

Band gap evolution in Ruddlesden-Popper phases

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We investigate the variation of the band gap across the Ruddlesden-Popper (RP) series ($A_{n+1}B_nX_{3n+1}$) in model chalcogenide, oxide, and halide materials to understand the factors influencing the band gap evolution with n . In contrast to the oxides and halides, we find the band gaps of the chalcogenides evolve differently with the thickness of the perovskite blocks in these natural superlattices. We show that octahedral rotations (i.e., deviation of the B-X-B bond angles from 180°) and quantum confinement effects compete to decide the band gap evolution of RP phases. The insights gained here will allow us to rationally design layered perovskite phases for electronics and optoelectronics.

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Perovskites host a variety of emergent phenomena such as colossal magnetoresistance [1–4], ferroelectricity [5–7], and superconductivity [8,9], and offer great structural and chemical flexibility to tune physical properties. The perovskite structure, with a chemical formula of ABX_3 , consists of an octahedrally coordinated cation (B-site) connected by the corners to form a three-dimensional network. Further, perovskites can form two-dimensional layered superlattices called Ruddlesden-Popper (RP) phases, where a perovskite block of varying unit cell thickness n is sandwiched between rock salt layers (AX) to form a natural superlattice. These RP phases possess the general formula $A_{n+1}B_nX_{3n+1}$ with alternating perovskite blocks displaced by half a unit cell in the in-plane direction [see Fig. 1(a)]. The perovskite ABX_3 is the end member of the RP series with $n = \infty$.

Perovskite oxides containing early transition metals such as Ti, Zr, and main group elements such as Sn are wide band gap semiconductors, but the corresponding chalcogenides possess band gap in the visible-infrared energies. Our ability to control and modify the band gap of such semiconductors would vastly expand their range of applications, especially as heterostructures. Alloying is a common approach to tune the band gap of such semiconductors, yet the accompanying disorder has the undesirable effect of lowering carrier mobility [15,16]. RP phases offer an alternative approach to create long range ordered structures to tune the physical properties such as band gap [13,14,17–23]. While the changes in the band gap through alloying can be understood in terms of orbital composition (by chemical substitutions) of the valence and/or conduction-band edge states, it is yet unclear how the

quantum confinement through reduced dimensionality, and details of the crystal structure of the RP phases, modify the band gap with respect to the ABX_3 parent material. There have been many studies on the electronic properties of these layered compounds such as oxides [24–26] and hybrid halides [14,27–30]. A fundamental understanding of the factors at play is crucial to design and tailor emerging perovskite based electronic and photonic materials.

To motivate our study, we summarize the band gap evolution of three representative materials: oxide ($Sr_{n+1}Ti_nO_{3n+1}$), halide ($BA_2MA_{n-1}Pb_nI_{3n+1}$, where MA is CH_3NH_3 and BA is $CH_3(CH_2)_3NH_3$), and chalcogenide ($Ba_{n+1}Zr_nS_{3n+1}$) RP phases in Figs 1(b) and 1(c) [10–14,31]. We use a combination of electronic structure calculations and photoluminescence spectroscopy measurements on single crystals of $Ba_{n+1}Zr_nS_{3n+1}$ RP series ($n = \infty, 1, 2$) to determine their band gap and compare them with trends in oxides and halides reported in the literature. We find that the band gaps of $Ba_{n+1}Zr_nS_{3n+1}$ are much lower than that of the parent perovskite, $BaZrS_3$, while the gaps of $Sr_{n+1}Ti_nO_{3n+1}$ and $BA_2MA_{n-1}Pb_nI_{3n+1}$ are higher than that of $SrTiO_3$ and $MAPbI_3$. Our results clearly indicate that the factors controlling the band evolution in the chalcogenides are different from oxides and halides. To understand the origin of these contrasting trends, we carried out in depth first principles calculations on the chalcogenide RP phases.

