

Directed growth of hydrogen lines on graphene: High-throughput simulations powered by evolutionary algorithm

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We set up an evolutionary algorithm combined with density functional tight-binding calculations to investigate hydrogen adsorption on flat graphene and graphene monolayers curved over substrate steps. During the evolution, candidates for the new generations are created by adsorption of an additional hydrogen atom to the stable configurations of the previous generation, where a mutation mechanism is also incorporated. Afterwards a two-stage selection procedure is employed. Selected candidates act as the parents of the next generation. The evolutionary algorithm predicts formation of lines of hydrogen atoms on flat graphene. In curved graphene, the evolution follows a similar path except for a new mechanism, which aligns hydrogen atoms on the line of minimum curvature. The mechanism is due to the increased chemical reactivity of graphene along the minimum radius of curvature line (MRCL) and to sp^3 bond angles being commensurate with the kinked geometry of hydrogenated graphene at the substrate edge. As a result, the reaction barrier is reduced considerably along the MRCL and hydrogenation continues like a mechanical chain reaction. This growth mechanism enables lines of hydrogen atoms along the MRCL, which has the potential to overcome substrate or rippling effects and could make it possible to define edges or nanoribbons without actually cutting the material.

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One of the most attractive features of two-dimensional materials is their ability to be functionalized in more effective ways than conventional materials. However, graphene lacks an energy band gap, a requirement for graphene to be useful in digital electronics applications. Adsorption of hydrogen atoms is a direct way to alter chemical and physical properties of graphene [1] and hydrogenation in a controlled way was shown to open a band gap [2–9]. There are proposals to tune the band gap of graphene by hydrogen adsorbed nanoripples [10–12] and forming superlattices consisting of lines of adsorbed hydrogen atoms [13,14]. It is well known that curvature enhances chemical reactivity of graphene and related materials by decreasing the activation barrier for adsorbates [15–22]. This property was used to enhance the hydrogen storage capacity of graphene and CNTs [23–27]. A straightforward way to deform graphene is to introduce steps in the underlying substrate. Such deformation also affects electronic and thermal transport properties [28–30].

Stability of small hydrogen clusters on single and multilayer graphene, as well as on carbon nanotubes, has been studied by several groups theoretically and experimentally [17,31–40]. Also there have been attempts to determine the most stable graphene like clusters and to control the size of the hydrogen islands [41,42]. Those studies were focused either on individual dimer and trimer configurations [32,36] or the configurations were generated from extensions of ortho- and para positions

[31], but progression of the hydrogenation process was not addressed on flat or curved graphene.

Here, we perform high-throughput calculations within an evolutionary framework. We demonstrate formation of lines of hydrogen atoms on flat and curved graphene sheets from one side. On curved graphene, hydrogenation is predicted to take place as a chain reaction and long lines of hydrogen atoms are shown to be energetically more favorable along the minimum radius of curvature line (Fig. 1).

Methods. We employ a density functional theory based tight-binding (DFTB) method, where we use the DFTB+ code [43] and the mio-1-1 parameter set [44]. Density functional theory (DFT) is also used to check the compatibility of the two methods [45,46]. Periodic boundary conditions are employed in all simulations. For flat graphene, a $7 \times 7 \times 1$ supercell of the primitive unit cell is used (see Fig. 2) with a k -point sampling of $10 \times 10 \times 1$ in the Monkhorst-Pack scheme [47]. We fix the supercell lattice parameters corresponding to the carbon-carbon distance of pristine graphene. The vacuum region is set to 10 \AA to avoid interplane interactions for flat geometry, while it is chosen to be larger than 50 \AA for the curved geometries. A unit cell which consists of 144 atoms is built for obtaining the curved geometry and $1 \times 10 \times 1$ supercells of this unit cell are used (see Fig. 2) with k -point samplings of $1 \times 3 \times 1$ or higher. Structures are optimized until the maximum force component is below the $2 \times 10^{-2} \text{ eV/\AA}$. We have checked the strain on graphene supercell after adsorption of hydrogen atoms by reoptimizing the lattice parameters. We have used the most stable hexamer configuration and found that the supercell

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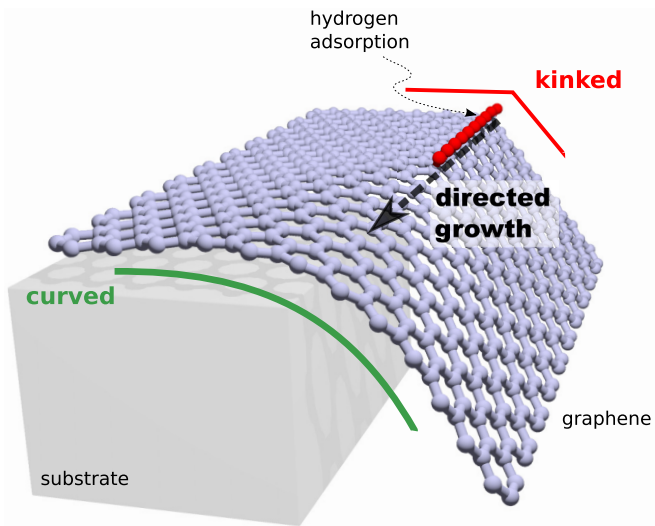


FIG. 1. Illustration of the directed growth of hydrogen atoms on the minimum radius of curvature line. Propagation of the hydrogen atoms along the first and the second minimum radius of curvature lines leads to formation of a kink line.

has shrunk by only 0.35%, which indicates that the adsorption induced strain does not affect our simulations considerably. We disregard spin polarization in our calculations since the energy difference due to spin polarization is much less than the threshold in the evolutionary algorithm as explained below.

