

Evolution of structural and magnetic properties of multifunctional bismuth iron garnets upon Ca and Y doping

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A multiscale approach is reported to understand the influence of the Ca and Y co-substitution in Bi-rich iron garnet thin films. Recently, it has been demonstrated that site-selective co-substitution of Ca^{2+} and Y^{3+} in bismuth iron garnet (BIG) leads to either *n*- or *p*-type semiconductor behavior. However, the evolution of the structural and magnetic properties of bismuth iron garnet upon doping is still unknown. In the (Ca,Y):BIG, thin films grown by pulsed laser deposition onto $\text{Gd}_3\text{Ga}_5\text{O}_{12}$ substrates, structural investigations confirm the epitaxial growth of doped thin films with high crystallinity and a complete strain relaxation from 20 nm above the film/substrate interface. While x-ray diffraction only evidences a single-phase garnet, the presence of secondary phase nanocrystallites, that are absent in pure BIG grown in similar conditions, is observed by aberration-corrected scanning transmission electron microscopy. These nanocrystallites form in between garnet grains as textured and poorly crystallized hematite. Despite the presence of nanoneedles, Ca and Y co-substitution preserves the giant Faraday rotation of pure BIG and maintains the Curie temperature above 590 K. Only minor energy shifts (80 meV) or small intensity changes (10%) of the Faraday rotation are observed upon doping or annealing and are mainly related to band-gap evolution and cell volume change. Furthermore, the easy magnetization axis rotates towards in the out-of-plane direction upon doping which is also promising for potential applications in spintronics.

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I. INTRODUCTION

Ternary oxide thin films and their doped counterparts present a wide range of functional properties. However, due to the presence of two or more cations, the growth of such films is often a challenging task. It especially concerns the control of the stoichiometry and homogeneity of the cation distribution in the films [1]. The phase diagram is often complexified upon doping and various secondary phases may be favoured to the detriment of the material properties.

Bismuth iron garnet (BIG, $\text{Bi}_3\text{Fe}_5\text{O}_{12}$) is one of the remarkable ternary functional oxide in particular for its magneto-optical properties. Pure BIG possesses, among other properties, a giant Faraday rotation (θ_F) of $-17^\circ \mu\text{m}^{-1}$ at 580 nm [2] and a significant magneto-electrical coupling [3]. BIG films can mostly be synthesized by out-of-equilibrium techniques such as pulsed laser deposition (PLD). While the possibility to grow single-phase BIG by PLD with high structural quality [4] has already been shown, the co-doping of this material might induce a structural disorder that would alter its properties. It is a topic of current interest, as the co-doping of BIG was recently used to develop an additional functionality in this material. Co-substitution of Ca and Y aims at developing a magnetic semiconductor based on BIG.

Ca is expected to induce spin-polarized *p*-type conduction. A complementary concentration of Y is supposed to maintain 2.5 Bi per f.u. to preserve the magnetic properties of BIG. Ca and Y co-substituted BIG, $\text{Bi}_{2.5}\text{Ca}_x\text{Y}_{0.5-x}\text{Fe}_5\text{O}_{12}$ (hereafter $\text{B}(\text{Ca}_x\text{Y}_{0.5-x})\text{IG}$) thin films with $x = \{0.0; 0.1; 0.2; 0.3\}$ grown onto $\text{Gd}_3\text{Ga}_5\text{O}_{12}$ (GGG) (001) substrates have shown an electrical conductivity increase of at least eight orders of magnitude compared to yttrium iron garnet (YIG) [5]. Indeed, it was determined that the resistivity can be modified by either Ca doping or by the presence of oxygen vacancies in $\text{B}(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ films. Furthermore, interfacial and doping effects are known to possibly lead to interesting magnetic anisotropy mechanisms in such transition metal oxide thin films [6–8].

To further understand the influence of the doping on the magnetic properties of the $\text{B}(\text{Ca}_x\text{Y}_{0.5-x})\text{IG}$ thin films, we combine macroscopic and microscopic scale investigations. Indeed, such a study of Bi-rich iron garnets was still lacking and could allow to fine tune their physical properties. In this paper, we first focus on the investigation of the structural and microstructural properties using both x-ray diffraction and electron microscopy techniques. The strain relaxation and the occurrence of secondary phases are thus investigated down to the nanometer scale. Secondly, the magneto-optical and magnetic properties of these doped $\text{B}(\text{Ca}_x\text{Y}_{0.5-x})\text{IG}$ films as a function of the concentration of the dopants were measured using by Faraday spectroscopy and Kerr rotation and discussed with respect to state-of-the-art undoped BIG.

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II. EXPERIMENTAL DETAILS

$\text{Bi}_{2.5}\text{Ca}_x\text{Y}_{0.5-x}\text{Fe}_5\text{O}_{12}$ ($x = 0.0, 0.1, 0.2,$ and 0.3) thin films with thicknesses ranging from 150 to 210 nm were grown by PLD on GGG (001) substrates. The BIG targets substituted with Ca and Y have been prepared from high purity powders (99.99% for Ca precursors and 99.999% for all other precursors) using a standard ceramic processing method. An excimer KrF laser with a wavelength of 248 nm and pulse duration of 20 ns was used for the film deposition. The laser fluency and frequency were maintained at about $1.2 \times 10^{-4} \text{ J m}^{-2}$ and 2 Hz respectively for all the samples of the series. The samples were grown at 1050 K (nominal temperature at the backside of the heater) in a stable oxygen pressure of 0.7 Pa. After the growth, the sample is cooled down in the growth atmosphere at an average rate of 5 K min^{-1} . The films were annealed *ex situ* (post-annealing hereafter) at 870 K in an O_2 flux of 50 ml min^{-1} for 48 hours (TA48) or 96 hours (TA96). The long annealing time was chosen to ensure the complete film oxygenation, a much shorter annealing times at a slightly higher temperature would lead to the same results.

