# **Stability, metallicity, and magnetism in niobium silicide nanofilms**

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Modern superconducting qubits based on two-dimensional (2D) transmons typically involve the growth of Nb thin films on high-resistivity Si substrates. Since imperfections at the Nb-Si heterointerface have been implicated as a source of two-level systems that limit quantum coherence times, detailed characterization and understanding of niobium silicide interfacial layers are critical to improving superconducting qubit technology. While bulk binary intermetallic niobium silicide phases are well understood, the thermodynamic phase stability and properties of ultrathin niobium silicides, such as those found at the Nb-Si heterointerface in 2D transmons, have not yet been explored. Here, we report finite-sized effects for ultrathin niobium silicide films using density functional theory calculations and predict nanoscale stabilization of  $Nb<sub>6</sub>Si<sub>5</sub>$  over the bulk α-Nb<sub>5</sub>Si<sub>3</sub> phase. This result is consistent with our experimental observations of a niobium silicide interfacial layer between a sputtered Nb thin film and the underlying Si substrate. Furthermore, our calculations show that  $Nb_6Si_5$ nanofilms are nonmagnetic, making them superior to nanofilms of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> that exhibit antiferromagnetic correlations detrimental to long coherence times in superconducting qubits. By providing atomic-scale insight into niobium silicide nanofilms, this paper can help guide ongoing efforts to optimize Nb-Si heterointerfaces for long coherence times in superconducting qubits.

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### **I. INTRODUCTION**

Two-dimensional (2D) transmons, which are widely used in superconducting qubit technology, often involve the growth of niobium thin films on high-resistivity silicon substrates [\[1–3\]](#page-8-0). Previous reports pertaining to device performance of transmons have shown that interfacial composition and structure can affect the coherence time of superconducting qubits [\[4–7\]](#page-8-0). Since niobium and silicon are known to form bulk binary intermetallic niobium silicides that exhibit a range of stable compositions  $[5,8-12]$  $[5,8-12]$ , it is likely that niobium silicide interfacial layers are present in 2D transmon architectures. Previous bulk niobium silicide structural studies have focused on understanding the phase stability and microstructure evolu-tion from room temperature to 2600 °C [\[5,6,9–](#page-8-0)[18\]](#page-9-0), where the relevant high-temperature silicides are  $Nb<sub>3</sub>Si$  and  $\beta$ - $Nb<sub>5</sub>Si<sub>3</sub>$ [\[18\]](#page-9-0) and the low-temperature silicides are  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>, NbSi,

and NbSi<sub>2</sub>. In addition, the superconducting properties of three polymorphs of  $Nb<sub>3</sub>Si$  and NbSi have been explored [\[17\]](#page-9-0). On the other hand, the thermodynamic phase stability of niobium silicides in the ultrathin regime, which are likely to be present at the Nb-Si heterointerface, has not yet been reported, despite their likely role in influencing coherence times of superconducting qubits [\[3](#page-8-0)[,19,20\]](#page-9-0). Although previous x-ray diffraction (XRD) and reflectivity studies suggested that the interfacial Nb-Si composition changes from  $Nb<sub>3</sub>Si$ to Nb $Si<sub>2</sub>$  through coexistence of Nb<sub>3</sub>Si and Nb<sub>5</sub>Si<sub>3</sub> with increasing temperature [\[13,14\]](#page-9-0), this model is inconsistent with the nanometer-scale niobium silicides observed at the Nb-Si heterointerface in 2D transmons. Consequently, a thorough atomic-scale investigation of niobium silicide nanofilms is desirable to understand and mitigate potential sources of two-level systems that compromise coherence times in superconducting qubits.

Here, we investigate finite-sized effects on the stability and properties of niobium silicide nanofilms using a combination of first-principles calculations, x-ray reflectivity (XRR), and

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transmission electron microscopy (TEM). Our density functional theory (DFT) calculations show that a transition in the stable silicide from  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> to Nb<sub>6</sub>Si<sub>5</sub> occurs as the film thickness decreases due to vibrational entropy contributions, along with a decrease in carrier density for both phases. These thickness-dependent predictions of the silicide composition are consistent with XRR and TEM measurements on niobium silicides found in interfacial layers between a sputtered Nb thin film and the underlying silicon substrate. Furthermore, our calculations indicate that niobium silicide nanofilms are nonmagnetic in contrast to bulk  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>, which exhibits itinerant antiferromagnetism at its surface that provides dissipation channels beyond localized paramagnetic defects. Overall, in this paper, we provide atomic-scale insight into ultrathin niobium silicides that is likely to inform processing methods aimed at maximizing coherence time in superconducting qubits.

### **II. METHODS**

#### **A. First-principles calculations**

Our total energy calculations were based on DFT within the generalized gradient approximation utilizing the strongly constrained and appropriately normed (SCAN) functional [\[21,22\]](#page-9-0) implemented in the Vienna *ab initio* Simulation Package (VASP)  $[23,24]$ . We used a 400 eV plane-wave cutoff energy for all calculations and the projector augmented wave method [\[25,26\]](#page-9-0) with Nb 5*s*, 4*p*, and 4*d* electrons, and Si 3*s* and 3*p* electrons treated as valence states, except for the phonon calculations where we used a 500 eV cutoff energy. We verified that the slab calculations with energy cutoff of 500 eV lead to total energy differences  $\langle 1 \text{ meV/atom} \rangle$ compared with those with an energy cutoff of 400 eV. The *k*-point meshes for Nb<sub>3</sub>Si, Nb<sub>2</sub>Si, α-Nb<sub>5</sub>Si<sub>3</sub>, β-Nb<sub>5</sub>Si<sub>3</sub>,  $\gamma$ -Nb<sub>5</sub>Si<sub>3</sub>, Nb<sub>3</sub>Si<sub>2</sub>, Nb<sub>5</sub>Si<sub>4</sub>, Nb<sub>6</sub>Si<sub>5</sub>, NbSi, and NbSi<sub>2</sub> are set to  $3 \times 3 \times 6$ ,  $6 \times 6 \times 6$ ,  $6 \times 6 \times 3$ ,  $3 \times 3 \times 6$ ,  $4 \times 4 \times 6$ ,  $4 \times 4 \times 6$ ,  $4\times4\times2$ ,  $5\times3\times2$ ,  $10\times10\times6$ , and  $8\times8\times6$ , respectively, for their conventional unit cell. The *k*-point meshes for nanofilms of Nb<sub>3</sub>Si, α-Nb<sub>5</sub>Si<sub>3</sub>,  $\beta$ -Nb<sub>5</sub>Si<sub>3</sub>,  $\gamma$ -Nb<sub>5</sub>Si<sub>3</sub>, Nb<sub>3</sub>Si<sub>2</sub>, Nb<sub>5</sub>Si<sub>4</sub>,  $Nb_6Si_5$ , NbSi, and NbSi<sub>2</sub> are set to  $4 \times 4 \times 1$ ,  $6 \times 6 \times 1$ ,  $4 \times 4 \times 1$ , 6×6×1, 6×6×1, 4×4×1, 5×2×1, 7×6×1, and 6×6×1,

respectively, as indicated in Table I. In the slab calculations, the number of *k* points along each direction satisfies  $k_i \cdot a_i$ 40, where *ki* and *ai* are the number of *k* points and lattice parameters along direction  $i = x, y, z$ , respectively. Then the total energy differences are  $\langle 1 \text{ meV/atom upon further in-} \rangle$ creasing the density of the *k*-point meshes. Gaussian smearing (0.10 eV width) for the Brillouin zone integrations is used for the metals. In the surface calculations, both the internal atomic positions and the in-plane lattice parameters are fully relaxed along with the out-of-plane lattice parameter, which includes the addition of 15 Å of vacuum.

