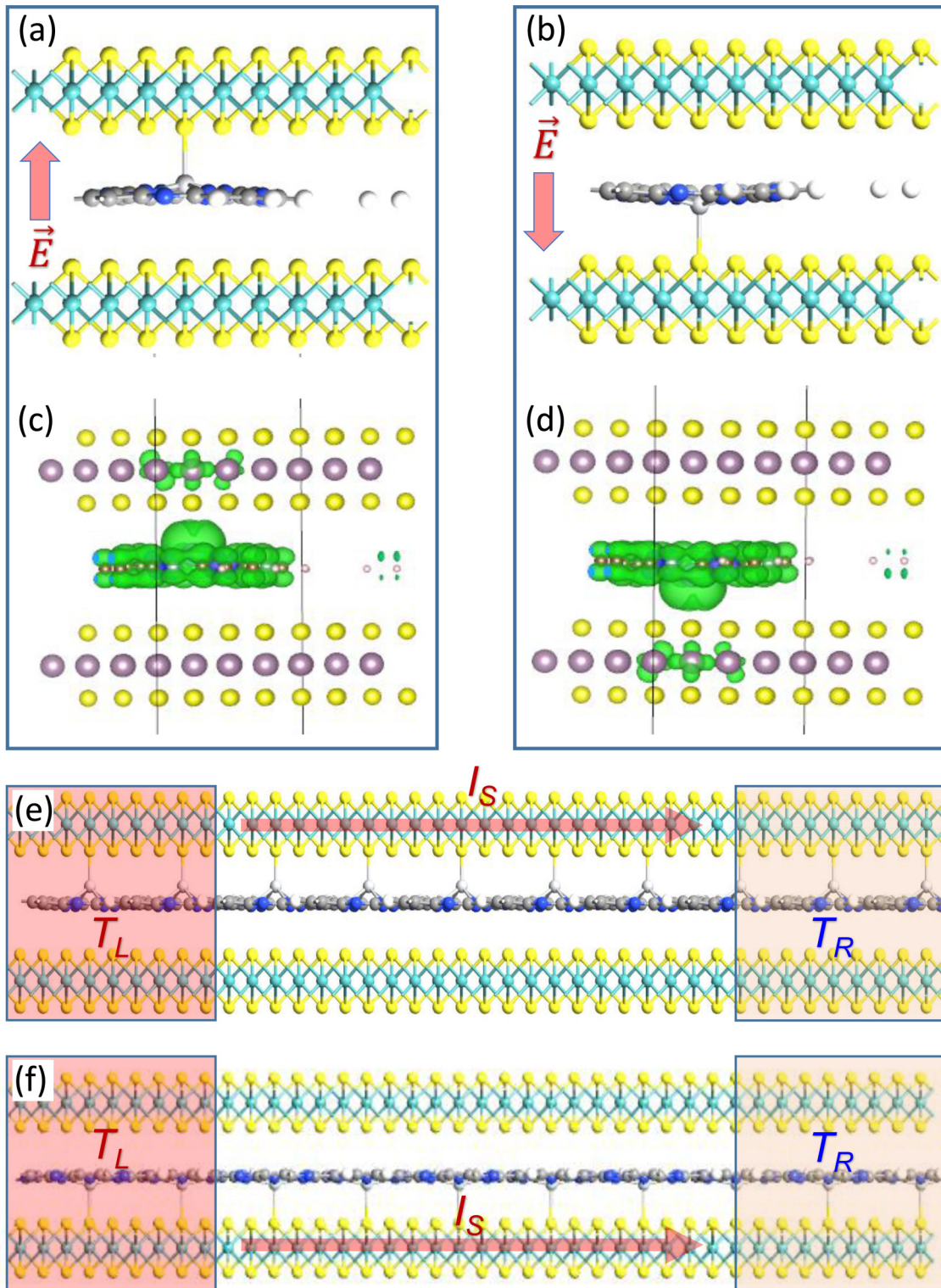


FIG. 3. (a, b) Two schematic structures of TiP-intercalated MoS₂ bilayer, where the TiP molecule is sandwiched between two MoS₂ monolayers to produce two opposite FE states by flipping an external electric field. (c, d) The spin distributions of the related FE states. (e, f) Two schematics of the TiP-intercalated-MoS₂-bilayer-based devices with the temperatures T_L and T_R to illustrate the occurrence of layer-dependent SSE.