The Faraday rotation spectroscopy and Curie temperature measurements were done using a custom designed experimental magneto-optical (MO) setup described in the work of Deb *et al.* [9]. The applied magnetic field was perpendicular to the film plane (out-of-plane, o-o-p). Faraday rotation spectroscopy measurements were performed at 300 K with applied field values of $\pm 0.5 \text{ T}$ which was sufficient to reach full magnetic saturation. A very similar optical bench was used to determine the magneto-optical Kerr effect, modified for reflection measurements parallel (in-plane, i-p) or perpendicular (o-o-p) to the film plane [10]. In the Kerr setup, the applied magnetic field was either $\pm 0.4 \text{ T}$ o-o-p or $\pm 0.3 \text{ T}$ i-p and the light source was a He-Ne laser with a wavelength of 633 nm. The Curie temperature (T_C) was determined from the Faraday rotation at saturation at 550 nm with the sample mounted in a furnace that can reach 800 K. X-ray diffraction (XRD) was performed on a Seifert four-circle x-ray diffractometer using Cu $K_{\alpha 1}$ wavelength with an angular resolution of 0.001° .

For electron spectromicroscopy studies, cross-sectional electron transparent samples were prepared by focused ion-beam (FIB) on a SCIOS dual-beam platform (FEI-Thermofischer). A JEOL 2010F operated at 100 kV was used for low-magnification bright-field imaging and selected area electron diffraction (SAED). A Nion UltraSTEM 200 with spherical aberration correction (Cs) was used for atomic resolution dark-field imaging and for electron energy-loss spectroscopy (EELS). The microscope was operated at 100 kV with 30 and 50 mrad of convergence and collection angles, respectively. The probe current was approximately 50 pA. The geometric phase analysis (GPA) was performed with the FRWRTOOLS plug in for DIGITALMICROGRAPH [11]. The mask size used was around $1/2a_{\text{GGG}}$ (0.4 nm^{-1}). A set of two identical images oriented at 90° to each other was systematically acquired with a $4096 \times 4096 \text{ px}^2$ resolution to extract in-plane and out-of-plane relative strain maps [12] and therefore to investigate the evolution of the local lattice parameters through the film/substrate interface as well as the strain distribution in the doped BIG films.

A. Results and discussion

As-grown $\text{B}(\text{Ca}_x\text{Y}_{0.5-x})\text{IG}$ films tend to present oxygen off-stoichiometry [5]. Hence, post-annealings under oxygen flux (TA48 and TA96) were performed to aim for oxygen stoichiometric thin films. Figure 1(a) presents typical θ - 2θ x-ray diffraction patterns for as-grown and post-annealed films. All the reflections belong to the garnet phase oriented along [001] with full width at half maximum (FWHM) below 0.15° in 2θ . These FWHM values are 0.05 to 0.10° lower than previous values reported in the literature [13–15], indicating that the investigated films have a lower o-o-p mosaicity. Figure 1(b) displays a zoom on the (004) reflection of the as-grown and post-annealed $\text{B}(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ where the presence of Laue oscillations reveal that these films have a coherent crystal structure over the probed volume, i.e., hundreds of nm^3 . It should be noted that Laue oscillations were only reported for much lower concentrations of Bi, i.e., up to 1.5 Bi per formula unit (f.u.), in Bi-doped YIG systems either grown by PLD [16] or by liquid phase epitaxy [8]. These oscillations are detected for the films without or with a low Ca concentration, i.e., $x \leq 0.1$ per f.u. The absence of Laue oscillations for higher Ca content indicates a higher structural disorder. After TA48 and TA96, all the films keep the same structural features with an identical crystal symmetry as the as-grown films [Figs. 1(a) and 1(b) for $\text{B}(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$]. Contrary to what has been observed for pure BIG films [17], the long annealing times are not detrimental to the doped film quality. The presence of Laue oscillations in combination with the low FWHM confirms the high structural quality of the films based on the XRD results. The epitaxial growth of the films with cube-on-cube relation is confirmed by reflection high-energy electron diffraction (not shown here).

All the as-grown co-substituted films possess a slightly larger or equal o-o-p lattice parameter than stoichiometric BIG, i.e., 1.262 nm [4] [Fig. 1(c)]. *A priori*, this trend is unexpected since Bi^{3+} is larger than Y^{3+} and Ca^{2+} ($r_{\text{Y}^{3+}} = 104 \text{ pm} < r_{\text{Ca}^{2+}} = 114 \text{ pm} < r_{\text{Bi}^{3+}} = 117 \text{ pm}$) [18] and Y-doped BIG was already experimentally reported with a smaller volume [19] assuming a cubic unit cell. Indeed, the in-plane lattice parameter of TA96 $\text{B}(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ was also measured using the (012) reflection ($1.27 \pm 0.2 \text{ nm}$) and it is not significantly different from the out-of-plane lattice parameter. The TA48 films present a decrease of 0.1%–0.3% of their o-o-p lattice parameters compared to their as-grown state indicating the effective filling of the oxygen sublattice. Then, the larger o-o-p lattice parameters of the as-grown films strongly indicate that they are oxygen off-stoichiometric [20]. After TA96, the o-o-p does not significantly decrease within the error margins suggesting that the oxygen sublattice was already completely filled after TA48. For both as-grown and TA48 films, the Ca-doped thin films have a 0.5% larger o-o-p lattice parameter than $\text{B}(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ that indicates the effective substitution of Ca in the garnet lattice [21].

After probing the evolution of the structural properties of the doped BIG films upon annealing and doping at the macroscopic scale, the as-grown and TA96 $\text{B}(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ and as-grown $\text{B}(\text{Ca}_{0.3}\text{Y}_{0.2})\text{IG}$ films were selected to investigate their local structural and chemical characteristics by

