

## Anomalous evolution of the magnetocaloric effect in dilute triangular Ising antiferromagnets $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$

Mario Falsaperna,<sup>1</sup> Johnathan M. Bulled,<sup>2</sup> Gavin B. G. Stenning,<sup>3</sup> Andrew L. Goodwin,<sup>2</sup> and Paul J. Saines<sup>1,\*</sup>

<sup>1</sup>*School of Chemistry and Forensic Science, Ingram Building, University of Kent, Canterbury CT2 7NH, United Kingdom*

<sup>2</sup>*Inorganic Chemistry Laboratory, South Parks Road, Oxford OX1 3QR, United Kingdom*

<sup>3</sup>*ISIS Neutron and Muon Source, STFC Rutherford Appleton Laboratory, Chilton, Didcot OX11 0QX, United Kingdom*



(Received 4 March 2022; revised 18 November 2022; accepted 1 December 2022; published 22 December 2022)

We investigate the effects of diamagnetic doping in the solid-solution series  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$ , in which the parent  $\text{Tb}(\text{HCO}_2)_3$  phase has previously been shown to host a combination of frustrated and quasi-one-dimensional (quasi-1D) physics, giving rise to a triangular Ising antiferromagnetic ground state that lacks long range 3D order. Heat capacity measurements show three key features: (i) a low temperature Schottky anomaly is observed, which is constant as a function of  $x$ ; (ii) the transition temperature and associated entropy change are both surprisingly robust to diamagnetic doping; and (iii) an additional contribution at  $T < 0.4$  K appears with increasing  $x$ . The origin of this unusual behavior is rationalized in terms of the fragmentation of quasi-1D spin chains by the diamagnetic  $\text{Y}^{3+}$  dopant. Magnetocaloric measurements show a nonlinear dependence on  $x$ . The mass-weighted magnetocaloric entropy decreases across the series from the promising values in  $\text{Tb}(\text{HCO}_2)_3$ ; however, the magnetocaloric entropy per magnetic  $\text{Tb}^{3+}$  ion first decreases then increases with increasing  $x$ . Our results establish  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  as a model system in which to explore the functional ramifications of dilution in a low-dimensional magnet.

DOI: [10.1103/PhysRevMaterials.6.124410](https://doi.org/10.1103/PhysRevMaterials.6.124410)

### I. INTRODUCTION

The magnetocaloric effect (MCE) is an entropically driven phenomenon that has long been used for ultralow (sub-2 K) cryogenic cooling. The effect is observed in all magnetic materials upon application and subsequent removal of an external magnetic field [1]: an entropy decrease is caused by aligning magnetic moments in an applied field, and this entropy can be recovered when the field is removed. Magnetocalorics are a promising solid-state alternative to vapor compression refrigeration for cryogenic temperatures. This is particularly the case for the regimes in which liquid helium is conventionally used, due to this being an increasingly scarce and expensive resource [2]. An important development in the field is the recent appreciation that unconventional magnetic order can play a key role in optimizing MCE materials for applications at lower applied fields [3–6].

Historically, Gd-based magnetocalorics have been favored because  $\text{Gd}^{3+}$  ( $S = 7/2$ ) has the largest spin-only maximum magnetic entropy change  $\Delta S_m^{\text{max}} = R \ln(2S + 1)$  of any magnetic ion [7]. Indeed, a number of Gd-containing oxides and alloys have been reported to show good magnetocaloric properties for low temperature cooling; arguably the most famous is gadolinium gallium garnet (GGG), which is the benchmark material for cooling applications under 10 K [8]. Such materials are, however, often densely packed structures where strong interactions among the magnetic moments result in the emergence of long-range order at relatively high temperature,

commonly restricting their use as magnetocalorics, meaning that they are unsuitable for cooling in lower temperature ranges.

In this context, coordination polymers and metal-organic frameworks (MOFs)—with their versatile structural chemistry—offer an attractive mechanism of optimizing MCE by targeting structures that are predisposed to unconventional magnetic order [9]. For example, it is straightforward to engineer low-dimensional motifs, such as magnetic chains and sheets. When combined with magnetic frustration between these low-dimensional units, the long-range order in these materials can be suppressed to very low temperatures—even in structures with a relatively high density of magnetic ions. Competing magnetic interactions in turn enable the optimization of magnetocaloric properties when magnetic order is achieved [9,10]. The usual focus is on designing structures featuring triangular motifs, which are responsible for the competition of antiferromagnetic interactions; examples include the triangular, kagome, and trillium nets [6,11,12].

The  $\text{Ln}(\text{HCO}_2)_3$  coordination frameworks ( $\text{Ln} = \text{Gd}^{3+}, \text{Tb}^{3+}, \text{Dy}^{3+}, \text{Ho}^{3+}, \text{Er}^{3+}$ ) comprise one such family of modern MCE materials [13]. These systems have proven to be highly efficient magnetocalorics over a wide temperature range (2–20 K). While  $\text{Gd}(\text{HCO}_2)_3$  has the strongest performance at ultralow temperatures and high applied fields, it has been found that replacing Gd with Ising-like Tb and Ho leads to enhanced performance above 4 K in more modest applied fields of up to 2 T [13]. This reduced field requirement is ideal from an applications perspective since it can be achieved using permanent magnets [13]. The attractive properties of  $\text{Tb}(\text{HCO}_2)_3$  can be attributed to their highly

\*Corresponding author: P.Saines@kent.ac.uk

anisotropic and frustrated magnetism: strongly coupled ferromagnetic [ $J_{\text{intra-chain}} = 1.5(5)$  K]  $\text{Tb}^{3+}$  chains are packed on a triangular lattice with much weaker and antiferromagnetic interchain coupling [ $J_{\text{inter-chain}} = 0.03(1)$  K] [14]. It is the frustration of this state that allows chain magnetization to be reversed easily under low applied fields.

$\text{Tb}(\text{HCO}_2)_3$  enters a partially ordered triangular Ising antiferromagnet (TIA) state below 1.6 K [14,15], in which ferromagnetic long-range order is achieved along the direction of the chains, with short-range order between them due to the frustrated triangular lattice. Consistent with the proposed origin of the magnetocaloric properties of  $\text{Tb}(\text{HCO}_2)_3$ , neutron diffraction studies have shown that the application of weak magnetic fields helps to stabilize the TIA phase; however, at fields above 0.2 T, the system transforms to a simple ferromagnetic state in which all chains are aligned [16].

