## Enhanced van der Waals epitaxy via electron transfer enabled interfacial dative bond formation

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Enhanced van der Waals (vdW) epitaxy of semiconductors on a layered vdW substrate is identified as the formation of dative bonds. For example, despite that NbSe<sub>2</sub> is a vdW layered material, first-principles calculations reveal that the bond strength at a CdTe-NbSe<sub>2</sub> interface is five times as large as that of vdW interactions at a CdTe-graphene interface. The unconventional chemistry here is enabled by an effective net electron transfer from Cd dangling-bond states at a CdTe surface to metallic nonbonding NbSe<sub>2</sub> states, which is a necessary condition to activate the Cd for enhanced binding with Se.

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Epitaxial growth of materials with a large lattice and/or crystal symmetry mismatch on substrates via weak van der Waals (vdW) forces [1] has recently attracted much attention [2], especially after the concept of two-dimensional (2D) heterojunctions was proposed by Geim [3]. By definition, vdW epitaxy requires that both in-plane and out-of-plane orientations are well aligned between the overgrown materials and underlying substrates through vdW binding. To date, there exist ample examples of successful vdW epitaxy of a 2D layered vdW material on another 2D layered vdW substrate [4–7]. It is tempting to apply the same concept to the growth of ordinary semiconductors of a three-dimensional (3D) crystal structure on a layered substrate. Since one can mechanically peel off or chemically etch off a thin 2D layer and then place it on another substrate [8], the success of 3D on 2D growth could redefine the scope and applicability of epitaxy for applications not possible before. For example, a number of studies have been undertaken to achieve high-quality 3D nanowires (NWs) on 2D layered vdW substrates [9–14].

However, towards the goal of growing 3D materials with a continuous film morphology instead of the discrete NWs, the success is limited. Currently, the already-realized 3D-on-2D vdW epitaxy systems possess a spread of misorientation alignment in contrast to 2D-on-2D, unless with well-controlled growth techniques, e.g., the step-flow growth of single-crystal GaN on a "ragged" graphene [15]. This is because vdW binding is weak and the resulting energy landscape may not exhibit clearly defined minima as a function of the in-plane orientation angle that is a must for high-quality epitaxy. For example, in the recent vdW epitaxy experiment of CdTe on graphene [16], the measured full-width-at-half-maximum (FWHM) in-plane orientation dispersion is  $\sim 14^{\circ}$ . In contrast, a significantly smaller FWHM around 5° was found for CdTe-on-NbSe<sub>2</sub> [17]. This noticeable difference here is quite surprising because, judged from interlayer binding  $(E_{\rm B})$  of the layered structures, both NbSe<sub>2</sub> and graphene are typical vdW materials ( $E_B = 19.57 \text{ meV/Å}^2 \text{ versus } 18.32 \text{ meV/Å}^2 \text{)}$  [18].

Theories based on the idea of coincident-site lattice (CSL) matching have been applied to explain the 2D-on-2D vdW epitaxy [7,19]. The epitaxial relationship is realized here not

only by the interfacial interaction, but also by the lattice matching condition, i.e., by a minimization of the lattice strains. In 3D-on-2D vdW epitaxy, however, the same CSL matching assumption no longer holds because lattice-strain energy will increase with the thickness of the 3D material. To overcome such a difficulty, a cluster model has been used to simulate the growth of 3D structure. In general, however, there is no theory that can apply to the vdW epitaxy of a 3D solid on a 2D substrate or to the understanding of substrate dependence observed experimentally.

In this paper, we develop a first-principles theory for 3D vdW epitaxy on a 2D substrate. By a comparative study of CdTe-on-NbSe<sub>2</sub> and CdTe-on-graphene (G), the physics of significantly enhanced structural order in vdW epitaxy is elucidated. We find that when the dangling-bond electrons on the Cd atoms at the contacting surface are transferred to nonbonding NbSe<sub>2</sub> states, the formation of directional Cd-Se dative bonds is activated. The interfacial bond strength of CdTe-on-NbSe<sub>2</sub> is about five times that of CdTe-on-G but is significantly weaker than the usual Cd-Se bonds. As such, the enhanced binding can significantly reduce in-plane orientation dispersion, while keeping the highly desirable incommensurate and defect-free properties of the epitaxial films. While NbSe<sub>2</sub> is a metallic substrate, we expect the same principle for enhanced vdW epitaxy may also apply to a semiconducting substrate.

