

## Temperature-induced valence-state transition in double perovskite $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$

Z. Y. Zhao<sup>1,2,3</sup>, S. Calder<sup>4</sup>, M. H. Upton<sup>5</sup>, H. D. Zhou<sup>2</sup>, Z. Z. He<sup>3</sup>, M. A. McGuire<sup>1</sup>, and J.-Q. Yan<sup>1</sup>

<sup>1</sup>Materials Science and Technology Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA

<sup>2</sup>Department of Physics and Astronomy, University of Tennessee, Knoxville, Tennessee 37996, USA

<sup>3</sup>State Key Laboratory of Structural Chemistry, Fujian Institute of Research on the Structure of Matter, Chinese Academy of Sciences, Fuzhou, Fujian 350002, People's Republic of China

<sup>4</sup>Neutron Scattering Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA

<sup>5</sup>X-ray Science Division, Argonne National Laboratory, Argonne, Illinois 60439, USA



(Received 23 August 2021; accepted 4 May 2022; published 19 May 2022)

In this paper, a temperature-induced valence-state transition is studied in a narrow composition range  $0.2 \leq x \leq 0.375$  of  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  by means of x-ray and neutron powder diffraction, resonant inelastic x-ray scattering, magnetic susceptibility, electrical resistivity, and specific heat measurements. The valence-state transition involves an electron transfer between Tb and Ir leading to the valence-state change between  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phases. This first-order transition has a dramatic effect on the lattice, transport properties, and the long-range magnetic order at low temperatures for both Tb and Ir ions.  $\text{Ir}^{5+}$  ion has an electronic configuration of  $5d^4$  ( $J_{\text{eff}} = 0$ ), which is expected to be nonmagnetic. In contrast,  $\text{Ir}^{4+}$  ion with a configuration of  $5d^5$  ( $J_{\text{eff}} = 1/2$ ) favors a long-range magnetic order. For  $x = 0.1$  with  $\text{Tb}^{3+}/\text{Ir}^{5+}$  configuration to the lowest temperature (2 K) investigated in this paper, a spin-glass behavior is observed around 5 K indicating  $\text{Ir}^{5+}$  ( $J_{\text{eff}} = 0$ ) ions act as a spacer reducing the magnetic interactions between  $\text{Tb}^{3+}$  ions. For  $x = 0.5$  with  $\text{Tb}^{4+}/\text{Ir}^{4+}$  configuration below the highest temperature 400 K of this paper, a long-range antiferromagnetic order at  $T_N = 40$  K is observed highlighting the importance of  $\text{Ir}^{4+}$  ( $J_{\text{eff}} = 1/2$ ) ions in promoting the long-range magnetic order of both Tb and Ir ions. For  $0.2 \leq x \leq 0.375$ , a temperature-induced valence-state transition from high-temperature  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase to low-temperature  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase occurs in the temperature range  $180 \text{ K} \leq T \leq 325 \text{ K}$  and the transition temperature increases with  $x$ . The compositional dependence demonstrates the ability to tune the valence state for a critical region of  $x$  that leads to a concurrent change in magnetism and structure. This tuning ability could be employed with suitable strain in thin films to act as a switch as the magnetism is manipulated.

DOI: [10.1103/PhysRevMaterials.6.054410](https://doi.org/10.1103/PhysRevMaterials.6.054410)

### I. INTRODUCTION

The complex interplay among spin-orbit coupling (SOC), on-site Coulomb interaction, noncubic crystal field, and electronic bandwidths leads to rich exotic phenomena and novel physics in  $4d/5d$  transition-metal compounds [1–3]. One important manifestation is the nontrivial  $J_{\text{eff}} = 1/2$  Mott state in  $\text{Sr}_2\text{IrO}_4$  with tetravalent  $\text{Ir}^{4+}$  ( $5d^5$ ) ions, in which the lower  $J_{\text{eff}} = 3/2$  band is fully occupied leaving the higher  $J_{\text{eff}} = 1/2$  band half filled, see Fig. 1(a) [4]. Such a spin-orbit-entangled  $J_{\text{eff}} = 1/2$  scenario can give rise to unique magnetic ground states in  $4d^5$  and  $5d^5$  compounds, such as Kitaev quantum spin liquid [5]. Compounds containing transition-metal ions with  $4d^3$  or  $5d^3$  configuration can host magnetism with magnetic ordering temperatures even above room temperature [6–10]. In contrast to the rich magnetic phenomena for  $4d/5d$  ions with 3 or 5 electrons, a nonmagnetic state is expected for  $J_{\text{eff}} = 0$  compounds in which  $5d$  transition-metal ions have four electrons that are paired in  $J_{\text{eff}} = 3/2$  band, see Fig. 1(b). Despite the theoretical prediction of excitonic magnetism and tremendous experimental efforts, the search for an intrinsic long-range magnetic order in  $J_{\text{eff}} = 0$  compounds is still ongoing [11–31]. One challenge is to distinguish the intrinsic magnetism from effects related to defects or unintentional doping.

The preference of a nonmagnetic ground state for  $d^4$  ions indicates the possibility to switch on/off of magnetism by controlling the charge transfer between  $d^4$  and  $d^3$  or  $d^5$  ions. One approach toward this magnetism control is intermetallic charge transfer driven by temperature, chemical or hydrostatic pressure, or other external stimuli such as electric or magnetic fields. The intermetallic charge transfer is quite rare in transition-metal oxides [32]. However, rare-earth ions Pr, Ce, Tb can stabilize in different oxidization states in perovskite structured oxides, which makes possible charge transfer between these rare-earth and transition-metal ions. One good example of such an intermetallic charge transfer is  $(\text{Pr},\text{Y})_{1-x}\text{Ca}_x\text{CoO}_3$  in which the charge transfer from Pr to Co ions at low temperatures changes the valence state of both Pr and Co ions and induces a metal-insulator transition accompanied with magnetic and structural anomalies [33].

A similar charge transfer was also reported in  $\text{Sr}_2\text{TbRu}_{1-x}\text{Ir}_x\text{O}_6$  [34,35] and  $\text{Ba}_2\text{PrRu}_{1-x}\text{Ir}_x\text{O}_6$  [36,37] where mixing Ru and Ir at the transition metal site induces a charge transfer between the rare-earth and transition-metal ions. This first-order valence-state transition induces a sudden change of lattice and magnetic properties. The effect of  $J_{\text{eff}} = 0$  ions and valence-state change on the magnetic properties is well illustrated by the evolution of magnetic

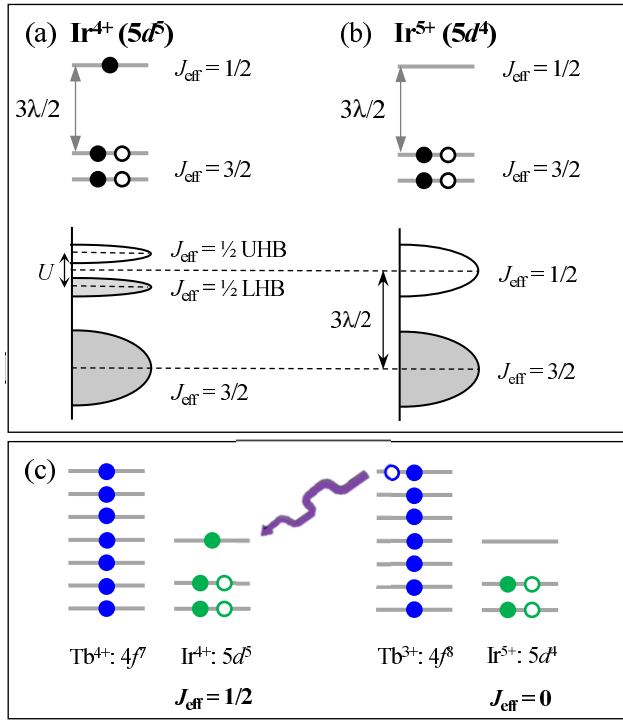


FIG. 1. [(a), (b)] Schematic diagrams of electron filling on  $t_{2g}$  level split by spin-orbit coupling (SOC) for  $\text{Ir}^{4+}$  ( $5d^5$ ) and  $\text{Ir}^{5+}$  ( $5d^4$ ) configurations.  $\lambda$  is the strength of SOC,  $U$  is the on-site Coulomb interaction. UHB: upper Hubbard band. LHB: lower Hubbard band. (c) Electronic configuration of  $\text{Tb}^{4+}/\text{Ir}^{4+}$  and  $\text{Tb}^{3+}/\text{Ir}^{5+}$ . The arrow illustrates that the valence-state transition between the high temperature  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and the low temperature  $\text{Tb}^{4+}/\text{Ir}^{4+}$  is accompanied by an electron transfer between Tb and Ir ions.