When investigating the magnetic spin orders in the nanofilm of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>, the DFT plus Hubbard *U* method [\[27\]](#page-9-0) is used with the Hubbard *U* and the exchange parameter *J* set to 3 and 1 eV, respectively. The same *U* and *J* values are also applied to bulk  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> and body-centered cubic Nb for computing the formation energy with the magnetic orders in the surface, where the magnetic moment on Nb is set to zero.

### **B. Formation energy calculations**

The formation energy  $(E_{x/y})$  of these  $Nb_xSi_y$  bulk phases and surface structures are calculated by the following formula:

$$
E_{x/y} = \frac{E_{\text{Nb}_x \text{Si}_y} - xE_{\text{Nb}} - yE_{\text{Si}}}{x + y},
$$
 (1)

where  $E_{Nb_xSi_y}$  is the total energy of various  $Nb_xSi_y$  at the ground state, and  $E_{Nb}$  and  $E_{Si}$  are the monoatomic energy of the Nb atom and Si atom in their bulk phases, respectively.

By considering the temperature effects on the formation energy, we added the temperature-dependent part of the electronic free energy  $(E_{el})$  and the phononic free energy  $(E_{ph})$  as in Ref. [\[28\]](#page-9-0). The electronic free energy is written as

$$
E_{\rm el}(V,T) = H_{\rm el}(V,T) - TS_{\rm el}(V,T),\tag{2}
$$

where the electronic density of states (DOS; *ge*) and Fermi-Dirac distribution function  $(f)$  are used to compute the electronic enthalpy and entropy, which can be expressed as

$$
H_{\rm el}(V,T) = \int_{-\infty}^{+\infty} g_e(\varepsilon) \cdot f(\varepsilon) \cdot \varepsilon d\varepsilon - \int_{-\infty}^{\varepsilon_{\rm F}} g_e(\varepsilon) \cdot \varepsilon d\varepsilon, \tag{3}
$$

<span id="page-2-0"></span>and

$$
S_{\rm el}(V,T) = -k_{\rm B} \int_{-\infty}^{+\infty} g_{\epsilon}(\varepsilon) \cdot \{f(\varepsilon) \ln [f(\varepsilon)] + [1 - f(\varepsilon)] \ln [1 - f(\varepsilon)]\} d\varepsilon.
$$
 (4)

The phononic free energy is written as

$$
E_{\text{ph}}(V, T) = \frac{1}{N_q} \sum_{q, \sigma} \frac{\hbar \omega_{q, \sigma}}{2} + k_{\text{B}} T \cdot \log \left[ 1 - \exp \left( - \frac{\hbar \omega_{q, \sigma}}{k_{\text{B}} T} \right) \right] \quad (5)
$$

where  $q$  and  $\sigma$  represent the reciprocal coordinate and phonon branch, respectively, and  $\omega$  is the vibrational frequency.

Here, the harmonic phonons and electronic DOS at the equilibrium volume *V* are used to efficiently calculate the free energies, which are especially suitable for a moderate temperature range  $< 1000 \text{ K}$  since the effects of thermal expansion in the free energies are usually small [\[29,30\]](#page-9-0) and expected to be even less important in some relative free energies (e.g., formation free energy considered here).

The formation free energy at finite temperature includes the electronic free energy and phononic free energy as

$$
E_{x/y}^T = E_{x/y}^{\text{DFT}} + \frac{E_{\text{el}}^{\text{Nb}_x \text{Si}_y} + E_{\text{ph}}^{\text{Nb}_x \text{Si}_y} - x(E_{\text{el}}^{\text{Nb}} + E_{\text{ph}}^{\text{Nb}}) - y(E_{\text{el}}^{\text{Si}} + E_{\text{ph}}^{\text{Si}})}{x + y}.
$$
\n(6)

### **C. Niobium thin film preparation**

Si (111) wafers, 76.2 mm diameter (WaferPro, Santa Clara, CA), were prepared with the standardized RCA cleaning procedure and then hydrogen passivated using a wet chemical treatment established for Si(111) [\[31\]](#page-9-0). Following passivation, wafers were immediately placed in a transport vessel and sealed in an Ar environment. Wafers were shipped to the Quantum Processing Group at National Institute of Standards and Technology for Nb deposition within 24 h of hydrogen passivation. During transfer from the shipping container to the load lock, the sample was briefly exposed to atmosphere. The sample was loaded into a sputtering tool having a base pressure  $< 1 \times 10^{-8}$  Torr equipped with reflection high-energy electron diffraction (RHEED) for surface analysis. RHEED patterns taken of the  $H : Si(111)$  indicated a crystalline, unreconstructed surface. A 40-nm-thick Nb film was deposited using DC magnetron sputtering at a pressure of 3 mTorr with 15 sccm Ar flow from a 3-inch-diameter Nb target having a metals basis purity of 99.95%. A 300 W sputtering power was used, resulting in a deposition rate of 1.3 A/s, which was monitored using a quartz crystal microbalance. The film was deposited at room temperature. After Nb deposition, RHEED patterns were observed to be consistent with a textured Nb(110) surface.

#### **D. TEM**

Cross-sectional TEM samples of Nb thin films were performed using conventional focused ion beam lift-out on a  $Ga<sup>+</sup>$ -based Helios Nanolab operating at 30 kV. A spherical



FIG. 1. The Zintl phases for 10 select niobium silicides with Nb and Si indicated by pink and green spheres, respectively. The Nb*<sup>n</sup>* polyhedra around the Zintl anions in each phase are indicated except for in the  $Nb<sub>6</sub>Si<sub>5</sub>$  phase. The Nb polyhedra around polyanionic groups  $Si_2^{4-}$  and  $Si_2^{4-}$  can be found in the other phases, such as the Nb polyhedron in Nb<sub>2</sub>Si about Si<sup>4</sup><sup>-</sup> and the Nb polyhedron in  $\gamma$ -Nb<sub>5</sub>Si<sub>3</sub> about  $\text{Si}'^{4-}_{2}$ .

aberration corrected JEOL ARM200CF microscope operating at 200 kV was utilized to acquire high-resolution scanning TEM (STEM) images perpendicular to the Nb [110] zone axis. Images were collected with a JEOL annular darkfield (90–370 mrad) detector under an 8  $\mu$ s dwell time and low-pass filtered using ImageJ. Stoichiometric STEM-energydispersive x-ray spectroscopy (EDS) was conducted with dual Oxford silicon drift detectors.

### **E. XRR**

XRR measurements were performed with a Smartlab SE diffractometer equipped with a 9 kW Cu rotating anode operated at 45 kV and 160 mA. A Ge (220) twobounce monochromator was utilized to have a monochromatic beam ( $\lambda = 1.5406 \text{ Å}$ ). The collimated beam was  $0.1 \times 5 \text{ mm}^2$ . XRR measurements are plotted in terms of the scattering vector  $Q = 4\pi \sin(\theta)/\lambda$ , normalized to the measured incident beam intensity, and corrected for geometrical footprint and background signal. The XRR analysis was performed using MOTOFIT software [\[32\]](#page-9-0). The XRR fitting is obtained from electron density profiles that simulate the Si/Nb<sub>x</sub>Si<sub>y</sub>/Nb/NbO/Nb<sub>2</sub>O<sub>5</sub> heterostructure. The stochiometric determination of Nb*x*Si*<sup>y</sup>* was obtained from fitting the electron density of this layer.