It is well known that diamagnetic impurities readily disrupt low-dimensional magnetic states [17–21], so the unusual discovery of the TIA state in  $\text{Tb}(\text{HCO}_2)_3$  raises the question of how this state responds to the introduction of such impurities, and in turn how diamagnetic impurities affect the magnetocaloric properties observed. In principle, replacing  $\text{Tb}^{3+}$  with diamagnetic  $\text{Y}^{3+}$  should be viable, given that the two cations have similar ionic radii: 1.095 and 1.075 Å for 9-coordinated  $\text{Tb}^{3+}$  and  $\text{Y}^{3+}$ , respectively [22]. Indeed we report here the synthesis and characterization of a family of Y-doped MOFs, the  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  frameworks. Heat capacity measurements show that the TIA state in this family is surprisingly robust to the introduction of diamagnetic impurities, and we discover an unexpected additional contribution to the low-temperature heat capacity at higher Y compositions. We ascribe this additional entropic contribution to the effect of spin-chain fragmentation. This may be related to the unusual experimental observation that, while a decrease in magnetocaloric properties is observed initially with Y doping, higher levels of diamagnetic defect density actually enhance the per-spin magnetocaloric effect. We discuss the implications of our results in the context of MCE materials.

## II. EXPERIMENT

Samples of  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  ( $x = 0.025, 0.05, 0.10, 0.20, 0.40, 0.60, 0.80$ ) were synthesized following a previously reported procedure [15]. Combinations of  $\text{Y}(\text{NO}_3)_3 \cdot 6\text{H}_2\text{O}$  (99.9%, Acros Organics) and  $\text{Tb}(\text{NO}_3)_3 \cdot 6\text{H}_2\text{O}$  (99%, Acros Organics) in different molar ratios were dissolved in 4.75 ml formic acid (99%, Acros Organics) with the addition of 0.25 ml ethanol used to slow down the reactions. After several minutes of stirring,  $\text{NO}_y$  was released, and white products precipitated out of solution. The products were filtered under vacuum and washed several times using ethanol.

Sample purity was assessed by powder x-ray diffraction (PXRD) using a Bragg-Brentano PANalytical X'PERT 3 diffractometer equipped with an Empyrean  $\text{CuK}_\alpha$  LFF source ( $\lambda = 1.5046$  Å) and a X'Celerator linear detector with the samples mounted on zero-background silicon sample holders. The resulting patterns were analyzed for phase purity using the program RIETICA, employing the Le Bail fitting method [23,24].

TABLE I. Comparison of the nominal and experimental compositions for  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  determined from x-ray fluorescence.

Nominal composition	Experimental composition
$\text{Tb}_{0.975}\text{Y}_{0.025}(\text{HCO}_2)_3$	$\text{Tb}_{0.99(6)}\text{Y}_{0.01(6)}(\text{HCO}_2)_3$
$\text{Tb}_{0.95}\text{Y}_{0.05}(\text{HCO}_2)_3$	$\text{Tb}_{0.96(5)}\text{Y}_{0.04(5)}(\text{HCO}_2)_3$
$\text{Tb}_{0.90}\text{Y}_{0.10}(\text{HCO}_2)_3$	$\text{Tb}_{0.91(4)}\text{Y}_{0.09(4)}(\text{HCO}_2)_3$
$\text{Tb}_{0.80}\text{Y}_{0.20}(\text{HCO}_2)_3$	$\text{Tb}_{0.819(19)}\text{Y}_{0.181(19)}(\text{HCO}_2)_3$
$\text{Tb}_{0.60}\text{Y}_{0.40}(\text{HCO}_2)_3$	$\text{Tb}_{0.63(3)}\text{Y}_{0.37(3)}(\text{HCO}_2)_3$
$\text{Tb}_{0.40}\text{Y}_{0.60}(\text{HCO}_2)_3$	$\text{Tb}_{0.44(8)}\text{Y}_{0.56(8)}(\text{HCO}_2)_3$
$\text{Tb}_{0.20}\text{Y}_{0.80}(\text{HCO}_2)_3$	$\text{Tb}_{0.25(12)}\text{Y}_{0.75(12)}(\text{HCO}_2)_3$

Compositional analysis of the cations present in the  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  series was carried out via energy dispersive x-ray fluorescence (EDXRF) measurements using a PANalytical Epsilon 3 spectrometer. Results obtained were calibrated by using a calibration curve determined from physically ground mixtures of  $\text{Y}(\text{HCO}_2)_3$  and  $\text{Tb}(\text{HCO}_2)_3$  with different Tb:Y molar ratios; namely, 97.5:2.5, 95:5, 90:10, 75:25, 50:50, and 27:75. Scanning electron microscopy (SEM) measurements and further energy-dispersive x-ray spectroscopy analysis (EDX) on selected regions of the samples were carried out using a Hitachi S3400N microscope. Powder samples were deposited on carbon tabs placed on aluminium sample holders, without further preparation, such as coating or surface polishing. Images of regions of approximately  $56 \times 44 \mu\text{m}^2$  were acquired using a 10-kV electron beam and a secondary electron (SE) detector.

DC susceptibility and isothermal magnetization measurements for  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$ , with  $x = 0.025, 0.05, 0.10$ , were performed using a Quantum Design MPMS or MPMS-3 superconducting quantum interference device (SQUID) magnetometer, with powder samples placed in gelatin capsules placed within pierced straws with a diamagnetic background. Heat capacity data between 4 and 14 K for  $\text{Tb}(\text{HCO}_2)_3$  and 250 mK and 4 K for  $\text{Tb}(\text{HCO}_2)_3$  and  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$ , with  $x = 0.05, 0.10, 0.20$ , and 0.40, were collected using a Quantum Design PPMS-Dynacool at the ISIS support laboratories, Rutherford Appleton Laboratories, UK.

## III. RESULTS AND DISCUSSION

In order to determine the compositions of our  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  samples, we used x-ray fluorescence (XRF) measurements. Our results suggest the experimental compositions are close to the nominal ones expected from the synthesis (see Table I). EDX measurements were also performed on selected regions of each sample, confirming there was no indication of significant inhomogeneity in the distribution of metals in the materials (see Figs. S1–S7 and Tables S1–S7 in the Supplemental Material [25]). There was some small variation between different regions of the sample, which can be primarily attributed to the surface roughness of the powder samples and which is accounted for in the uncertainty of the measurements. Overall, the average stoichiometries are in good agreement with those determined from bulk XRF analysis. Nominal stoichiometries have been used for the normalization of our data per amount of Tb present in each sample.