properties with Ir substitution in  $\text{Sr}_2\text{TbRu}_{1-x}\text{Ir}_x\text{O}_6$  [35].  $\text{Sr}_2\text{Tb}^{3+}\text{Ru}^{5+}\text{O}_6$  shows a long-range magnetic order at 41 K. With increasing substitution of  $\text{Ru}^{5+}$  ( $4d^3$ ) by  $J_{\text{eff}} = 0$   $\text{Ir}^{5+}$  ( $5d^4$ ) ions, the magnetic order is suppressed and disappears around  $x = 0.8$ . With  $x \geq 0.85$ , the transfer of one electron from  $\text{Tb}^{3+}$  to  $\text{Ru}^{5+}/\text{Ir}^{5+}$  site results in  $\text{Sr}_2\text{Tb}^{4+}(\text{Ru}_{1-x}\text{Ir}_x)^{4+}\text{O}_6$  phase which shows a long range magnetic order around 50 K. This compositional dependence suggests the nonmagnetic nature of  $5d^4$   $\text{Ir}^{5+}$  ( $J_{\text{eff}} = 0$ ) and highlights the importance of  $5d^5$   $\text{Ir}^{4+}$  ( $J_{\text{eff}} = 1/2$ ) in the long-range magnetic order of both rare-earth and transition-metal ions in this system.

Mixing Ba and Sr without disturbing the transition-metal site in  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  was proposed to induce a valence-state transition, which has been studied from the structural point of view at room temperature [38].  $\text{Ba}_2\text{Tb}^{3+}\text{Ir}^{5+}\text{O}_6$  ( $x = 0$ ) crystallizes in a cubic structure with a  $Fm\bar{3}m$  space group [see Fig. 2(a)] and is paramagnetic down to 2 K [39], while  $\text{Sr}_2\text{Tb}^{4+}\text{Ir}^{4+}\text{O}_6$  ( $x = 2$ ) crystallizes in a monoclinic structure with a  $P2_1/n$  space group [see Fig. 2(a)] and undergoes two antiferromagnetic (AFM) transitions at 51 K and 25 K [40,41]. On account of the smaller size of Sr cations, the lower tolerance factor (0.992 for  $\text{Ba}_2\text{TbIrO}_6$  [39] and 0.959 for  $\text{Sr}_2\text{IrO}_6$  [41]) induces the tilting and distortion of the  $\text{TbO}_6/\text{IrO}_6$  octahedra and  $\text{SrO}_{12}$  dodecahedra, which is responsible for the change of the crystal structure from cubic to

monoclinic. With increasing  $x$  in  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$ , the lattice parameter shows a sudden drop around  $x = 0.35$  suggesting a valence-state change from  $\text{Tb}^{3+}/\text{Ir}^{5+}$  to  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase.

Partial substitution of  $\text{Ba}^{2+}$  by  $\text{Sr}^{2+}$  in  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  is expected to reduce the tolerance factor, which measures the stability and distortion of perovskites. The transition from  $\text{Tb}^{3+}/\text{Ir}^{5+}$  to  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase with increasing  $x$  signals that a smaller tolerance factor stabilizes the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase. For most perovskites, the tolerance factor has a positive temperature dependence. This indicates that  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  members near the critical composition  $x = 0.35$  can have a temperature-induced valence-state transition between the high-temperature  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and the low-temperature  $\text{Tb}^{4+}/\text{Ir}^{4+}$  configurations. This thermally induced valence-state transition assisted by chemical pressure has not been studied yet. More importantly, the valence-state transition can have a dramatic effect on the magnetic properties considering the change of the electronic configuration of Ir and might be employed to tune magnetism, as shown in Fig. 1(c). In this paper, we investigate the thermally-driven valence-state transition in  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  with the motivation of understanding its effect on the low-temperature magnetism and possible switchable magnetism using the transition between  $J_{\text{eff}} = 0$  and  $J_{\text{eff}} = 1/2$  at Ir site. The thermally-driven valence-state transition was investigated in the composition range  $0.2 \leq x \leq 0.375$  by measuring x-ray and neutron powder diffraction, resonant inelastic x-ray scattering, magnetic susceptibility, electrical resistivity, and specific heat. The valence-state transition has a dramatic effect on the electronic configuration of Ir and thus the long-range magnetic order at low temperatures for both Tb and Ir ions. A long range magnetic order is observed in  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{4+}\text{Ir}^{4+}\text{O}_6$  but absent in  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{3+}\text{Ir}^{5+}\text{O}_6$ . The valence-state change is associated with a dramatic first-order structural change of the lattice. Consequently, control of the lattice, through strain or pressure, is a potential route to further control and drive the valence state and associated magnetic order. This would yield a switchable mechanism to turn on and off the magnetism, which deserves further investigation.

## II. EXPERIMENTS

Polycrystalline  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  samples ( $x = 0, 0.1, 0.2, 0.325, 0.35, 0.375, 0.4, 0.5,$  and  $2$ ) were synthesized by the solid-state reaction method.  $\text{BaCO}_3$ ,  $\text{SrCO}_3$ ,  $\text{Tb}_4\text{O}_7$ , and  $\text{IrO}_2$  were used as starting materials. The stoichiometric and homogeneous mixture was pelletized and fired from  $1000^\circ\text{C}$  to  $1200^\circ\text{C}$  for up to 6 days with intervening regrindings and repelletizings.

Powder x-ray diffraction (XRD) was carried out on a PANalytical X'Pert Pro MPD powder x-ray diffractometer using  $\text{Cu } K_{\alpha 1}$  radiation. Room-temperature diffractions for all compositions were performed in the range  $10^\circ \leq 2\theta \leq 90^\circ$ . Variable-temperature XRD patterns were collected from room temperature down to 20 K using an Oxford PheniX closed cycle cryostat.

Magnetic susceptibility ( $\chi$ ) was measured in the temperature range  $2 \text{ K} \leq T \leq 380 \text{ K}$  on a Magnetic Property Measurement System (Quantum Design, QD). Specific heat ( $C_p$ ) was measured by the relaxation method between 2 K and