less influenced by the coupling between Ti and S atoms. In Figs. 4(a) to 4(d), we plotted the band structures of the TiP-MoS₂ bilayer as L_{Ti-S} is increased from 13.9967 to 13.5967 Å by a step of 0.2 Å. One can find that with the increasing of

L_{Ti-S} , the spin-splitting energy bands shift downwards, making the spin-up and spin-down bands tend to be symmetrical about the Fermi level, indicating that two nearly symmetrical spin-dependent transport channels form in the spin-splitting

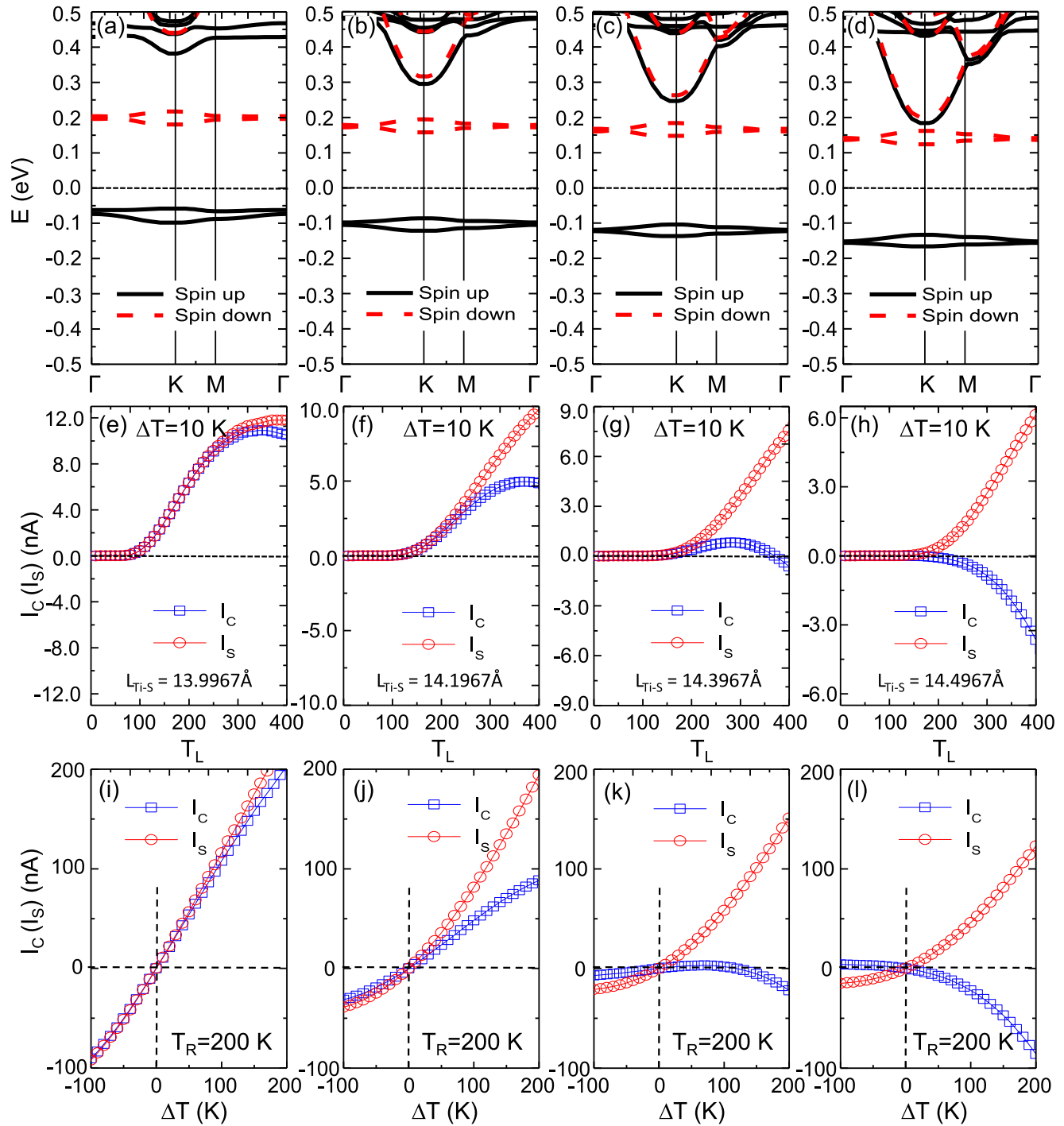


FIG. 4. (a)–(d) Spin-dependent band structures of TiP-intercalated bilayer MoS₂ when the length of Ti-S bond $L_{\text{Ti-S}}$ gradually changes from 13.9967 to 14.5967 Å. (e)–(h) The charge current I_c and the spin current I_s of the related spin caloritronic devices versus the temperature T_L in the left lead at the temperature gradient $\Delta T = 10$ K. (i)–(l) I_c and I_s versus ΔT at the device temperature $T_R = 200$ K.

transmission spectra. The numerical results for the thermally driven charge current I_c and the spin current I_s support the above conclusion. In Figs. 4(e) and 4(f), we plotted I_c and I_s versus T_L for $\Delta T = 10$ K, and in Figs. 4(i) to 4(l), plotted I_c and I_s versus ΔT at $T_R = 200$ K for the TiP-intercalated-MoS₂-bilayer-based devices. It is interesting that as $L_{\text{Ti-S}}$ increases, I_c is reduced remarkably as T_L or ΔT increases, while I_s keeps finite values for any case. In particular, for the device with $L_{\text{Ti-S}} = 14.3967$ Å, I_c is reduced nearly to zero in

a large region of device temperature settings, indicating that a nearly pure spin current is obtained in the device. Note that the corresponding spin-Seebeck coefficients adjusted by the strength of Ti-S bonds confirm further the above findings (see Figs. S2 and S3 in the Supplemental Material [51]). These properties indicate that we obtain an effective way to read the corresponding FE states without any energy dissipation since the charge current is forbidden while the nearly pure spin current is generated. Moreover, by using the inverse spin Hall

