Stability, metallicity, and magnetism in niobium silicide nanofilms

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Modern superconducting qubits based on two-dimensional (2D) transmons typically involve the growth of Nb thin films on high-resistivity Si substrates. Since imperfections at the Nb-Si heterointerface have been implicated as a source of two-level systems that limit quantum coherence times, detailed characterization and understanding of niobium silicide interfacial layers are critical to improving superconducting qubit technology. While bulk binary intermetallic niobium silicide phases are well understood, the thermodynamic phase stability and properties of ultrathin niobium silicides, such as those found at the Nb-Si heterointerface in 2D transmons, have not yet been explored. Here, we report finite-sized effects for ultrathin niobium silicide films using density functional theory calculations and predict nanoscale stabilization of Nb₆Si₅ over the bulk α -Nb₅Si₃ phase. This result is consistent with our experimental observations of a niobium silicide interfacial layer between a sputtered Nb thin film and the underlying Si substrate. Furthermore, our calculations show that Nb₆Si₅ nanofilms are nonmagnetic, making them superior to nanofilms of α -Nb₅Si₃ that exhibit antiferromagnetic correlations detrimental to long coherence times in superconducting qubits. By providing atomic-scale insight into niobium silicide nanofilms, this paper can help guide ongoing efforts to optimize Nb-Si heterointerfaces for long coherence times in superconducting qubits.

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I. INTRODUCTION

Two-dimensional (2D) transmons, which are widely used in superconducting qubit technology, often involve the growth of niobium thin films on high-resistivity silicon substrates [1–3]. Previous reports pertaining to device performance of transmons have shown that interfacial composition and structure can affect the coherence time of superconducting qubits [4–7]. Since niobium and silicon are known to form bulk binary intermetallic niobium silicides that exhibit a range of stable compositions [5,8–12], it is likely that niobium silicide interfacial layers are present in 2D transmon architectures. Previous bulk niobium silicide structural studies have focused on understanding the phase stability and microstructure evolution from room temperature to 2600 °C [5,6,9–18], where the relevant high-temperature silicides are Nb₃Si and β -Nb₅Si₃ [18] and the low-temperature silicides are α -Nb₅Si₃, NbSi, and NbSi₂. In addition, the superconducting properties of three polymorphs of Nb₃Si and NbSi have been explored [17]. On the other hand, the thermodynamic phase stability of niobium silicides in the ultrathin regime, which are likely to be present at the Nb-Si heterointerface, has not yet been reported, despite their likely role in influencing coherence times of superconducting qubits [3,19,20]. Although previous x-ray diffraction (XRD) and reflectivity studies suggested that the interfacial Nb-Si composition changes from Nb₃Si to NbSi2 through coexistence of Nb3Si and Nb5Si3 with increasing temperature [13,14], this model is inconsistent with the nanometer-scale niobium silicides observed at the Nb-Si heterointerface in 2D transmons. Consequently, a thorough atomic-scale investigation of niobium silicide nanofilms is desirable to understand and mitigate potential sources of two-level systems that compromise coherence times in superconducting qubits.

Here, we investigate finite-sized effects on the stability and properties of niobium silicide nanofilms using a combination of first-principles calculations, x-ray reflectivity (XRR), and

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TABLE I. Structural information for select niobium silicide phases. Here, $g_{\rm F}^{\rm Nord}$	' represents the density of states per Nb-d orbital at the
Fermi level. Units of electron density are $e^{A^{-3}}$. Information for the Nb ₂ Si, γ -Nb ₅ Si ₃	, and Nb ₅ Si ₄ surface structures are not shown because of
their high surface energies. — indicates not applicable.	

Composition	Space group	Metallic	$g_{\mathrm{F}}^{\mathrm{Nb}-d}$	Electron density	Zintl phase	Zintl anion(s)	Surface plane	Surface termination
Nb ₃ Si	$P4_2/n$	Yes	0.69	2.001	No		(001)	Nb + Si
Nb ₂ Si	I4/mcm	Yes	0.51	1.951	Yes	Si_2^{4-}	(111)	
α -Nb ₅ Si ₃	I4/mcm	Yes	0.41	1.907	Yes	Si ⁶ ₂ , Si ⁴	(001)	Si
β -Nb ₅ Si ₃	I4/mcm	Yes	0.41	1.919	Yes	Si_{2}^{4-}, Si^{4-}	(001)	Nb + Si
γ -Nb ₅ Si ₃	$P6_3/mcm$	Yes	0.70	1.890	Yes	Si_2^{4-}	(001)	_
Nb_3Si_2	P4/mbm	Yes	0.95	1.892	Yes	Si_{2}^{6-}	(001)	Nb + Si
Nb ₅ Si ₄	$P4_{1}2_{1}2$	Yes	0.65	1.827	Yes	Si_2^{6-}	(001)	_
Nb ₆ Si ₅	Ibam	Yes	0.67	1.816	Yes	Si ^{4–} , Si ^{4–} , Si ^{4–}	(100)	Nb + Si
NbSi	Pnma	Yes	0.80	1.785	Yes	Si ^{4–}	(100)	Nb + Si
NbSi ₂	<i>P</i> 6 ₂ 22	Yes	0.68	1.575	No		(001)	Nb + Si