### **III. RESULTS AND DISCUSSION**

### **A. Bulk niobium silicide phase stability**

At room temperature, the most stable structure for bulk niobium silicide is α-Nb5Si3, exhibiting tetragonal *I*4/*mcm* symmetry, where it adopts the  $Cr<sub>5</sub>B<sub>3</sub>$  prototype structure with 4 f.u. in a conventional cell  $[9,11,18]$  $[9,11,18]$ . The Nb cations form  $Nb_{10}$  and  $Nb_{12}$  polyhedra, which coordinate anionic Si monomers and Si-Si dimers of length  $d = 2.4$  Å (Fig. 1). Here,  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> may be described as a valence-precise com-

<span id="page-3-0"></span>

FIG. 2. (a) Projected density of states (PDOS) for  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> and its (b) projected crystal orbital Hamilton population (pCOHP) with positive, negative, and zero values indicating bonding, antibonding, and nonbonding interactions for the specified atom pair. (c) The density functional theory (DFT) strongly constrained and appropriately normed (SCAN) 0 K Nb-Si convex hull for 10 niobium silicide phases is formed by  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> and NbSi<sub>2</sub>. (d) Formation free energy as a function of temperature with respect to bulk Nb and Si following Eq. [\(6\)](#page-2-0) in the Methods. The small changes  $\sim$ 0 K in (d) are due to the electronic entropic contributions in Eq. [\(6\)](#page-2-0), which are usually neglected but included here.

pound as  $(Nb^{3+})_5(Si^{4-})(Si_2^{6-})(5e^-)$  using Zintl bonding principles [\[21,22\]](#page-9-0), which implies that Nb has a nominal  $4d<sup>2</sup>$ electronic configuration (the  $+2$  oxidation state for Nb is eliminated because this would make  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> a diamagnetic semiconductor, whereas it exhibits metallic conductivity [\[11](#page-8-0)[,33\]](#page-9-0)). Although Nb 4*d*-Si 3*p* orbital hybridization restricts full electron transfer, both anions are diamagnetic with closed-shell configurations. Thus, we expect the remaining five delocalized electrons to occupy the Nb 4*d* orbitals participating in Nb-Nb and Nb-Si bonding. Overall, these features make bulk  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> a metallic paramagnet.

Our calculated electronic DOS shows that the Fermi level is indeed located in a region with many states consisting of multiple fractionally occupied Nb 4*d* orbitals [Fig. 2(a)]. There are ∼0.41 states per Nb *d* orbital, leading to an itinerant electron gas in the open 4*d* shell of Nb. We find Si 3*s* states with  $\sigma_g$  bonding and  $\sigma_u^*$  antibonding characters located between −12 and −8 eV, as confirmed from our projected crystal orbital Hamilton population (pCOHP) anal-ysis [\[34–36\]](#page-9-0) [Fig. 2(a)], indicating the presence of Zintl  $Si_2^{6-}$ dimers. Modest hybridization exists between the Nb and Si orbitals throughout the entire energy range, with the Nb 4*d* states spanning −6 to 3 eV. Metallic Nb-Nb bonding mainly occurs over the energy range from  $-3$  to 2.5 eV and leads to the formation of the pseudogap in the DOS, which separates the filled bonding states from the empty antibonding states. The Fermi energy is located in a region just above the pseudogap, which can lead to compositional disorder or the formation of a glass state in intermetallic phases [\[37\]](#page-9-0). The electron filling for stoichiometric  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> is such that the Fermi level is just above this minimum energy, suggesting that reducing the number of valence electrons could shift the Fermi level to lower energy through defect formation or deviations from pristine stoichiometry.

With increasing temperature, niobium silicides with different compositions form. We computed the Nb-Si convex hull by selecting low-energy niobium silicide compositions with their prototype structures specified in parentheses based on previous studies  $[9,11]$ : Nb<sub>3</sub>Si (PTi<sub>3</sub>), Nb<sub>2</sub>Si (Au<sub>2</sub>Cu),  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> (Cr<sub>5</sub>B<sub>3</sub>),  $\beta$ -Nb<sub>5</sub>Si<sub>3</sub> (W<sub>5</sub>Si<sub>3</sub>),  $\gamma$ -Nb<sub>5</sub>Si<sub>3</sub> (Mn<sub>5</sub>Si<sub>3</sub>),  $Nb_3Si_2$  (U<sub>3</sub>Si<sub>2</sub>),  $Nb_5Si_4$  (Zr<sub>5</sub>Si<sub>4</sub>),  $Nb_6Si_5$  (Ti<sub>6</sub>Ge<sub>5</sub>), NbSi (FeB), and NbSi<sub>2</sub> (CrSi<sub>2</sub>). The Nb<sub>2</sub>Si (Si<sup>4</sup><sup>-</sup>), Nb<sub>5</sub>Si<sub>3</sub>- $\beta$  (Si<sup>4</sup><sup>-</sup>) and Si<sup>4-</sup>), Nb<sub>5</sub>Si<sub>3</sub>- $\gamma$  (Si<sub>2</sub><sup>-</sup>), Nb<sub>3</sub>Si<sub>2</sub> (Si<sub>2</sub><sup>5</sup>), Nb<sub>5</sub>Si<sub>4</sub> (Si<sub>2</sub><sup>6</sup>),  $Nb_6Si_5(Si_4^{4-}, Si_2^{4-}, and Si'_2^{4-})$ , and NbSi  $(Si_2^{4-})$  compositions can also be regarded as Zintl phases [\[38\]](#page-9-0), where the Zintl anions are specified in Table [I.](#page-1-0) One calculation [\[9\]](#page-8-0) found that  $Nb<sub>2</sub>Si$  is closer to the hull than NbSi, whereas another calculation [\[11\]](#page-8-0) reported that NbSi is closer to the hull than  $Nb<sub>2</sub>Si$ . Our 0 K convex hull obtained from DFT using the SCAN functional reproduces the previously reported convex hull and reconciles this controversy. Our results show that both phases are close to the hull. In addition, our calculations using the SCAN functional further confirmed that the  $NbSi<sub>2</sub>$ has  $P6<sub>2</sub>22$  symmetry, in contrast to the previously reported *Fddd* structure [\[12\]](#page-9-0). These findings indicate that DFT-SCAN is a suitable level of theory to describe niobium silicides and thus was chosen to compute thickness effects in niobium silicide nanofilms.

Figure 2(b) shows that the convex hull is determined by  $\alpha$ -Nb<sub>5</sub>S<sub>13</sub> and NbS<sub>12</sub>, which is consistent with the experimental phase diagram  $[18]$  since they are the low-temperature stable silicides.  $Nb<sub>3</sub>Si$  is also very close to the convex hull (∼11.4 meV/atom from the hull) because it is experimen-tally stable over the 1765–1915 °C range [\[18\]](#page-9-0). For the other compositions above the hull, we find that  $\beta$ -Nb<sub>5</sub>Si<sub>3</sub> and Nb<sub>3</sub>Si<sub>2</sub> have formation energies of ∼37 meV/atom higher than  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>. We then calculated the thermal stability of the low-temperature phases (i.e.,  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> and NbSi<sub>2</sub>) by including the temperature-dependent part of the electronic free energy and the vibrational free energy (see the Methods and Fig. S1 in the Supplemental Material [\[39\]](#page-9-0)). We excluded  $\beta$ -Nb<sub>5</sub>Si<sub>3</sub>- $\beta$  [\[9](#page-8-0)[,18\]](#page-9-0) from this calculation and instead focused on  $Nb_3Si_2$  and  $Nb_6Si_5$  because, as we show below,  $Nb_6Si_5$  is stabilized by finite-sized effects. Here, we find that  $Nb<sub>3</sub>Si<sub>2</sub>$ becomes stable at intermediate temperatures, ranging from  $\sim$ 500 to 1500 K between the previously reported  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> and  $NbSi<sub>2</sub>$  phases forming the convex hull at 0 K.