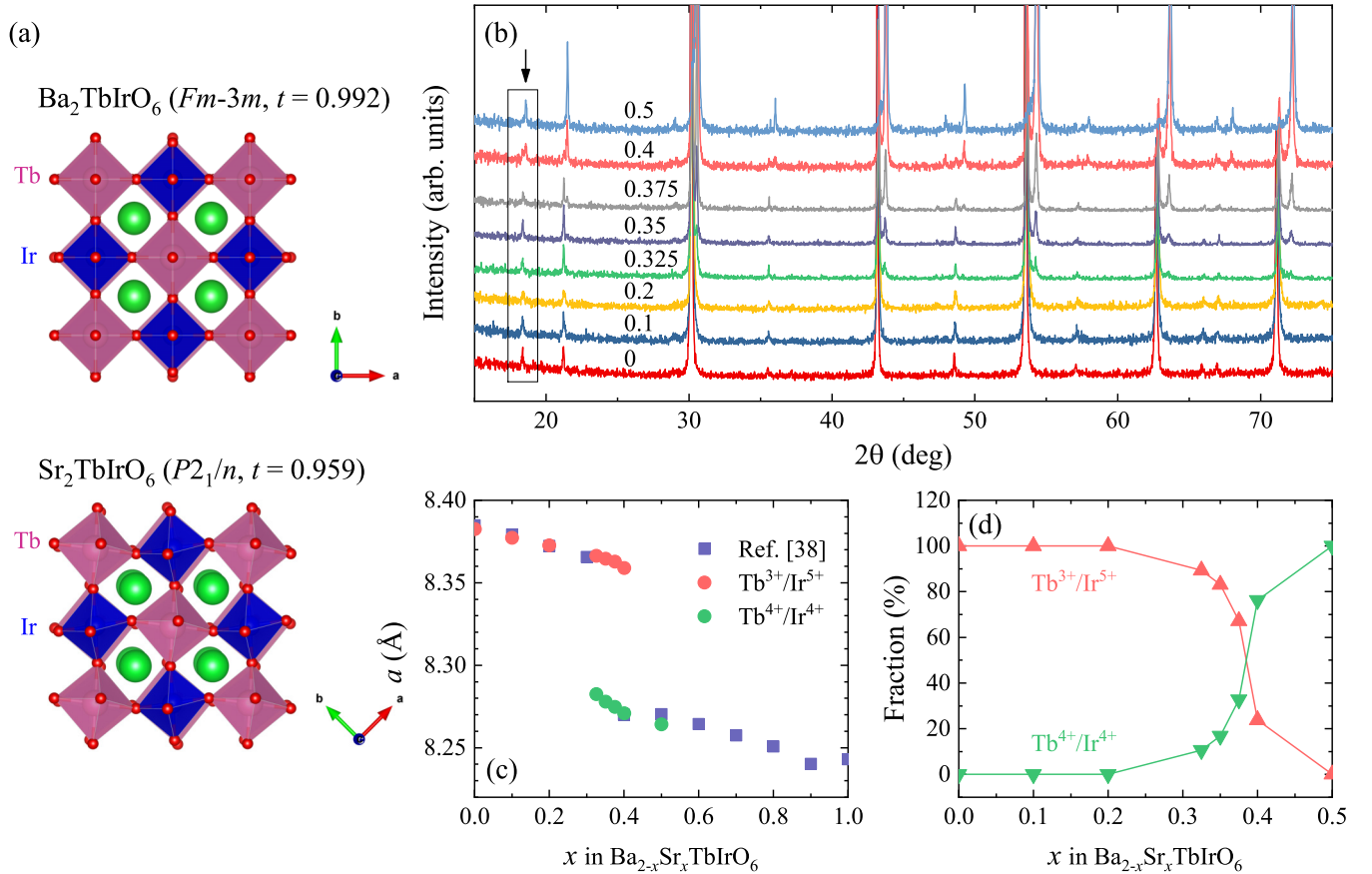


FIG. 2. (a) Crystal structures of  $\text{Ba}_2\text{TbIrO}_6$  and  $\text{Sr}_2\text{TbIrO}_6$  projected in the  $ab$  plane. The space group and tolerance factor  $t$  are also given. (b) Powder x-ray diffraction patterns of  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  collected at room temperature. The superlattice indicating the ordered arrangement of Tb and Ir cations is highlighted by the rectangle. In the composition range plotted, both the  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{3+}\text{Ir}^{5+}\text{O}_6$  and  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{4+}\text{Ir}^{4+}\text{O}_6$  phases are cubic with a space group  $Fm\bar{3}m$ . (d) Evolution with  $x$  of the fraction of  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{3+}\text{Ir}^{5+}\text{O}_6$  and  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{4+}\text{Ir}^{4+}\text{O}_6$  determined from the Rietveld refinements of the diffraction patterns shown in (b) (see Fig. S1 in Supplemental Material [42] for details).

300 K using a QD Physical Property Measurement System (PPMS). Electrical resistivity ( $\rho$ ) was also measured between 100 K and 380 K on the PPMS.

Neutron powder diffraction was performed on the HB-2A Powder Diffractometer at the High Flux Isotope Reactor, Oak Ridge National Laboratory. The sample was contained in an annular Al sample holder to reduce the absorption from Ir. Diffraction patterns were collected from 1.5 K to 250 K in a helium cryostat. Wavelengths of 2.41 Å and 1.54 Å were selected from a vertically focusing germanium monochromator from the Ge113 and Ge115 reflection, respectively.

Resonant inelastic x-ray scattering (RIXS) was performed on the MERIX beamline, 27-ID, at the Advanced Photon Source, Argonne National Laboratory. The finely ground powder samples were contained in a custom Al sample holder with Kapton windows for the three compositions of  $x = 0.1, 0.2, 2.0$ . The incident energy was tuned to the Ir  $L_3$ -edge (11.215 keV) resonant edge to enhance the Ir scattering. The inelastic energy was measured with the use of a Si(844) analyzer. The energy resolution was determined to be 35 meV at full width half maximum, based on fitting the quasielastic line to a charge peak. The scattering plane and incident photon polarization were both horizontal, i.e.,  $\pi$  incident polarization, with the incident beam focused to a size of  $40 \times 25$

microns<sup>2</sup> ( $H \times V$ ) at the sample position. To minimize the elastic scattering, measurements were performed with  $2\theta$  at  $90^\circ$  in horizontal geometry. Temperature-dependent measurements were collected from 5 K to 295 K using a closed cycle refrigerator.

### III. RESULTS AND DISCUSSIONS

#### A. Valence-state transition in $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$ from room-temperature XRD

Figure 2(b) shows the powder XRD patterns of  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  ( $0 \leq x \leq 0.5$ ) collected at room temperature. All these samples were fired in air at  $1200^\circ\text{C}$  for 48 hours. The existence of the superlattice reflection for all compositions at  $2\theta \approx 19^\circ$  indicates an ordered arrangement of Tb and Ir ions. For  $x = 0$ , the Rietveld refinement (see Fig. S1 in Supplemental Material [42]) confirms the cubic structure, and the lattice parameters agree well with previous reports of  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{3+}\text{Ir}^{5+}\text{O}_6$  [38]. With increasing Sr concentration, extra reflections are observed above  $x = 0.325$ . These extra reflections can also be indexed with the cubic  $Fm\bar{3}m$  structure but with a smaller lattice parameter. According to Refs. [38,39], this new cubic phase is  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{4+}\text{Ir}^{4+}\text{O}_6$ .

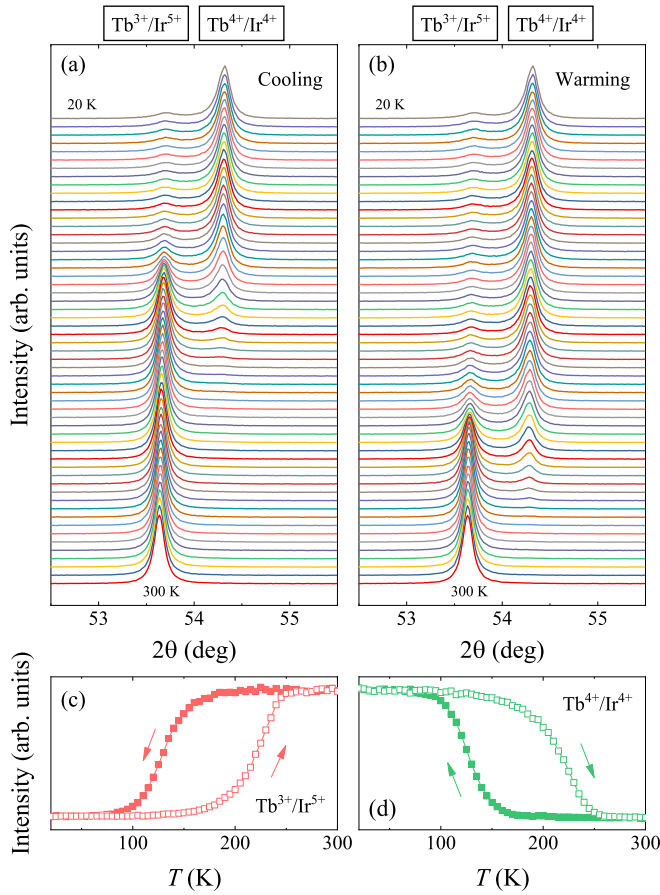


FIG. 3. Evolution with temperature of the cubic (422) peak for  $x = 0.2$  monitored upon (a) cooling and (b) warming in the temperature range  $20 \text{ K} \leq T \leq 300 \text{ K}$ . The peak sitting at  $2\theta \approx 53.6^\circ$  is from the  $\text{Tb}^{3+}/\text{Ir}^{5+}$ , while the one at  $2\theta \approx 54.3^\circ$  from the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase. [(c), (d)] Temperature dependencies of the (422) peak intensity for  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase, respectively. The arrows denote the direction of sweeping temperature.