transmission electron microscopy (TEM). Our density functional theory (DFT) calculations show that a transition in the stable silicide from α -Nb₅Si₃ to Nb₆Si₅ occurs as the film thickness decreases due to vibrational entropy contributions, along with a decrease in carrier density for both phases. These thickness-dependent predictions of the silicide composition are consistent with XRR and TEM measurements on niobium silicides found in interfacial layers between a sputtered Nb thin film and the underlying silicon substrate. Furthermore, our calculations indicate that niobium silicide nanofilms are nonmagnetic in contrast to bulk α -Nb₅Si₃, which exhibits itinerant antiferromagnetism at its surface that provides dissipation channels beyond localized paramagnetic defects. Overall, in this paper, we provide atomic-scale insight into ultrathin niobium silicides that is likely to inform processing methods aimed at maximizing coherence time in superconducting qubits.

II. METHODS

A. First-principles calculations

Our total energy calculations were based on DFT within the generalized gradient approximation utilizing the strongly constrained and appropriately normed (SCAN) functional [21,22] implemented in the Vienna *ab initio* Simulation Package (VASP) [23,24]. We used a 400 eV plane-wave cutoff energy for all calculations and the projector augmented wave method [25,26] with Nb 5s, 4p, and 4d electrons, and Si 3s and 3p electrons treated as valence states, except for the phonon calculations where we used a 500 eV cutoff energy. We verified that the slab calculations with energy cutoff of 500 eV lead to total energy differences <1 meV/atom compared with those with an energy cutoff of 400 eV. The k-point meshes for Nb₃Si, Nb₂Si, α -Nb₅Si₃, β -Nb₅Si₃, γ -Nb₅Si₃, Nb₃Si₂, Nb₅Si₄, Nb₆Si₅, NbSi, and NbSi₂ are set to $3 \times 3 \times 6$, $6 \times 6 \times 6$, $6 \times 6 \times 3$, $3 \times 3 \times 6$, $4 \times 4 \times 6$, $4 \times 4 \times 6$, $4 \times 4 \times 2$, $5 \times 3 \times 2$, $10 \times 10 \times 6$, and $8 \times 8 \times 6$, respectively, for their conventional unit cell. The k-point meshes for nanofilms of Nb₃Si, α -Nb₅Si₃, β -Nb₅Si₃, γ -Nb₅Si₃, Nb₃Si₂, Nb₅Si₄, Nb₆Si₅, NbSi, and NbSi₂ are set to $4 \times 4 \times 1$, $6 \times 6 \times 1$, $4 \times 4 \times 1$, $6 \times 6 \times 1$, $6 \times 6 \times 1$, $4 \times 4 \times 1$, $5 \times 2 \times 1$, $7 \times 6 \times 1$, and $6 \times 6 \times 1$, respectively, as indicated in Table I. In the slab calculations, the number of k points along each direction satisfies $k_i \cdot a_i > 40$, where k_i and a_i are the number of k points and lattice parameters along direction i = x, y, z, respectively. Then the total energy differences are < 1 meV/atom upon further increasing the density of the k-point meshes. Gaussian smearing (0.10 eV width) for the Brillouin zone integrations is used for the metals. In the surface calculations, both the internal atomic positions and the in-plane lattice parameters are fully relaxed along with the out-of-plane lattice parameter, which includes the addition of 15 Å of vacuum.

When investigating the magnetic spin orders in the nanofilm of α -Nb₅Si₃, the DFT plus Hubbard *U* method [27] is used with the Hubbard *U* and the exchange parameter *J* set to 3 and 1 eV, respectively. The same *U* and *J* values are also applied to bulk α -Nb₅Si₃ and body-centered cubic Nb for computing the formation energy with the magnetic orders in the surface, where the magnetic moment on Nb is set to zero.

B. Formation energy calculations

The formation energy $(E_{x/y})$ of these Nb_xSi_y bulk phases and surface structures are calculated by the following formula:

$$E_{x/y} = \frac{E_{\mathrm{Nb}_x\mathrm{Si}_y} - xE_{\mathrm{Nb}} - yE_{\mathrm{Si}}}{x+y},\tag{1}$$

where $E_{Nb_xSi_y}$ is the total energy of various Nb_xSi_y at the ground state, and E_{Nb} and E_{Si} are the monoatomic energy of the Nb atom and Si atom in their bulk phases, respectively.

By considering the temperature effects on the formation energy, we added the temperature-dependent part of the electronic free energy (E_{el}) and the phononic free energy (E_{ph}) as in Ref. [28]. The electronic free energy is written as

$$E_{\rm el}(V,T) = H_{\rm el}(V,T) - TS_{\rm el}(V,T),$$
(2)

where the electronic density of states (DOS; g_e) and Fermi-Dirac distribution function (f) are used to compute the electronic enthalpy and entropy, which can be expressed as

$$H_{\rm el}(V,T) = \int_{-\infty}^{+\infty} g_e(\varepsilon) \cdot f(\varepsilon) \cdot \varepsilon d\varepsilon - \int_{-\infty}^{\varepsilon_{\rm F}} g_e(\varepsilon) \cdot \varepsilon d\varepsilon, \quad (3)$$

and

$$S_{\rm el}(V,T) = -k_{\rm B} \int_{-\infty}^{+\infty} g_e(\varepsilon) \cdot \{f(\varepsilon) \ln [f(\varepsilon)] + [1 - f(\varepsilon)] \ln [1 - f(\varepsilon)] \} d\varepsilon.$$
(4)

The phononic free energy is written as

$$E_{\rm ph}(V,T) = \frac{1}{N_q} \sum_{q,\sigma} \frac{\hbar \omega_{q,\sigma}}{2} + k_{\rm B}T \cdot \log\left[1 - \exp\left(-\frac{\hbar \omega_{q,\sigma}}{k_{\rm B}T}\right)\right]$$
(5)

where q and σ represent the reciprocal coordinate and phonon branch, respectively, and ω is the vibrational frequency.