The first-principles calculations were performed using density functional theory [32,33] and the screened hybrid functional HSE06 [34,35] as implemented in the VASP code [36,37]. The interactions between the valence electrons and the ionic cores are described using projector augmented wave potentials [38,39]. For structure optimization, we used the generalized gradient approximation PBEsol [40,41] for exchange and correlation, while band structures were computed

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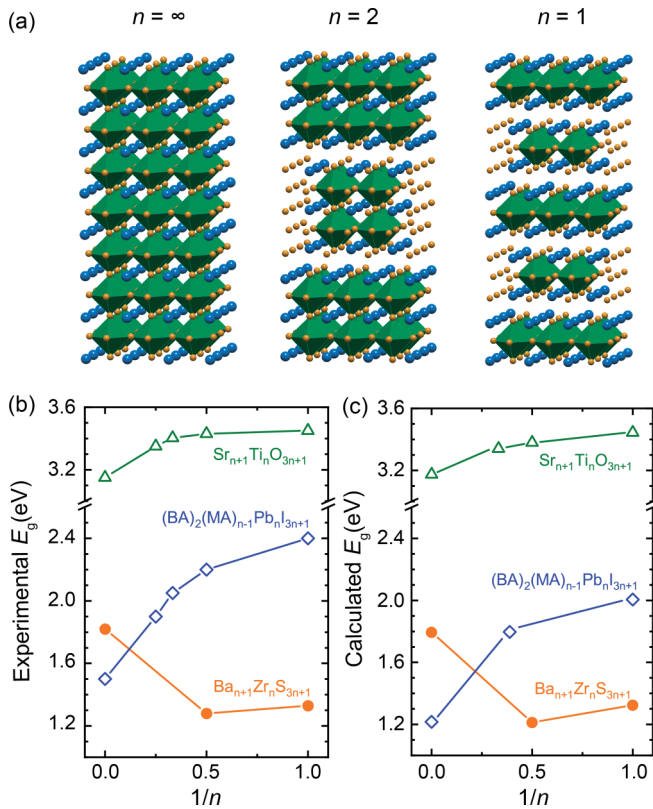


FIG. 1. (a) Schematic crystal structures of the Ruddlesden-Popper (RP) phases ABX_3 ($n = \infty$), $A_3B_2X_7$ ($n = 2$), and A_2BX_4 ($n = 1$). Band gaps of Ba-Zr-S, Sr-Ti-O, and (BA)(MA)-Pb-I RP series from (b) experiments and (c) calculations. The experimental values of Sr-Ti-O and (BA)(MA)-Pb-I series are from Refs. [10–14]. The calculated values of the (BA)(MA)-Pb-I band gaps are from Refs. [13,14].

using the HSE06 hybrid functional. All the calculations were performed with a kinetic energy cutoff of 500 eV for the plane wave basis set. We used Γ -centered $6 \times 6 \times 6$ grid for the 5-atom cubic ABX_3 structures, and similar density k meshes for the 20-atom orthorhombic structure, and the tetragonal RP A_2BX_4 and $A_3B_2X_7$ structures. The calculated lattice parameters are in good agreement with experimental data [42,43] (see Supplemental Material [44]).

Polycrystalline and single crystal samples of the three Ba-Zr-S RP series compounds were synthesized by solid-state reaction and salt flux growth, respectively, using methods similar to those reported earlier [45,46]. We performed structural characterization using x-ray diffraction (XRD) and optical characterization using photoluminescence (PL) spectroscopy. We performed single crystal diffraction studies at 100 K. Powder XRD studies were performed on the ground crystallites with $Cu K\alpha$ radiation in Bragg-Brentano geometry at room temperature. There will be a separate report on the details of crystal growth and x-ray diffraction analysis of the single crystals. Obtained structural parameters are included in the Supplemental Material [44]. PL measurements of the three materials were performed on the single crystals at room temperature with a microscope in back-reflecting geometry. Emission spectra in the 1.5–2.2 eV range were collected in