The intensity of those reflections from  $\text{Tb}^{4+}/\text{Ir}^{4+}$  increases with more Sr substitution. Figure 2(c) shows the evolution with Sr content of the room-temperature lattice parameters. Also plotted are the data from Ref. [38], and the results agree well. With increasing  $x$ , the lattice parameter gradually decreases and shows a sudden drop around  $x_c = 0.325$ , which corresponds to the valence-state transition with electron configuration from  $\text{Tb}^{3+}/\text{Ir}^{5+}$  to  $\text{Tb}^{4+}/\text{Ir}^{4+}$  state. From room-temperature powder XRD patterns, these two cubic phases coexist in the composition range  $0.325 \leq x \leq 0.4$ . Figure 2(d) shows how Sr content affects the fractions of the  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phases in  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$ . The fraction of the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase is dramatically enhanced in  $x = 0.4$  with only a few percentage of residual  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase.

We noticed that the fraction of these two cubic phases depends on the sintering conditions. For example, for  $x = 0.35$ , about 17%wt of  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase was found when the pellet was fired at  $1200^\circ\text{C}$  for 48 hours. This fraction increases to 33%wt when the sample was heat treated at  $1250^\circ\text{C}$  for 48 hours or at  $1200^\circ\text{C}$  for 144 hours (see Fig. S2 in Supplemental

Material for details [42]). This processing dependence might be related to variation of Ir deficiency and/or the oxygen content in the sample after an extended sintering.

### B. Temperature-induced valence-state transition in $\text{Ba}_{1.8}\text{Sr}_{0.2}\text{TbIrO}_6$

The above room-temperature XRD studies show that the doping-induced valence-state transition occurs in a narrow composition range around  $x_c = 0.325$ . As explained in Sec. I, one would expect a thermally driven valence-state transition near  $x_c = 0.325$  considering the temperature dependence of the tolerance factor for most perovskites. To verify this, we investigated the structure, valence state of Ir, magnetic and transport properties, magnetic structure of  $\text{Ba}_{1.8}\text{Sr}_{0.2}\text{TbIrO}_6$  by measuring low-temperature x-ray and neutron powder diffraction, RIXS, magnetic susceptibility, and electrical resistivity. This composition is particularly investigated because it is single phase at room temperature as shown in Fig. 2. Therefore, the appearance of the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase, i.e., the valence-state transition, could be better resolved upon cooling.

*Low-temperature XRD.* The variable-temperature powder XRD patterns were recorded down to 20 K. Figures 3(a) and 3(b) show the evolution with temperature of the (422) reflection upon cooling and warming, respectively. At 300 K, one single peak is observed at  $2\theta \approx 53.6^\circ$ , suggesting that the sample has a single  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase. With decreasing temperature, a weak peak centering around  $2\theta \approx 54.3^\circ$ , which is the (422) reflection of the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase, starts to

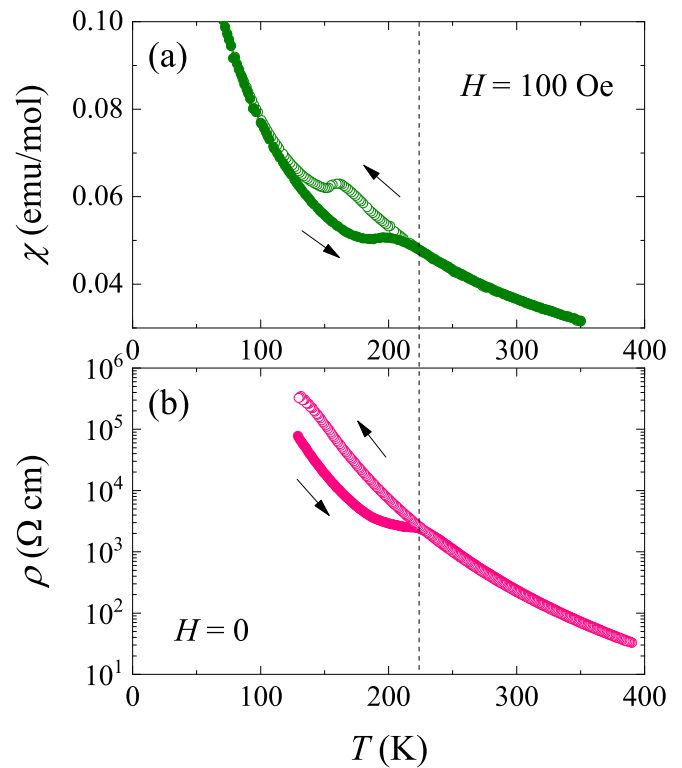


FIG. 4. Temperature dependence of (a) magnetic susceptibility and (b) electrical resistivity for  $x = 0.2$  measured upon warming and cooling as marked by arrows.

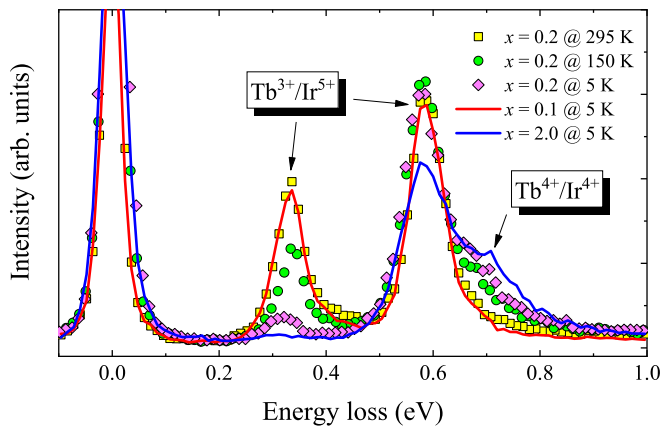


FIG. 5. RIXS spectra as a function of energy loss measured for  $x = 0.2$ . Data collected on  $x = 0.1$  and  $x = 2$  are used as a reference for  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and  $\text{Tb}^{4+}/\text{Ir}^{4+}$  configurations, respectively.

appear below  $T_{v,\downarrow} = 150$  K, as seen in Fig. 3(a). The peak intensity of  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase increases upon further cooling, while the peak intensity of  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase decreases. After dwelling at 20 K for about one hour, the profile of these two peaks were monitored upon warming. The peak intensity of  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase starts to decrease around  $T_{v,\uparrow} = 180$  K while that of  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase starts to increase. Above about 250 K, only the  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase is left. We also performed low-temperature x-ray powder diffraction measurements on  $x = 0.1$  and  $0.5$ . As shown in the Supplemental Material (Fig. S3) [42], we did not observe similar dramatic change in peak intensity.

The appearance of the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase at lower temperatures provides a clear evidence for the temperature-induced valence-state transition from  $\text{Tb}^{3+}/\text{Ir}^{5+}$  to  $\text{Tb}^{4+}/\text{Ir}^{4+}$  configuration in  $\text{Ba}_{1.8}\text{Sr}_{0.2}\text{TbIrO}_6$ . The different transition temperatures  $T_{v,\uparrow} \approx 180$  K and  $T_{v,\downarrow} \approx 150$  K indicate a first-order nature of this transition. The transition is not complete at

20 K, leading to a mixed-phase state due to the polycrystalline nature of our samples.

*Magnetic and transport response to the valence-state transition.* The magnetic susceptibility  $\chi(T)$  as a function of temperature measured in an applied field of 100 Oe is shown in Fig. 4(a). Upon cooling,  $\chi(T)$  shows a step-like change around 170 K. While upon warming, the change occurs around 200 K. The obvious hysteresis in  $\chi(T)$  is consistent with that observed in low-temperature XRD measurements and is a clear evidence for the first-order nature of this valence-state transition. A Curie-Weiss fitting of the magnetic susceptibility above 200 K gives an effective moment of  $9.70 \mu_B$  and a Weiss constant of  $-21$  K. The effective moment is as expected for  $\text{Tb}^{3+}$  and similar to that of  $x = 0.1$  presented later.