#### **B. Niobium silicide nanofilm phase stability**

Next, we investigate the phase stability for the niobium silicides in unsupported nanofilm geometries including surface and finite thickness effects. We allow for relaxation normal to the film, no surface reconstruction, and no adsorption. Favorable surface orientations and compositions for the different silicide phases are created by conducting an atomic population analysis (i.e., density-derived electrostatic and chemical (DDEC) analysis  $[40,41]$ ). The overlap population (OP) is expressed as

$$
A_{i,j}|_{i \neq j} = 2 \int \frac{\rho_i(\mathbf{r_i}) \rho_j(\mathbf{r_j})}{\rho(\mathbf{r})} d^3 \mathbf{r},\tag{7}
$$

<span id="page-4-0"></span>

FIG. 3. Slab structures for the specified niobium silicide compositions with nominal thickness of 1.5–2.4 nm.

where  $A_{i,j}$  is the OP, and  $r_i$  and  $r_j$  are the positions for atoms  $i$  and  $j$ , respectively. Using Eq. [\(1\)](#page-1-0), we define the  $[h \; k \; l]$ directional-dependent OP as

$$
\text{OP}_{hkl} = \sum_{i}^{N} \frac{1}{2} A_{i,j} |_{i \neq j} \left| \frac{(\mathbf{r_j} - \mathbf{r_i}) \cdot \mathbf{R}}{|\mathbf{r_j} - \mathbf{r_i}||\mathbf{R}|} \right|,\tag{8}
$$

where we consider the summation of the OP among the nearest-neighboring atoms *j* for all the atoms *i* in the unit cell along a specified direction **R** with Miller indices *h*, *k*, and *l*. If OP*hkl* is small along a direction, we consider that the energetic cost to break the bonds along this direction is also small. Small OP*hkl* , therefore, would correspond to plane normal directions for likely cleavage planes to generate finite-sized 2D silicide nanofilms.

With this method, we find that the OP*hkl* value is the smallest along the [001] direction in  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>, which is consistent with a previous detailed first-principles study on the surface of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> [\[8](#page-8-0)[,42\]](#page-9-0). The surface directions for the other compositions are [001] for  $Nb<sub>3</sub>Si$ , [111] for  $Nb<sub>2</sub>Si$ , [001] for β-Nb<sub>5</sub>Si<sub>3</sub>, [001] for γ-Nb<sub>5</sub>Si<sub>3</sub>, [001] for Nb<sub>3</sub>Si<sub>2</sub>, [001] for  $Nb_5Si_4$ , [100] for  $Nb_6Si_5$ , [100] for NbSi, and [001] for NbSi2 (Tables S2–S11 in the Supplemental Material [\[39\]](#page-9-0)). We then determined the two surface terminations for each slab structure along these directions using a layer-resolved  $OP<sub>hkl</sub>$ , where the surface termination is selected base on the layer giving the smallest OP*hkl* value (Tables S12–S17 in the Supplemental Material [\[39\]](#page-9-0)). Throughout, we use symmetric slab geometries with identical surface terminations (Fig. 3).

Using these slab structures, we then compute the surface energies according to the expression [\[8\]](#page-8-0):

$$
\gamma = \frac{1}{2A} \bigg[ E_{\text{slab}} - \frac{1}{n_s} N_{\text{Si}} \mu_{\text{Nb}_{n_s} \text{Si}_{n_s}}^{\text{bulk}} - \left( N_{\text{Nb}} - \frac{n_n}{n_s} N_{\text{Si}} \right) \mu_{\text{Nb}} \bigg], \qquad (9)
$$

where  $\gamma$  is the surface energy,  $E_{\text{slab}}$  is the 0 K total energy of the slab structure, *A* is the surface area, and  $n_n$  and  $n_s$ are the number of Nb and Si atoms in the specified niobium silicide phases, respectively. Here,  $N_{Nb}$  and  $N_{Si}$  are the total number of Nb and Si atoms in the surface layer



FIG. 4. (a) Surface energy as a function of the chemical potential of Nb without finite temperature effects included for the various silicides. (b) The formation energy vs the inverse of the thickness, *h*<sup>−1</sup>, which is obtained by performing density functional theory (DFT) at 0 K. The filled circle at  $h^{-1} = 0$  for each composition corresponds to its bulk formation energy. Inset in (b): Enlargement of thickness-dependent crossover between −0.33 and −0.27 eV/atom with inverse thickness ranging from 0.08 to  $0.12 \text{ Å}^{-1}$ , where the transition is from α-Nb<sub>5</sub>Si<sub>3</sub> to Nb<sub>6</sub>Si<sub>5</sub> at ~0.1 Å<sup>-1</sup> as indicated by the dashed vertical line.

(SL), respectively, which can be further expressed as  $N_{Nb}$  =  $n_{\text{Nb}}^{\text{BL}} + n_{\text{Nb}}^{\text{SL}}$  and  $N_{\text{Si}} = n_{\text{Si}}^{\text{BL}} + n_{\text{Si}}^{\text{SL}}$ , where  $n_i^{\text{BL}}$  and  $n_i^{\text{SL}}$  (*i* = Nb, Si) are the number of atoms in the bulk layers (BLs) and SLs, respectively. Here,  $\mu$  represents the chemical potential and  $n_n \mu_{Nb} + n_s \mu_{Si} = \mu_{Nb_n}^{bulk}$  for a niobium silicide. Furthermore, to form a niobium silicide, the requirements of  $\mu_{Nb} \le \mu_{Nb}^{bulk}$  and  $\mu_{Si} \le \mu_{Si}^{bulk}$  must be fulfilled, which leads to  $\frac{1}{n_a}(\mu_{Nb_mSi_{n_s}}^{bulk} - n_s\mu_{Si}^{bulk}) \leq \mu_{Nb} \leq \mu_{Nb}^{bulk}$ .

Figure  $4(a)$  shows the calculated surface energies for the seven different niobium silicides. The  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> surface energy as a function of Nb chemical potential is in good agreement with the previous first-principles results [\[8\]](#page-8-0). Interestingly, we find that the surface energies of  $\beta$ -Nb<sub>5</sub>Si<sub>3</sub>, NbSi, and  $Nb_6Si_5$  are lower than that of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>. From the surface energies, we further investigate the thickness dependence of the nanofilm phase stabilities. First, we obtain the surface formation energy at a different thickness (*h*), approximately estimated by the distance between the top and bottom surfaces, by changing  $n_{\text{Nb}}^{\text{BL}}$  and  $n_{\text{Si}}^{\text{BL}}$  through the addition of additional BLs. Then the formation energy for the nanofilms of different thicknesses *h* is obtained by using this quantity in a modified expression for the bulk formation energy [Eq. [\(3\)](#page-1-0)]. Here, we assume the surface energy is independent of film thickness in the nanofilms, which is reasonable [\[28\]](#page-9-0) and consistent with our assessments. Figure  $4(b)$  shows the formation energies for the nanofilms with varying thickness. We find the interpolated formation energies for the bulk compositions agree well with our DFT calculations, which further confirms



FIG. 5. (a) The entropic electronic and phononic contributions to the nanoscale silicide formation energy as a function of the temperature for nanofilms of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> (2.37 nm),  $\beta$ -Nb<sub>5</sub>Si<sub>3</sub> (1.52 nm),  $Nb<sub>3</sub>Si<sub>2</sub>$  (1.75 nm), and  $Nb<sub>6</sub>Si<sub>5</sub>$  (1.56 nm). (b) Formation energy vs inverse of the thickness in the Nb-rich region including entropic effects at 700 K shows a transition. Here, we predict the formation energy from 0 to 700 K with a uniform shift for the thickness range considered, where the uniform values are the entropic electronic and phononic contributions at 700 K at 1.56 and 2.37 nm for  $Nb<sub>6</sub>Si<sub>5</sub>$  and  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>, respectively. The formation energy at 700 K for  $\beta$ -Nb<sub>5</sub>Si<sub>3</sub> is also shown to indicate finite-temperature effects do not stabilize it over  $Nb<sub>6</sub>Si<sub>5</sub>$  nanofilms.

the reliability of the approximation. In addition, we find that the dependencies do not change irrespective of the surface energy and the Nb chemical potential in Eq [\(3\)](#page-1-0). At large thickness, we find  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> is stable, consistent with the bulk phase diagram reporting high stability of this phase.