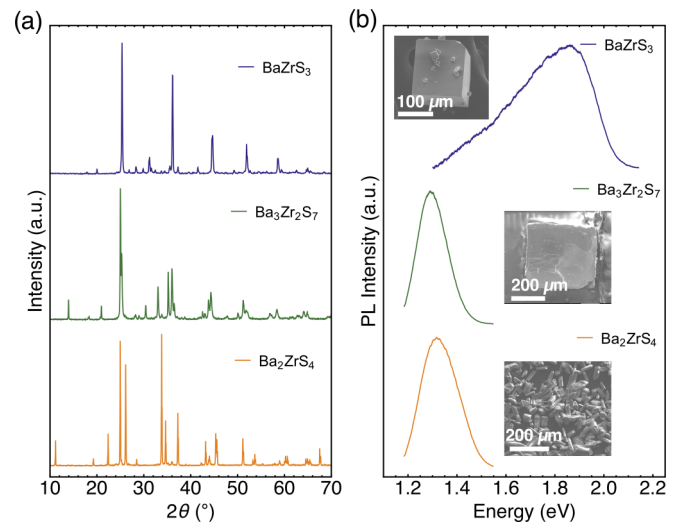


FIG. 2. Structural and optical characterization of the $Ba_{n+1}Zr_nS_{3n+1}$ RP series. (a) X-ray diffraction patterns from ground crystallites of $BaZrS_3$, $Ba_3Zr_2S_7$, and Ba_2ZrS_4 . (b) Photoluminescence spectra and scanning electron microscopy images (insets) of $BaZrS_3$, $Ba_3Zr_2S_7$, and Ba_2ZrS_4 crystallites.

a setup with 532 nm excitation laser while the lower energy range (1.2–1.5 eV) were collected in another setup with 785 nm excitation laser.

As noted earlier, the RP phases of the Sr-Ti-O and (BA,MA)-Pb-I systems follow the trend of increasing band gap with decreasing number of ABX_3 perovskite layers that are separated by an AX layer. In contrast, we find that for the Ba-Zr-S system, the band gap of $BaZrS_3$ is significantly larger than the gaps of $Ba_3Zr_2S_7$ and Ba_2ZrS_4 , as shown in Figs. 1(b) and 1(c). Our calculated band gaps of $BaZrS_3$, $Ba_3Zr_2S_7$, and Ba_2ZrS_4 are 1.79 eV ($n = \infty$), 1.21 eV ($n = 2$), and 1.33 eV ($n = 1$), which are in agreement with previous calculations [23,47]. To verify this predicted anomalous band gap evolution, we performed PL spectroscopy measurements on single crystals of $BaZrS_3$, $Ba_3Zr_2S_7$, and Ba_2ZrS_4 . First, we structurally characterized these materials using XRD. The XRD patterns for the ground powders of the single crystals are shown in Fig. 2(a). The distinct low-angle reflections in XRD are clear fingerprints of the RP phases and agree well with the larger unit cells with alternating perovskite and rock-salt layers. The PL spectra and the scanning electron microscopy (SEM) images are shown in Fig. 2(b). $BaZrS_3$ ($n = \infty$) showed a relatively broad PL peak centered at 1.82 eV while the two RP phases showed narrower PL peaks at 1.28 eV ($n = 2$) and 1.33 eV ($n = 1$), respectively. Thus, our experimental studies confirm the theoretically predicted anomalous band gap evolution in chalcogenide RP phases of Ba-Zr-S.

Now, to address the origin of the anomalous band gap evolution in chalcogenide RP phases compared to the oxides and halides, we need to understand the factors influencing the position and orbital character of the conduction and valence bands in the perovskite and RP phases. The valence-band maximum (VBM) and conduction-band minimum (CBM) of the early transition metal (Ti, Zr, Hf) perovskites and related phases have significant contributions from the orbitals of the species that constitute the octahedra (Zr and S in the case