Flat graphene. There are several previous studies related to structural properties of hydrogen adsorption on flat graphene [31–38]. It was shown that the most preferable positions for hydrogen dimers are the ortho- and parapositions. Ortho (O)-, meta (M)-, and para (P)-positions correspond to the first, second, and third nearest neighboring sites, respectively (see Fig. 2). Trimer and tetramer adsorption follows extensions of ortho- and parapositions consequently. Before performing high-throughput DFTB simulations, we compare DFTB results against DFT for a relatively large set consisting of 60 configurations, which cover the configurations investigated in the literature [31,32,36]. Details of the comparison are given in the Supplemental Material (Fig. S14) [48], which clearly show that DFT and DFTB results are in very good agreement.

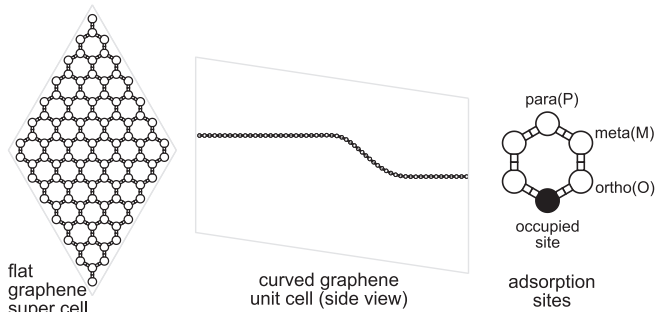


FIG. 2. Flat and curved graphene structures are shown and the adsorption sites are labeled as ortho (O)-, para (P)-, and meta (M)-configurations with respect to the occupied site.

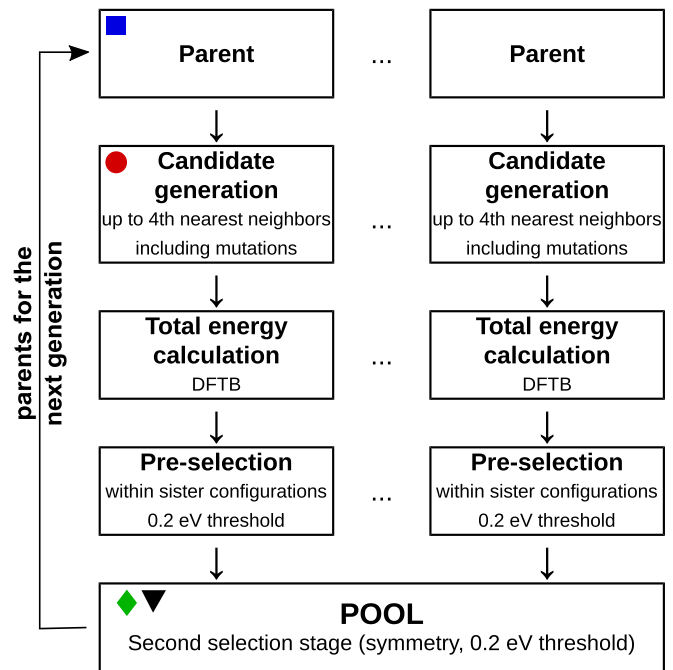


FIG. 3. Flow chart of the evolutionary algorithm. The algorithm starts with generation of candidate configurations (red circles) from the parent configurations (blue squares). After DFTB based total energy calculation of the relaxed geometries, preselection is performed among the sister configurations, where the threshold energy is set to 0.2 eV. Preselected configurations are collected at a pool and a second selection procedure is carried out taking total energy and symmetry properties into consideration. Successful candidates (green diamonds) are considered as the stable configurations of the current generation and they are used as parents for the next generation. Candidates that are eliminated at the pool-selection stage are marked with black triangles. (Blue squares, green diamonds, and black triangles are used correspondingly in Figs. 4, 6, and 7, whereas red circles are used in Figs. S2–S8 [48].)

We study hydrogen adsorption on flat graphene by using an evolutionary approach, which relies on the selection of favorable configurations by comparing their total energies (see Fig. 3). The algorithm starts with a monomer as the *parent* configuration, from which the *candidate* dimer configurations are generated. The candidate generations include all available adsorption sites up to the fourth nearest neighboring site of the existing occupied sites. The total energies of the relaxed candidate configurations are calculated. The threshold value for the *preselection* stage is set to 0.2 eV above the minimum energy of the members of the same *family*, i.e., candidates originating from the same parent. Afterwards, a second selection stage is performed, which will be referred to as the *pool selection*. In pool selection, the energy threshold is set to 0.2 eV above the global minimum energy of all candidates in the pool. Binding of a hydrogen atom induces an out-of-plane displacement of the carbon atom, which leads to an activation barrier of 0.2 eV. According to previous studies, chemisorption can take place if hydrogens surpass this activation barrier [31,35,38,38,49–51]. For this reason, 0.2 eV is chosen as a threshold value. Symmetry is the second criterion during the pool selection. If there are geometrically equivalent

candidates due to symmetries, only one of them is proceeded to the next generation. The successful candidates, i.e., stable configurations, are then the parents for the *next generation*.

Starting from dimers, we include a *mutation* mechanism during candidate generation. Mutations alter the configurations of the parent by hopping one of the hydrogens to an available nearest neighboring site. Afterwards, the candidates are generated by adsorption of a hydrogen atom to up to the fourth nearest neighboring site, as usual. We simulated all possible mutations on flat graphene from dimers to hexamers, which make 5355 configurations in total. The predicted stable configurations up to tetramers are in exact agreement with literature. Above this size, the evolutionary algorithm finds stable configurations which were not predicted before.

The results of the high-throughput simulations employing the evolution scheme are summarized in Fig. 4. Different generations are grouped as rows and depicted with dashed lines. For each generation the number of panels is the sum of the number of successful candidates from previous generation and the number of mutants that could yield stable configurations. The parents are marked with blue squares, while the green diamonds show the members of the new generation, i.e., the candidates which succeed both selection stages. All candidate configurations are shown in Figs. S2–S6 [48] with red circles. If the selection process was carried out only within sister configurations (i.e., without pool selection) the new generation would have a higher number of stable configurations. The configurations that are eliminated during pool selection are marked with black triangles.