A detailed account of first-principles theories used in the study is given in the Supplemental Material (SM) [20] along with the formulation of the interfacial formation energy,  $E_{\rm form}$ . Under near-equilibrium growth condition, the probability of forming CdTe clusters can be estimated, within the canonical ensemble assumption, by

$$P_{\text{cluster}} = \frac{1}{ZN_{\text{cluster}}} e^{-E_{\text{form}}/kT}, \tag{1}$$

where Z is the canonical partition function,  $N_{\text{cluster}}$  is the number of atoms in a cluster, and kT is the thermal energy of 0.05 eV corresponding to a growth temperature of 300 °C.

To proceed, we consider the nucleation of stable clusters in the early stage of growth, because they are likely to determine the epitaxial relationship of the film with respect to the substrate [21]. These clusters should be the smallest possible, yet large enough not to rotate by thermal excitation. Since our focus is on the growth on a substrate, here we

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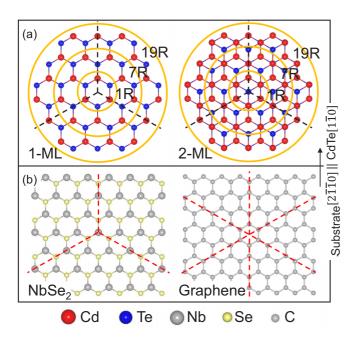


FIG. 1. Atomic structures of (a) 1-ML and 2-ML CdTe(111) clusters, in which the 1, 7, and 19 hexagon rings have been marked. (b)  $NbSe_2$  and graphene substrates. Dashed lines show the various crystal symmetries.

consider only flat clusters that can best wet the substrate, whose atomic structures (in a top view) are shown in Fig. 1(a) for 1-ML- and 2-ML-thickness, respectively. We will pay special attention to the 1, 7, and 19 hexagon-ring clusters (termed 1R, 7R, and 19R, respectively), because they are the most compact clusters in this size range with a least number of edge dangling bonds. In our definition, the A atoms of the binary AB compounds are in contact with the substrate. At 1-ML, the A/B atom ratios are 3:3, 12:12, and 27:27. At 2-ML, the ratios are 6:4, 24:19, and 54:46. Hence, stable 2-ML clusters are intrinsically A-atom rich. The atomic structures of bare NbSe<sub>2</sub> and graphene substrates are given in Fig. 1(b), showing that NbSe<sub>2</sub> has only a threefold rotational symmetry, whereas graphene has a sixfold rotational symmetry.

Epitaxial growth can happen either laterally or vertically (Fig. S1 of SM [20]). To determine which cluster(s) are vital to the experimentally observed epitaxial relationship, we have calculated numerous clusters. It is found that clusters with A = Cd have noticeably stronger interfacial binding energies than clusters with A = Te. Hence, herein we will discuss only clusters with Cd contacting the substrate. Figures 2(a) and 2(b) show the calculated formation energy for 1R, 7R, 19R clusters and bulk films ( $\infty R$ ) with 1-, 2-, and 4-ML thicknesses, which reveals that the formation energies of CdTe-on-NbSe2 are generally lower than those of CdTe-on-G. The corresponding atomic structures are described in Figs. S2 and S3 of the SM [20]. As the 1-ML clusters are stoichiometric, their formation energy is independent of the growth conditions. On the other hand, due to the dependence on the chemical potential, the formation energy of 2-ML clusters spans an energy range, as represented by the vertical bar in Figs. 2(a) and 2(b). Because all the 2-ML clusters are Cd-rich, therefore it makes sense to use the lower bounds in the following discussion. It shows

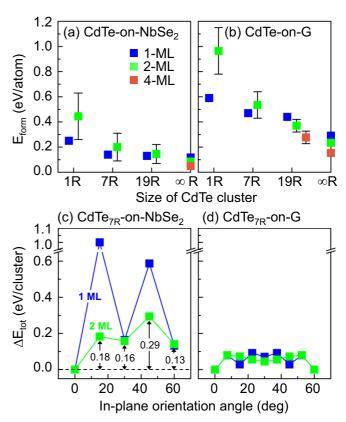


FIG. 2. (a, b) Formation energies for stable CdTe clusters at different thicknesses on (a) NbSe $_2$  and (b) graphene (G) substrates. Energy for the 2-ML-thick clusters is generally a function of the growth condition with lower bound = Cd-rich and upper bound = Cd-poor. (c, d) Total energy difference as a function of the in-plane orientation angle between the CdTe $_{7R}$  cluster and (c) NbSe $_2$  and (d) graphene substrate, respectively.

that the 2-ML clusters are more stable than the 1-ML clusters except 1R clusters, which also makes sense because the 2-ML clusters structural-wise are much closer to bulk films.