In contrast, the  $Nb<sub>6</sub>Si<sub>5</sub>$  phase is stable for nanofilms. Therefore, we predict a thickness-dependent phase transition occurs at ∼1 nm mainly driven by the lower surface energy of  $Nb_6Si_5$ . The stability of the  $Nb_6Si_5$  nanofilm with decreasing thickness has not been previously reported but can be justified because of its significantly lower surface energy than  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>. In addition, we find that the low surface energy of  $\beta$ -Nb<sub>5</sub>Si<sub>3</sub> makes it competitive with  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> and Nb<sub>6</sub>Si<sub>5</sub> nanofilms as the film thickness decreases.

One way to synthesize nanoscale niobium silicides is via thin film deposition of several monolayers of Nb from a metallic source. The favorable silicide composition that forms depends on deposition method and temperature, assuming a constant niobium flux and unit sticking coefficient, which permits aggregation of adatoms to form a conformal layer, along with Si diffusion. To assess thermal stability, we calculated the formation free energies of nanofilms of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>, β-Nb<sub>5</sub>Si<sub>3</sub>,  $Nb<sub>3</sub>Si<sub>2</sub>$ , and  $Nb<sub>6</sub>Si<sub>5</sub>$ , using the same method employed to evaluate bulk thermal stability (Methods and Fig. S2 in the Supplemental Material  $[39]$ ). Figure  $5(a)$  shows that the entropic contributions in nanofilm  $Nb<sub>6</sub>Si<sub>5</sub>$  are greater than those of the other nanoscale silicides. The entropy increment with increasing temperature is largely due to vibrational contributions. We find  $Nb_6Si_5$  has a lower Debye temperature of 435 vs 460 K for bulk  $\alpha$ -Nb<sub>5</sub>S<sub>13</sub> obtained from our phonon calculations [\[11](#page-8-0)[,43,44\]](#page-9-0) (Table S18 in the Supplemental Material [\[39\]](#page-9-0)). Figure  $5(b)$  shows this effect leads to a critical thickness of 1.2 nm where the  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>-to-Nb<sub>6</sub>Si<sub>5</sub> transition occurs, which decreases to a critical thickness of 1 nm when the vibrationalfree-energy contribution is omitted at finite temperature [Fig. [4\(b\)\]](#page-4-0). Although  $\beta$ -Nb<sub>5</sub>Si<sub>3</sub> and Nb<sub>3</sub>Si<sub>2</sub> are also favored compared with  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> at high temperatures [Fig. 5(a)], we do not predict a thickness-dependent transition to occur between these phases. However, we have neglected the effects of the Si-silicide interface that may act to template and further favor the formation of one silicide phase over another.

Analysis of the DOS provides a postulate for why the surface energy of  $Nb_6Si_5$  is lower than that of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>. Since there is no adsorption or reconstruction, the change in surface energy is a result of the redistribution of delocalized electrons near the surface. This redistribution enhances the degree of metal-metal bonding character, influences the Fermi level position, and may partly compensate the energy penalty because the metal-metal interaction is crucial to stabilize an intermetallic compound [\[33,37,45](#page-9-0)[–47\]](#page-10-0). As can be seen from Fig.  $6(a)$ , the DOS around the Fermi level at the  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> (001) surface of the 2.4 nm nanofilm becomes higher than that of the bulk [see Fig. [2\(a\)\]](#page-3-0), which indicates that the Nb-Nb *d* orbital interactions are weaker at the surface [\[33,37,45](#page-9-0)[–47\]](#page-10-0). From our pCOHP analysis, we find that the Nb-Nb *d* orbital interactions are nonbonding for both the bulk and surface structures in  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>. A nonbonding state itself does not stabilize the surface structure, but the high DOS at the Fermi level in the intermetallic compounds may result in a magnetic instability [\[34,](#page-9-0)[48–51\]](#page-10-0), and the high DOS can be reduced by forming a magnetically ordered state that will help with compensating the energy penalty. Interestingly, Figs. [6\(b\)](#page-6-0) and [6\(c\)](#page-6-0) show that the DOS and pCOHP, respectively, present a completely different scenario for the  $Nb<sub>6</sub>Si<sub>5</sub>$  (100) surface structure of a 1.5 nm film. Although there is also an increase in the number of states around the Fermi level, the Nb-Nb *d* orbital interactions in the SLs exhibit bonding character, which can directly help stabilize the surface structure and partly compensate for the change in coordination in  $Nb<sub>6</sub>Si<sub>5</sub>$ . This change in chemical bonding at the surface likely explains why the surface energy of  $Nb_6Si_5$  is lower than that of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>.

#### **C. Magnetism in niobium silicides**

As mentioned above, the high DOS at the Fermi level in the intermetallic compounds may result in magnetic instability. We now investigate possible magnetism at the surfaces of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> and Nb<sub>6</sub>Si<sub>5</sub>. To find the possible magnetic structures for the two compositions, we rely on a crystal orbital Hamilton population (COHP) analysis, which is usually adopted for analyzing the magnetic ground states of intermetallic compounds [\[34,](#page-9-0)[48–51\]](#page-10-0). Figure [7](#page-6-0) shows the electronic structures and pCOHPs for the surface structures of nanofilms of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> (∼2.4 nm) and Nb<sub>6</sub>Si<sub>5</sub> (∼1.5 nm). We find the Fermi level located in a region of nonbonding states in the

<span id="page-6-0"></span>

FIG. 6. (a) Projected density of states (PDOS) and projected crystal orbital Hamilton population (pCOHP) for the  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> (001) surface of the 2.4 nm nanofilm. PDOS and pCOHP for (b) bulk  $Nb_6Si_5$  and (c)  $Nb_6Si_5$  (100) surface of the 1.5 nm nanofilm.



FIG. 7. (a) Projected density of states (PDOS) and projected crystal orbital Hamilton population (pCOHP) for the  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> (001) surface with zero magnetic moments at the density funtional theory  $(DFT)+U = 3$  eV level. Positive (negative) density of states (DOS) indicates the spin-up (spin-down) channel. The positive, zero, and negative values in the pCOHP indicate bonding, nonbonding, and antibonding interactions, respectively, for the spin-up channel in solid lines. The meaning is reversed for the spin-down channel indicated in broken lines. (b) PDOS and pCOHP for the  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> (001) surface with an antiferromagnetic surface spin structure at the DFT+ $U = 3$  eV level. (c) Spin density distributions of the antiferromagnetic interactions on the α-Nb<sub>5</sub>Si<sub>3</sub> surface. Yellow spin density indicates spin-up and blue indicates spin-down electrons. The resolution for the isosurface plot is 0.0028 eV Å<sup>-3</sup>. The black arrows indicate the alignment of the spins without considering spin-orbital effects. (d) The band structure for α-Nb<sub>5</sub>Si<sub>3</sub> with (left) nonmagnetic, (center) magnetic with no magnetic moments, and (right) antiferromagnetic surface spin configurations.

<span id="page-7-0"></span>electronic structure of the nonmagnetic surface of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>. In contrast, the Fermi level is in the bonding states for the nonmagnetic configuration of the  $Nb<sub>6</sub>Si<sub>5</sub>$  surface. Thus, given many states at the Fermi level and the position relative to the bonding and nonbonding states [Figs.  $6(a)$  and  $6(c)$ ], we expect the nanoscale silicides to be susceptible to different magnetic states. Here,  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> should favor an antiferromagnetic spin configuration, and  $Nb<sub>6</sub>Si<sub>5</sub>$  should be nonmagnetic (or weakly paramagnetic) according to previous electronic structure studies on the magnetic transition metals and intermetallic binary compounds [\[34](#page-9-0)[,48–51\]](#page-10-0). Therefore, we focus on understanding the magnetic state of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>.