Here, the harmonic phonons and electronic DOS at the equilibrium volume V are used to efficiently calculate the free energies, which are especially suitable for a moderate temperature range < 1000 K since the effects of thermal expansion in the free energies are usually small [29,30] and expected to be even less important in some relative free energies (e.g., formation free energy considered here).

The formation free energy at finite temperature includes the electronic free energy and phononic free energy as

$$E_{x/y}^{T} = E_{x/y}^{\text{DFT}} + \frac{E_{\text{el}}^{\text{Nb}_{x}\text{Si}_{y}} + E_{\text{ph}}^{\text{Nb}_{x}\text{Si}_{y}} - x(E_{\text{el}}^{\text{Nb}} + E_{\text{ph}}^{\text{Nb}}) - y(E_{\text{el}}^{\text{Si}} + E_{\text{ph}}^{\text{Si}})}{x + y}.$$
(6)

C. Niobium thin film preparation

Si (111) wafers, 76.2 mm diameter (WaferPro, Santa Clara, CA), were prepared with the standardized RCA cleaning procedure and then hydrogen passivated using a wet chemical treatment established for Si(111) [31]. Following passivation, wafers were immediately placed in a transport vessel and sealed in an Ar environment. Wafers were shipped to the **Ouantum Processing Group at National Institute of Standards** and Technology for Nb deposition within 24 h of hydrogen passivation. During transfer from the shipping container to the load lock, the sample was briefly exposed to atmosphere. The sample was loaded into a sputtering tool having a base pressure $< 1 \times 10^{-8}$ Torr equipped with reflection high-energy electron diffraction (RHEED) for surface analysis. RHEED patterns taken of the H: Si(111) indicated a crystalline, unreconstructed surface. A 40-nm-thick Nb film was deposited using DC magnetron sputtering at a pressure of 3 mTorr with 15 sccm Ar flow from a 3-inch-diameter Nb target having a metals basis purity of 99.95%. A 300 W sputtering power was used, resulting in a deposition rate of 1.3 A/s, which was monitored using a quartz crystal microbalance. The film was deposited at room temperature. After Nb deposition, RHEED patterns were observed to be consistent with a textured Nb(110) surface.

D. TEM

Cross-sectional TEM samples of Nb thin films were performed using conventional focused ion beam lift-out on a Ga⁺-based Helios Nanolab operating at 30 kV. A spherical



FIG. 1. The Zintl phases for 10 select niobium silicides with Nb and Si indicated by pink and green spheres, respectively. The Nb_n polyhedra around the Zintl anions in each phase are indicated except for in the Nb₆Si₅ phase. The Nb polyhedra around polyanionic groups Si₂⁴⁻ and Si'₂⁴⁻ can be found in the other phases, such as the Nb polyhedron in Nb₂Si about Si₂⁴⁻ and the Nb polyhedron in γ -Nb₅Si₃ about Si'₂⁴⁻.

aberration corrected JEOL ARM200CF microscope operating at 200 kV was utilized to acquire high-resolution scanning TEM (STEM) images perpendicular to the Nb [110] zone axis. Images were collected with a JEOL annular darkfield (90–370 mrad) detector under an 8 μ s dwell time and low-pass filtered using ImageJ. Stoichiometric STEM-energydispersive x-ray spectroscopy (EDS) was conducted with dual Oxford silicon drift detectors.

E. XRR

XRR measurements were performed with a Smartlab SE diffractometer equipped with a 9 kW Cu rotating anode operated at 45 kV and 160 mA. A Ge (220) twobounce monochromator was utilized to have a monochromatic beam ($\lambda = 1.5406$ Å). The collimated beam was 0.1×5 mm². XRR measurements are plotted in terms of the scattering vector $Q = 4\pi \sin(\theta)/\lambda$, normalized to the measured incident beam intensity, and corrected for geometrical footprint and background signal. The XRR analysis was performed using MOTOFIT software [32]. The XRR fitting is obtained from electron density profiles that simulate the Si/Nb_xSi_y/Nb/NbO/Nb₂O₅ heterostructure. The stochiometric determination of Nb_xSi_y was obtained from fitting the electron density of this layer.