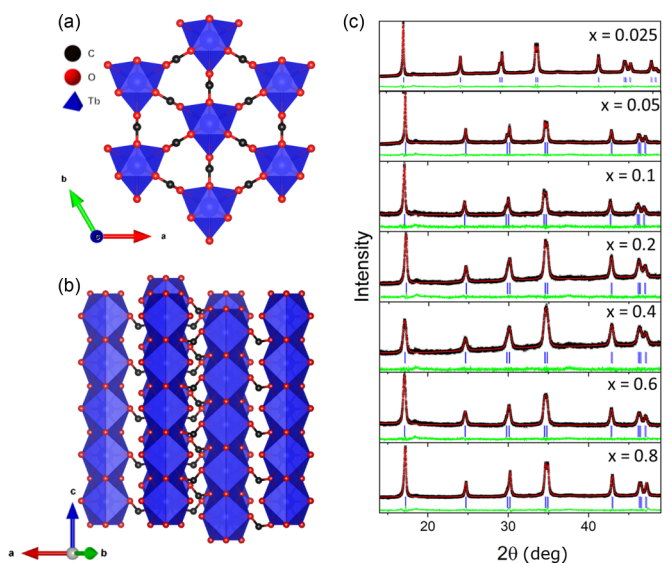


FIG. 1. Crystal structure of  $\text{Tb}(\text{HCO}_2)_3$  with (a) one-dimensional infinite chains connected by formate ligands and arranged on a triangular lattice on the  $ab$  plane and (b) face-sharing chains propagating along the  $c$  axis. (c) Conventional powder  $x$ -ray diffraction patterns ( $\lambda = 1.5046 \text{ \AA}$ ) of  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  fitted using the Le Bail method to highlight phase purity. The crosses and red and green lines are experimental and calculated intensities and the difference curve. Vertical markers indicate the positions of the Bragg reflections.

Our room-temperature powder  $x$ -ray diffraction measurements show that all the members of the series share the same rhombohedral  $R3m$  structure as the parent  $\text{Tb}(\text{HCO}_2)_3$  and  $\text{Y}(\text{HCO}_2)_3$  phases (see Fig. 1). Le Bail fits to powder  $x$ -ray diffraction patterns confirmed the phase purity of our samples, with the absence of peak broadening upon higher Y doping suggesting relatively high sample homogeneity for all the samples (see Table S8 for refinement statistics [25]). In this structure,  $\text{LnO}_9$  coordination polyhedra form face-sharing chains propagating down the  $c$  axis. Neighboring chains are then joined to one another via formate ligands, resulting in

a triangular arrangement within the  $ab$  plane [13–15]. The lattice parameters decrease with higher Y doping, as would be expected given the smaller size of  $\text{Y}^{3+}$ , showing subtle deviations from Vegard’s law which may indicate some degree of dopant anticlustering (see Fig. S8 [25]) [26].

Field cooled (FC) magnetic susceptibility  $\chi(T)$  measurements of the  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  frameworks, with  $x = 0.025, 0.05, 0.10$ , were carried out in a 0.1-T field from 2 to 300 K [see Fig. 2(a) and Figs. S9–S11 of the Supplemental Material [25]]. These susceptibility data did not show any indication of long-range magnetic ordering within this temperature range. This observation is consistent with previous magnetic susceptibility measurements on  $\text{Tb}(\text{HCO}_2)_3$ , for which no deviation from paramagnetic behavior is observed to well below 2 K [13–15]. The inverse susceptibilities of our  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  samples were well fitted using the Curie-Weiss law from 10 to 300 K; the corresponding  $\theta_{\text{CW}}$  values are given in Table II. From mean-field theory, one expects  $\theta_{\text{CW}}$  to scale with  $\text{Tb}^{3+}$  concentration if there is no variation in the strength of magnetic interactions on dilution by diamagnetic ions. Our data reflect this trend, and so we assume that the coupling among  $\text{Tb}^{3+}$  spins is likely to be similar across the whole series to that present in the parent  $\text{Tb}(\text{HCO}_2)_3$  framework—i.e., ferromagnetic intrachain and antiferromagnetic interchain coupling. Effective magnetic moments  $\mu_{\text{eff}}$  were found to be close to the reported experimental value for  $\text{Tb}(\text{HCO}_2)_3$  and also the  $9.75\mu_B$  value expected from the Russel-Saunders coupling scheme (see Table II) [13].

Magnetization measurements from 12 K down to 2 K are consistent with paramagnetic behavior (see Figs. S12–S16 [25]). Observed normalized values of saturation magnetization  $M_{\text{sat}}$  at 2 K and a magnetic field of 5 T are close to the theoretical value of  $4.50 \mu_B \text{ atom}_{\text{Tb}}^{-1}$  expected for Ising behavior, for which  $M_{\text{sat}}$  is expected to be close to  $gJ/2$ , suggesting significant single ion anisotropy. They are, however, significantly lower than the reported value of  $5.77(4)\mu_B \text{ atom}^{-1}$  previously reported for  $\text{Tb}(\text{HCO}_2)_3$  [see Fig. 2(b) and Table II] [13].

Heat capacity  $C(T)$  data were measured for  $\text{Tb}(\text{HCO}_2)_3$  and  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  with  $x = 0.05, 0.10, 0.20$ , and  $0.40$  in zero-field conditions. The heat capacity includes nuclear,

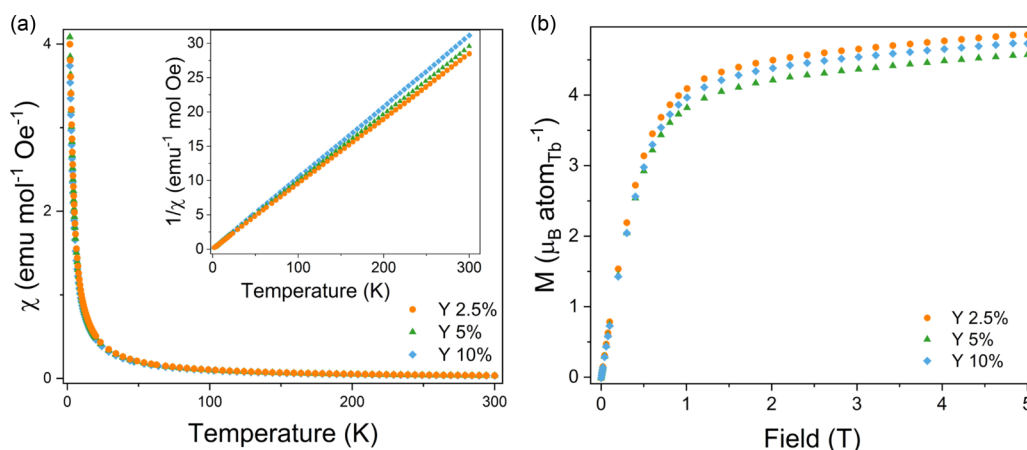


FIG. 2. (a) FC molar susceptibility  $\chi(T)$  for  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  with  $x = 0.025, 0.05, 0.10$ , measured from 2–300 K in a field of 0.1 T; the inverse molar susceptibility  $\chi^{-1}(T)$  is presented in the inset. (b) Magnetization plot of  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  ( $x = 0.025, 0.05$ , and  $0.10$ ) collected at 2 K for fields up to 5 T.