The reduced coordination from broken bonds at the surface may enhance the effective electron-electron interactions in the silicides. Therefore, we performed DFT+*U* calculations, which showed sizable magnetic moments confined to the surface niobium atoms for  $U \geq 3$  eV despite the strong metallicity. This high *U* value is reasonable compared with the 4 eV adopted in previous studies of niobium oxides [\[52\]](#page-10-0). The final magnetic configurations were determined by random spin generation and symmetry-constrained spin generation (see Fig. S6 in the Supplemental Material [\[39\]](#page-9-0)). We find an antiferromagnetic spin order for  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> [Fig. [7\(c\)\]](#page-6-0), which collapses to a nonmagnetic solution for  $U \leq 2.5 \text{ eV}$ , because the metallicity competes with local moment formation on the surface Nb atoms. To understand the origin of the itinerant antiferromagnetic state at the surface, we further calculate the pCOHPs for two scenarios: (i) no magnetic moments and  $U = 3$  eV and (ii) with magnetic moments at  $U = 3$  eV. Figures [7\(a\)](#page-6-0) and [7\(b\)](#page-6-0) show that the local Coulomb interaction from the  $+U$  reduces the DOS at the Fermi level in  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>. In  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>, we find increased interaction strength *U* does not induce a Stoner ferromagnetic instability because the nonbonding states at the Fermi level favor an antiferromagnetic spin order. Spin polarization of the electronic structure would not lead to energy stabilization if the frontier orbitals are nonbonding in character. This finding is consistent with previous COHP analysis on the intermetallic compounds, leading to a further decease of the DOS at the Fermi level [\[34](#page-9-0)[,48–51\]](#page-10-0). Although the magnetic surface structure of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> and the role of the onsite repulsion *U* require future experimental validation, our analysis shows that the formation of a 2D spin-density wave reduces the size of the Fermi surface and further stabilizes the surface structure [Fig.  $7(d)$ ]. Here, we find that the formation energy of  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> can be lowered by 13 meV/atom at 2.4 nm compared with the nonmagnetic state. Furthermore, the calculated magnetic moment on the surface niobium atoms is ~0.24  $\mu_B/Nb$ , which could be further decreased in the experiment at finite temperature because of the effects of the spin fluctuations that are not included in our model [\[53,54\]](#page-10-0).

While magnetism can be one source of qubit decoherence, metallicity can also contribute to decoherence [\[3,4\]](#page-8-0). Therefore, we investigate the thickness-dependent metallicity by examining the DOS at the Fermi level  $(g_F)$ . The values range from 0.4 to 0.8 states per surface atom per electronvolt, which is comparable with 0.2–0.3 states per atom per electronvolt of the prototypical metals Al and Au  $[55,56]$ , but <2.7 states per atom per electronvolt of 2D  $MoSi<sub>2</sub>$  nanofilms [\[28\]](#page-9-0). As can be seen from Fig.  $8$ ,  $g_F$  decreases with decreasing nanofilm



FIG. 8. Number of states at the Fermi level as a function of the inverse of the thickness in  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> (red) and Nb<sub>6</sub>Si<sub>5</sub> (yellow). Here, the states are counted only from Nb in the structure we computed at each thickness for an accurate prediction of the changes of metallicity because almost all the density of states (DOS) at the Fermi level is from Nb.

thickness for both  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> and Nb<sub>6</sub>Si<sub>5</sub>, suggesting that the nanofilms are more resistive than their bulk counterparts.

### **D. Experimental characterization of niobium silicide nanofilms**

To experimentally evaluate our computational findings, we prepared 40 nm Nb thin films on Si (111) substrates using DC sputtering and characterized the Nb/Si interface with TEM



FIG. 9. (a) High- and (b) low-magnification annular dark-field scanning transmission electron microscopy (STEM) images of the amorphous Nb/Si interface (outlined in gray) present in DC sputter deposited Nb thin films on Si(111). Energy-dispersive x-ray spectroscopy (EDS) of Nb (green) and Si (blue) revealed a Nb-rich composition at the interface with  $54\pm1$  at.% Nb and  $46\pm1$  at.% Si.

<span id="page-8-0"></span>

FIG. 10. (a) X-ray reflectivity (XRR) of the 40 nm Nb thin film on Si (111). The fitting resulted in 1.2 nm  $Nb<sub>x</sub>Si<sub>y</sub>$ , 38.5 nm Nb, 1.3 nm NbO, and 2.4 nm  $Nb<sub>2</sub>O<sub>5</sub>$  from bottom to top of the film. (b) Electron density slab profile for the multiple interfaces in the film. The electron density of the Nb*x*Si*<sup>y</sup>* layer is 1.866*e*<sup>−</sup> Å<sup>−</sup>3.

and XRR. Annular dark-field STEM images reveal an amorphous interfacial layer between the crystalline Si substrate and the crystalline Nb thin film with an approximate thickness of 1.5 nm, as shown in Fig. [9.](#page-7-0) Analysis of the interfacial layer by EDS indicates an elemental composition of  $54 \pm 1$ at.% Nb and  $46 \pm 1$  at.% Si. This composition is consistent with the  $Nb<sub>6</sub>Si<sub>5</sub>$  stoichiometry. Analysis of the film by XRR reveals a layer stack consisting of 2.4 nm  $Nb<sub>2</sub>O<sub>5</sub>$ , 1.3 nm NbO, 38.5 nm Nb, and 1.2 nm Nb*x*Si*y*, on bulk Si, from top to bottom (Fig. 10). The thickness of the Nb/Si interfacial layer as measured by XRR is in good agreement with the value determined by TEM. The XRR measured electron density of the Nb*x*Si*<sup>y</sup>* layer is 1.866*e*<sup>−</sup> Å<sup>−</sup>3, which agrees to within 3% of the predicted value for Nb<sub>6</sub>Si<sub>5</sub> (1.816*e*<sup>−</sup> Å<sup>−3</sup>). In comparison,  $Nb<sub>3</sub>Si$  would have a 7% higher and  $NbSi<sub>2</sub>$  a 20% lower predicted electron density than measured.

### **IV. CONCLUSIONS**

By performing first-principles calculations, we predict two stable compositions with decreasing thickness in the

nanofilm:  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> at larger thickness and Nb<sub>6</sub>Si<sub>5</sub> at lower thickness. The critical thickness for the transition between stable nanofilm compositions is  $\sim$ 1 and 1.2 nm at 0 and 700 K, respectively. The stable  $Nb<sub>6</sub>Si<sub>5</sub>$  phase is also consistent with experimental XRR and TEM measurements, whose thickness is ∼1.2 nm. Therefore, we suggest that Nb-Si heterointerfaces in 2D transmon structures obtained by sputter-depositing Nb films on silicon substrates may not be atomically sharp, which has likely implications for achieving long qubit-coherence times. Furthermore, we also predict that  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> nanofilms may be antiferromagnetic, whereas  $Nb<sub>6</sub>Si<sub>5</sub>$  nanofilms are nonmagnetic based on bond-character analysis.