III. RESULTS AND DISCUSSION

A. Bulk niobium silicide phase stability

At room temperature, the most stable structure for bulk niobium silicide is α -Nb₅Si₃, exhibiting tetragonal *I4/mcm* symmetry, where it adopts the Cr₅B₃ prototype structure with 4 f.u. in a conventional cell [9,11,18]. The Nb cations form Nb₁₀ and Nb₁₂ polyhedra, which coordinate anionic Si monomers and Si-Si dimers of length d = 2.4 Å (Fig. 1). Here, α -Nb₅Si₃ may be described as a valence-precise com-



FIG. 2. (a) Projected density of states (PDOS) for α -Nb₅Si₃ and its (b) projected crystal orbital Hamilton population (pCOHP) with positive, negative, and zero values indicating bonding, antibonding, and nonbonding interactions for the specified atom pair. (c) The density functional theory (DFT) strongly constrained and appropriately normed (SCAN) 0 K Nb-Si convex hull for 10 niobium silicide phases is formed by α -Nb₅Si₃ and NbSi₂. (d) Formation free energy as a function of temperature with respect to bulk Nb and Si following Eq. (6) in the Methods. The small changes ~0 K in (d) are due to the electronic entropic contributions in Eq. (6), which are usually neglected but included here.

pound as $(Nb^{3+})_5(Si^{4-})(Si^{6-})(5e^-)$ using Zintl bonding principles [21,22], which implies that Nb has a nominal $4d^2$ electronic configuration (the +2 oxidation state for Nb is eliminated because this would make α -Nb₅Si₃ a diamagnetic semiconductor, whereas it exhibits metallic conductivity [11,33]). Although Nb 4*d*-Si 3*p* orbital hybridization restricts full electron transfer, both anions are diamagnetic with closed-shell configurations. Thus, we expect the remaining five delocalized electrons to occupy the Nb 4*d* orbitals participating in Nb-Nb and Nb-Si bonding. Overall, these features make bulk α -Nb₅Si₃ a metallic paramagnet.

Our calculated electronic DOS shows that the Fermi level is indeed located in a region with many states consisting of multiple fractionally occupied Nb 4d orbitals [Fig. 2(a)]. There are ~ 0.41 states per Nb d orbital, leading to an itinerant electron gas in the open 4d shell of Nb. We find Si 3s states with σ_g bonding and σ_u^* antibonding characters located between -12 and -8 eV, as confirmed from our projected crystal orbital Hamilton population (pCOHP) analysis [34–36] [Fig. 2(a)], indicating the presence of Zintl Si_2^{6-} dimers. Modest hybridization exists between the Nb and Si orbitals throughout the entire energy range, with the Nb 4dstates spanning -6 to 3 eV. Metallic Nb-Nb bonding mainly occurs over the energy range from -3 to 2.5 eV and leads to the formation of the pseudogap in the DOS, which separates the filled bonding states from the empty antibonding states. The Fermi energy is located in a region just above the pseudogap, which can lead to compositional disorder or the formation of a glass state in intermetallic phases [37]. The electron filling for stoichiometric α -Nb₅Si₃ is such that the Fermi level is just above this minimum energy, suggesting that reducing the number of valence electrons could shift the Fermi level to lower energy through defect formation or deviations from pristine stoichiometry.

With increasing temperature, niobium silicides with different compositions form. We computed the Nb-Si convex hull by selecting low-energy niobium silicide compositions with their prototype structures specified in parentheses based on previous studies [9,11]: Nb₃Si (PTi₃), Nb₂Si (Au₂Cu), α -Nb₅Si₃ (Cr₅B₃), β -Nb₅Si₃ (W₅Si₃), γ -Nb₅Si₃ (Mn₅Si₃), Nb₃Si₂ (U₃Si₂), Nb₅Si₄ (Zr₅Si₄), Nb₆Si₅ (Ti₆Ge₅), NbSi (FeB), and NbSi₂ (CrSi₂). The Nb₂Si (Si₂^{4–}), Nb₅Si₃- β (Si₂^{4–}) and Si^{4-}), $Nb_5Si_3-\gamma$ (Si_2^{4-}), Nb_3Si_2 (Si_2^{6-}), Nb_5Si_4 (Si_2^{6-}), Nb_6Si_5 (Si_4^{4-} , Si_2^{4-} , and Si'_2^{4-}), and NbSi (Si_2^{4-}) compositions can also be regarded as Zintl phases [38], where the Zintl anions are specified in Table I. One calculation [9] found that Nb₂Si is closer to the hull than NbSi, whereas another calculation [11] reported that NbSi is closer to the hull than Nb₂Si. Our 0 K convex hull obtained from DFT using the SCAN functional reproduces the previously reported convex hull and reconciles this controversy. Our results show that both phases are close to the hull. In addition, our calculations using the SCAN functional further confirmed that the NbSi₂ has P6222 symmetry, in contrast to the previously reported Fddd structure [12]. These findings indicate that DFT-SCAN is a suitable level of theory to describe niobium silicides and thus was chosen to compute thickness effects in niobium silicide nanofilms.

Figure 2(b) shows that the convex hull is determined by α -Nb₅Si₃ and NbSi₂, which is consistent with the experimental phase diagram [18] since they are the low-temperature stable silicides. Nb₃Si is also very close to the convex hull (~11.4 meV/atom from the hull) because it is experimentally stable over the 1765–1915 °C range [18]. For the other compositions above the hull, we find that β -Nb₅Si₃ and Nb₃Si₂ have formation energies of \sim 37 meV/atom higher than α -Nb₅Si₃. We then calculated the thermal stability of the low-temperature phases (i.e., α -Nb₅Si₃ and NbSi₂) by including the temperature-dependent part of the electronic free energy and the vibrational free energy (see the Methods and Fig. S1 in the Supplemental Material [39]). We excluded β -Nb₅Si₃- β [9,18] from this calculation and instead focused on Nb₃Si₂ and Nb₆Si₅ because, as we show below, Nb₆Si₅ is stabilized by finite-sized effects. Here, we find that Nb₃Si₂ becomes stable at intermediate temperatures, ranging from \sim 500 to 1500 K between the previously reported α -Nb₅Si₃ and NbSi₂ phases forming the convex hull at 0 K.