Figures 2(a) and 2(b) show that, regardless the choice of the substrate, the smallest 1R clusters have relatively high energies and hence prefer to grow laterally. As the size increases, however, results for CdTe-on-NbSe2 can be quite different from those for CdTe-on-G. In the former case, the energy differences between the 7R and 19R clusters are rather small, e.g.,  $\Delta E_{form} < 0.02\,\text{eV/atom}$  for both 1- and 2-ML clusters. The difference between the 2-ML 7R cluster and 2-ML film is also in the same energy range. Even when a thicker 4-ML film forms, the energy lowering from that of the 2-ML film is <0.02 eV/atom. Using Eq. (1) and Fig. 2(a), we determine that the 2-ML and 1-ML 7R clusters are the most abundant clusters during the initial growth stage. Hence, they should be used to study the epitaxial relationship between CdTe and NbSe<sub>2</sub>. In contrast, in the case of CdTe-on-G,  $\Delta E_{\text{form}}$  is on the order of 0.1 eV/atom between 2-ML 7R and 19R, between 2-ML 19R and 2-ML film, and between 2-ML film and 4-ML film. From Eq. (1) and Fig. 2(b), the most abundant clusters on graphene substrate are 4-ML and 2-ML 19R clusters, followed by 2-ML and 1-ML 7R clusters. In addition to clusters of equal size at different layers, clusters combining monolayers of different sizes (e.g., 2-ML 1R+7R) are also considered, with the results summarized in Fig. S4 of the SM [20].

To determine the epitaxial relationship of the cluster with respect to the substrate, we need to examine how the total energy of the system,  $E_{\text{tot}}$ , varies with in-plane orientation angle of the cluster. This is shown in Fig. 2(c) for 2-ML  $CdTe_{7R}$ -on-NbSe<sub>2</sub>, where 0° is defined as  $CdTe[1\bar{1}0] \parallel$ Substrate[2110]. It takes about 0.2 eV/cluster to rotate the cluster by 30°, but the structure is highly unstable. It will take 0.29 eV/cluster to rotate the cluster by 60°, which is 0.13 eV/cluster higher in energy than the (unrotated) 0° result. Given that  $kT \approx 0.05 \,\mathrm{eV}$ , the barrier here is large enough to fix the epitaxial relationship of the clusters before they grow into the larger and less-rotatable 19R clusters. Hence, we conclude that CdTe should take the parallel epitaxy (namely 0°). It appears that using 1-ML CdTe<sub>7R</sub>-on-NbSe<sub>2</sub>, the same conclusion can also be reached. In contrast, for 2-ML CdTe<sub>7R</sub>on-G in Fig. 2(d), it takes only 0.08 eV/cluster to rotate the cluster by 30°, which is 0.05 eV/cluster higher in energy than the  $0^{\circ}$  result. This barrier is unlikely to fix the epitaxial relationship for it is too close to the thermal energy of 0.05 eV. Hence, both 0° and 30° epitaxies exist for CdTe on graphene. As clusters grow larger, their rotation becomes less likely, because our calculation shows a much larger rotation barrier of 0.39 eV/cluster for CdTe-on-G, when the size is 19R. This is indeed what was observed by experimental XRD pole figure measurements [16,17] showing a significantly larger FWHM for CdTe-on-G ( $\sim$ 14°) than that for CdTe-on-NbSe<sub>2</sub> ( $\sim$ 5°).

To understand the physical origin of the different energy landscape between NbSe2 and graphene, next we consider the change in the electron density  $(\Delta \rho)$  due to the interface formation, shown in Fig. 3 for a 2-ML CdTe<sub>7R</sub> cluster on (a–c) NbSe<sub>2</sub> and (d) graphene, respectively. It shows that, while  $\Delta \rho$  associated with the interface formation is significant for CdTe-on-NbSe<sub>2</sub>, the same can be neglected for CdTe-on-G when the charge contour is identical to that in Fig. 3(c) (the result at 1/10 contour value is given in Fig. S5 in the SM [20]). These results are consistent with our Bader analysis, which shows a total of 4.76-electron transfer from CdTe to NbSe<sub>2</sub> for CdTe<sub>7R</sub>-on-NbSe<sub>2</sub>, but only a total of 0.92-electron transfer for CdTe<sub>7R</sub>-on-G. The smaller transfer to graphene is consistent with the fact that vdW force is rooted in dipole-dipole interaction that does not involve much transfer of electrons.