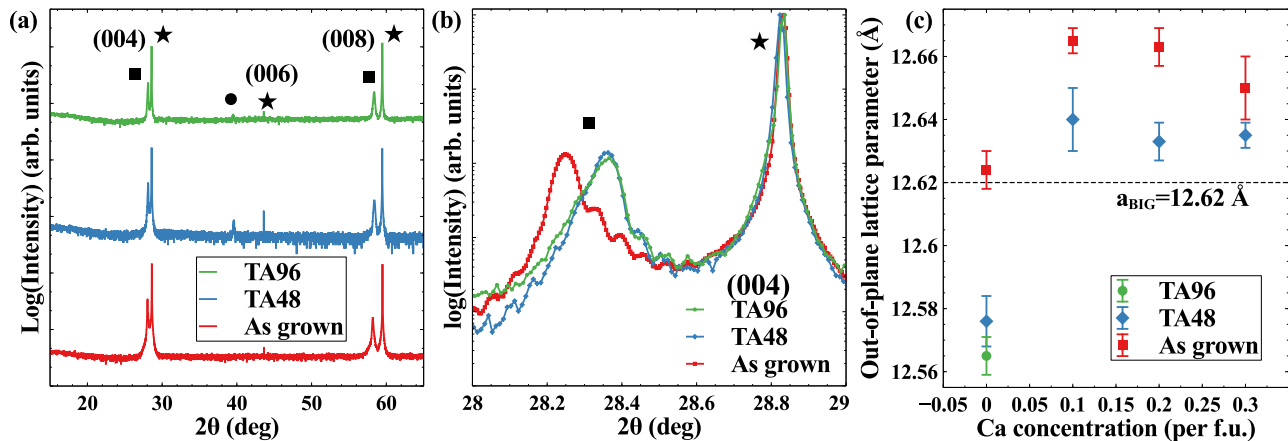


FIG. 1. (a) θ - 2θ XRD scans of $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ before and after TA48 and TA96. The peaks corresponding to $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$, GGG and Pt contact pads are highlighted by a square, a star and a circle, respectively. (b) Zoom of a) on the (004) reflection. (c) Evolution of out-of-plane lattice parameter with the nominal Ca concentration for as-grown, TA48 and TA96 thin films.

electron spectro-microscopy. Figure 2(a) shows a typical low magnification TEM bright-field image of the as-grown $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$. The selected area electron diffraction pattern in Fig. 2(b) confirms the high structural quality of the film. A typical STEM bright-field image displayed in Fig. 2(c) shows, at higher magnification, that $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ exhibits columnar growth, with column widths of ≈ 40 nm that can also be distinguished in Fig. 2(a). Secondary phase nanoneedles are observed mostly in between garnet grains and one of them is highlighted by two white arrowheads in Fig. 2(c). Their widths varies from 5 to 30 nm. They start to form at about 20 nm above the film/substrate interface and reach the surface of the film. The nanocrystallites are still present after TA96 and were observed in all doped BIG films that were investigated using electron microscopy.

The chemical and electronic natures of the nanoneedles were further locally probed by STEM-EELS to determine which phase these nanocrystallites belong to. The O K and Fe $L_{2,3}$ absorption edges of the secondary phase inclusions are compared with those of pure BIG films and of a hematite ($\alpha\text{-Fe}_2\text{O}_3$) reference in Fig. 3(a). The O K edge of $\alpha\text{-Fe}_2\text{O}_3$ consists of the A1 peak at 530 eV and of the B peak at 540 eV

[22]. A1 corresponds to the hybridization of O $2p$ states with Fe $3d$ states while B is assigned to the hybridization of O $2p$ states with Fe $4s$ and $4p$ states [23]. In BIG, the O K edge has an additional peak at 533 eV labeled A2 that corresponds notably to the hybridization of O $2p$ states with Bi $6p$ states [24]. The O K edge of nanoneedles does not possess the A2 peak and the B peak is more intense than the A1 peak, similar to $\alpha\text{-Fe}_2\text{O}_3$. The Bi $M_{4,5}$ edge was also probed (not shown here) in the nanocrystallites and exhibited a large intensity decay. A part of the garnet phase is always probed by EELS along with the nanoneedles as their diameters are thinner than the thickness of the FIB lamella (≈ 70 nm). Thus a residual intensity of the Bi $M_{4,5}$ edge is observed in the nanocrystallites. The absence of the A2 peak, together with the lower Bi $M_{4,5}$ intensity indicate a strong Bi depletion in the nanocrystallites. Besides, the Fe $L_{2,3}$ edges of pure BIG, nanocrystallite and $\alpha\text{-Fe}_2\text{O}_3$ [Fig. 3(a) right panel] show the typical fine structures of Fe^{3+} [25]. These results strongly indicate that the nanocrystallites are mainly composed of a binary ferric oxide.

A typical STEM-HAADF image with atomic-scale resolution is presented in Fig. 3(b) at the boundary between the

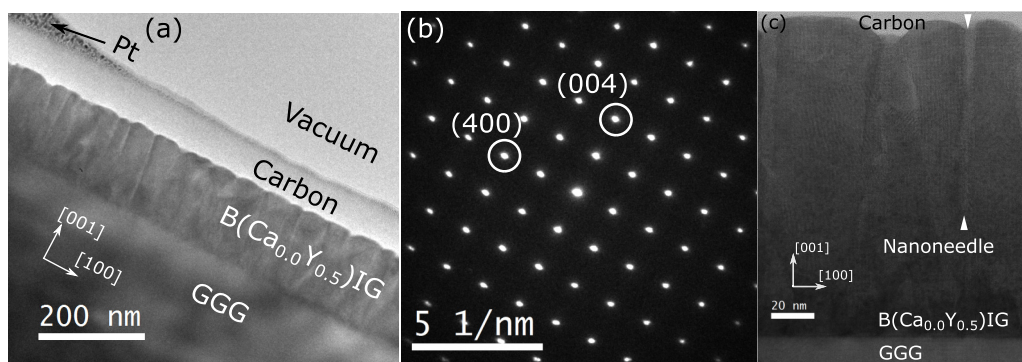


FIG. 2. (a) TEM bright-field low-magnification image of as-grown $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$. (b) Diffraction pattern of a selected area in the film shown in (a). The (004) and (400) reflections are highlighted by white circles. (c) STEM bright-field image of as-grown $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$. The presence of a nanocrystallite is highlighted by two white arrowheads.