Figure 4(b) shows the temperature dependence of the electrical resistivity,  $\rho(T)$ . A resistive behavior is observed below 400 K. Upon cooling,  $\rho(T)$  increases from about  $20 \Omega\text{cm}$  at 400 K to  $3 \times 10^5 \Omega\text{cm}$  at 130 K, below which the sample is too resistive for any reliable data from our machine. When measured on warming,  $\rho(T)$  exhibits a kink around 220 K, where the hysteresis in  $\chi(T)$  occurs. We also measured  $\rho(T)$  for  $x = 0.1$  and  $0.5$  where no valence-state transition is expected (data not shown). We did not see any anomaly as observed in Fig. 4(b).

*Resonant inelastic x-ray scattering.* To verify that the anomalies in the low-temperature XRD study is indeed from the transition between  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phases due to the charge transfer between Tb and Ir ions, we measured RIXS for three  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  samples with  $x = 0.1, 0.2,$  and  $2$ . RIXS is element specific and measures directly transitions between  $d-d$  orbitals; therefore, it is a powerful probe to provide direct information on the valence states of the Ir ions in this compound [43]. At 295 K, as shown in Fig. 5, the spectrum for  $x = 0.2$  exhibits two peaks around 0.3 and 0.6 eV. At lower temperatures, two features are observed: (i) the intensity of the high-energy peak is nearly temperature independent while the low-energy peak is significantly suppressed; (ii) a shoulder around 0.7 eV gradually arises. To explain the

TABLE I. Structural parameters of  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  ( $x = 0.2$ ) at different temperatures obtained from Rietveld refinement of neutron powder diffraction patterns. The coexistence of the  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phases with a reasonable phase fraction allows us to extract the structural parameters of each phase. The space group is  $Fm\bar{3}m$  for both phases. The position of oxygen ( $x, 0, 0$ ) is presented. Refinement of the Ba/Sr ratio found agreement with the nominal composition. The refinement also suggests a stoichiometric amount of oxygen. The oxidation states of Tb and Ir estimated from bond valence sum (BVS) are also shown. For the BVS calculation [44],  $\text{Tb}^{4+}$ ,  $R_0 = 2.018 \text{ \AA}$  and  $B = 0.395$ . For  $\text{Ir}^{4+}$ ,  $R_0 = 1.909 \text{ \AA}$  and  $B = 0.258$ .

	$\text{Tb}^{3+}/\text{Ir}^{5+}$ phase			$\text{Tb}^{4+}/\text{Ir}^{4+}$ phase		
	250 K	165 K	60 K	250 K	165 K	60 K
$a$ ( $\text{\AA}$ )	8.3754(2)	8.3737(2)	8.3715(3)	8.2920(2)	8.2885(2)	8.2885(2)
$x_0$	0.2344(2)	0.2328(4)	0.2329(6)	0.2407(3)	0.2412(3)	0.2412(3)
Ba/Sr-O ( $\text{\AA}$ )	2.96402(10)	2.96405(18)	2.9632(3)	2.93268(10)	2.93132(10)	2.93132(10)
Tb-O ( $\text{\AA}$ )	2.2245(17)	2.237(4)	2.236(6)	2.150(3)	2.145(3)	2.145(3)
BVS $\text{Tb}^{4+}$	3.56	3.45	3.46	4.30	4.35	4.35
Ir-O ( $\text{\AA}$ )	1.9632(17)	1.949(4)	1.950(6)	1.996(3)	1.999(3)	1.999(3)
BVS $\text{Ir}^{4+}$	4.86	5.14	5.12	4.28	4.23	4.23
$\angle\text{Tb-O-Ir}$ (deg)	180	180	180	180	180	180
Fraction	100%	34.7(4)%	22.8(3)%	0%	65.3(6)%	77.2%

evolution of the peak intensity with temperature, the RIXS spectra of  $x = 0.1$  and 2 are also plotted as a reference. At 295 K, the spectrum of  $x = 0.2$  matches well with the  $x = 0.1$  curve, indicating a pure  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase. At lower temperatures, the emergence of the shoulder feature indicates the presence of the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase, which is therefore a very direct evidence for the valence-state transition between  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and  $\text{Tb}^{4+}/\text{Ir}^{4+}$  states. The weak but visible low-energy peak for  $x = 0.2$  at 5 K supports the phase coexistence as deduced from the variable-temperature XRD results.

**Nuclear and magnetic structure from neutron powder diffraction.** Figure 6(a) shows the Rietveld refinement of the neutron powder diffraction pattern for  $x = 0.2$  collected at 60 K, which is consistent with the XRD result including both  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phases below  $T_v$ . Some extra strong reflections are observed at 3 K in Fig. 6(b). The  $d$  spacing proves that this set of magnetic peaks come from the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase. Figure 6(c) shows the temperature dependence of the peak intensity at  $2\theta = 23.8^\circ$ , which confirms the long-range magnetic order at 40 K. The positions of the magnetic reflections are compatible with a propagation vector  $\mathbf{k} = (0, 0, 1)$ . A representational analysis approach was utilized with the aid of the SARAH program [45]. For a propagation vector  $\mathbf{k} = (0, 0, 1)$  and magnetic Tb ions at  $(0.5, 0.5, 0.5)$  and Ir ions at  $(0, 0, 0)$  in the  $Fm\bar{3}m$  space group, there are two symmetry allowed irreducible representations:  $\Gamma_3$  and  $\Gamma_9$  in Kovalevs scheme.  $\Gamma_9$  confines the spins on both Ir and Tb ions to the  $c$  axis and was found to provide the best fit to the data. Any determination of canting away from the  $c$  axis is beyond the limits of the data. As illustrated in the inset to Fig. 6(c), both the magnetic moments of the  $\text{Tb}^{4+}$  and  $\text{Ir}^{4+}$  spins are aligned along the  $c$  direction. The  $\text{Tb}^{4+}$  and  $\text{Ir}^{4+}$  sublattices couple ferromagnetically in the  $ab$  plane, which are further arranged antiferromagnetically along the  $c$  direction. The deduced magnetic moment is  $5.98(4) \mu_B$  for  $\text{Tb}^{4+}$  ion and  $0.5(1) \mu_B$  for  $\text{Ir}^{4+}$  ion. It should be noted that the low signal from Ir makes accurate isolation of the signal challenging and these values are best fits only.

The coexistence of the  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phases with a reasonable phase fraction allows us to obtain the structural parameters of each phase from Rietveld refinement of the neutron powder diffraction patterns collected at different temperatures. As shown in Table I, the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase has a smaller lattice parameter than the  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase. This is consistent with that determined by x-ray powder diffraction. The  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase has an elongated Ir-O bond but shortened Ba-O and Tb-O bonds compared to the  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase. Also shown in Table I are the oxidation states of Tb and Ir estimated from bond valence sum, which in general agree with the expected oxidation states of Tb and Ir ions in each phase.