effect (ISHE) [52,53], the pure spin current can be converted to an observable voltage between two boundaries of the MoS₂ monolayer, which can be detected directly in experiments.

It should be noted that the physical mechanism of spin-Seebeck signals in the present TiP-intercalated-MoS₂-bilayer-based device can be expanded to other 0D FE systems, which are composed of VP molecules intercalated between MoSe₂ or MoTe₂ bilayer (see Figs. S4 to S7 in the Supplemental Material [51], for more details). Thus, we believe that the response signals from the SSE provide us an effective route to realize the readout and manipulation of the FE states in 0D MF materials.

IV. CONCLUSION

In summary, we designed theoretically some spin caloritronic devices based on 0D MF materials, which are constructed by the SMMs, such as the magnetic TiP molecules, intercalated within 2D materials, such as the MoS₂ bilayer. The SMMs can exhibit two opposite FE states as they are absorbed by the upper or lower MoS₂ monolayer, which can

be switched by an external electric field. The *ab initio* calculations combined with the NEGF theory show that the MoS₂ monolayer coupled with the SMMs are spin polarized to provide two spin channels for spin-up and spin-down electrons, respectively. As a temperature gradient is applied in the above MoS₂ monolayer, a well-defined conduction electron-based SSE occurs, and the spin current generated in the MoS₂ monolayer is tightly combined with the FE state in the coupled TiP molecule. By adjusting the length of Ti-S bonds, a pure thermal spin current can be achieved. These transport characteristics support that we can apply the spin-Seebeck signals to realize the readout of the FE states in 0D FE materials. Our theoretical results not only put forwards a low-power-dissipation strategy to read the SMM-based FE states, but also develop a new research field of spin-ferroelectro-caloritronics, focusing on the interplay of electrons' spin and the FE states in the presence of temperature gradient.

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