TABLE II. Magnetic properties extracted from FC susceptibility and magnetization measurements of  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  samples. Magnetic properties for  $x = 0$  were measured from Saines *et al.* [13].

$x$	$\theta_{\text{CW}}(\text{K})$	$ \theta_{\text{CW}} /(1-x)$ (K)	$\text{Tb}^{3+}$ magnetic moment ( $\mu_{\text{B}} \text{ atom}^{-1}$ )	$M_{\text{sat}}$ ( $\mu_{\text{B}} \text{ atom}^{-1}$ )	$M_{\text{sat}}$ ( $\mu_{\text{B}} \text{ atom}_{\text{Tb}}^{-1}$ )
0.0	-0.9	0.9	9.62	5.77(4)	5.77(4)
0.025	-0.86(5)	0.88(5)	9.417(2)	4.73(2)	4.86(2)
0.05	-1.11(8)	1.17(8)	9.511(2)	4.34(2)	4.57(2)
0.10	-0.79(8)	0.88(8)	9.771(2)	4.25(2)	4.73(2)

electronic, lattice, and magnetic contributions:  $C(T) = C_{\text{nuc}} + C_{\text{el}} + C_{\text{lat}} + C_{\text{mag}}$ . Here, the electronic term  $C_{\text{el}}$  can safely be ignored as the materials are insulators. The lattice contribution  $C_{\text{lat}}$  was estimated using a Debye fit to the heat capacity data for  $\text{Tb}(\text{HCO}_2)_3$  between 8 and 14 K, where phonon population is the dominant process at play. We obtained a Debye temperature of 156.2(1.8) K, which we used for all values of  $x$  [27]. The value of  $C_{\text{lat}}$  is very small at the temperatures of

$$C_{\text{nuc}} = \frac{\Delta^2 R}{9T^2} \frac{\exp(-\Delta/3T)[1 + \exp(-\Delta/3T)]^4 + 4 \exp(-\Delta/T)}{[1 + \exp(-\Delta/3T) + \exp(-2\Delta/3T) + \exp(-\Delta/T)]^2},$$

where the single adjustable parameter  $\Delta$  captures the hyperfine splitting [28]. We found  $\Delta = 0.437(2)$  K for  $\text{Tb}(\text{HCO}_2)_3$ , which is consistent with many other Tb-containing systems, including Tb metal itself (see Table S9 [25]) [28–30] suggesting this value solely depends on the internal electronic structure of Tb and is independent of the local chemical environment. Therefore, this parameter is here assumed to be constant with respect to stoichiometry and subtracted from the measured heat capacity for all samples. Doing so leads to the curious result that this hyperfine coupling contribution does not account for the entirety of the observed low-temperature

relevance to magnetic ordering ( $T < 4$  K) (see Fig. S17 [25]). Finally, it was possible to estimate the nuclear contribution  $C_{\text{nuc}}$  due to the Schottky anomaly, which arises below 0.8 K as a result of magnetic hyperfine coupling of the electronic spins in the  $4f$  orbitals of terbium and the magnetic moment of the terbium nucleus ( $I = 3/2$ ). This contribution was estimated by fitting to the low-temperature data  $0.4 < T < 0.8$  K using the expression

heat capacity of those members with higher concentrations of  $\text{Y}^{3+}$  (see Fig. 3). The resulting  $C_{\text{mag}}(T)$  data, obtained following subtraction of lattice and nuclear contributions, show that  $\text{Tb}(\text{HCO}_2)_3$  has the strongest magnetic contribution to the heat capacity, with this contribution decreasing with higher  $\text{Y}^{3+}$  concentration in the other samples, as would be expected.

The values for the temperatures of the maxima of the heat capacity curves, indicative of the transition temperature and the strength of the correlations within the system, were extracted and these were found to be centered at 1.54 K for

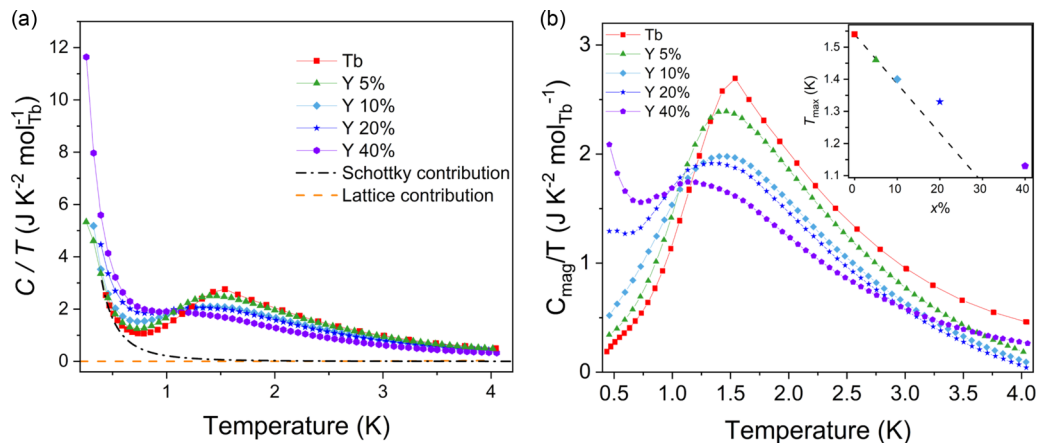


FIG. 3. Plot of magnetic heat capacity  $C_{\text{mag}}/T$ , normalized per moles of Tb, for  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  ( $x = 0, 0.05, 0.10, 0.20, 0.40$ ) (a) measured between 300 mK and 4 K in zero field conditions and (b) after subtracting the hyperfine coupling contribution for the Tb cations. In the latter case, the data are shown down to 0.4 K, the lowest limit for the fits for the hyperfine coupling. Values of  $T_{\text{max}}$  are shown in the inset, with the dashed line representing the trend as predicted by mean field theory.

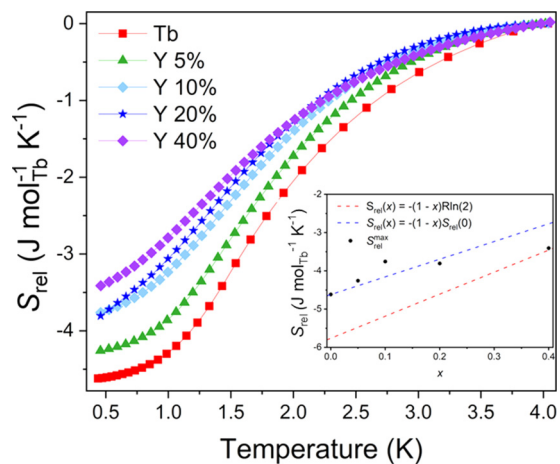


FIG. 4. Magnetic entropies per moles of Tb extracted from the heat capacity data for the  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  ( $x = 0, 0.05, 0.10, 0.20, 0.40$ ) series in zero-field conditions. The inset shows the maximal values and the  $S_{\text{rel}}$  models derived from statistics.