### C. Evolution with $x$ of the valence-state transition and low-temperature magnetic order of $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$

In order to understand how the valence-state transition evolves with the chemical pressure, we measured  $\chi(T)$  curves of six different  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  samples with  $0.1 \leq x \leq 0.5$ . Figures 7(a)–7(e) show the  $\chi(T)$  data below 100 K. For  $x = 0.1$ ,  $\chi(T)$  increases upon cooling and exhibits a slope change around 5 K, below which  $\chi(T)$  measured in field-

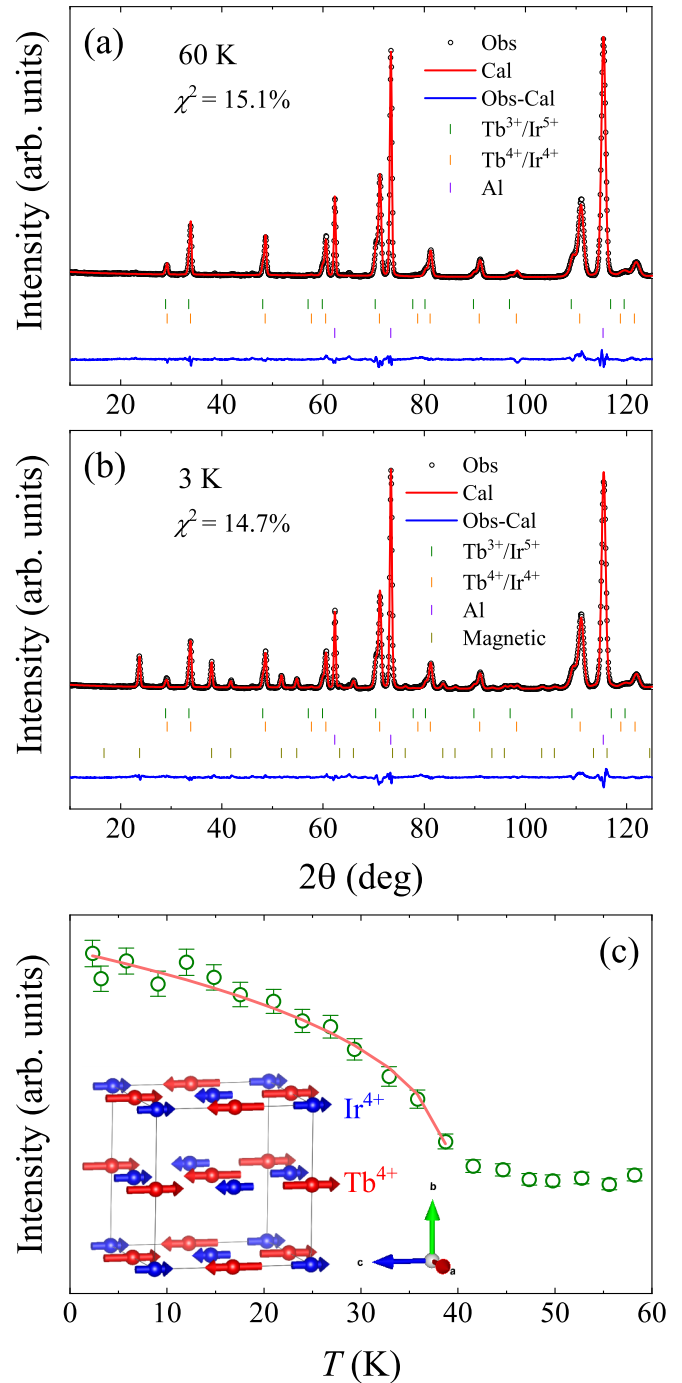


FIG. 6. Neutron powder diffraction performed with a wavelength of  $2.41 \text{ \AA}$  on  $x = 0.2$  at (a) 60 K and (b) 3 K. In panel (a), the vertical-tick marks from top to bottom correspond to  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase (green),  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase (orange), and Al can (blue). The additional set of vertical tick marks in panel (b) at the bottom are the magnetic reflections. (c) Temperature dependence of the peak intensity around  $2\theta = 23.8^\circ$ . The solid line is a fit as described in the text. The inset is the arrangement of  $\text{Tb}^{4+}$  spins (red) and  $\text{Ir}^{4+}$  spins (blue).

cooling (FC) mode starts to diverge from that collected in zero-field cooling (ZFC) mode. For  $x = 0.5$ , the slope change is absent but a kink at 40 K can be well resolved. For other compositions, both the slope change around 5 K and the kink

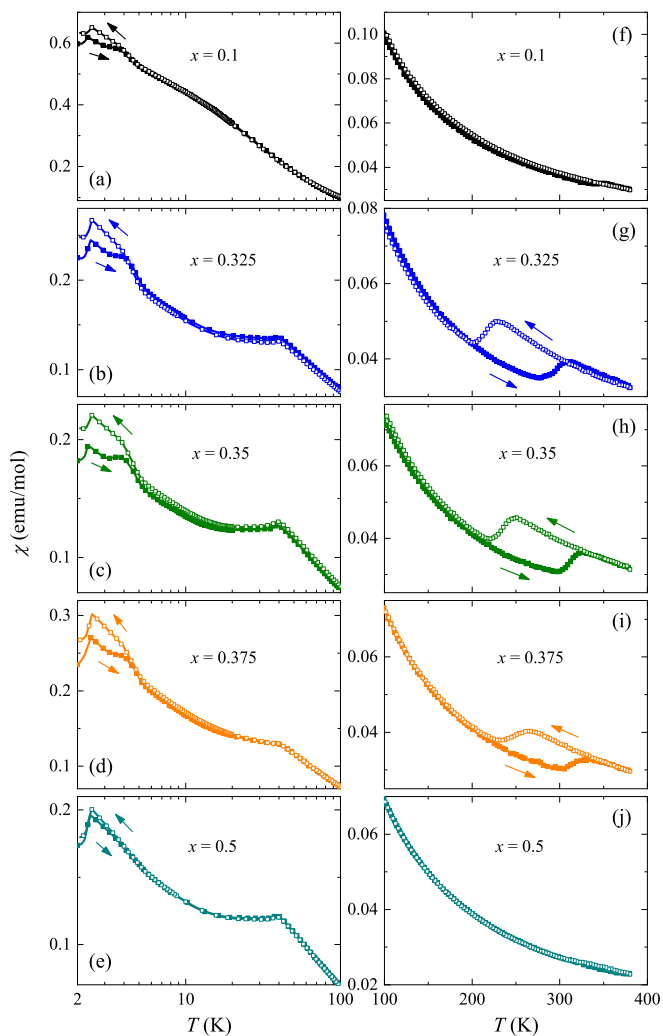


FIG. 7. Temperature dependence of magnetic susceptibility for  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$  series measured in  $H = 100$  Oe.  $x = 0.5$  sample was measured in a magnetic field of 500 Oe. Panels [(a)–(e)] highlight the features at low temperatures. The magnetic susceptibility of  $x = 0.2$  is similar to that of  $x = 0.325$  shown in panel (b). Panels [(f)–(j)] highlight the valence-state transition at high temperatures. Solid (open) symbols are measured in ZFC (FC) process. The drop of the magnetic susceptibility near 3 K comes from a small amount of  $\text{Tb}_2\text{O}_3$  impurity that is present in all samples studied in this paper.

around 40 K are present. A sudden drop of  $\chi(T)$  upon cooling across  $\approx 2.5$  K is observed in all compositions and comes from a small amount of  $\text{Tb}_2\text{O}_3$  impurity [46] that can barely be observed by room-temperature x-ray powder diffraction. At high temperatures, see Figs. 7(f)–7(j), a paramagnetic behavior is observed for  $x = 0.1$  and 0.5 up to 380 K, while a clear first-order transition is observed for  $0.2 \leq x \leq 0.375$  in the temperature range  $180 \text{ K} \leq T \leq 320 \text{ K}$ . The valence-state transition shifts to higher temperatures with increasing  $x$ . A Curie-Weiss fitting of the high-temperature magnetic susceptibility for  $x = 0.1$  gives an effective moment of  $9.74 \mu_B$  and a Weiss constant of  $-16 \text{ K}$ . This effective moment is as expected for  $\text{Tb}^{3+}$  ions and confirms the  $\text{Tb}^{3+}/\text{Ir}^{5+}$  state for  $x = 0.1$ . The Curie-Weiss fitting of  $x = 0.5$  gives an effective moment