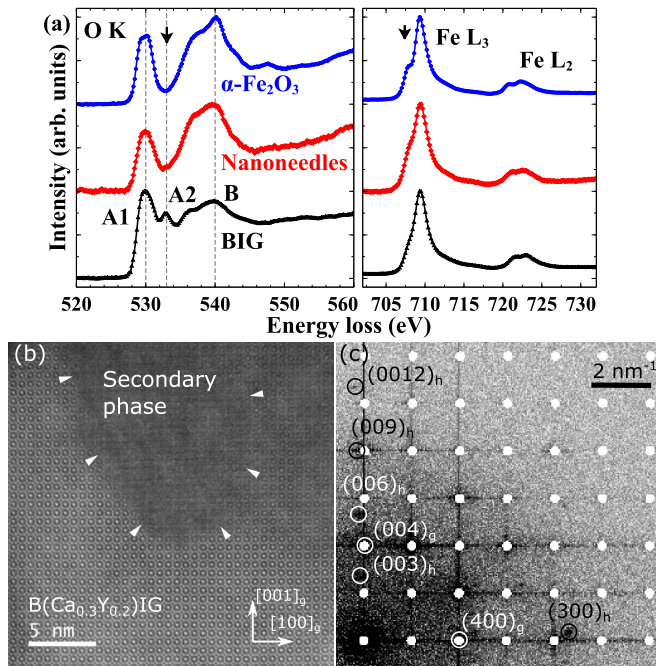


FIG. 3. (a) Sum of O K and Fe L edges spectra acquired in $\alpha\text{-Fe}_2\text{O}_3$, nanocrystallites and BIG in blue, red and black, respectively. The nanocrystallite spectrum is the sum of 1500 spectra of 30 ms each with a dispersion of 0.18 eV ch^{-1} . The two other spectra are the sum of 10 times more spectra acquired the same way. (b) HAADF image of as-grown B(Ca_{0.3}Y_{0.2})IG and a part of nanocrystallite highlighted by white arrowheads. (c) Fourier transform modulus of (b) with inverse grayscale contrasts. The reflections from the nanocrystallite are noted (mnp)_h and those of the garnet are noted (mnp)_g. The interplanar distance of hematite (009)_h = 0.159 nm almost coincides with the (008)_g = 0.158 nm of garnet film.

garnet and the secondary phases. A typical nanocrystallite appears as a low intensity area marked by white arrowheads in line with the observed Bi depletion. Atomic planes of the nanocrystallite are visible but they often appear with a faint contrast or show a structural disorder. It indicates that the ferric iron oxide is rather weakly crystallized and this feature could explain the absence of $\alpha\text{-Fe}_2\text{O}_3$ peaks in the XRD patterns. In Fig. 3(b), the fast Fourier transform (FFT) of Fig. 3(a) exhibits the reflections of the garnet lattice (with a g subscript) and additional reflections (with a h subscript) from the nanocrystallite. In Fig. 3(c), the reflections of the nanocrystallites correspond to a hematite ($R\bar{3}c$) observed along the $[010]_h$ zone axis (hexagonal system). These results, correlated with those obtained by EELS, indicate that the secondary phase has the same structure as that of the $\alpha\text{-Fe}_2\text{O}_3$. As shown in Fig. 3(c), the hematite (009)_h planes (interplanar distance of 0.159 nm) almost coincide with the garnet (008)_g planes (interplanar distance of 0.158 nm) resulting in an interfacial relationship as observed in Fig. 3(b). More generally, it is observed that the $[001]_h$ axis of many observed nanocrystallites makes an angle ranging roughly from 2° to 25° with the $[001]_g$ axis of the garnet phase as derived from the FFTs of STEM-HAADF images. The secondary phase is then made of poorly crystallized hematite nanocrystallites with a textured

orientation with respect to the garnet grains. It is interesting to note that the presence of these nanocrystallites is not detected by conventional macroscopic techniques such as XRD. This underlines the importance of transmission electron spectroscopy studies to provide a local and detailed chemical and crystallographic analysis of such microstructural features of materials. The latter assertion is especially true in the case of Bi-rich thin films that do not exist as bulk and which space group is not yet fully known.

While pure BIG thin films, less than 100 nm thick, can be grown by PLD under similar conditions to those of the (Ca,Y):BIG [4], the occurrence of secondary phase inclusions was already reported in pure BIG in other research groups. These inclusions are most often composed of BiFeO₃ [14,26] and Bi₂Fe₄O₉ [27]. Their formation occurs at high ($\text{PO}_2 > 17 \text{ Pa}$) or low ($\text{PO}_2 < 0.1 \text{ Pa}$) oxygen partial pressure during the growth and they are usually detected directly by XRD. The only example of secondary phase inclusions not detectable by XRD was reported by Kahl *et al.* [15] in BIG grown by PLD on GGG but the structural and chemical natures of these inclusions were not identified.

More generally, secondary phase inclusions are often observed in bismuth iron oxides. A classic example of such well-studied oxide is BiFeO₃ (BFO). As for BIG, the PLD growth of BFO still remains a complex topic and is only possible in a narrow range of partial oxygen pressures. For PO_2 below $\approx 0.7 \text{ Pa}$, inclusions of $\alpha\text{-Fe}_2\text{O}_3$, maghemite ($\gamma\text{-Fe}_2\text{O}_3$) or more scarcely magnetite (Fe_3O_4) form while for PO_2 above ca. 2.7 Pa the formation of Bi₂O₃ occurs [28–30]. These effects originate mainly from the high volatility of Bi ions [29] and it is likely that the same mechanism is present in the growth of BIG. In some cases, these secondary phase inclusions can be nanometric in size and may remain undetectable by conventional macroscopic techniques such as XRD [31]. In the case of BFO, the addition of dopants change the PLD growth conditions necessary to obtain single-phase thin films [31–33]. By comparison with the growth characteristics of BFO, it can thus be concluded that the unexpected formation of $\alpha\text{-Fe}_2\text{O}_3$ in B(Ca_xY_{0.5-x})IG thin films originate from an insufficient oxidation during growth.