In the first row of Fig. 4, one observes that only two candidates, D_2 and D_4 , are selected for the new generation from the parent monomer. They correspond to the ortho- and parapositions. These configurations are selected from 72 candidates (see Fig. S2 [48]), which are composed of one nonmutant and three mutant parents. In fact, there are six favorable adsorption sites but four members $D_3, D_5; D_1, D_6$ are equivalents of D_2 and D_4 , respectively. In agreement with the previous results, the metaposition is found to be unfavorable. The orthopositioned configuration is more stable than the parapositioned configuration, and there is only 59.2 meV energy difference between them. There is no direct correlation between the dihedral angles and the binding energies, but the C-H bond lengths (1.129 Å, 1.138 Å, and 1.142 Å for ortho, para, and meta, respectively) follow the same trend with the binding energies.

In generating trimers from dimers, there exist two non-mutant and 10 mutant parents, which enable 298 candidates (see Fig. S3 [48]). At the preselection stage, five successful configurations ($Tr_7, Tr_8, Tr_9, Tr_{10}$, and Tr_{11}) are found from two parents (D_2 and D_4), one being a mutant (Tr_9) (see the third panel in the second row in Fig. 4). The mutation switches a para configuration to a meta configuration, which is known to be unstable. It is then stabilized by adsorption of a hydrogen atom to the common orthopositions of both parent atoms. The stabilization mechanism is in agreement with the literature in the sense that the metaposition is not favorable, while the orthoposition is. Two configurations (Tr_{10} and Tr_{11}) are eliminated due to symmetry. The stable configuration Tr_8 occupies P-O positions, whereas Tr_7 occupies P-P positions.

For tetramers there exist three nonmutant and 21 mutant parents which generate 737 candidates (see Fig. S4 [48]). Among those candidates, we find four stable configurations ($Te_{14}, Te_{17}, Te_{18}$, and Te_{19}) from three parents (Tr_7, Tr_8 , and Tr_9), one being a mutant (Te_{14}) which can be seen in the third row of Fig. 4. The mutation alters a P-P configuration to a P-M configuration and with the new hydrogen we obtain a P-O-O geometry. It is again confirmed that metaposition is unfavorable. In the tetramer family, five members failed to continue to the next generation at the pool-selection stage (indicated with black triangles). Configuration Te_{17} is composed of P-O-O sites, whereas Te_{18} displays P-O-P geometry. One can make some predictions from the obtained results already. Te_{17} and Te_{18} are precursors of linear chains, whereas a deviation from the linear geometry appears in Te_{14} . The evolution of Te_{19} is rather indeterminate. It can either form a hexagonal ring or evolve into a double chain with armchair-type geometry. The former indicates clustering, while the latter stands for linear patterns.

Next, we generate pentamers from tetramers. There exist four nonmutant and 32 mutant parents, which generate 1242 candidates (see Fig. S5 [48]). Fourth row of Fig. 4 shows that the new generation is found to have seven stable members ($P_{21}, P_{22}, P_{23}, P_{26}, P_{28}, P_{29}$, and P_{30}) from four parents ($Te_{14}, Te_{17}, Te_{18}$, and Te_{19}). The new generation of pentamers does not involve new mutations. All members of the new generation are composed of either only orthopositioned or mixtures of ortho- and parapositioned hydrogens. There are no O-O-O-O configurations; therefore, formation of a hexagonal ring is energetically suppressed at this stage. More interestingly, lines with armchair-type geometry become the most favorable configurations.

Hexamer configurations are the last step for our calculations on flat graphene. When we consider the results of the hexamer generations, there exist seven nonmutant and 69 mutant parents which produce 3006 candidates (see Fig. S6 [48]). From those candidates, the new generation contains 10 nonmutant stable members ($H_{37}, H_{44}, H_{45}, H_{46}, H_{47}, H_{48}, H_{50}, H_{52}, H_{53}$, and H_{54}), which can be seen in the fifth and sixth rows of Fig. 4. We eliminate 13 of the candidates due to symmetry or because of the ground state coming from a nephew, namely at the pool-selection stage. H_{37} is a mixture of linear and armchair-type geometries, resembling a broken line. H_{38} is eliminated due to the presence of an equivalent, H_{52} .

We have checked the strain on graphene supercell after adsorption of six hydrogen atoms by reoptimizing the lattice parameters for the armchair configuration. We find that the supercell has shrunk by only 0.35%, which indicates that the adsorption induced strain does not affect our simulations considerably.

In summary, we generated a pool which is composed of a total of 5355 candidates from dimers to hexamers. It is clear that ortho- and para extended combinations are favored, whereas combinations which consist of metaposition are not. The most striking and remarkable result is the alignment of hydrogen atoms in armchair-type geometry and H_{53} is found to be energetically the most preferable configuration. The next most favorable configuration is H_{45} , which has a linear alignment with hydrogen atoms occupying *A* and *B* sublattices evenly. An important note is in order here. Both armchair-type geometry and single line formation are in the armchair