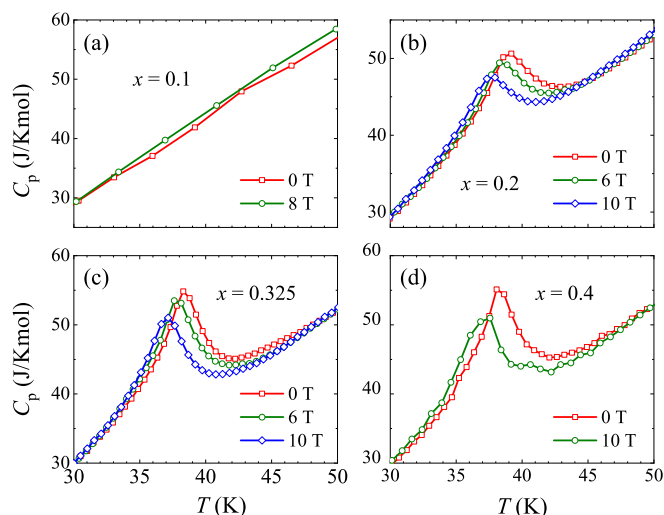


FIG. 8. Specific heat of selected compositions of  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$ .

of  $8.47 \mu_B$  and a Weiss constant of  $-30 \text{ K}$ . This effective moment is slightly larger than the expected value of  $8.13 \mu_B$  for  $\text{Tb}^{4+}/\text{Ir}^{4+}$  configuration.

The above complex temperature dependence of  $\chi(T)$  shows a close relation between the high-temperature valence-state transition with the low-temperature magnetic order. For  $x = 0.1$  with only  $\text{Tb}^{3+}/\text{Ir}^{5+}$  phase, no long-range magnetic order is observed but a spin-glass state is developed below  $\approx 5 \text{ K}$ . For  $x = 0.5$  with only  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase, the kink feature around 40 K is a signature for the long-range AFM order. The absence of the splitting between FC and ZFC  $\chi(T)$  indicates a collinear AFM spin arrangement as confirmed for the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase in  $x = 0.2$  by the neutron diffraction measurements. For other compositions with the valence-state transition, the incomplete transition results in the coexistence of  $\text{Tb}^{3+}/\text{Ir}^{5+}$  and  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phases. Therefore, both the slope change around 5 K and the kink around 40 K are observed in  $\chi(T)$ .

The magnetic order around 40 K can be well resolved in the temperature dependence of specific heat as shown in Fig. 8. For  $x = 0.1$ , no anomaly is observed around either 5 K or 40 K. The former is consistent with the spin-glass origin of the splitting of FC and ZFC curves; the latter confirms the absence of a long-range magnetic order. For other compositions, a  $\lambda$ -type anomaly due to the AFM order of the  $\text{Tb}^{4+}/\text{Ir}^{4+}$  phase shows up near  $T_N = 40 \text{ K}$ . Application of a magnetic field can suppress the magnetic order and reduce  $T_N$ .

#### IV. SUMMARY

In summary, we study the temperature-induced valence-state transition in a narrow composition range  $0.2 \leq x \leq 0.375$  in  $\text{Ba}_{2-x}\text{Sr}_x\text{TbIrO}_6$ . Upon cooling, one electron is transferred from  $\text{Tb}^{3+}$  to  $\text{Ir}^{5+}$  in the  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{3+}\text{Ir}^{5+}\text{O}_6$  phase leading to the formation of the  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{4+}\text{Ir}^{4+}\text{O}_6$  phase. No long-range magnetic order was observed in  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{3+}\text{Ir}^{5+}\text{O}_6$  where the  $\text{Ir}^{5+}$  has an electronic configuration of  $5d^4$  ( $J_{\text{eff}} = 0$ ). The observation of the long-range magnetic order with  $T_N = 40 \text{ K}$  in  $\text{Ba}_{2-x}\text{Sr}_x\text{Tb}^{4+}\text{Ir}^{4+}\text{O}_6$ , at

which both  $\text{Tb}^{4+}$  and  $\text{Ir}^{4+}$  ions order simultaneously, suggests an essential role of  $\text{Ir}^{4+}$  ( $J_{\text{eff}} = 1/2$ ) in mediating the magnetic interactions of Tb ions.

We noticed that the valence-state transition is not complete even at 2 K in our polycrystalline samples. Detailed studies on single crystals are desired to further understand the mechanism and effects of the valence-state transition. The first-order valence-state transition is sensitive to the chemical pressure induced by the size difference between  $\text{Ba}^{2+}$  and  $\text{Sr}^{2+}$  cations. It is thus reasonable to expect that strain field can be effective in controlling the valence-state transition and thus the magnetism. This kind of effect can be better tested in thin films on different substrates or using *in situ* strain fields. In addition, appropriate chemical doping that might induce electrical conductivity also deserves some efforts for novel phenomena accompanying the valence-state transition.

## ACKNOWLEDGMENTS

J.-Q.Y. would like to thank Nandini Trivedi, Patrick Woodward, and Jianshi Zhou for helpful discussions. Work at ORNL was supported by the US Department of Energy, Office of Science, Basic Energy Sciences, Materials Sciences and Engineering Division. Synthesis of powder samples for neutron diffraction measurement and part of the manuscript preparation by Z.Y.Z. were supported by the National Natural Science Foundation of China (Grant No. 52072368). This research used resources at the High Flux Isotope Reactor, a DOE office of Science User Facility operated by the Oak Ridge National Laboratory. This research used resources of the Advanced Photon Source, a U.S. Department of Energy (DOE) Office of Science User Facility operated for the DOE Office of Science by Argonne National Laboratory under Contract No. DE-AC02-06CH11357.