GPA were performed to determine the local lattice parameter variations in the garnet phase, in both i-p and o-o-p directions, especially at the film/substrate interface. A typical STEM-HAADF image of as-grown B(Ca_{0.0}Y_{0.5})IG used for the GPA is shown in Fig. 4(a). The extracted i-p and o-o-p relative strain maps of the film are displayed in Figs. 4(b) and 4(c), respectively. Extracted profiles from both the o-o-p and i-p strain maps of as-grown and TA96 B(Ca_{0.0}Y_{0.5})IG are displayed in Figs. 4(d) and 4(e), respectively. For both TA96 and as-grown films, the strain relaxation mechanisms are similar. The compressive strain of about 2% induced by the substrate is fully relaxed on $\approx 20 \text{ nm}$ from the film/substrate interface by in-plane pseudo-periodic dislocations. This strain relaxation mechanism is analogous to that of BIG on substituted-GGG [4]. For the as-grown film, the relaxed lattice parameters are 1.269 nm i-p and 1.261 nm o-o-p. The i-p strain is relaxed over a length of 15 nm i-p by approximately one dislocation every 18 nm. For the TA96 film, the relaxed lattice parameters are 1.263 nm i-p and 1.268 nm o-o-p. The i-p strain is relaxed over a length of 21 nm i-p by approximately one dislocation

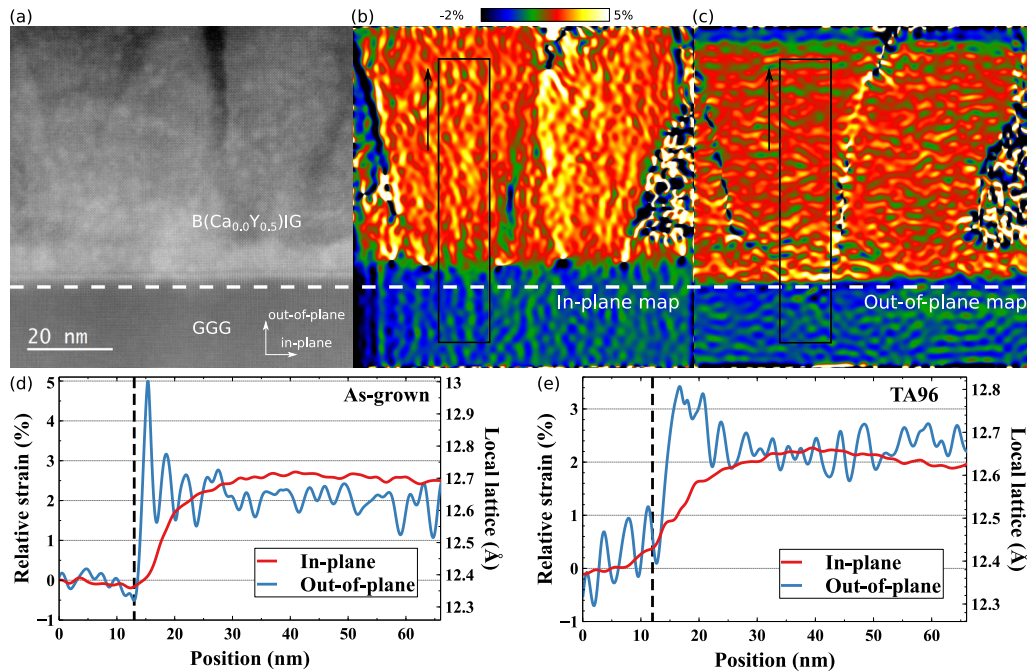


FIG. 4. (a) High-resolution HAADF image of the film substrate/interface for as-grown $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$. Extracted in-plane (b) and out-of-plane (c) relative strain maps from GPA on a) where the substrate is taken as reference. (d) Extracted profiles from the i-p and o-o-p relative strain maps of (b) and (c), respectively. The black boxes in (b) and (c) indicate the profile extraction regions. (e) Extracted profiles for TA96 $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ from the i-p and o-o-p relative strain maps derived from GPA. The black dashed line indicates the position of the film/substrate interface.

every 27 nm. These results are consistent with those obtained by XRD where a lower strain is expected in TA96 $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$. For both TA96 and as-grown films, the o-o-p lattice parameter is fully relaxed right from the film/substrate interface contrary to the i-p lattice parameter. This difference of relaxation lengths induces locally a tetragonal deformation of the unit cell in the strained region with a o-o-p/i-p lattice parameters ratio of up to 2% for both as-grown and TA96 films. In the relaxed region the unit cell of the films remains cubic supporting the assumption that the unit cell volume can be derived from the o-o-p lattice parameter. The films are structurally homogeneous over almost their whole thickness and the annealing tends to decrease the density of misfit dislocations. The presence of a textured secondary phase in the upper part of the film does not play a role in the relaxation of the film.

In the following, the results obtained by Faraday spectroscopy and Kerr rotation are discussed, particularly in relation to the structural and microstructural properties presented above. The Faraday rotation spectra between 1.5 and 4 eV were acquired for as-grown and TA48 $B(\text{Ca}_x\text{Y}_{0.5-x})\text{IG}$ as shown in Figs. 5(a) and 5(b), respectively. All the spectra of the substituted garnets show overall spectral shapes and intensities similar to the Faraday rotation spectrum of BIG despite the presence of the secondary phase inclusions in the doped films. Except for $B(\text{Ca}_{0.3}\text{Y}_{0.2})\text{IG}$, an increase of the Faraday rotation intensity between 8% to 14% is observed upon annealing for the substituted thin films. The effect of this post-annealing could not be verified for pure BIG, since the garnet phase in undoped film is not stable

under TA48 (870 K) but at least the θ_F does not evolve upon annealing for 48 hours at 625 K under an O_2 flux of 50 ml min^{-1} . In addition, a blue shift is also observed for Ca and Y co-substituted BIG MO spectra.

In BIG, the Faraday rotation (intensity, fine structures) is driven by magneto-optical transitions from the ground state to the excited states mainly corresponding to the different Fe sublattices. There are three cation sublattices in the garnet structure. The Bi sites are surrounded by eight O anions forming a dodecahedral (T_h) cage while the Fe sites are surrounded by either four or six O anions forming tetrahedral (T_d) or octahedral cages (O^h), respectively. Charge-transfer transitions from filled states with a strong O 2p character to Fe 3d empty states are believed to be responsible for the MO effects in the visible range in iron garnets [34,35]. These states are both split by a strong exchange interaction and the Fe 3d states are further split by the spin-orbit coupling. The Bi 6p states are hybridized with empty and filled Fe 3d states and with filled O 2p states [34–37]. This hybridization leads to a strong increase of the spin-orbit coupling for both O 2p and Fe 3d states that yields an enhancement of the Faraday effect.