$\text{Tb}(\text{HCO}_2)_3$ , close to the reported transition temperature to the TIA state for this system [see inset Fig. 3(b)] [15]. There is a surprisingly modest decrease in this transition temperature with  $\text{Y}^{3+}$  doping. Even where almost half of the  $\text{Tb}^{3+}$  cations are replaced with  $\text{Y}^{3+}$  in  $\text{Tb}_{0.60}\text{Y}_{0.40}(\text{HCO}_2)_3$ , the TIA transition still occurs at a similar temperature, being reduced by less than 30% of the undoped  $\text{Tb}(\text{HCO}_2)_3$ . Further heat capacity measurements were performed under different applied fields on  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  members with  $x = 0.10, 0.20$ , and  $0.40$ . These data show that the magnetic component of the heat capacity  $C_{\text{mag}}$  is suppressed with higher applied fields, confirming that the features observed are magnetic in nature (see Figs. S18–S20 [25]).

The low-temperature magnetic entropy loss  $S_{\text{rel}}$ , was extracted from the zero-field heat capacity data using the thermodynamic relationship  $S_{\text{rel}}(T) = -\int_T^{T_{\text{max}}} C_{\text{mag}}(T')/T' dT'$ , with  $T_{\text{max}} = 4$  K chosen as useful limiting temperature well above the TIA transition (see Fig. 4 and Table III). The total loss down to 0.5 K (the lowest temperature point for which we have reliable data), which we call the maximal magnetic entropy  $S_{\text{rel}}^{\text{max}}$ , decreases with magnetic dilution more quickly than the TIA ordering temperature—even when normalized by the amount of Tb present. The shape of the  $S_{\text{rel}}(T)$  function varies as  $x$  is increased, which is a result of the low-temperature specific-heat feature observed for Y-doped samples.

TABLE III. Maximal magnetic entropy loss associated with the TIA transition for the  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  solid solutions with  $x = 0, 0.05, 0.10, 0.20$ , and  $0.40$ .

Sample	$-S_{\text{rel}}^{\text{max}}$ ( $\text{J kg}^{-1} \text{K}^{-1}$ )	$-S_{\text{rel}}^{\text{max}}$ ( $\text{J mol}^{-1} \text{K}^{-1}$ )
$\text{Tb}(\text{HCO}_2)_3$	15.72	4.62
$\text{Tb}_{0.95}\text{Y}_{0.05}(\text{HCO}_2)_3$	13.93	4.26
$\text{Tb}_{0.90}\text{Y}_{0.10}(\text{HCO}_2)_3$	11.79	3.76
$\text{Tb}_{0.80}\text{Y}_{0.20}(\text{HCO}_2)_3$	10.86	3.81
$\text{Tb}_{0.60}\text{Y}_{0.40}(\text{HCO}_2)_3$	7.69	3.41

Our key observations from heat capacity measurements of the  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  series are (i) that the peak at  $\sim 1.5$  K, associated with formation of the TIA state in  $\text{Tb}(\text{HCO}_2)_3$ , broadens and shifts to only moderately lower temperature with  $\text{Y}^{3+}$  doping, and (ii) that there is an additional low-temperature contribution to the heat capacity at high levels of diamagnetic doping fraction. The former indicates that the formation of the TIA state caused by the ordering of the 1D chains within  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  is surprisingly robust to magnetic dilution. The entropy loss associated with formation of the TIA state—i.e., the area under the main broad peak in  $C_{\text{mag}}/T$ —decreases in magnitude with increasing  $x$ ; this affect is stronger than the reduction in  $T_{\text{max}}$  and suggests that the extent of magnetic ordering is affected more by doping than the magnetic transition temperature. We interpret (ii) as arising from an entropic contribution due to the presence of short chains, which are a result of the  $\text{Y}^{3+}$  ions breaking the strongly interacting quasi-one-dimensional (quasi-1D) chains into small segments. Because of the much weaker interchain interactions, we would not expect these short chains to order until significantly below the TIA transition, at which temperature they contribute to the upturn in  $C_{\text{mag}}/T$  seen at the lowest temperatures. Simple statistical arguments, assuming no dopant clustering, give an entropy of  $S_{\text{rel}}(x) = -(1-x)R \ln 2$  associated with complete intrashort-chain order. We find good qualitative agreement to the experimental values of  $S_{\text{rel}}(T)$  evaluated at 0.7 K, the relevant turning point in  $C_{\text{mag}}/T$  (see inset to Fig. 4). Since our integral only spans a portion of this in-chain ordering,  $S_{\text{rel}}(x) = -(1-x)S_{\text{rel}}(0)$  is a more appropriate comparison. We intend to investigate the behavior of these short chains in more detail in a forthcoming computational study.

The magnetic entropy change  $-\Delta S_{\text{m}}$  as a function of applied magnetic field was extracted from the magnetization data using the Maxwell relation  $\Delta S_{\text{m}}(T) = \int [\delta M(T, H)/\delta T]_H dH$  from 2 to 12 K for  $x = 0.025, 0.05, 0.10, 0.20$ , and  $0.40$  (see Fig. 5 and Figs. S20 and S21 of the Supplemental Material for  $\Delta B = 5-0$  and  $2-0$  T field changes [25]; see Figs. S23 and S24 for  $\Delta B = 1-0$  T [25]. See Table IV for maximum entropy changes). In determining the volumetric values, the crystallographic densities of each of the measured members of the series were estimated by calculating the ratio between the formula weights of each member and the unit cell volumes determined from the Le Bail fits to the powder diffraction data (see Table S10 for density used [25]) [22]. Compared to the values reported for  $\text{Tb}(\text{HCO}_2)_3$  [13], those found for the doped samples clearly show that the magnetocaloric performance of this material decreases due to Y doping as a function of sample weight or volume. However, the gravimetric entropy changes of the  $x = 0.40$  sample increase again for 2-0 and 1-0 T field changes compared to the  $x = 0.20$  compound. Interestingly, normalized values per mole of  $\text{Tb}^{3+}$  are lower compared to the  $-\Delta S_{\text{m}}^{\text{max}}$  for the parent compound  $\text{Tb}(\text{HCO}_2)_3$ , with the decrease in  $-\Delta S_{\text{m}}^{\text{max}}$  with respect to Y doping more dramatic for low values of  $x$ —particularly for more modest applied field changes. This trend is then reversed at higher concentrations, with  $\text{Tb}_{0.60}\text{Y}_{0.40}(\text{HCO}_2)_3$  having the highest  $-\Delta S_{\text{m}}^{\text{max}}$  among the Y-doped samples with respect to the amount of  $\text{Tb}^{3+}$  present for all field changes considered. Exceptionally

TABLE IV. Maximum entropy changes extracted from magnetization data for the  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  solid solutions ( $x = 0, 0.025, 0.05, 0.10$ ) for field changes of 5-0, 2-0, and 1-0 T.