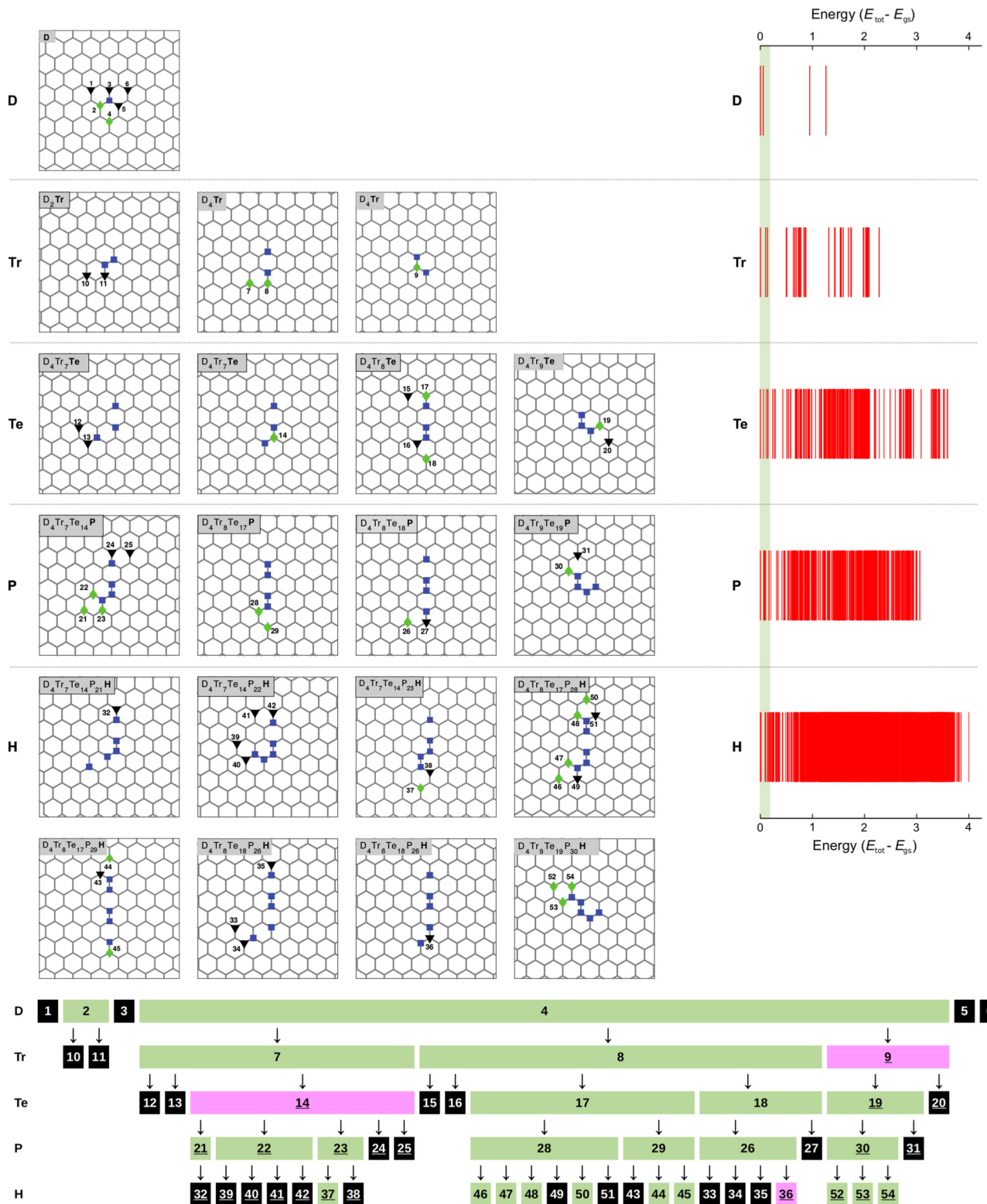


FIG. 4. Evolution of generations on flat graphene. Parent atoms (blue squares), stable configurations (green diamonds), and configurations that are eliminated at the pool selection stage (black triangles) are shown throughout the evolution (upper left). Generations are separated by dotted lines and denoted as D, Tr, Te, P, and H for dimers, trimers, tetramers, pentamers, and hexamers, respectively. Each panel corresponds to a family; the family tree is denoted at the upper left corner of each panel. The evolution of generations can also be tracked at the lower panel, where each row stands for a generation and each box for a candidate with the same enumeration with the geometry plots. The stable, eliminated, and mutant configurations are shown with green, black, and pink boxes, respectively. Relative total energies of simulated configurations are shown on the right, where the green zone indicates the 200 meV threshold value. The complete list of simulated geometries can be found in Figs. S2–S6 and their corresponding energies at Table SI [48]. See also the Supplemental Material [56].