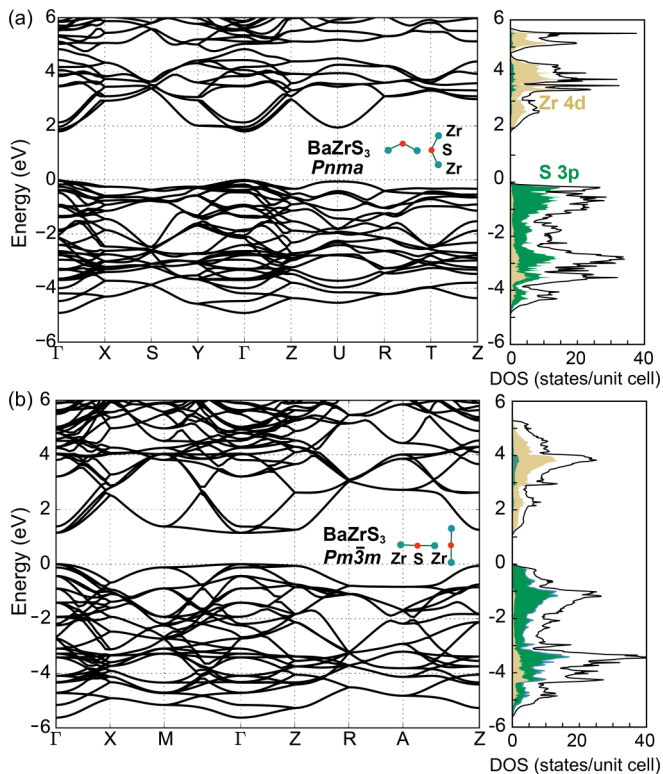


FIG. 3. Effects of the octahedral rotations on the electronic structure of BaZrS_3 . Electronic band structure and orbital-projected density of states of (a) relaxed BaZrS_3 , featuring octahedral rotations as indicated in the inset, and (b) hypothetical cubic perovskite BaZrS_3 , where all the octahedral rotations are removed, keeping the same volume as the relaxed structure. The zero in the energy axes was arbitrarily placed at the top of the valence band for each case.

of BaZrS_3) and almost none from the orbitals of the A-site species. Specifically, the lowest energy conduction bands are largely composed of transition metal d orbitals, while highest energy valence bands are composed of chalcogen p orbitals. Therefore, one could expect that the band gap would be significantly influenced by the arrangement of the network of BX_6 corner-sharing octahedra, i.e., octahedral tilting, rotation, and distortion. We then discuss how these structural modifications to the highly symmetric corner shared octahedral connectivity affect the band gap of the $\text{Ba}_{n+1}\text{Zr}_n\text{S}_{3n+1}$ RP series for decreasing thickness of the perovskite blocks, i.e., from $n = \infty$ to $n = 2$ and $n = 1$.

First, we compare the electronic band structure and orbital-projected density of states of BaZrS_3 in the orthorhombic $Pnma$ structure (stable at room temperature) with those of the hypothetical cubic structure where we removed the octahedral tilt and rotation but keeping the same equilibrium volume per formula unit. Orthorhombic BaZrS_3 displays an in-plane Zr-S-Zr bond angle of 156.6° and out-of-plane Zr-S-Zr bond angle of 160.0° , with in-plane Zr-S bond lengths of 2.527 \AA and 2.538 \AA , and out-of-plane Zr-S bond lengths of 2.521 \AA , thus featuring a small distortion of the octahedra. By removing the octahedral tilting and rotation the band gap is significantly reduced, by as much as 0.65 eV , as shown in Fig. 3. The octahedral distortion has a negligible contribution to the band

gap, changing it by only 0.06 eV . From the orthorhombic to the cubic structure, we find that most of the change in the gap is due to a broadening of the valence band, pushing up the VBM by 0.63 eV , while the CBM is pushed down by only 0.02 eV . The dispersion and width of the conduction band and valence band are also affected by the octahedral rotations, as seen by comparing Figs. 3(a) and 3(b). Deviation of Zr-S-Zr angle from 180° leads to smaller hopping integrals in a tight-binding picture, and therefore narrower and less dispersive bands.