Sample	$\Delta B = 5-0 \text{ T}$			$\Delta B = 2-0 \text{ T}$			$\Delta B = 1-0 \text{ T}$		
	$-\Delta S_m^{\text{max}}$ ( $\text{J kg}^{-1} \text{K}^{-1}$ )	$-\Delta S_m^{\text{max}}$ ( $\text{mJ cm}^{-3} \text{K}^{-1}$ )	$-\Delta S_m^{\text{max}}$ ( $\text{J mol}_{\text{Tb}}^{-1} \text{K}^{-1}$ )	$-\Delta S_m^{\text{max}}$ ( $\text{J kg}^{-1} \text{K}^{-1}$ )	$-\Delta S_m^{\text{max}}$ ( $\text{mJ cm}^{-3} \text{K}^{-1}$ )	$-\Delta S_m^{\text{max}}$ ( $\text{J mol}_{\text{Tb}}^{-1} \text{K}^{-1}$ )	$-\Delta S_m^{\text{max}}$ ( $\text{J kg}^{-1} \text{K}^{-1}$ )	$-\Delta S_m^{\text{max}}$ ( $\text{mJ cm}^{-3} \text{K}^{-1}$ )	$-\Delta S_m^{\text{max}}$ ( $\text{J mol}_{\text{Tb}}^{-1} \text{K}^{-1}$ )
$\text{Tb}(\text{HCO}_2)_3$	15.74	61.62	4.62	12.06	47.23	3.55	8.08	31.64	2.38
$\text{Tb}_{0.975}\text{Y}_{0.025}(\text{HCO}_2)_3$	13.98	54.04	4.20	10.14	39.21	3.04	6.42	24.82	1.92
$\text{Tb}_{0.95}\text{Y}_{0.05}(\text{HCO}_2)_3$	13.10	50.39	4.00	9.45	36.33	2.89	6.15	23.64	1.88
$\text{Tb}_{0.90}\text{Y}_{0.10}(\text{HCO}_2)_3$	13.29	50.67	4.24	9.58	36.52	3.06	6.07	23.13	1.93
$\text{Tb}_{0.80}\text{Y}_{0.20}(\text{HCO}_2)_3$	12.83	47.85	4.49	9.45	35.24	3.31	5.77	21.52	2.02
$\text{Tb}_{0.60}\text{Y}_{0.40}(\text{HCO}_2)_3$	10.80	38.34	4.79	9.95	35.31	4.41	6.07	21.56	2.69

$\text{Tb}_{0.60}\text{Y}_{0.40}(\text{HCO}_2)_3$  has a higher normalized  $-\Delta S_m^{\text{max}}$  than that of the parent compound  $\text{Tb}(\text{HCO}_2)_3$  for all the applied field changes (see insets in Fig. 5 and Fig. S23, as well as Figs. S21, S22, and S24 [25]).

When compared to other magnetically dilute MCE materials, such as the Ga-doped  $\text{La}_{0.7}(\text{Ba}, \text{Sr})_{0.3}\text{Mn}_{1-x}\text{Ga}_x\text{O}_3$  ( $x =$

0, 0.1, 0.2) [31], the Cr-doped  $\text{La}_{0.65}\text{Eu}_{0.05}\text{Sr}_{0.3}\text{Mn}_{1-x}\text{Cr}_x\text{O}_3$  ( $x = 0.05, 0.1, \text{ and } 0.15$ ) [32], and the Sn-substituted  $\text{RCO}_2$  ( $R = \text{Gd}, \text{Tb}, \text{Dy}$ ) alloys, the  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  series follows similar trends with respect to its initial decrease in  $-\Delta S_m^{\text{max}}$  with  $\text{Y}^{3+}$  doping—i.e., lower transition temperatures and lower values of  $-\Delta S_m^{\text{max}}$  when higher concentrations of nonmagnetic impurities are present. This has also been observed in the geometrically frustrated  $\text{Tm}_{1-x}\text{Lu}_x\text{B}_4$ , which features a Shastry-Sutherland lattice, for  $x < 0.06$  [33]. However, for  $\text{Tm}_{0.7}\text{Lu}_{0.3}\text{B}_4$  the trend is reversed. Monte Carlo modeling suggested that in  $\text{Tm}_{1-x}\text{Lu}_x\text{B}_4$  small concentrations of nonmagnetic ions relieve the degeneracy of the ground state for this magnetic system, which results in a decrease in ground-state entropy and, therefore, of the MCE. Conversely, higher concentrations of nonmagnetic dopant result in the formation of nearly independent clusters which are responsible for a significant degeneracy of the ground state, leading to a higher zero-field entropy change and, ultimately, in an improvement of the MCE [33]. This observation is compatible with the putative role of fragmented chains discussed here [33]. Indeed, theoretical studies of selective doping of the sublattices of a triangular Ising antiferromagnet have shown that it is possible to achieve a similar effect, i.e., an increase in the maxima of entropy change when higher concentration of nonmagnetic dopants are present in such a system [34].

These results should be understood in the context of the promising magnetocaloric behavior of  $\text{Tb}(\text{HCO}_2)_3$  emerging from the frustration of its strongly coupled ferromagnetic chains leading to a significant zero-field entropy, which is suppressed on application of relatively small fields. We propose that the initial decrease in normalized  $-\Delta S_m^{\text{max}}(x)$  with increasing  $x$  is caused by the rapid suppression of this geometric frustration due to local symmetry breaking. This is reflected in the initial decrease in normalized  $-\Delta S_m^{\text{max}}$  being somewhat greater for more modest applied fields. Conversely, as the concentration of  $\text{Y}^{3+}$  increases further there are likely a higher number of short chains present, which leads to a significantly more disordered state in the absence of an applied magnetic field and thus a greater change in the normalized  $-\Delta S_m^{\text{max}}$ .