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- [1] A. A. Murthy, J.-Y. Lee, C. Kopas, M. J. Reagor, A. P. McFadden, D. P. Pappas, M. Checchin, A. Grassellino, and A. Romanenko, TOF-SIMS analysis of decoherence sources in Nb superconducting qubits, [Appl. Phys. Lett.](https://doi.org/10.1063/5.0079321) **120**, 044002 (2021).
- [2] A. Romanenko, R. Pilipenko, S. Zorzetti, D. Frolov, M. Awida, S. Belomestnykh, S. Posen, and A. Grassellino, Three-Dimensional Superconducting Resonators at *T* < 20 MK with [Photon Lifetimes up to](https://doi.org/10.1103/PhysRevApplied.13.034032)  $\tau = 2$  s, Phys. Rev. Applied 10, 34032 (2020).
- [3] W. D. Oliver and P. B. Welander, Materials in superconducting quantum bits, MRS Bull. **38**[, 816 \(2013\).](https://doi.org/10.1557/mrs.2013.229)
- [4] D. R. Heslinga and T. M. Klapwijk, Schottky barrier and contact [resistance at a niobium/silicon interface,](https://doi.org/10.1063/1.100793) Appl. Phys. Lett. **54**, 1048 (1989).
- [5] F. Nava, P. A. Psaras, K. N. Tu, H. Takai, S. Valeri, and O. Bisi, Electrical and structural characterization of Nb-Si thin alloy film, [J. Mater. Res.](https://doi.org/10.1557/JMR.1986.0327) **1**, 327 (1986).
- [6] L. Xu, R. Lingling, G. Sitian, Z. Liqi, and T. Xingfu, Strain study of Nb-Si{001} interface based on geometric phase analysis, [J. Aeronaut. Mater.](https://doi.org/10.11868/j.issn.1005-5053.2016.000114) **38**, 96 (2018).
- [7] D. S. Wisbey, J. Gao, M. R. Vissers, F. C. S. da Silva, J. S. Kline, L. Vale, and D. P. Pappas, Effect of metal/substrate interfaces on radio-frequency loss in superconducting coplanar waveguides, J. Appl. Phys. **108**[, 093918 \(2010\).](https://doi.org/10.1063/1.3499608)
- [8] S. Y. Liu, J. X. Shang, F. H. Wang, S. Liu, Y. Zhang, D. Li, D. Shields, W. Xue, Y. Liu, H. Dang, and S. Wang, Oxidation of the two-phase  $Nb/Nb_5Si_3$  composite: The role of energetics, [thermodynamics, segregation, and interfaces,](https://doi.org/10.1063/1.4773447) J. Chem. Phys. **138**, 014708 (2013).
- [9] Y. Chen, T. Hammerschmidt, D. G. Pettifor, J. X. Shang, and Y. Zhang, Influence of vibrational entropy on structural stability of [Nb-Si and Mo-Si systems at elevated temperatures,](https://doi.org/10.1016/j.actamat.2009.02.014) Acta Mater. **57**, 2657 (2009).
- [10] S. Prasad and A. Paul, Growth mechanism of phases by interdiffusion and diffusion of species in the niobium-silicon system, Acta Mater. **59**[, 1577 \(2011\).](https://doi.org/10.1016/j.actamat.2010.11.022)
- [11] B. Wan, F. Xiao, Y. Zhang, Y. Zhao, L. Wu, J. Zhang, and H. Gou, Theoretical study of structural characteristics, mechanical properties and electronic structure of metal ( $TM = V$ , Nb and Ta) silicides, [J. Alloys Compd.](https://doi.org/10.1016/j.jallcom.2016.04.253) **681**, 412 (2016).
- <span id="page-9-0"></span>[12] S. L. Wang and Y. Pan, Insight into the structures, melting points, and mechanical properties of NbSi<sub>2</sub> from first-principles calculations, [J. Am. Ceram. Soc.](https://doi.org/10.1111/jace.16345) **102**, 4822 (2019).
- [13] T. Nakanishi, M. Takeyama, A. Noya, and K. Sasaki, Formation of metal-rich silicides in the initial stage of interfacial reactions in Nb/Si systems, [J. Appl. Phys.](https://doi.org/10.1063/1.359584) **77**, 948 (1995).
- [14] N. Suresh, D. M. Phase, A. Gupta, and S. M. Chaudhari, Electron density fluctuations at interfaces in Nb/Si bilayer, trilayer, [and multilayer films: An x-ray reflectivity study,](https://doi.org/10.1063/1.373479) J. Appl. Phys. **87**, 7946 (2000).
- [15] R. J. Grylls, B. P. Bewlay, H. A. Lipsitt, and H. L. Fraser, Characterization of silicide precipitates in Nb-Si and Nb-Ti-Si alloys, [Philos. Mag. A](https://doi.org/10.1080/01418610108216647) **81**, 1967 (2001).
- [16] Y. Chen, J. X. Shang, and Y. Zhang, Effects of alloying element Ti on  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub> and Nb<sub>3</sub>Al from first principles, J. Phys.: Condens. Matter **19**, 016215 (2007).
- [17] T. Proslier, J. A. Klug, J. W. Elam, H. Claus, N. G. Becker, and M. J. Pellin, Atomic layer deposition and superconduct[ing properties of NbSi films,](https://doi.org/10.1021/jp201873b) J. Phys. Chem. C **115**, 9477 (2011).
- [18] M. E. Schlesinger, H. Okamoto, A. B. Gokhale, and R. [Abbaschian, The Nb-Si \(niobium-silicon\) system,](https://doi.org/10.1007/BF02671971) J. Ph. Equilibria **14**, 502 (1993).
- [19] C. Wang, X. Li, H. Xu, Z. Li, J. Wang, Z. Yang, Z. Mi, X. Liang, T. Su, C. Yang *et al.*, Transmon qubit with relaxation time exceeding 0.5 milliseconds, [arXiv:2105.09890.](http://arxiv.org/abs/arXiv:2105.09890)
- [20] A. P. M. Place, L. V. H. Rodgers, P. Mundada, B. M. Smitham, M. Fitzpatrick, Z. Leng, A. Premkumar, J. Bryon, A. Vrajitoarea, S. Sussman *et al.*, New material platform for superconducting transmon qubits with coherence times exceeding 0.3 milliseconds, [Nat. Commun.](https://doi.org/10.1038/s41467-021-22030-5) **12**, 1779 (2021).
- [21] J. Sun, R. C. Remsing, Y. Zhang, Z. Sun, A. Ruzsinszky, H. Peng, Z. Yang, A. Paul, U. Waghmare, X. Wu, M. L. Klein, and J. P. Perdew, Accurate first-principles structures and energies of diversely bonded systems from an efficient density functional, [Nature Chem.](https://doi.org/10.1038/nchem.2535) **8**, 831 (2016).
- [22] J. Sun, A. Ruzsinszky, and J. P. Perdew, Strongly Constrained and Appropriately Normed Semilocal Density Functional, Phys. Rev. Lett. **115**[, 036402 \(2015\).](https://doi.org/10.1103/PhysRevLett.115.036402)
- [23] G. Kresse and J. Furthmüller, Efficient iterative schemes for *ab initio* total-energy calculations using a plane-wave basis set, Phys. Rev. B **54**[, 11169 \(1996\).](https://doi.org/10.1103/PhysRevB.54.11169)
- [24] G. Kresse and J. Furthmüller, Efficiency of *ab-initio* total energy calculations for metals and semiconductors using a plane-wave basis set, [Comput. Mater. Sci.](https://doi.org/10.1016/0927-0256(96)00008-0) **6**, 15 (1996).
- [25] G. Kresse and D. Joubert, From ultrasoft pseudopotentials to [the projector augmented-wave method,](https://doi.org/10.1103/PhysRevB.59.1758) Phys. Rev. B **59**, 1758 (1999).
- [26] [P. E. Blöchl, Projector augmented-wave method,](https://doi.org/10.1103/PhysRevB.50.17953) Phys. Rev. B **50**, 17953 (1994).
- [27] A. I. Liechtenstein, V. I. Anisimov, and J. Zaanen, Densityfunctional theory and strong interactions: Orbital ordering in Mott-Hubbard insulators, Phys. Rev. B **52**[, R5467\(R\) \(1995\).](https://doi.org/10.1103/PhysRevB.52.R5467)
- [28] L.-F. Huang and J. M. Rondinelli, Stable  $M_0$ Si<sub>2</sub> nanofilms [with controllable and high metallicity,](https://doi.org/10.1103/PhysRevMaterials.1.063001) Phys. Rev. Materials **1**, 063001(R) (2017).
- [29] L.-F. Huang and J. M. Rondinelli, Electrochemical phase diagrams for ti oxides from density functional calculations, Phys. Rev. B **92**[, 245126 \(2015\).](https://doi.org/10.1103/PhysRevB.92.245126)