To be more quantitative the commonly accepted model to explain the MO spectrum of BIG was applied. This model is based on two magneto-optical transitions (so-called diamagnetic) from a degenerate filled state to Fe empty states split by the exchange interaction and the effective spin-orbit induced by hybridization with Bi 6p empty states [9]. A diamagnetic transition is parametrized by a transition energy (E), an energy splitting (Δ), a line-width (Γ) and the product (Nf) of the

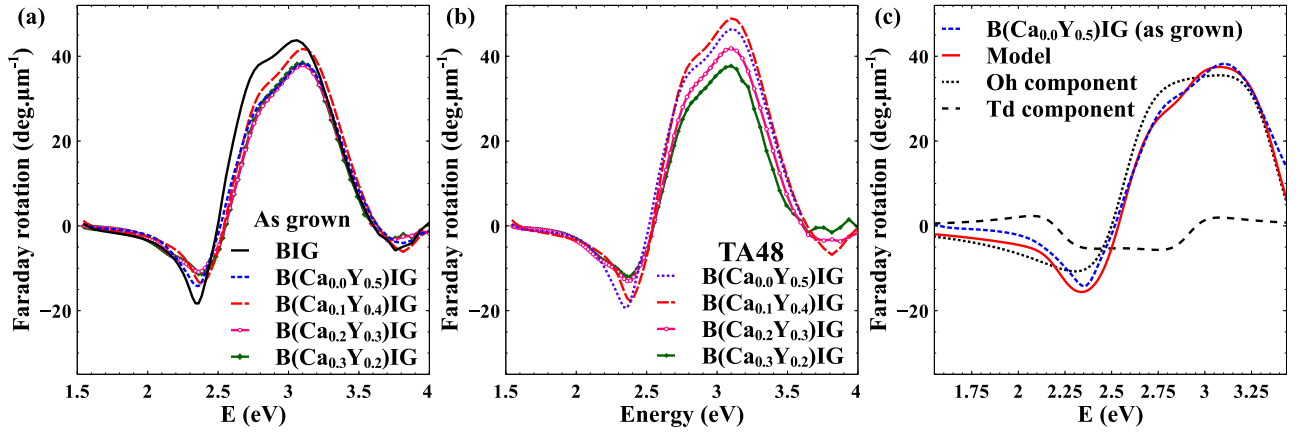


FIG. 5. (a) Faraday rotation spectra for as grown thin films. (b) Faraday rotation spectra for TA48 thin films. (c) Experimental Faraday rotation spectrum of $B(\text{Ca}_{0.0}\text{Y}_{0.3})\text{IG}$ (blue dashed line) with its corresponding theoretical model (red line). The black dotted and dashed lines correspond to the octahedral and tetrahedral components of the theoretical model, respectively.

number of active centers (N) and oscillator strength (f). Γ and Δ drive the shape and the intensity of the transition while Nf is only linked to its intensity. The transitions at around $E_{\text{Oh}} = 3.0$ eV and $E_{\text{Td}} = 2.5$ eV are associated with the Fe Oh and Fe Td sublattices, respectively [9,38]. A typical fit result is presented in Fig. 5(c) and the extracted parameters (Nf and E) are shown in Table I. One should note that the least-square fitting of Td transition yields noisier results due to its lower intensity, therefore the main interpretation is based on the Oh transition parameters in the following. A blue shift of $\Delta E_{r,\text{Oh}} = 60$ meV with respect to BIG is observed for $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ while for Ca containing films a shift of $\Delta E_{\text{Oh}} = 80$ meV is determined. Significant changes in Nf are also obtained after annealing and are discussed below especially concerning the Oh transition.

A blue shift of the MO transitions was observed in $\text{Y}_{3-x}\text{Bi}_x\text{Fe}_5\text{O}_{12}$ thin films with decreasing Bi content [16]. This feature can be explained by the band gap increase from BIG (2.3 eV [39]) to YIG (3.0 eV [40]). The blue shift of MO spectra for Ca and Y co-substituted BIG confirms the lower concentration of Bi with respect to pure BIG [9]. The transition intensity Nf of as-grown films is lower than the one of BIG as this quantity scales with the Bi concentration. However, for TA48 films Nf_{Oh} increases and it can be clearly seen in Fig. 5(b) that the Faraday

rotation even reaches higher values for $B(\text{Ca}_{0.1}\text{Y}_{0.4})\text{IG}$ and $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ than that of pure BIG. These high Nf_{Oh} values can be related to the decrease of the unit cell volume upon annealing which increases the hybridization between the Bi, O and Fe electronic states. As-grown thin films might also present Fe^{2+} due to oxygen off-stoichiometry [5]. This could reduce the magneto-optical effects while in TA48 films all Fe should tend to 3+ valence yielding an enhanced Faraday rotation.

Its high T_C is an important asset of the BIG especially for ambient temperature applications and was therefore systematically probed in the doped BIG. The variations of T_C for the $B(\text{Ca}_x\text{Y}_{0.5-x})\text{IG}$ series are displayed in Fig. 6(a) as a function of the nominal stoichiometry and in Fig. 6(b) as a function of the o-o-p lattice parameter. The $B(\text{Ca}_x\text{Y}_{0.5-x})\text{IG}$ films have T_C between 602 to 658 K. This behavior is expected since the T_C of the parent phases ranges from 560 K for YIG to 660 K for BIG with a monotonous change within $\text{Y}_{3-x}\text{Bi}_x\text{Fe}_5\text{O}_{12}$ thin films [16]. The volume of the unit cell is expected to have the strongest influence on the T_C . When the unit cell volume decreases, the O 2p and Fe 3d orbitals are more overlapped and the superexchange interaction is therefore enhanced resulting in a direct increase of the T_C . Besides, the evolution of the Fe-O-Fe bonding angles also influences the superexchange interaction [41]. In particular,

TABLE I. Transition energies and Nf values of the Oh and Td components of the fitted theoretical model before and after TA48 for all thin films. The transitions energies and Nf values of BIG are also displayed for comparison.