#### IV. CONCLUSION

In this work we have reported the synthesis of members of the  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  series of coordination frameworks. We have monitored the evolution of the magnetic and magnetocaloric properties of these materials upon changing the

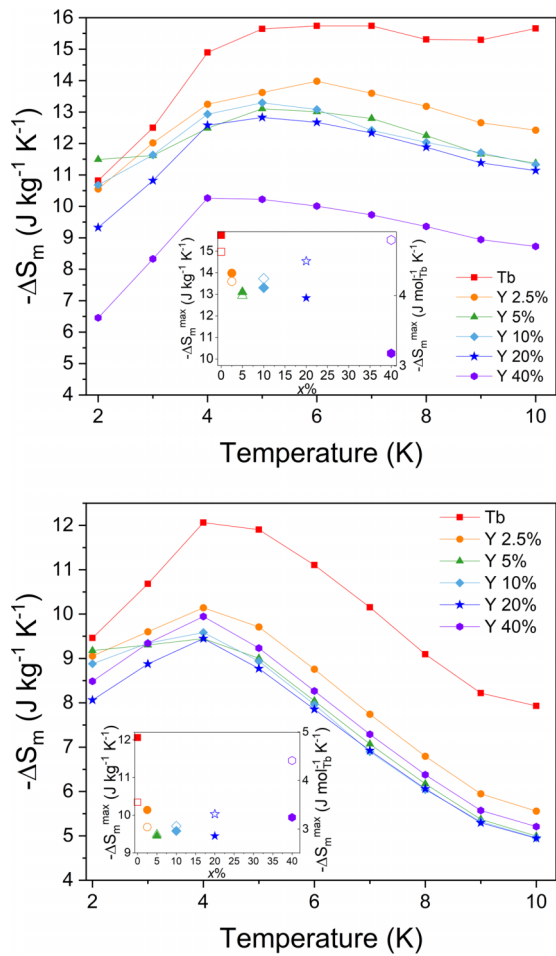


FIG. 5. Gravimetric magnetic entropy changes extracted from the magnetization data for  $\text{Tb}_{1-x}\text{Y}_x(\text{HCO}_2)_3$  ( $x = 0, 0.025, 0.05, 0.10, 0.20, 0.40$ ) series for  $\Delta B = 5-0 \text{ T}$  (top) and  $\Delta B = 2-0 \text{ T}$  (bottom). Insets show the values of  $-\Delta S_m^{\text{max}}$  in gravimetric (full symbols) and normalized molar (hollow symbols) units for each sample.

composition of the sample via both magnetization and heat capacity measurements. The latter have allowed us to observe the low temperature evolution of the TIA transition with the addition of diamagnetic impurities. Maxima in the heat capacity are observed in data measured for all samples up to  $x = 0.40$ , confirming that these undergo a transition to the TIA state, with the transition shifting to slightly lower temperatures. These results indicate that the emergence of the TIA state is quite robust and only slightly affected by the presence of low concentrations of diamagnetic impurities, although the extent of 1D order in this state likely decreases with  $Y^{3+}$  doping as indicated by the smaller magnetic entropies. Furthermore, fits to the data have shown that an additional contribution to the magnetic heat capacity is present, with this increasing with the amount of Y in the sample. This contribution is ascribed to an entropic effect caused by the increasing presence of shorter segments along the chains of the  $Tb_{1-x}Y_x(HCO_2)_3$ .

We have found the incorporation of diamagnetic ions to reduce the magnetocaloric properties of these compounds, determined for low Y-doped samples, namely  $x = 0.025, 0.05, 0.10, 0.2,$  and  $0.4$ , with values of entropy change  $-\Delta S_m^{\max}$  reduced in magnitude relative to the parent material,  $Tb(HCO_2)_3$ —particularly for lower applied fields. However, among doped samples, the lowest values of  $-\Delta S_m^{\max}$ , normalized per amount of Tb present, are obtained for  $x = 0.05$ ,

while the values of entropy change increase significantly for higher values of  $x$ , independent of the applied fields. We have proposed a mechanism for this effect, resulting from two competing implications of diamagnetic doping, but thorough theoretical investigation of this effect is required. Overall, this work has highlighted that, while the emergence of the TIA state in  $Tb(HCO_2)_3$  is surprisingly robust to the dilution of magnetic cations responsible for it by diamagnetic impurities, the disruption of the 1D ferromagnetic chains that play a key role in its emergence leads to an unusual trend in the magnetocaloric properties when normalized for the amount of magnetic cation present. As mentioned, we plan to gain further insight about the behavior of these systems via computational studies.

### ACKNOWLEDGMENTS

The authors gratefully acknowledge financial support from the European Research Council (Grant No. 788144), Engineering and Physical Sciences Research Council (Grant No. EP/T027886/1), and the Leverhulme Trust (Grant No. RPG-2018-268). Low temperature PPMS measurements were carried out on the EPSRC Advanced Materials Characterization Suite (Grant No. EP1M0052411) at the materials characterization lab at ISIS, Harwell.