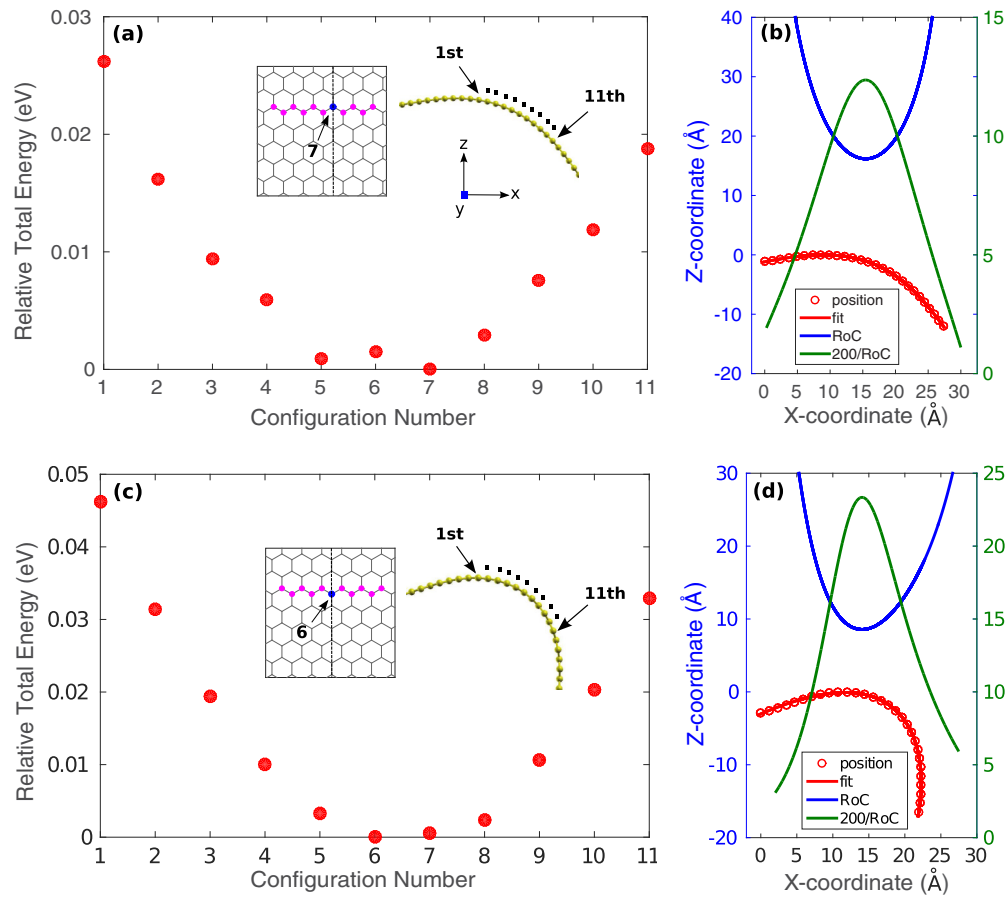


FIG. 5. Curvature and binding to curved graphene. Energetics of single hydrogen adsorption on curved graphene with bending angles 52° and 90° [(a) and (c), respectively]. In the insets top view and side view of the configurations are illustrated. Pink dots denote tested configurations and blue dots show most favorable positions. Configurations 7 and 6 ensure the positions of the minimum radius of curvature lines (MRCL) for 52° and 90° bending. The MRCLs are depicted in the insets. In (b) and (d) red circles indicate graphene atoms, the blue lines show the radius of curvature (ROC), and the green lines show the inverse radius of curvature (IROC).

direction, the former being a double line and consisting of orthopositions only. In addition, H_{44} is less stable than H_{45} because of unpaired sublattice sites. Energy difference between H_{45} and H_{53} is only 2.67 meV per adsorbant. The sixfold para configuration (see Conf-2 in Fig. S13 [48]) is a special case, whose relative total energy is lower than line formations. It does not appear as a stable configuration at the end of the evolution procedure, because its precursor was eliminated at the pool selection stage of tetramers.

Armchair-type line formation was previously shown to be more stable than zigzag-type line formation, as well as formation of triangular and circular clusters [52], but single lines were not investigated in that work. Single line geometries of tetramers were reported on bilayer graphene but longer lines were not observed [53]. On graphene/SiC(0001) line formations were reported to be as short as a dimer [54], which are in either ortho- or para configurations. Interestingly, scanning tunneling microscopy images show important electronic contribution of the substrate and the modulation in adsorption energy was reported to be as high as 230 meV. Similarly, Moiré superstructures are known to influence hydrogen adsorption on graphene [2]. Therefore, we speculate that the lack of experimental observation of hydrogen lines on flat graphene may be due to the substrate effects.

Curved graphene. A strategy to overcome these effects could be incorporating bending so that substrate induced ripples are overridden by a strong bending and the potential landscape altered by the substrate becomes a minor ingredient compared to the increased chemical reactivity along the minimum radius of curvature line (MRCL). In what follows, we examine hydrogen line formation on curved graphene surfaces.

Armchair direction has the lowest bending modulus [55] and it is also the favored direction for formation of hydrogen lines. Therefore, we consider the substrate direction to be aligned with the armchair direction. Periodic boundary conditions in both directions, parallel and perpendicular to the step edge, are applied. Instead of simulating the atomistic details of the substrate, its influence is included by bending graphene over a step. However, long range interactions like hydrogen substrate interaction are neglected. Bending is achieved through constrained relaxation of the atomic positions, where the atoms away from the step edge are fixed and those close to the step edge are free during optimization of the atomic forces. The bending angles are chosen to be 52° and 90° , which are determined by considering the bond angles and the strength of substrate graphene interaction. The 52° corresponds to the projection of the tetrahedral angle of sp^3 hybridized carbons, and 90° stands for strong interaction between graphene and