In the following, therefore, we will focus on 2-ML CdTe<sub>7R</sub>-on-NbSe<sub>2</sub> for a possible mechanism of enhanced vdW epitaxy. It appears that one can understand the electron transfer qualitatively by examining the planar-averaged  $\overline{\Delta\rho}(z)$ in Fig. 3(a) with three characteristic features: (1) a depletion of electrons near the Cd atoms at the bottom surface of the cluster, (2) an accumulation of electrons in the interfacial region between Cd and Se, and (3) a weakening of the Nb-Se bonding beneath the interface. One can find more details in the side view in Fig. 3(b) where the nonaveraged  $\Delta \rho(\vec{r})$  is shown. Electrons depleted from surface Cd atoms accumulate in the region between the Cd and Se atoms at the interface, as can be seen in Fig. 3(b). Accordingly, electrons in the bonding states in the next layer between Nb and Se atoms retract somewhat back to the respective atoms. Accompanied by the retraction,  $\sim$ 1% Nb-Se bond elongation is observed.

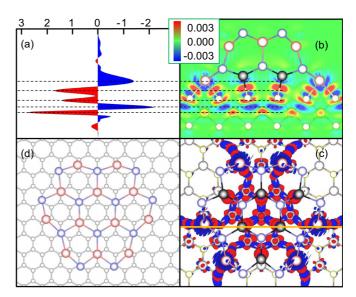


FIG. 3. Electron density change  $(\Delta \rho)$  near the interface between 2-ML CdTe<sub>7R</sub> and (a–c) NbSe<sub>2</sub> and (d) graphene substrate. (a) Planer-averaged  $\overline{\Delta \rho}(z)$  (e/Å). (b) Side view and (c) top view of  $\Delta \rho(\overrightarrow{r})$  (e/Å<sup>3</sup>): red = accumulation and blue = depletion. For clarity, in panel (b) only atoms near the selected plane, denoted by the orange line in (c), are shown. In panels (c) and (d), on the other hand, only the bottom layer of the CdTe cluster is shown, with charge contour value of  $\pm$  0.003 e/Å<sup>3</sup>. To make a distinction between the corner and central atoms, the six central Cd atoms are darkened.

To understand what happens in CdTe-on-NbSe<sub>2</sub>, we plot the atomic site-decomposed density of state (DOS) in Fig. 4(a) for interfacial atoms, showing a noticeable orbital interactions between the Cd and Se states (cf. Fig. S6 of the SM [20]

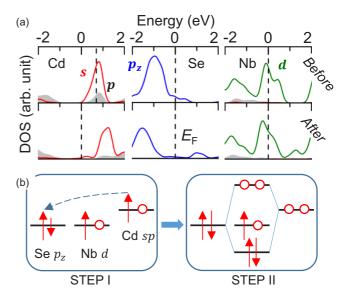


FIG. 4. (a) Site-decomposed DOS for interfacial Cd, Se, and Nb atoms before and after the formation of the interface between 2-ML CdTe $_{7R}$  cluster and NbSe $_2$  substrate. (b) A schematic diagram summarizing the electron transfer in step I and dative bond formation through level repulsion between interfacial Cd and Se states in step II. A shorter spin arrow in panel (b) indicates that in that spin channel, there is still room to accept electrons.

for DOS over a wider energy range). In the plot, electrostatic potentials are used to align the states before and after the interface formation. As a result of the interactions, the originally half-occupied Cd-sp states are fully emptied and subsequently pushed up in energy, while the nearly fully occupied Se- $p_z$  states are fully occupied and subsequently pushed down. These occupation changes enable dative bond formation between an empty cation state and doubly occupied anion state. Figure 4(b) summarizes schematically the main results in Figs. 3 and 4(a) in terms of the above two steps: (I) an electron transfer across the interface and (II) a level repulsion through orbital interaction and the subsequent dative bond formation.