- [1] L. Mañosa, A. Planes, and M. Acet, Advanced materials for solid-state refrigeration, *J. Mater. Chem. A* **1**, 4925 (2013).
- [2] A. H. Olafsdottir and H. U. Sverdrup, Assessing the past and future sustainability of global helium Resources, Extraction, supply and Use, using the integrated assessment model Q WORLD7, *Bioph. Econ. Sustain.* **5**, 6 (2020).
- [3] P. Mukherjee, Y. Wu, G. I. Lampronti, and S. E. Dutton, Magnetic properties of monoclinic lanthanide Orthoborates,  $LnBO_3$ ,  $Ln = Gd, Tb, Dy, Ho, Er, Yb$ , *Mater. Res. Bull.* **98**, 173 (2018).
- [4] R. J. C. Dixey and P. J. Saines, Optimization of the magnetocaloric effect in low applied magnetic fields in  $InoHCO_3$  frameworks, *Inorg. Chem.* **57**, 12543 (2018).
- [5] M. Falsaperna, G. B. G. Stenning, I. da Silva, and P. J. Saines, Magnetocaloric  $Ln(HCO_2)(C_2O_4)$  Frameworks: Synthesis, structure and magnetic properties, *J. Mater. Chem. C* **9**, 13209 (2021).
- [6] J. M. Bulled, J. A. M. Paddison, A. Wildes, E. Lhotel, S. J. Cassidy, B. Pato-Doldán, L. C. Gómez-Aguirre, P. J. Saines, and A. L. Goodwin, Geometric Frustration on the Trillium Lattice in a Magnetic Metal-Organic Framework, *Phys. Rev. Lett.* **128**, 177201 (2022).
- [7] J. W. Sharples and D. Collison, Lanthanides and the Magnetocaloric Effect, in *Lanthanides and Actinides in Molecular Magnetism* (Wiley-VCH Verlag GmbH & Co. KGaA, Weinheim, 2015), pp. 293–314.
- [8] Y. Z. Zheng, G. J. Zhou, Z. Zheng, and R. E. P. Winpenny, Molecule-Based magnetic coolers, *Chem. Soc. Rev.* **43**, 1462 (2014).
- [9] M. Falsaperna and P. J. Saines, Development of magnetocaloric coordination polymers for low temperature cooling, *Dalton Trans.* **51**, 3394 (2022).
- [10] M. E. Zhitomirsky, Enhanced magnetocaloric effect in frustrated magnets, *Phys. Rev. B* **67**, 104421 (2003).
- [11] A. P. Ramirez, Strongly geometrically frustrated magnets, *Annu. Rev. Mater. Sci.* **24**, 453 (1994).
- [12] M. Mekata, Kagome: The story of the basketweave lattice, *Phys. Today* **56(2)**, 12 (2003).
- [13] P. J. Saines, J. A. M. Paddison, P. M. M. Thygesen, and M. G. Tucker, Searching beyond gd for magnetocaloric Frameworks: magnetic properties and interactions of the  $Ln(HCO_2)_3$  series, *Mater. Horiz.* **2**, 528 (2015).
- [14] D. R. Harcombe, P. G. Welch, P. Manuel, P. J. Saines, and A. L. Goodwin, One-Dimensional magnetic order in the metal-organic framework  $Tb(HCOO)_3$ , *Phys. Rev. B* **94**, 174429 (2016).
- [15] R. J. C. Dixey, F. Orlandi, P. Manuel, P. Mukherjee, S. E. Dutton, and P. J. Saines, Emergent magnetic order and correlated disorder in formate metal-organic frameworks, *Philos. Trans. R. Soc., A* **377**, 20190007 (2019).
- [16] R. J. C. Dixey, P. Manuel, F. Orlandi, P. Mukherjee, S. E. Dutton, G. B. G. Stenning, and P. J. Saines, In situ observation of the magnetocaloric effect through neutron diffraction in the  $Tb(DCO_2)_3$  and  $tbdco_3$  frameworks, *J. Mater. Chem. C* **8**, 12123 (2020).
- [17] G. B. Martins, M. Laukamp, J. Riera, and E. Dagotto, Local Enhancement of Antiferromagnetic Correlations by Nonmagnetic Impurities, *Phys. Rev. Lett.* **78**, 3563 (1997).
- [18] A. Zorko, D. Arçon, A. Lappas, and Z. Jagličić, Magnetic versus non-magnetic doping effects in the haldane chain compound  $PbNi_2V_2O_{10}$ , *New J. Phys.* **8**, 60 (2006).
- [19] J. Das, A. v. Mahajan, J. Bobroff, H. Alloul, F. Alet, and E. S. Sørensen, Comparison of  $S = 0$  and  $S = 1/2$  impurities in the

- haldane chain compound  $\text{Y}_2\text{BaNiO}_5$ , *Phys. Rev. B* **69**, 144404 (2004).
- [20] T. I. Arbutova, I. B. Smolyak, S. V. Naumov, and A. A. Samokhvalov, Effect of doping on the magnetic properties of the low-dimensional antiferromagnet  $\text{CuO}$ , *Phys. Solid State* **40**, 1702 (1998).
- [21] I. Kruk, J. E. L. Waldron, and M. A. Green, Titanium doping of the metallic one-dimensional Antiferromagnet,  $\text{Nb}_{12}\text{O}_{29}$ , *Inorganics (Basel)* **7**, 66 (2019).
- [22] R. D. Shannon, Revised effective ionic radii and systematic studies of interatomic distances in halides and chalcogenides, *Acta Crystallogr.* **A32**, 751 (1976).
- [23] B. Hunter, Rietica - a Visual rietveld program, in *AINSE Symposium on Neutron Scattering Powder Diffraction; Australian Neutron Beam Users Group Meeting*, Vol. 31 (Lucas Heights, NSW, Australia, 2000), pp. 20–44.
- [24] A. le Bail, H. Duroy, and J. L. Fourquet, Ab-Initio structure determination of  $\text{Li}_2\text{WO}_6$  by x-ray powder diffraction, *Mater. Res. Bull.* **23**, 447 (1988).
- [25] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevMaterials.6.124410> for additional information in the form of electron microscopy, crystallographic, magnetometry and heat capacity data.
- [26] M. Castellanos and A. R. West, Deviations from Vegard's law in oxide solid solutions. The systems  $\text{Li}_2\text{TiO}_3$ - $\text{MgO}$  and  $\text{Li}_2\text{TiO}_3$ - $\text{Na}_2\text{TiO}_3$ , *J. Chem. Soc., Faraday Trans. 1* **76**, 2159 (1980).
- [27] P. Debye, Zur theorie der spezifischen wärmen, *Ann. Phys.* **344**, 789 (1912).
- [28] E. C. Heltemes and C. A. Swenson, Nuclear contribution to the heat capacity of terbium metal, *J. Chem. Phys.* **35**, 1264 (1961).
- [29] D. Neogy and A. Chatterji, Magnetic Properties, Schottky heat Capacity, and the nuclear quadrupole splitting of the 8.42 KeV excited state of  $\text{Tm}^{3+}$  on tetragonal sites in  $\text{CaF}_2$ , *J. Chem. Phys.* **68**, 5647 (1978).
- [30] D. Neogy, P. Paul, and K. N. Chattopadhyay, Investigation of Magnetic, thermal and hyperfine properties of  $\text{Tb}^{3+}$  in the single crystal of terbium trifluoromethanesulfonate nonahydrate, *J. Magn. Magn. Mater.* **283**, 164 (2004).
- [31] R. Tlili, A. Omri, M. Bekri, M. Bejar, E. Dhahri, and E. K. Hlil, Effect of GA substitution on magnetocaloric effect in  $\text{La}_{0.7}(\text{Ba}, \text{Sr})_{0.3}\text{Mn}_{1-x}\text{Ga}_x\text{O}_3$  ( $0.0 \leq x \leq 0.20$ ) polycrystalline at room temperature, *J. Magn. Magn. Mater.* **399**, 143 (2016).
- [32] R. Bellouz, M. Oumezzine, E. K. Hlil, and E. Dhahri, Effect of Cr substitution on magnetic and magnetic entropy change of  $\text{La}_{0.65}\text{Eu}_{0.05}\text{Sr}_{0.3}\text{Mn}_{1-x}\text{Cr}_x\text{O}_3$  ( $0.05 \leq x \leq 0.15$ ) rhombohedral nanocrystalline near room temperature, *J. Magn. Magn. Mater.* **375**, 136 (2015).
- [33] Mat. Orendáč *et al.*, Tuning the magnetocaloric effect in the Lu-doped frustrated Shastry-Sutherland system  $\text{TmB}_4$ , *Phys. Rev. B* **102**, 174422 (2020).
- [34] M. Borovský and M. Žukovič, Enhanced magnetocaloric effect due to selective dilution in a triangular Ising antiferromagnet, *Acta Phys. Pol. A* **131**, 645 (2017).