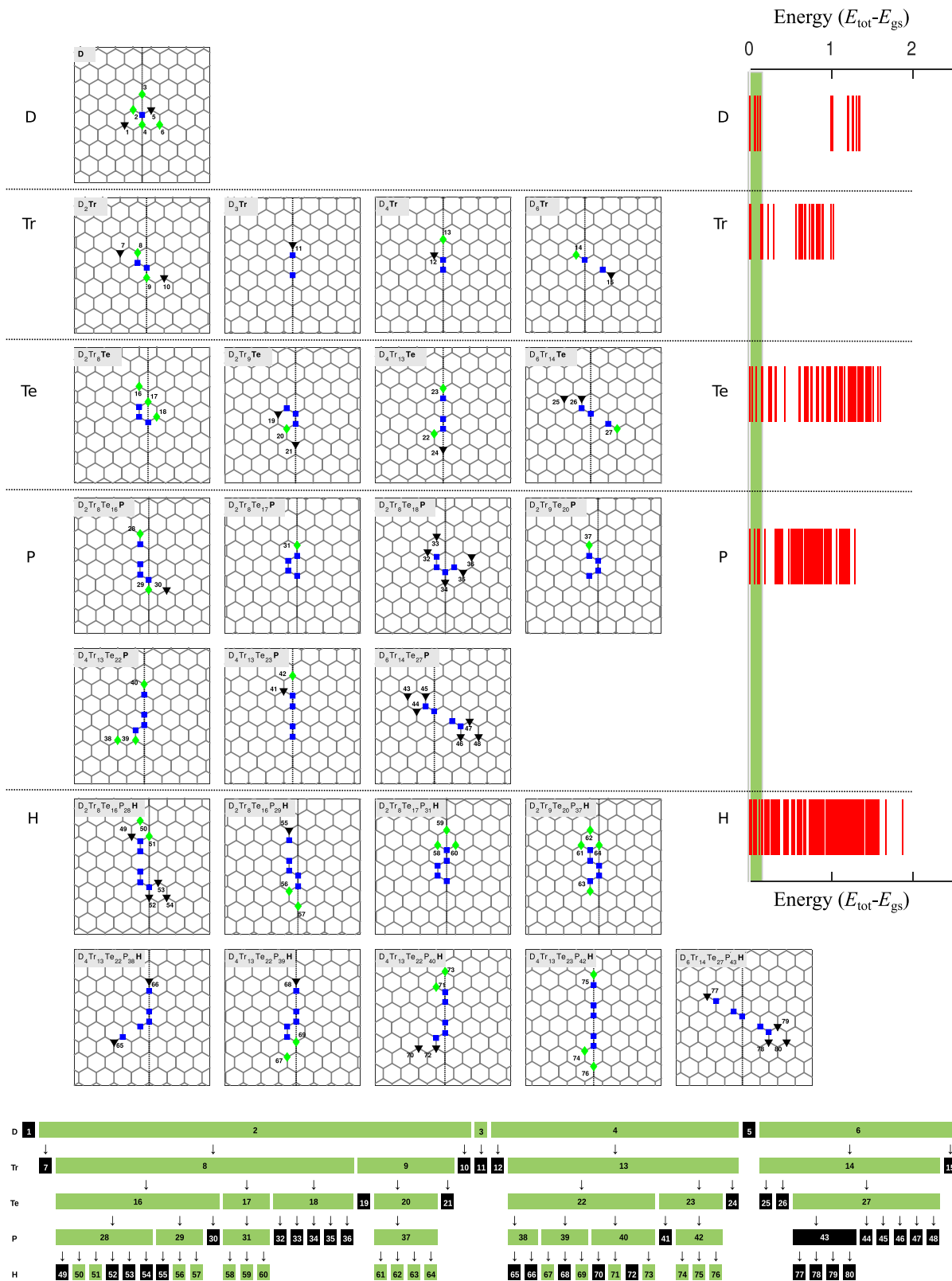


FIG. 6. Evolution of generations during the hydrogenation of curved graphene (52°). The same color codes and notation are applied as in Fig. 4. The complete list simulated structures can be found in Fig. S7 [48].

the substrate. In the absence of hydrogenation, the bending angles are determined solely by the interaction strength. The radius of curvature (ROC) is defined as $R = |(1 + y'')^{3/2} / y''|$ and calculated numerically using the interpolated curve. The

lengths of the curved parts across the step are chosen so as to remove the tensile stress after hydrogenation. For different interaction strengths, which correspond to different substrates, ROC is found to be in the range between 13.5 Å and 3.3 Å,

where the step height is kept as 10 Å [28,30]. In Figs. 5(b) and 5(d) the positions of carbon atoms (red circles) and the fitted curve (red curve) are plotted together with the calculated ROC (blue) and its inverse (green). In Figs. 5(a) and 5(c), the total energies are plotted with reference to the minimum energy configurations as the adsorption site is varied for both bending angles. Top and side views of tested adsorption sites are indicated from 1 to 11 in the insets. The reactivity of graphene increases with reduced ROC, and the total energy increases almost symmetrically with increasing ROC, where the minimum energy is achieved at the site with the smallest ROC. In 52° bending the minimum ROC is 16 Å, while in 90° bending we find the minimum ROC close to 10 Å, which are close to the previous results [30]. We also perform single hydrogen adsorption calculations on curved graphene for 90° bending by using SIESTA. All trends in total energy from DFT are reproduced by DFTB (see Fig. S14 [48] and Fig. S15 [48]). Binding energies are calculated using

$$E_{\text{binding}}^{(n)} = (E_{\text{graphene}} + nE_{\text{H}} - E_{\text{graphene}+\text{H}_n})/n. \quad (1)$$

The binding energies of single hydrogen on 90°-bent graphene are larger than those of the 52°-bent graphene due to the curvature effect (see Table S-XIII [48] and Table S-XVI [48] for 52° bending and Table S-XVIII [48] and Table S-XXI [48] for 90° bending).

The number of atoms in the simulation cell is significantly larger for curved graphene. On top of that, the number of possible configurations is multiplied because of the broken symmetries due to bending. These make it impossible to simulate all possible configurations. Therefore, equipped with the information from the evolution on flat graphene, we reduce the number of candidates significantly on curved graphene by focusing on the formation of lines of hydrogen atoms.

52° bending. In Fig. 5(a), it is shown that configuration-7 is the most favorable adsorption site for hydrogen on curved graphene (52°), which coincides with the MRCL. Configuration-7 is taken as the parent for the dimer generation. Successful candidates as well as those eliminated during the pool selection are shown in Fig. 6, while all tested candidates on 52°-bent graphene are presented in Fig. S7 [48]. We note that enumeration of configurations in Fig. S7 [48] is independent of the enumeration in Fig. 6.

For dimers, we consider 21 candidates, which are distributed equally on the left- and the right-hand sides of the MRCL (see first row of Fig. S7 [48]). At the preselection stage, six candidates (D₁...D₆) are found to be stable (Fig. 6). When the selection process is considered, dimers (52°) produced more parents for the next generation than flat graphene (0°) due to the symmetry breaking with the curvature. However, these parents are ortho- and parapositioned hydrogens as in flat graphene. Only two candidates D₁ and D₅ are eliminated during the pool selection. Relative total energies and binding energies per hydrogen atom of 21 candidates are summarized in Table S-II [48] and Table S-XII [48], respectively. The most favorable dimer configuration is found to be D₄ on 52°-bent graphene.

For trimers, 43 candidates are generated from four parents (see the second row of Fig. S7 [48]). Only four of them succeed after the selection process (see Fig. 6). For all trimer configura-

tions considered, P-O positioned Tr₁₁ and P-O positioned Tr₁₄ making a 60° angle with the MRCL are found to be the most stable configurations. It is interesting that no P-P positioned configurations appear in 52° bending, whereas P-P positioned D₄Tr₇ (0°) is one of the most favorable configurations. It is expected that a P-P positioned configuration would be generated from D₃Tr (52°) but two of the parent's atoms are located on the MRCL and this causes an increase in the energy cost to adsorb a third hydrogen at the paraposition. Relative total energies and binding energies per hydrogen are summarized in Table S-III [48] and Table S-XIII [48], respectively.