B. Niobium silicide nanofilm phase stability

Next, we investigate the phase stability for the niobium silicides in unsupported nanofilm geometries including surface and finite thickness effects. We allow for relaxation normal to the film, no surface reconstruction, and no adsorption. Favorable surface orientations and compositions for the different silicide phases are created by conducting an atomic population analysis (i.e., density-derived electrostatic and chemical (DDEC) analysis [40,41]). The overlap population (OP) is expressed as

$$A_{i,j}|_{i\neq j} = 2 \int \frac{\rho_i(\mathbf{r}_i)\rho_j(\mathbf{r}_j)}{\rho(\mathbf{r})} d^3 \mathbf{r},$$
(7)



FIG. 3. Slab structures for the specified niobium silicide compositions with nominal thickness of 1.5–2.4 nm.

where $A_{i,j}$ is the OP, and r_i and r_j are the positions for atoms *i* and *j*, respectively. Using Eq. (1), we define the $[h \ k \ l]$ directional-dependent OP as

$$OP_{hkl} = \sum_{i}^{N} \frac{1}{2} A_{i,j}|_{i \neq j} \left| \frac{(\mathbf{r_j} - \mathbf{r_i}) \cdot \mathbf{R}}{|\mathbf{r_j} - \mathbf{r_i}||\mathbf{R}|} \right|,$$
(8)

where we consider the summation of the OP among the nearest-neighboring atoms j for all the atoms i in the unit cell along a specified direction **R** with Miller indices h, k, and l. If OP_{*hkl*} is small along a direction, we consider that the energetic cost to break the bonds along this direction is also small. Small OP_{*hkl*}, therefore, would correspond to plane normal directions for likely cleavage planes to generate finite-sized 2D silicide nanofilms.

With this method, we find that the OP_{*hkl*} value is the smallest along the [001] direction in α -Nb₅Si₃, which is consistent with a previous detailed first-principles study on the surface of α -Nb₅Si₃ [8,42]. The surface directions for the other compositions are [001] for Nb₃Si, [111] for Nb₂Si, [001] for β -Nb₅Si₃, [001] for γ -Nb₅Si₃, [001] for Nb₅Si₄, [100] for Nb₆Si₅, [100] for NbSi, and [001] for NbSi₂ (Tables S2–S11 in the Supplemental Material [39]). We then determined the two surface terminations for each slab structure along these directions using a layer-resolved OP_{*hkl*}, where the surface termination is selected base on the layer giving the smallest OP_{*hkl*} value (Tables S12–S17 in the Supplemental Material [39]). Throughout, we use symmetric slab geometries with identical surface terminations (Fig. 3).

Using these slab structures, we then compute the surface energies according to the expression [8]:

$$\gamma = \frac{1}{2A} \left[E_{\text{slab}} - \frac{1}{n_s} N_{\text{Si}} \mu_{\text{Nb}_{n_s} \text{Si}_{n_s}}^{\text{bulk}} - \left(N_{\text{Nb}} - \frac{n_n}{n_s} N_{\text{Si}} \right) \mu_{\text{Nb}} \right], \quad (9)$$

where γ is the surface energy, E_{slab} is the 0 K total energy of the slab structure, A is the surface area, and n_n and n_s are the number of Nb and Si atoms in the specified niobium silicide phases, respectively. Here, N_{Nb} and N_{Si} are the total number of Nb and Si atoms in the surface layer



FIG. 4. (a) Surface energy as a function of the chemical potential of Nb without finite temperature effects included for the various silicides. (b) The formation energy vs the inverse of the thickness, h^{-1} , which is obtained by performing density functional theory (DFT) at 0 K. The filled circle at $h^{-1} = 0$ for each composition corresponds to its bulk formation energy. Inset in (b): Enlargement of thickness-dependent crossover between -0.33 and -0.27 eV/atom with inverse thickness ranging from 0.08 to 0.12 Å^{-1} , where the transition is from α -Nb₅Si₃ to Nb₆Si₅ at $\sim 0.1 \text{ Å}^{-1}$ as indicated by the dashed vertical line.