Strictly speaking, the two-step chemistry in Fig. 4(b) deviates from the standard dative-bond picture, because the bond formation here relies on the emptying of Cd dangling-bond states, which becomes possible only because of the presence of Nb nonbonding d states [see Fig. 4(a)]. These states serve as a reservoir to accept excess electrons. If NbSe<sub>2</sub> were a semiconductor, for example, the Se lone pair would be fully occupied. The 2-ML CdTe<sub>7R</sub> cluster, on the other hand, has an excess of  $(24 - 19) \times 2 = 10$  electrons (distributed over 12) Cd atoms with 18 dangling bonds). Because the fully occupied Se lone pairs have no room to accept these electrons, the strength of the dative bonds will be greatly reduced. In reality, the Nb-d states accept electrons not only from the CdTe states but also from the Se- $p_z$  states. Therefore, on the appearance, electron transfer takes place between Cd dangling-bond and Se- $p_7$  lone-pair states, as schematically illustrated in Fig. 4(b). In short, the net charge transfer is from Cd unpaired electrons in CdTe clusters to the nonbonding Nb-d states, after which the Cd forms dative bonds with the substrate Se.

For CdTe-on-G, in principle there can also be an electron transfer from the CdTe to metallic graphene states, which would also suggest a significantly enhanced vdW binding through dative bond formation, which, however, does not happen. This is because NbSe<sub>2</sub> is considerably more electronegative than graphene, as evidenced by their different work functions:  $\Phi = 5.9$  and 4.6 eV for NbSe<sub>2</sub> and graphene [22,23], respectively. These values may be contrasted to the electron affinity ( $\chi = 4.3 \,\text{eV}$ ) for CdTe [24]. Hence, the driving force for electron transfer from CdTe to NbSe2 is much greater than that to graphene, as having also being revealed by our Bader analysis. Note that, while an electron transfer can enhance interfacial binding, it may not be enough to enhance vdW epitaxy, because the latter also requires an enhancement of directional bonding. It is thus the second step, namely, the formation of dative bonds, that plays the key role in the enhanced vdW epitaxy. On this note, graphene is not a good substrate for significantly enhanced vdW epitaxy, because its  $p_z$  orbital is engaged in aromatic  $sp^2$  bonding and there is an energy barrier to change the hybridization from  $sp^2$  to  $sp^3$  to make a dative bond [25]. The dative bond energy for CdTe-on-NbSe<sub>2</sub> (1.3 eV/CdSe) is less than the standard Cd-Se bond strength of 2.1 eV/CdSe of wurtzite CdSe (cf. Fig. S7 of the SM [20]), which is in accordance with the slightly longer Cd-Se bond length (2.7–2.8 Å at interface vs 2.6 Å in wurtzite crystal). One can write the above interfacial binding energy per CdSe in terms of energy per CdTe to yield 1.88 eV/CdTe at the CdTe-NbSe<sub>2</sub> interface, which is five times as large as that of 0.38 eV/CdTe at the CdTe-G interface.

The mechanism for enhanced vdW epitaxy discussed above is clearly beyond just CdTe-NbSe<sub>2</sub>. It should apply broadly to other substrates as well, as long as the interfacial dative bond formation can be activated by a removal of excess electrons at the cation sites. For example, recently experiments showed epitaxial growth of other 3D films on layered vdW substrates, in particular, PbSe-on-Bi<sub>2</sub>Se<sub>3</sub> [26] and PbI<sub>2</sub>-on-Mica [27]. In both cases, our calculations show noticeably enhanced interfacial binding energies (see Fig. S8 in the SM [20] and discussion therein). It is worthy noted that, at PbSe(001)-on-Bi<sub>2</sub>Se<sub>3</sub>(0001) interface, electrons transfer from Pb dangling bonds to neighboring Se atoms happen before the interface formation. The emptied Pb orbitals then form dative bonds with substrate Se, which exemplifies that enhanced vdW epitaxy can come solely from dative bond formation.

In summary, an electronic theory that differentiates the epitaxy of 3D semiconductors on seemingly identical vdW layered substrates is proposed. Application to the prototypical CdTe epitaxy on NbSe<sub>2</sub> and graphene, by means of firstprinciples calculation, reveals the origin for their differences, in particular, the enhanced vdW epitaxy of CdTe on NbSe<sub>2</sub> can now be understood as the formation of interfacial dative bonds. Unlike a standard dative-bond mechanism, however, here electron transfer between surface Cd dangling-bond states and nonbonding NbSe2 states must precede the bond formation. Understanding and harnessing this unexplored regime of epitaxy is at the cusp of materials physics, which offers great potential not only to grow epitaxial 3D crystals and superlattices on 2D vdW substrates, but also to understand how the bonding chemistry operates in naturally occurring layered crystals, which can be vital for novel crystal design.

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