Tetramer generation consists of 94 candidates from four parents (see the third row of Fig. S7 [48]). Seven candidates are selected as parents for the next generation. Tetramer configurations that are stable on flat graphene are favored on the 52°-bent case, as well (Fig. 6). One should note that the stable configurations are either mixtures of ortho- and parapositions or pure orthopositioned configurations. In addition, pure P-P-P positioned configurations are eliminated at the preselection stage in 52° bending, while those of flat graphene are eliminated at pool-selection stage. Another point is O-O-P positioned Te₁₆ tends to form a single line on the second MRCL, the parallel line on the left or on the right of the MRCL. In family D₂Tr₉Te, Te₂₀ is kept in order to observe the effect of a shift in the position parallel to the MRCL in the subsequent generation. It can be seen from Table S-IV [48] and Table S-XIV [48] that Te₂₃ (Te₃ in Fig. S7 [48]), which supports linear growth on the MRCL, is the most favorable configuration.

In generating pentamers from tetramers, 108 candidates have been analyzed (see the fourth and the fifth rows of Fig. S7 [48]). These candidates are derived from seven parents; thus we examine seven families in this generation. The first significant difference in terms of the number of families between flat and curved graphene is realized in pentamers. P₂₂ (0°) was selected for next generation but the corresponding geometry P₃₃ (52°) fails at the pool-selection stage. Linear hydrogen chain formation on the first and the second MRCL becomes definite with the configurations P₄₂, P₄₀, and P₂₈. In addition, armchair-type geometry reappears with P₃₁ and P₃₇. It is interesting to note that, although P₃₀ is closer to the MRCL than P₃₈, P₃₀ is eliminated. The reason can be that most of the parents on the MRCL lift carbon atoms and the formation of kink on MRCL makes it easier to adsorb a hydrogen atom. That is, the reaction barrier is lowered, giving rise to a mechanical chain reaction. The same configuration on flat graphene P₂₁ was also transferred to the next generation. There are two families D₂Tr₈Te₁₈P and D₆Tr₁₄Te₂₇P in pentamers, which cannot produce any successful candidates. Nevertheless, we proceed them to the next generation in order to check the growth of lines across the MRCL. In tetramers, it was possible to have linear configurations making 60° angles with the MRCL but in pentamers those formations are all eliminated and only lines along the MRCL are favored, a direct consequence of curvature. In 90° bending, this effect becomes more pronounced, as it will be discussed below.

Finally, in generating hexamers from pentamers, 195 candidates from nine parents are investigated (see the sixth and the

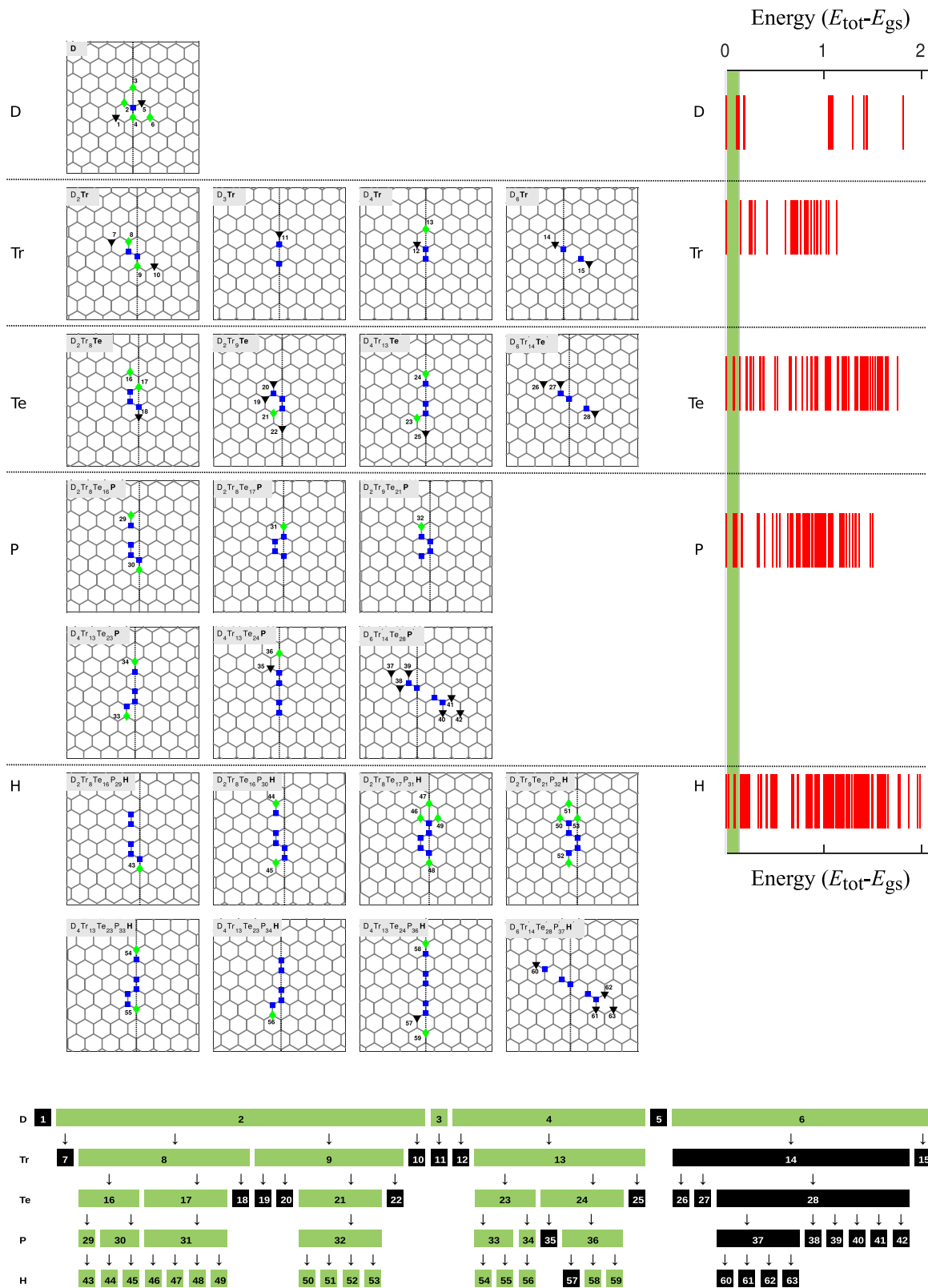


FIG. 7. Evolution of generations during the hydrogenation of curved graphene (90°). The same color codes and notation are applied as in Fig. 4. The complete list of simulated structures can be found in Fig. S8 [48].