(SL), respectively, which can be further expressed as $N_{\text{Nb}} = n_{\text{Nb}}^{\text{BL}} + n_{\text{Nb}}^{\text{SL}}$ and $N_{\text{Si}} = n_{\text{Si}}^{\text{BL}} + n_{\text{Si}}^{\text{SL}}$, where n_i^{BL} and n_i^{SL} (i = Nb, Si) are the number of atoms in the bulk layers (BLs) and SLs, respectively. Here, μ represents the chemical potential and $n_n \mu_{\text{Nb}} + n_s \mu_{\text{Si}} = \mu_{\text{Nb}n_s \text{Si}n_s}^{\text{bulk}}$ for a niobium silicide. Furthermore, to form a niobium silicide, the requirements of $\mu_{\text{Nb}} \leq \mu_{\text{Nb}}^{\text{bulk}}$ and $\mu_{\text{Si}} \leq \mu_{\text{Si}}^{\text{bulk}}$ must be fulfilled, which leads to $\frac{1}{n_n}(\mu_{\text{Nb}n_n \text{Si}n_s}^{\text{Lm}} - n_s \mu_{\text{Si}}^{\text{bulk}}) \leq \mu_{\text{Nb}} \leq \mu_{\text{Nb}}^{\text{bulk}}$. Figure 4(a) shows the calculated surface energies for the

seven different niobium silicides. The α -Nb₅Si₃ surface energy as a function of Nb chemical potential is in good agreement with the previous first-principles results [8]. Interestingly, we find that the surface energies of β -Nb₅Si₃, NbSi, and Nb₆Si₅ are lower than that of α -Nb₅Si₃. From the surface energies, we further investigate the thickness dependence of the nanofilm phase stabilities. First, we obtain the surface formation energy at a different thickness (h), approximately estimated by the distance between the top and bottom surfaces, by changing n_{Nb}^{BL} and n_{Si}^{BL} through the addition of additional BLs. Then the formation energy for the nanofilms of different thicknesses h is obtained by using this quantity in a modified expression for the bulk formation energy [Eq. (3)]. Here, we assume the surface energy is independent of film thickness in the nanofilms, which is reasonable [28] and consistent with our assessments. Figure 4(b) shows the formation energies for the nanofilms with varying thickness. We find the interpolated formation energies for the bulk compositions agree well with our DFT calculations, which further confirms



FIG. 5. (a) The entropic electronic and phononic contributions to the nanoscale silicide formation energy as a function of the temperature for nanofilms of α -Nb₅Si₃ (2.37 nm), β -Nb₅Si₃ (1.52 nm), Nb₃Si₂ (1.75 nm), and Nb₆Si₅ (1.56 nm). (b) Formation energy vs inverse of the thickness in the Nb-rich region including entropic effects at 700 K shows a transition. Here, we predict the formation energy from 0 to 700 K with a uniform shift for the thickness range considered, where the uniform values are the entropic electronic and phononic contributions at 700 K at 1.56 and 2.37 nm for Nb₆Si₅ and α -Nb₅Si₃, respectively. The formation energy at 700 K for β -Nb₅Si₃ is also shown to indicate finite-temperature effects do not stabilize it over Nb₆Si₅ nanofilms.

the reliability of the approximation. In addition, we find that the dependencies do not change irrespective of the surface energy and the Nb chemical potential in Eq (3). At large thickness, we find α -Nb₅Si₃ is stable, consistent with the bulk phase diagram reporting high stability of this phase.

In contrast, the Nb₆Si₅ phase is stable for nanofilms. Therefore, we predict a thickness-dependent phase transition occurs at ~1 nm mainly driven by the lower surface energy of Nb₆Si₅. The stability of the Nb₆Si₅ nanofilm with decreasing thickness has not been previously reported but can be justified because of its significantly lower surface energy than α -Nb₅Si₃. In addition, we find that the low surface energy of β -Nb₅Si₃ makes it competitive with α -Nb₅Si₃ and Nb₆Si₅ nanofilms as the film thickness decreases.

One way to synthesize nanoscale niobium silicides is via thin film deposition of several monolayers of Nb from a metallic source. The favorable silicide composition that forms depends on deposition method and temperature, assuming a constant niobium flux and unit sticking coefficient, which permits aggregation of adatoms to form a conformal layer, along with Si diffusion. To assess thermal stability, we calculated the formation free energies of nanofilms of α -Nb₅Si₃, β -Nb₅Si₃, Nb₃Si₂, and Nb₆Si₅, using the same method employed to evaluate bulk thermal stability (Methods and Fig. S2 in the Supplemental Material [39]). Figure 5(a) shows that the entropic contributions in nanofilm Nb₆Si₅ are greater than those of the other nanoscale silicides. The entropy increment with increasing temperature is largely due to vibrational contributions. We find Nb₆Si₅ has a lower Debye temperature of 435 vs 460 K for bulk α -Nb₅Si₃ obtained from our phonon calculations [11,43,44] (Table S18 in the Supplemental Material [39]). Figure 5(b) shows this effect leads to a critical thickness of 1.2 nm where the α -Nb₅Si₃-to-Nb₆Si₅ transition occurs, which decreases to a critical thickness of 1 nm when the vibrationalfree-energy contribution is omitted at finite temperature [Fig. 4(b)]. Although β -Nb₅Si₃ and Nb₃Si₂ are also favored compared with α -Nb₅Si₃ at high temperatures [Fig. 5(a)], we do not predict a thickness-dependent transition to occur between these phases. However, we have neglected the effects of the Si-silicide interface that may act to template and further favor the formation of one silicide phase over another.