$\text{Ba}_3\text{Zr}_2\text{S}_7$ ($n = 2$) crystallizes in two structures: the low temperature (LT) $\text{Ba}_3\text{Zr}_2\text{S}_7$ phase [48], featuring octahedral rotations, with equilibrium Zr-S-Zr in-plane bond angle of 167.0° and out-of-plane angle of 161.3° , and the room-temperature (RT) phase featuring in-plane and out-of-plane angles of 180° yet a small Ba/S displacement [49]. The calculated band gap for the LT phase is 1.56 eV and for the RT phase is 1.21 eV . This difference is attributed largely to the lack of octahedral rotations in the RT phase. For example, the removal of all the octahedral rotations and Ba/S displacements in the LT phase to make the octahedral arrangements ideal reduces the band gap to 1.25 eV , very close to the result for the RT phase.

On the other hand, Ba_2ZrS_4 ($n = 1$) compound crystallizes in one stable structure with all the Zr-S-Zr angles at 180° , i.e., there are no octahedral rotations, only octahedral distortion (four in-plane Zr-S bonds of 2.56 \AA and two out-of-plane bonds of 2.47 \AA) and a Ba/S (antiferroelectric) displacement. This high symmetry phase is stable up to the room temperature. The calculated band gap of the relaxed Ba_2ZrS_4 is 1.33 eV , compared to 1.19 for a hypothetical structure where the Ba/S displacement is removed, and 1.30 eV for another hypothetical structure, where the Ba/S displacement is removed and the octahedron is made perfect, i.e., all Zr-S bond lengths are equal and Zr-S-Zr angles are 180° . The relatively small differences in the band gap for these three Ba_2ZrS_4 structures indicate that the Ba/S displacement or octahedral distortion have negligible effects on the band gap compared to the octahedral rotations, similar to BaZrS_3 ($n = \infty$) and $\text{Ba}_3\text{Zr}_2\text{S}_7$ ($n = 2$).

We quantify the effects of octahedral tilting and rotations and quantum confinement on the band gap for the Ba-Zr-S system in Fig. 4(a), whose corresponding bond angle evolution is shown in Fig. S1 in the Supplemental Material [44]. The lower dashed line represents only the effects of quantum confinement. From ideal cubic BaZrS_3 ($n = \infty$, space group $Pm\bar{3}m$) to $\text{Ba}_3\text{Zr}_2\text{S}_7$ ($n = 2$, space group $I4/mmm$) the gap increases by 0.103 eV , and from $\text{Ba}_3\text{Zr}_2\text{S}_7$ to Ba_2ZrS_4 ($n = 1$, space group $I4/mmm$), the gap increases by only 0.049 eV . These changes represent purely the effects of quantum confinement, i.e., impact of decreasing the thickness of the perovskite blocks from $n = \infty$ to $n = 2$ to $n = 1$ layer on the electronic structure. This variation in the gap is much smaller than the changes brought about by the octahedral tilting and rotations. The upper dashed line in Fig. 4(a), connecting relaxed BaZrS_3 (space group $Pnma$) to LT $\text{Ba}_3\text{Zr}_2\text{S}_7$ (space group $P4_2/mnm$), and Ba_2ZrS_4 (space group $I4/mmm$) contains the effects of octahedral tilting and rotations and the quantum confinement. Since the latter is relatively small, as revealed by the lower line, we conclude that the effect