- 
- [1] W. Witczak-Krempa, G. Chen, Y. B. Kim, and L. Balents, *Annu. Rev. Condens. Matter Phys.* **5**, 57 (2014).
- [2] J. G. Rau, E. K.-H. Lee, and H.-Y. Kee, *Annu. Rev. Condens. Matter Phys.* **7**, 195 (2016).
- [3] R. Schaffer, E. K.-H. Lee, B.-J. Yang, and Y. B. Kim, *Rep. Prog. Phys.* **79**, 094504 (2016).
- [4] B. J. Kim, H. Jin, S. J. Moon, J. Y. Kim, B. G. Park, C. S. Leem, J. Yu, T. W. Noh, C. Kim, S. J. Oh, J. H. Park, V. Durairaj, G. Cao, E. Rotenberg, *Phys. Rev. Lett.* **101**, 076402 (2008).
- [5] H. Takagi, T. Takayama, G. Jackeli, G. Khaliullin, and S. E. Nagler, *Nat. Rev. Phys.* **1**, 264 (2019).
- [6] W. Schnelle, B. E. Prasad, C. Felser, M. Jansen, E. V. Komleva, S. V. Streltsov, I. I. Mazin, D. Khalyavin, P. Manuel, S. Pal, D. V. S. Muthu, A. K. Sood, E. S. Klyushina, B. Lake, J. C. Orain, H. Luetkens, *Phys. Rev. B* **103**, 214413 (2021).
- [7] W. Tian, C. Svoboda, M. Ochi, M. Matsuda, H. Cao, J.-G. Cheng, B. Sales, D. Mandrus, R. Arita, N. Trivedi, and J. Q. Yan, *Phys. Rev. B* **92**, 100404(R) (2015).
- [8] C. I. Hiley, D. O. Scanlon, A. A. Sokol, S. M. Woodley, A. M. Ganose, S. Sangiao, J. M. DeTeresa, P. Manuel, D. D. Khalyavin, M. Walker, M. R. Lees, and R. I. Walton, *Phys. Rev. B* **92**, 104413 (2015).
- [9] Y. G. Shi, Y. F. Guo, S. Yu, M. Arai, A. A. Belik, A. Sato, K. Yamaura, E. Takayama-Muromachi, H. F. Tian, H. X. Yang, J. Q. Li, T. Varga, J. F. Mitchell, and S. Okamoto, *Phys. Rev. B* **80**, 161104(R) (2009).
- [10] E. E. Rodriguez, F. Poineau, A. Llobet, B. J. Kennedy, M. Avdeev, G. J. Thorogood, M. L. Carter, R. Seshadri, D. J. Singh, and A. K. Cheetham, *Phys. Rev. Lett.* **106**, 067201 (2011).
- [11] G. Khaliullin, *Phys. Rev. Lett.* **111**, 197201 (2013).
- [12] O. N. Meetei, W. S. Cole, M. Randeria, and N. Trivedi, *Phys. Rev. B* **91**, 054412 (2015).
- [13] G. Cao, T. F. Qi, L. Li, J. Terzic, S. J. Yuan, L. E. DeLong, G. Murthy, and R. K. Kaul, *Phys. Rev. Lett.* **112**, 056402 (2014).
- [14] A. Nag, S. Middey, S. Bhowal, S. K. Panda, R. Mathieu, J. C. Orain, F. Bert, P. Mendels, P. G. Freeman, M. Mansson, H. M. Ronnow, M. Telling, P. K. Biswas, D. Sheptyakov, S. D. Kaushik, V. Siruguri, C. Meneghini, D. D. Sarma, I. Dasgupta, and S. Ray, *Phys. Rev. Lett.* **116**, 097205 (2016).
- [15] T. Dey, A. Maljuk, D. V. Efremov, O. Kataeva, S. Gass, C. G. F. Blum, F. Steckel, D. Gruner, T. Ritschel, A. U. B. Wolter, J. Geck, C. Hess, K. Koepf, J. vandenBrink, S. Wurmehl, and B. Buchner, *Phys. Rev. B* **93**, 014434 (2016).
- [16] S. Bhowal, S. Baidya, I. Dasgupta, and T. Saha-Dasgupta, *Phys. Rev. B* **92**, 121113(R) (2015).
- [17] L. T. Corredor, G. Aslan-Cansever, M. Sturza, K. Manna, A. Maljuk, S. Gass, T. Dey, A. U. B. Wolter, O. Kataeva, A. Zimmermann, M. Geyer, C. G. F. Blum, S. Wurmehl, and B. Buchner, *Phys. Rev. B* **95**, 064418 (2017).
- [18] K. Pajskr, P. Novák, V. Pokorný, J. Kolorenč, R. Arita, and J. Kuneš, *Phys. Rev. B* **93**, 035129 (2016).
- [19] B. Ranjbar, E. Reynolds, P. Kayser, B. J. Kennedy, J. R. Hester, and J. A. Kimpton, *Inorg. Chem.* **54**, 10468 (2015).
- [20] J. Chaloupka and G. Khaliullin, *Phys. Rev. Lett.* **116**, 017203 (2016).
- [21] J. Terzic, H. Zheng, F. Ye, H. D. Zhao, P. Schlottmann, L. E. De Long, S. J. Yuan, and G. Cao, *Phys. Rev. B* **96**, 064436 (2017).
- [22] B. F. Phelan, E. M. Seibel, D. Badoe, Jr., W. Xie, and R. Cava, *Solid State Commun.* **236**, 37 (2016).
- [23] S. Fuchs, T. Dey, G. Aslan-Cansever, A. Maljuk, S. Wurmehl, B. Büchner, and V. Kataev, *Phys. Rev. Lett.* **120**, 237204 (2018).
- [24] Q. Chen, C. Svoboda, Q. Zheng, B. C. Sales, D. G. Mandrus, H. D. Zhou, J.-S. Zhou, D. McComb, M. Randeria, N. Trivedi, and J. Q. Yan, *Phys. Rev. B* **96**, 144423 (2017).
- [25] F. Hammerath, R. Sarkar, S. Kamusella, C. Baines, H. H. Klauss, T. Dey, A. Maljuk, S. Gass, A. U. B. Wolter, H. J. Grafe, S. Wurmehl, and B. Buchner, *Phys. Rev. B* **96**, 165108 (2017).
- [26] Z. Y. Zhao, S. Calder, A. A. Aczel, M. A. McGuire, B. C. Sales, D. G. Mandrus, G. Chen, N. Trivedi, H. D. Zhou, and J.-Q. Yan, *Phys. Rev. B* **93**, 134426 (2016).
- [27] K. K. Wolff, S. Agrestini, A. Tanaka, M. Jansen, and L. H. Tjeng, *Z. Anorg. Allg. Chem.* **643**, 2095 (2017).
- [28] B. E. Prasad, T. Doert, C. Felser, and M. Jansen, *Chem. Eur. J.* **24**, 16762 (2018).
- [29] M. A. Laguna-Marco, E. Arias-Egido, C. Piquer, V. Cuartero, L. Hernández-López, P. Kayser, J. A. Alonso, J. A. T. Barker,



- G. Fabbri, C. A. Escanhoela, and T. Irifune, *Phys. Rev. B* **101**, 014449 (2020).
- [30] N. R. Davies, C. V. Topping, H. Jacobsen, A. J. Princep, F. K. K. Kirschner, M. C. Rahn, M. Bristow, J. G. Vale, I. da Silva, P. J. Baker, Ch. J. Sahle, Y.-F. Guo, D.-Y. Yan, Y.-G. Shi, S. J. Blundell, D. F. McMorrow, and A. T. Boothroyd, *Phys. Rev. B* **99**, 174442 (2019).
- [31] H. Gong, K. Kim, B. H. Kim, B. Kim, J. Kim, and B. Min, *J. Magn. Magn. Mater.* **454**, 66 (2018).
- [32] Y. Long and Y. Shimakawa, *New J. Phys.* **12**, 063029 (2010).
- [33] J. Hejtmánek, E. Šantavá, K. Knížek, M. Maryško, Z. Jiráček, T. Naito, H. Sasaki, and H. Fujishiro, *Phys. Rev. B* **82**, 165107 (2010).
- [34] Q. Zhou, B. J. Kennedy, K. S. Wallwork, M. M. Elcombe, Y. Lee, and T. Vogt, *J. Solid State Chem.* **178**, 2282 (2005).
- [35] Y. Doi, Y. Hinatsu, K.-i. Oikawa, Y. Shimojo, and Y. Morii, *J. Mater. Chem.* **10**, 1731 (2000).
- [36] M. Wakeshima, Y. Izumiyama, Y. Doi, and Y. Hinatsu, *Solid State Commun.* **120**, 273 (2001).
- [37] J. Sannigrahi, D. T. Adroja, C. Ritter, W. Kockelmann, A. D. Hillier, K. S. Knight, A. T. Boothroyd, M. Wakeshima, Y. Hinatsu, J. F. W. Mosselmans, and S. Ramos, *Phys. Rev. B* **99**, 184440 (2019).
- [38] Q. Zhou and B. J. Kennedy, *J. Solid State Chem.* **178**, 3589 (2005).
- [39] M. Wakeshima, D. Harada, and Y. Hinatsu, *J. Mater. Chem.* **10**, 419 (2000).
- [40] D. Harada, M. Wakeshima, Y. Hinatsu, K. Ohoyama, and Y. Yamaguchi, *J. Phys.: Condens. Matter* **12**, 3229 (2000).
- [41] D. Harada, M. Wakeshima, and Y. Hinatsu, *J. Solid State Chem.* **145**, 356 (1999).
- [42] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevMaterials.6.054410> for (1) Rietveld refinement of room-temperature x-ray powder diffraction patterns and phase fractions, (2) Rietveld refinement of room-temperature x-ray powder diffraction patterns of  $x = 0.35$  with different sintering conditions, and (3) low-temperature x-ray powder diffraction patterns for  $x = 0.1$  and  $0.5$ .
- [43] L. J. P. Ament, M. Van Veenendaal, T. P. Devereaux, J. P. Hill, and J. van den Brink, *Rev. Mod. Phys.* **83**, 705 (2011).
- [44] N. Brese and M. O'keeffe, *Acta Crystallogr. Sect. B: Struct. Sci.* **47**, 192 (1991).
- [45] A. Wills, *Phys. B: Condens. Matter* **276-278**, 680 (2000).
- [46] P. Veber, M. Velázquez, G. Gadret, D. Rytz, M. Peltz, and R. Decourt, *CrystEngComm* **17**, 492 (2015).