Analysis of the DOS provides a postulate for why the surface energy of Nb₆Si₅ is lower than that of α -Nb₅Si₃. Since there is no adsorption or reconstruction, the change in surface energy is a result of the redistribution of delocalized electrons near the surface. This redistribution enhances the degree of metal-metal bonding character, influences the Fermi level position, and may partly compensate the energy penalty because the metal-metal interaction is crucial to stabilize an intermetallic compound [33,37,45–47]. As can be seen from Fig. 6(a), the DOS around the Fermi level at the α -Nb₅Si₃ (001) surface of the 2.4 nm nanofilm becomes higher than that of the bulk [see Fig. 2(a)], which indicates that the Nb-Nb d orbital interactions are weaker at the surface [33,37,45-47]. From our pCOHP analysis, we find that the Nb-Nb d orbital interactions are nonbonding for both the bulk and surface structures in α -Nb₅Si₃. A nonbonding state itself does not stabilize the surface structure, but the high DOS at the Fermi level in the intermetallic compounds may result in a magnetic instability [34,48–51], and the high DOS can be reduced by forming a magnetically ordered state that will help with compensating the energy penalty. Interestingly, Figs. 6(b) and 6(c) show that the DOS and pCOHP, respectively, present a completely different scenario for the Nb₆Si₅ (100) surface structure of a 1.5 nm film. Although there is also an increase in the number of states around the Fermi level, the Nb-Nb d orbital interactions in the SLs exhibit bonding character, which can directly help stabilize the surface structure and partly compensate for the change in coordination in Nb₆Si₅. This change in chemical bonding at the surface likely explains why the surface energy of Nb_6Si_5 is lower than that of α -Nb₅Si₃.

C. Magnetism in niobium silicides

As mentioned above, the high DOS at the Fermi level in the intermetallic compounds may result in magnetic instability. We now investigate possible magnetism at the surfaces of α -Nb₅Si₃ and Nb₆Si₅. To find the possible magnetic structures for the two compositions, we rely on a crystal orbital Hamilton population (COHP) analysis, which is usually adopted for analyzing the magnetic ground states of intermetallic compounds [34,48–51]. Figure 7 shows the electronic structures and pCOHPs for the surface structures of nanofilms of α -Nb₅Si₃ (~2.4 nm) and Nb₆Si₅ (~1.5 nm). We find the Fermi level located in a region of nonbonding states in the



FIG. 6. (a) Projected density of states (PDOS) and projected crystal orbital Hamilton population (pCOHP) for the α -Nb₅Si₃ (001) surface of the 2.4 nm nanofilm. PDOS and pCOHP for (b) bulk Nb₆Si₅ and (c) Nb₆Si₅ (100) surface of the 1.5 nm nanofilm.



FIG. 7. (a) Projected density of states (PDOS) and projected crystal orbital Hamilton population (pCOHP) for the α -Nb₅Si₃ (001) surface with zero magnetic moments at the density functional theory (DFT)+U = 3 eV level. Positive (negative) density of states (DOS) indicates the spin-up (spin-down) channel. The positive, zero, and negative values in the pCOHP indicate bonding, nonbonding, and antibonding interactions, respectively, for the spin-up channel in solid lines. The meaning is reversed for the spin-down channel indicated in broken lines. (b) PDOS and pCOHP for the α -Nb₅Si₃ (001) surface with an antiferromagnetic surface spin structure at the DFT+U = 3 eV level. (c) Spin density distributions of the antiferromagnetic interactions on the α -Nb₅Si₃ surface. Yellow spin density indicates spin-up and blue indicates spin-down electrons. The resolution for the isosurface plot is 0.0028 eV Å⁻³. The black arrows indicate the alignment of the spins without considering spin-orbital effects. (d) The band structure for α -Nb₅Si₃ with (left) nonmagnetic, (center) magnetic with no magnetic moments, and (right) antiferromagnetic surface spin configurations.

electronic structure of the nonmagnetic surface of α -Nb₅Si₃. In contrast, the Fermi level is in the bonding states for the nonmagnetic configuration of the Nb₆Si₅ surface. Thus, given many states at the Fermi level and the position relative to the bonding and nonbonding states [Figs. 6(a) and 6(c)], we expect the nanoscale silicides to be susceptible to different magnetic states. Here, α -Nb₅Si₃ should favor an antiferromagnetic spin configuration, and Nb₆Si₅ should be nonmagnetic (or weakly paramagnetic) according to previous electronic structure studies on the magnetic transition metals and intermetallic binary compounds [34,48–51]. Therefore, we focus on understanding the magnetic state of α -Nb₅Si₃.