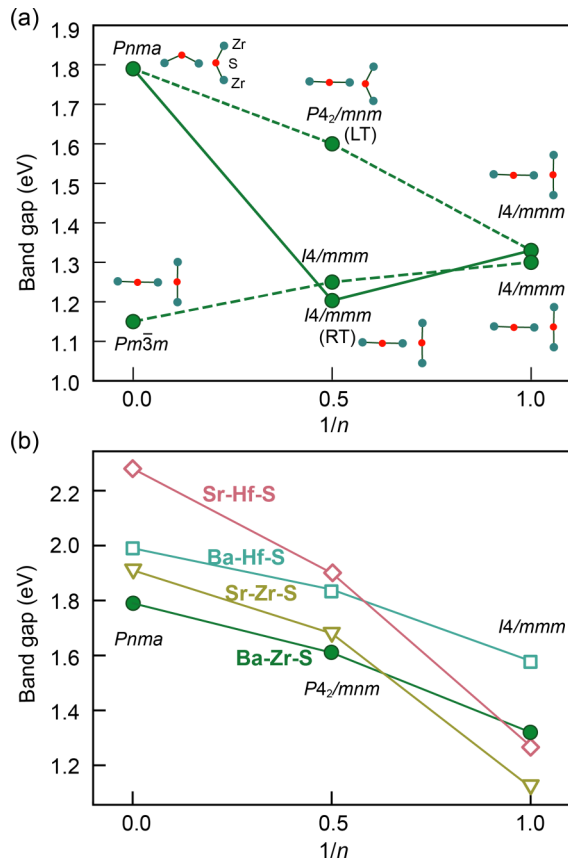


FIG. 4. Band gap evolution Ruddlesden-Popper phases of chalcogenides: (a) Calculated band gap of the relaxed BaZrS₃, Ba₃Zr₂S₇, and Ba₂ZrS₄, compared to the hypothetical phases where the octahedral rotations and Ba/S displacements are removed and the octahedra are made perfect; (b) Calculated band gap of Sr_{n+1}Hf_nS_{3n+1}, Sr_{n+1}Zr_nS_{3n+1} and Ba_{n+1}Hf_nS_{3n+1} for $n = \infty, 2, 1$ in the *Pnma*, *P4₂/mnm*, and *I4/mmm* structures, respectively, compared to the Ba_{n+1}Zr_nS_{3n+1} series.

of octahedral tilting and rotation on the band gap evolution of the Ba-Zr-S system is dominant. The effects of Ba/S antiferroelectric displacements on the gap of Ba₃Zr₂S₇ and Ba₂ZrS₄ are also small, as seen in the differences between the RT Ba₃Zr₂S₇ and ideal Ba₃Zr₂S₇ as well as between the two Ba₂ZrS₄ structures, where the upper value corresponds to the experimentally observed phase. Detailed band structure of all the relevant phases in Ba-Zr-S is shown in Fig. S2 in the Supplemental Material [44].

We found that other chalcogenide systems show band gap evolution similar to Ba-Zr-S. As shown in Fig. 4(b), the calculated band gap of the Ba-Hf-S, Sr-Zr-S, and Sr-Hf-S RP series also decrease with decreasing n . Thus, our calculations confirm the dominant role of octahedral tilting and rotations in determining band gap, irrespective of the differences in the chemistry for the chalcogenide perovskites. We list all the structural parameters of these materials in Table S1 and S2 in the Supplemental Material [44]. Consistent with our observations for Ba-Zr-S system, the perovskite ABX₃ ($n = \infty$) showed greater deviation of the metal-S-metal angles from 180° compared to the A₃B₂X₇ ($n = 2$) and A₂BX₄ ($n = 1$) in all the cases. The deviation quantitatively reflects the degree of octahedral tilting and proportionately greater band gap values. Finally, the seemingly strong dependence of the band gap on octahedral tilt and rotations in the chalcogenide series can be attributed to the stronger covalent character of the Zr-S, Hf-S bonds. Such stronger covalency implies in a stronger dependence of the VBM and CBM energies on the B-X-B bond angle (bending).

In conclusion, our study demonstrates the competition between quantum confinement and octahedral rotations to determine band gap evolution in the layered phases with octahedral coordination such as Ruddlesden Popper (RP) perovskite phases. We demonstrate that the influence of octahedral rotations is dominant in the chalcogenides such as Ba-Zr-S, unlike in semiconducting oxides and halides such as Sr-Ti-O and MA-Pb-I systems, where quantum confinement dictates band gap evolution. We expect that this understanding will be useful to design next generation semiconductors based on such layered phases for electronic and photonic applications.

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