	As-grown				TA48			
	Nf (10^{17}cm^{-3})		Energy (eV)		Nf (10^{17}cm^{-3})		Energy (eV)	
	Oh	Td	Oh	Td	Oh	Td	Oh	Td
BIG	3.89	1.11	2.91	2.47				
$B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$	3.47	0.38	2.97	2.57	4.04	0.72	2.96	2.52
$B(\text{Ca}_{0.1}\text{Y}_{0.4})\text{IG}$	3.67	0.25	2.99	2.61	4.25	0.31	2.99	2.61
$B(\text{Ca}_{0.2}\text{Y}_{0.3})\text{IG}$	3.57	0.21	2.99	2.56	3.98	0.33	2.98	2.55
$B(\text{Ca}_{0.3}\text{Y}_{0.2})\text{IG}$	3.75	0.34	2.99	2.63	4.25	0.60	2.96	2.57

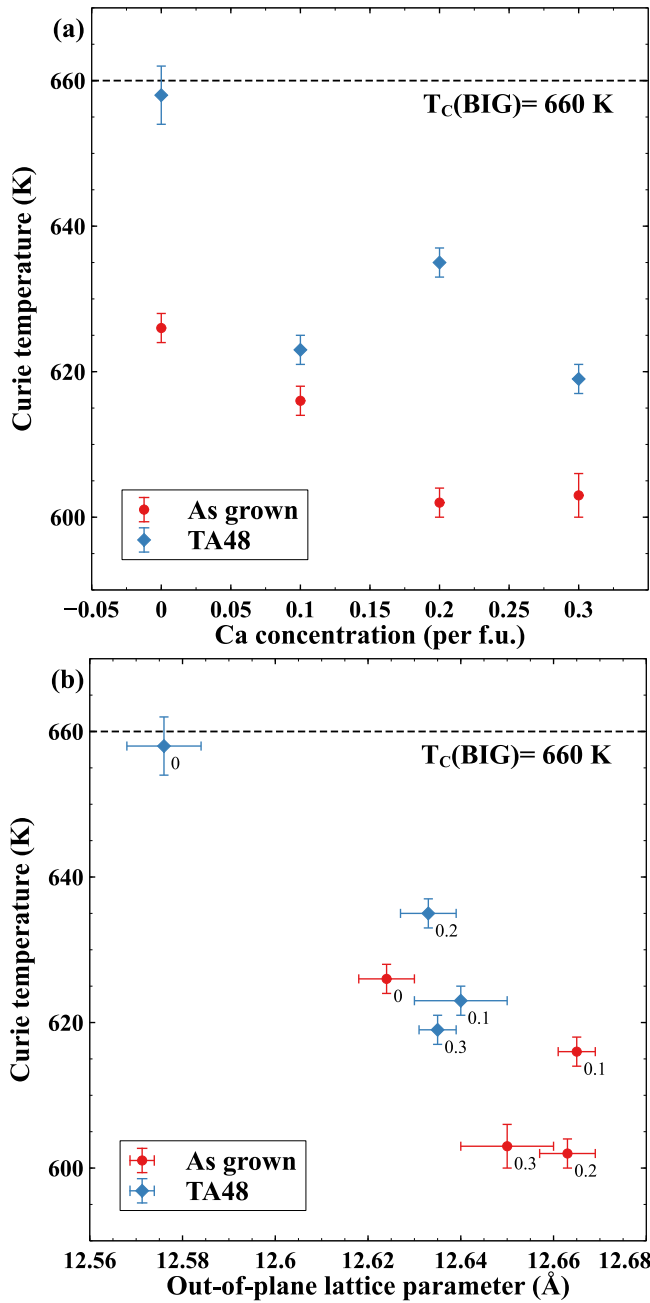


FIG. 6. (a) T_C as a function of the Ca concentration for all thin films before and after TA48. (b) T_C as a function of the o-o-p lattice parameter for all thin films before and after TA48. The corresponding Ca concentration is indicated at the bottom right of every point. The T_C of BIG is indicated by a dashed line for comparison.

these angles may change with the lattice parameters and might have an additional effect on the T_C . These results confirm that the magnetism in $B(\text{Ca}_x\text{Y}_{0.5-x})\text{IG}$ remains robust despite the Ca and Y co-substitution, the presence of minor secondary phase inclusions and, in the case of as-grown thin films, the oxygen off-stoichiometry.

The Kerr rotation was also measured to obtain a better understanding of the magnetic properties and identify a possible effect of the presence of the nanoneedles. For $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$, $B(\text{Ca}_{0.3}\text{Y}_{0.2})\text{IG}$ and BIG, the longitudinal (i-p direction)