seventh rows of Fig. S7 [48]). The second criterion of the pool selection, which is related to the symmetry properties, is not taken into account in order to display all possible preferential configurations. H_{53} , H_{54} , and H_{70} (Fig. 6) are eliminated in

curved graphene 52° bending but their corresponding configurations H_{47} and H_{46} in flat graphene are stable, which indicates that growth of single hydrogen lines in directions except the MRCL direction are suppressed. In summary, the most stable

configurations have an armchair-type pattern (H_{58} and H_{64}). Both evolve from D_2 but follow different paths. In addition, single-line formation is also favored. It is preferable when there are no unpaired hydrogens, while armchair-type orientation has the minimum energy even with unpaired hydrogens.

In order to examine directed growth for larger numbers of hydrogen atoms, we consider single-line and armchair-type configurations of 10 atoms. When hydrogen atoms lie along the MRCL, binding energy per hydrogen atom is enhanced by 116 meV and 131 meV compared to those that lie across the MRCL with 60° angle for single-line and armchair-type geometries, respectively. For 52° bending, the maximum length of stable single lines is as short as a tetramer across the MRCL with an angle of 60° .

90° bending. Relative total energies and the binding energies for 90° -bent graphene are listed in Tables S-VII–S-XI and Tables S-XVII–S-XXI. In Fig. 5(c), the most stable monomer, namely the parent of the dimers marks the position of the MRCL for 90° -bent graphene. The family tree is shown in Fig. 7, whereas a complete list of tested configurations can be found in Fig. S8 [48].

The first difference between 52° and 90° bending appears in the trimer generation. Tr_{14} is suppressed due to the stronger curvature effect in 90° bending, which succeeded in 52° . This means that only the lines as short as a hydrogen dimer are stable if they are not aligned with the MRCL. The family $D_6Tr(90^\circ)$ cannot produce any candidates that can succeed the pool selection. However, we proceed this family in order to check the energetics of lines across the MRCL. Family $D_2Tr_8Te_{18}P(52^\circ)$ is not observed in 90° bending, because its parent was eliminated in the previous generation. Family $D_4Tr_{13}Te_{23}P(90^\circ)$ is similar to $D_4Tr_{13}Te_{22}P(52^\circ)$ except the configuration P_{38} , which is also eliminated due to stronger curvature. The differences between 52° and 90° bending become more clear in hexamers. Even though $D_2Tr_8Te_{16}P_{28}H(52^\circ)$ and $D_2Tr_8Te_{16}P_{29}H(90^\circ)$ originate from the same parents, higher curvature does not allow succession of the configurations which are not on the MRCL. In 52° bending, hydrogens can prefer to be ordered along a short line across the MRCL within the same family, whereas 90° bending does not allow such a geometry. $H_{52}(52^\circ)$, which was eliminated, appears as a successful candidate as $H_{43}(90^\circ)$. This geometrical change reveals that single line formation on the second MRCL does not continue in 90° bending. In the family $D_2Tr_8Te_{16}P_{30}H$, H_{44} which is the same as $H_{55}(52^\circ)$, creates a single line on the second MRCL. Both H_{58} and H_{59} form a single line on the MRCL. H_{59} leaves an unoccupied site for this reason; H_{59} is less favored in total energy when compared to H_{58} . $H_{57}(90^\circ)$ is eliminated during the pool selection. However, $H_{74}(52^\circ)$,

which is identical to $H_{57}(90^\circ)$, succeeds through the whole selection process. This difference is originating from the the kink formation being stronger for 90° bending than it is in 52° bending. In summary, the main difference between 52° and 90° bending is in the length of hydrogen lines if they are not aligned with the MRCL. The number of eliminated candidates, especially in hexamer generation, are less than those of 52° bending due to the decrease in ROC. This result indicates that families of pentamer and hexamer generations are more stable than in 52° bending. As it is the case for 52° -bent graphene, armchair-type geometry is more favorable than the linear geometry along the MRCL. Binding energy per hydrogen atom in the armchair-type configuration is about 40 meV more than that of linear configuration. Growth of single line and armchair-type configurations consisting of 10 hydrogen atoms are compared along and across the MRCL and it is found that the binding energies per adsorbate are enhanced by 200 meV and 223 meV for single line and armchair-type geometries, respectively.

Considering lines consisting of six hydrogen atoms, bending increases the binding energies by 151 meV (176 meV) and 265 meV (289 meV) per hydrogen atom for 52° (90°) bending with single line and armchair-type configurations, respectively. This is a clear indication that curvature favors directed growth of hydrogen lines and it may overcome substrate effects.

Conclusion. High-throughput simulations show that our evolutionary algorithm is able to predict more stable configurations than those studied before. It is more preferable for hydrogen to adsorb on lines rather than making clusters, which obey the symmetries of the hexagonal lattice. Moreover, the line formation has a preferred crystallographic orientation, namely the armchair direction, while growth along the zigzag direction is suppressed. Combined with the effect of bending on chemical reactivity, the selection process eliminates hydrogen lines which are not aligned with the MRCL of bent graphene and a directed growth becomes possible. At intermediate bending angles, line formations crossing the MRCL are possible up to tetramers. When the ROC is smaller, the length shortens down to a hydrogen dimer. The growth can be viewed as a mechanical chain reaction. The reaction barrier is lowered by both bending of the surface and proximity to an occupied site. As a result kinked graphene can be fabricated, where the electrons on the opposite sides of the hydrogen line are decoupled [29].

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