The reduced coordination from broken bonds at the surface may enhance the effective electron-electron interactions in the silicides. Therefore, we performed DFT+U calculations, which showed sizable magnetic moments confined to the surface niobium atoms for $U \ge 3 \,\mathrm{eV}$ despite the strong metallicity. This high U value is reasonable compared with the 4 eV adopted in previous studies of niobium oxides [52]. The final magnetic configurations were determined by random spin generation and symmetry-constrained spin generation (see Fig. S6 in the Supplemental Material [39]). We find an antiferromagnetic spin order for α -Nb₅Si₃ [Fig. 7(c)], which collapses to a nonmagnetic solution for $U \leq 2.5 \text{ eV}$, because the metallicity competes with local moment formation on the surface Nb atoms. To understand the origin of the itinerant antiferromagnetic state at the surface, we further calculate the pCOHPs for two scenarios: (i) no magnetic moments and $U = 3 \,\mathrm{eV}$ and (ii) with magnetic moments at $U = 3 \,\mathrm{eV}$. Figures 7(a) and 7(b) show that the local Coulomb interaction from the +U reduces the DOS at the Fermi level in α -Nb₅Si₃. In α -Nb₅Si₃, we find increased interaction strength U does not induce a Stoner ferromagnetic instability because the nonbonding states at the Fermi level favor an antiferromagnetic spin order. Spin polarization of the electronic structure would not lead to energy stabilization if the frontier orbitals are nonbonding in character. This finding is consistent with previous COHP analysis on the intermetallic compounds, leading to a further decease of the DOS at the Fermi level [34,48–51]. Although the magnetic surface structure of α -Nb₅Si₃ and the role of the onsite repulsion U require future experimental validation, our analysis shows that the formation of a 2D spin-density wave reduces the size of the Fermi surface and further stabilizes the surface structure [Fig. 7(d)]. Here, we find that the formation energy of α -Nb₅Si₃ can be lowered by 13 meV/atom at 2.4 nm compared with the nonmagnetic state. Furthermore, the calculated magnetic moment on the surface niobium atoms is ${\sim}0.24~\mu_{\rm B}/{\rm Nb},$ which could be further decreased in the experiment at finite temperature because of the effects of the spin fluctuations that are not included in our model [53,54].

While magnetism can be one source of qubit decoherence, metallicity can also contribute to decoherence [3,4]. Therefore, we investigate the thickness-dependent metallicity by examining the DOS at the Fermi level (g_F). The values range from 0.4 to 0.8 states per surface atom per electronvolt, which is comparable with 0.2–0.3 states per atom per electronvolt of the prototypical metals Al and Au [55,56], but <2.7 states per atom per electronvolt of 2D MoSi₂ nanofilms [28]. As can be seen from Fig. 8, g_F decreases with decreasing nanofilm



FIG. 8. Number of states at the Fermi level as a function of the inverse of the thickness in α -Nb₅Si₃ (red) and Nb₆Si₅ (yellow). Here, the states are counted only from Nb in the structure we computed at each thickness for an accurate prediction of the changes of metallicity because almost all the density of states (DOS) at the Fermi level is from Nb.

thickness for both α -Nb₅Si₃ and Nb₆Si₅, suggesting that the nanofilms are more resistive than their bulk counterparts.

D. Experimental characterization of niobium silicide nanofilms

To experimentally evaluate our computational findings, we prepared 40 nm Nb thin films on Si (111) substrates using DC sputtering and characterized the Nb/Si interface with TEM



FIG. 9. (a) High- and (b) low-magnification annular dark-field scanning transmission electron microscopy (STEM) images of the amorphous Nb/Si interface (outlined in gray) present in DC sputter deposited Nb thin films on Si(111). Energy-dispersive x-ray spectroscopy (EDS) of Nb (green) and Si (blue) revealed a Nb-rich composition at the interface with 54 ± 1 at.% Nb and 46 ± 1 at.% Si.



FIG. 10. (a) X-ray reflectivity (XRR) of the 40 nm Nb thin film on Si (111). The fitting resulted in 1.2 nm Nb_xSi_y, 38.5 nm Nb, 1.3 nm NbO, and 2.4 nm Nb₂O₅ from bottom to top of the film. (b) Electron density slab profile for the multiple interfaces in the film. The electron density of the Nb_xSi_y layer is $1.866e^{-}$ Å⁻³.

and XRR. Annular dark-field STEM images reveal an amorphous interfacial layer between the crystalline Si substrate and the crystalline Nb thin film with an approximate thickness of 1.5 nm, as shown in Fig. 9. Analysis of the interfacial layer by EDS indicates an elemental composition of 54 ± 1 at.% Nb and 46 \pm 1 at.% Si. This composition is consistent with the Nb₆Si₅ stoichiometry. Analysis of the film by XRR reveals a layer stack consisting of 2.4 nm Nb₂O₅, 1.3 nm NbO, 38.5 nm Nb, and 1.2 nm Nb_xSi_y, on bulk Si, from top to bottom (Fig. 10). The thickness of the Nb/Si interfacial layer as measured by XRR is in good agreement with the value determined by TEM. The XRR measured electron density of the Nb_xSi_y layer is $1.866e^{-}$ Å⁻³, which agrees to within 3% of the predicted value for Nb₆Si₅ (1.816 e^{-} Å⁻³). In comparison, Nb₃Si would have a 7% higher and NbSi₂ a 20% lower predicted electron density than measured.

IV. CONCLUSIONS

By performing first-principles calculations, we predict two stable compositions with decreasing thickness in the nanofilm: α -Nb₅Si₃ at larger thickness and Nb₆Si₅ at lower thickness. The critical thickness for the transition between stable nanofilm compositions is ~1 and 1.2 nm at 0 and 700 K, respectively. The stable Nb₆Si₅ phase is also consistent with experimental XRR and TEM measurements, whose thickness is ~1.2 nm. Therefore, we suggest that Nb-Si heterointerfaces in 2D transmon structures obtained by sputter-depositing Nb films on silicon substrates may not be atomically sharp, which has likely implications for achieving long qubit-coherence times. Furthermore, we also predict that α -Nb₅Si₃ nanofilms may be antiferromagnetic, whereas Nb₆Si₅ nanofilms are nonmagnetic based on bond-character analysis.

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