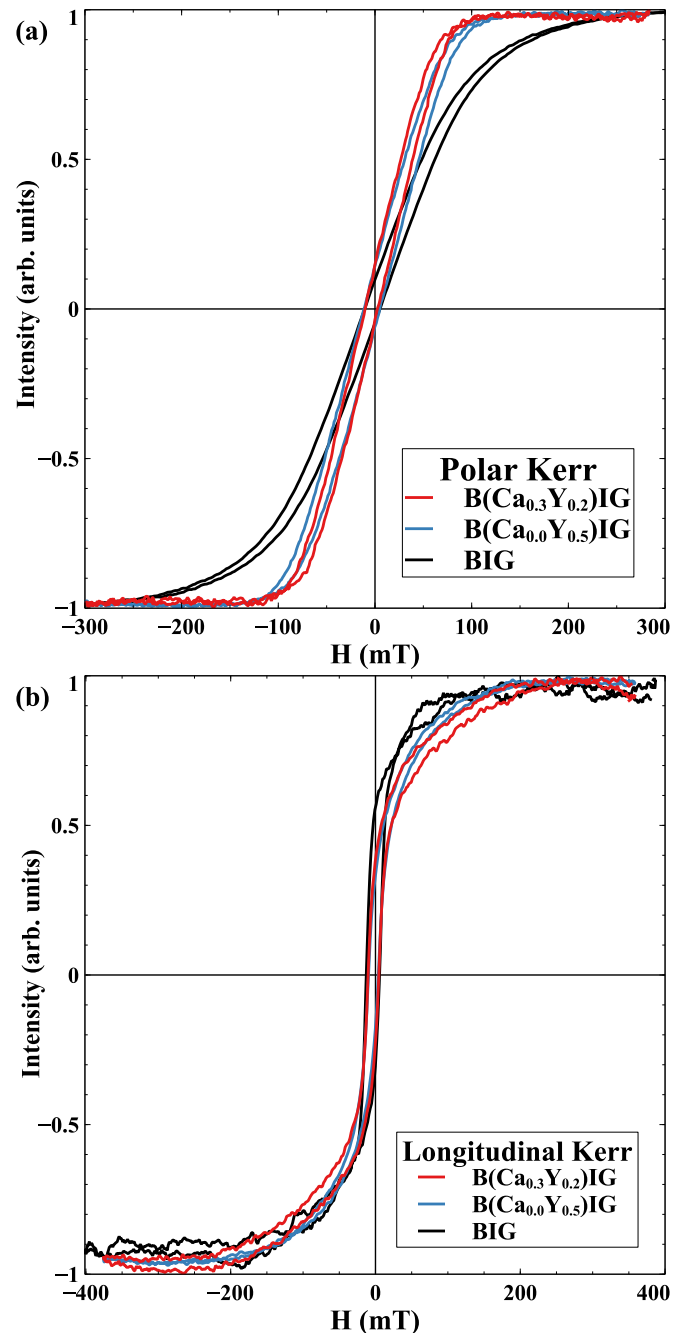


FIG. 7. (a) Kerr hysteresis cycles of BIG, $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ and $B(\text{Ca}_{0.3}\text{Y}_{0.2})\text{IG}$ in polar (o-o-p) configuration. (b) Kerr hysteresis cycles of BIG, $B(\text{Ca}_{0.0}\text{Y}_{0.5})\text{IG}$ and $B(\text{Ca}_{0.3}\text{Y}_{0.2})\text{IG}$ in longitudinal (i-p) configuration.

and polar (o-o-p direction) M-O Kerr effect were measured [Figs. 7(a) and 7(b), respectively]. The o-o-p saturation field ranges from 130 mT for $B(\text{Ca}_{0.3}\text{Y}_{0.2})\text{IG}$ to more than 300 mT for BIG. The i-p saturation field varies from 120 mT for BIG to 230 mT for $B(\text{Ca}_{0.3}\text{Y}_{0.2})\text{IG}$. For a few hundreds of nanometers thick thin films of BIG, its easy magnetization axis is parallel to the i-p direction [26,42]. However, for Ca and Y co-substituted BIG films, the easy magnetization axis changes from i-p to o-o-p. Considering the saturation magnetization of 10^5 A m^{-1} for this film, its perpendicular anisotropy can be

roughly estimated to be $\frac{M_s H_s}{2} = 7 \times 10^4 \text{ J m}^{-3}$. To understand the origin of this phenomenon, different contributions in the magnetic anisotropy compete and should be considered. First, the substrate-induced strain should be taken in account. For all films, the GGG substrate applies a compressive strain. This strain is at the origin of a negative magnetoelastic anisotropy that tends to put the observed magnetization in the film plane [8] and is therefore not responsible for the change in anisotropy. Similarly, the shape anisotropy is negative for a thin film and is not responsible for the o-o-p anisotropy. Another possibility resides in a change of the growth anisotropy upon doping as evidenced in Bi-substituted YIG [8]. The garnet thin films have nonequivalent dodecahedral sites due to the preferential direction induced by epitaxial growth [43]. A Bi population difference between these nonequivalent sites can yield the growth anisotropy that tends to rotate the easy magnetization axis in the o-o-p direction [44,45]. However, in BIG, all the dodecahedral sites are filled and the magnetization stays in-plane. Hence, in Ca and Y co-substituted BIG, a growth anisotropy might also contribute to the change of easy magnetization axis despite the absence of evidence to support this explanation in the present work. Assuming that the presence of nanoneedles at the grain boundaries limits the typical size of the magnetic domains to that of a garnet grain, the dipolar coupling between the grains may also induce the observed change in anisotropy [46]. It is also known that a columnar microstructure of magnetic thin films significantly enhances their perpendicular anisotropy [47]. Finally, an additional anisotropy could arise due to the presence of the oriented nanocrystallites. The hematite nanocrystallites are textured antiferromagnets and their interaction with the main ferrimagnetic garnet phase could yield an exchange anisotropy [48–50]. To probe a possible exchange bias due to the presence of the weakly crystallized secondary phase, classical field cooling experiments were performed in two configurations. On the one hand, Faraday rotation measurements were done after cooling from 700 to 300 K with an applied magnetic field perpendicular to the film plane. On the other hand, vibrating sample magnetometer was used to measure hysteresis curves after field cooling from 300 to 10 K in a magnetic field applied parallel to the film plane. In either configuration, no unambiguous exchange bias signature was detected.

III. CONCLUSION

Thin conducting films of $\text{Bi}_{2.5}\text{Ca}_x\text{Y}_{0.5-x}\text{Fe}_5\text{O}_{12}$ ($x=0.0; 0.1; 0.2; 0.3$) were grown on GGG (001) substrates as potential candidates for magnetic semiconductors at room temperature [5]. Detailed macroscopic and microscopic structural properties, strain relaxation, magneto-optical and magnetic properties of these doped $\text{B}(\text{Ca}_x\text{Y}_{0.5-x})\text{IG}$ films were investigated before and after thermal annealing under oxidizing conditions as a function of dopant concentration. The films show high structural quality evidenced by XRD with cube-on-cube epitaxial growth. Post-growth annealing in oxidizing atmosphere allowed the filling of the oxygen lattice while preserving structural properties of the films and decreasing the density of dislocations. Accordingly, a decrease of 0.1% to 0.3% of the o-o-p lattice parameter was observed upon annealing. Faraday rotation spectroscopy in the visible range reveals similar spectral signature to that of BIG. The Faraday rotation intensity increased upon annealing and reached up to 12% above that of undoped BIG over the studied spectral range (1.5 to 4 eV). The magnetic ordering remained robust upon doping and annealing with T_C of up to 660 K. As expected, the Curie temperature increased after annealing. The easy magnetization axis of the thin films goes from i-p to o-o-p as a possible effect of either the Ca and Y substitution on Bi site or the columnar microstructure of the thin films. The presence of a minor secondary phase between perfectly crystallized garnet grains was evidenced solely by (S)TEM while it was not detectable by XRD. After a detailed study by Cs-STEM/EELS, this secondary phase is identified as weakly crystallized and weakly textured $\alpha\text{-Fe}_2\text{O}_3$ nanoneedles. Oxygen-deficient atmosphere during the growth could be at the origin of the appearance of these nanoneedles. Despite the presence of the nanoneedles all the films exhibit state-of-the-art magnetic and magneto-optical properties.

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