- [30] L.-F. Huang, X.-Z. Lu, E. Tennessen, and J. M. Rondinelli, An efficient *ab-initio* quasiharmonic approach for the thermodynamics of solids, [Comput. Mater. Sci.](https://doi.org/10.1016/j.commatsci.2016.04.012) **120**, 84 (2016).
- [31] E. Huang, M. Satjapipat, S. Han, and F. Zhou, Surface structure and coverage of an oligonucleotide probe tethered onto a gold substrate and its hybridization efficiency for a polynucleotide target, Langmuir **17**[, 1215 \(2001\).](https://doi.org/10.1021/la001019i)
- [32] A. Nelson, Co-refinement of multiple-contrast neutron/x-ray reflectivity data using MOTOFIT, [J. Appl. Cryst.](https://doi.org/10.1107/S0021889806005073) **39**, 273 (2006).
- [33] Y. Chen, J. X. Shang, and Y. Zhang, Bonding characteristics and site occupancies of alloying elements in different  $Nb<sub>5</sub>Si<sub>3</sub>$  phases from first principles, Phys. Rev. B **76**[, 184204 \(2007\).](https://doi.org/10.1103/PhysRevB.76.184204)
- [34] S. Steinberg and R. Dronskowski, The crystal orbital Hamilton population (COHP) method as a tool to visualize and analyze [chemical bonding in intermetallic compounds,](https://doi.org/10.3390/cryst8050225) Crystals **8**, 225 (2018).
- [35] R. Dronskowski and P. E. Bloechl, Crystal orbital Hamilton populations (COHP): Energy-resolved visualization of chemical bonding in solids based on density-functional calculations, [J. Phys. Chem.](https://doi.org/10.1021/j100135a014) **97**, 8617 (2002).
- [36] V. L. Deringer, A. L. Tchougréeff, and R. Dronskowski, Crystal orbital Hamilton population (COHP) analysis as projected from plane-wave basis sets, [J. Phys. Chem. A](https://doi.org/10.1021/jp202489s) **115**, 5461 (2011).
- [37] P. Ravindran and R. Asokamani, Correlation between electronic structure, mechanical properties and phase stability in intermetallic compounds, [Bull. Mater. Sci.](https://doi.org/10.1007/BF02744780) **20**, 613 (1997).
- [38] U. Häussermann, V. F. Kranak, and K. Puhakainen, Hydrogenous Zintl phases: Interstitial versus polyanionic hydrides, in *Zintl Phases*, edited by T. Fässler (Springer, Berlin, Heidelberg, 2011), Vol. 139, pp. 143–161.
- [39] See Supplemental Material at http://link.aps.org/supplemental/ [10.1103/PhysRevMaterials.6.064402](http://link.aps.org/supplemental/10.1103/PhysRevMaterials.6.064402) for details of the phonon spectra for the select bulk and nanofilm niobium silicides; determination of the surface directions; determination of the surface terminations; determination of the Debye temperatures of Nb, Si,  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>, and Nb<sub>6</sub>Si<sub>5</sub>; and determination of the spin orders in  $\alpha$ -Nb<sub>5</sub>Si<sub>3</sub>.
- [40] T. A. Manz and N. G. Limas, Introducing DDEC6 atomic population analysis: Part 1. Charge partitioning theory and methodology, RSC Adv. **6**[, 47771 \(2016\).](https://doi.org/10.1039/C6RA04656H)
- [41] N. G. Limas and T. A. Manz, Introducing DDEC6 atomic population analysis: Part 2. Computed results for a wide range [of periodic and nonperiodic materials,](https://doi.org/10.1039/C6RA05507A) RSC Adv. **6**, 45727 (2016).
- [42] A. V. Mudring and J. D. Corbett, Unusual electronic and bonding properties of the Zintl phase  $Ca<sub>5</sub>Ge<sub>3</sub>$  and related Com[pounds. A theoretical analysis,](https://doi.org/10.1021/ja030216b) J. Am. Chem. Soc. **126**, 5277 (2004).
- [43] C. Toher, J. J. Plata, O. Levy, M. de Jong, M. Asta, M. B. Nardelli, and S. Curtarolo, High-throughput computational screening of thermal conductivity, Debye temperature, and Grüneisen parameter using a quasiharmonic Debye model, Phys. Rev. B **90**[, 174107 \(2014\).](https://doi.org/10.1103/PhysRevB.90.174107)
- [44] I. Papadimitriou, C. Utton, and P. Tsakiropoulos, The impact of Ti and temperature on the stability of  $Nb<sub>5</sub>Si<sub>3</sub>$  phases: A firstprinciples study, [Sci. Technol. Adv. Mater.](https://doi.org/10.1080/14686996.2017.1341802) **18**, 467 (2017).
- [45] V. L. Moruzzi, P. Oelhafen, and A. R. Williams, Stability in [ordered and amorphous transition-metal compounds,](https://doi.org/10.1103/PhysRevB.27.7194) Phys. Rev. B **27**, 7194 (1983).
- <span id="page-10-0"></span>[46] T. Hong, T. J. Watson-Yang, X.-Q. Guo, A. J. Freeman, T. Oguchit, and J.-H. Xu, Crystal structure, phase stability, and electronic structure of Ti-Al intermetallics:  $Ti<sub>3</sub>A1$ , Phys. Rev. B **43**, 1940 (1991).
- [47] W. Speier, L. Kumar, D. D. Sarma, R. A. de Groot, and J. C. [Fuggle, The electronic structure of 4](https://doi.org/10.1088/0953-8984/1/46/006)*d* and 5*d* silicides, J. Phys.: Condens. Matter **1**, 9117 (1989).
- [48] R. Dronskowski, K. Korczak, H. Lueken, and W. Jung, Chemically tuning between ferromagnetism and antiferromagnetism by combining theory and synthesis in iron/manganese rhodium borides, [Angew. Chem. Int. Ed.](https://doi.org/10.1002/1521-3773(20020715)41:14<2528::AID-ANIE2528>3.0.CO;2-6) **41**, 2528 (2002).
- [49] M. Amsler, S. S. Naghavi, and C. Wolverton, Prediction of superconducting iron-bismuth intermetallic compounds at high pressure, Chem. Sci. **8**[, 2226 \(2017\).](https://doi.org/10.1039/C6SC04683E)
- [50] V. Y. Verchenko, A. A. Tsirlin, D. Kasinathan, S. V. Zhurenko, A. A. Gippius, and A. v. Shevelkov, Antiferromagnetic ground state in the MnGa<sub>4</sub> [intermetallic compound,](https://doi.org/10.1103/PhysRevMaterials.2.044408) Phys. Rev. Materials **2**, 044408 (2018).
- [51] Z. Ryżyńska, J. R. Chamorro, T. M. McQueen, P. Wiśniewski, D. Kaczorowski, W. Xie, R. J. Cava, T. Klimczuk, and M. J. Winiarski, RuAl<sub>6</sub>—an endohedral aluminide superconductor, Chem. Mater. **32**[, 3805 \(2020\).](https://doi.org/10.1021/acs.chemmater.9b05277)
- [52] C. P. Koçer, K. J. Griffith, C. P. Grey, and A. J. Morris, Firstprinciples study of localized and delocalized electronic states in [crystallographic shear phases of niobium oxide,](https://doi.org/10.1103/PhysRevB.99.075151) Phys. Rev. B **99**, 075151 (2019).
- [53] W. F. Goh and W. E. Pickett, Competing magnetic instabilities [in the weak itinerant antiferromagnetic TiAu,](https://doi.org/10.1103/PhysRevB.95.205124) Phys. Rev. B **95**, 205124 (2017).
- [54] W. F. Goh and W. E. Pickett, A mechanism for weak itinerant antiferromagnetism: Mirrored van Hove singularities, [Europhys. Lett.](https://doi.org/10.1209/0295-5075/116/27004) **116**, 27004 (2016).
- [55] D. Kienle and A. W. Ghosh, Atomistic modeling of metalnanotube contacts, [J. Comput. Electron.](https://doi.org/10.1007/s10825-005-7116-7) **4**, 97 (2005).
- [56] T. Genieys, M. Sentis, and O. Utéza, Investigation of ultrashort laser excitation of aluminum and tungsten by reflectivity measurements, [Appl. Phys. A](https://doi.org/10.1007/s00339-020-3440-9) **126**, 263 (2020).