High-pressure behavior of CaMoO₄

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We report a high-pressure study of tetragonal scheelite-type CaMoO₄ up to 29 GPa. In order to characterize its high-pressure behavior, we have combined Raman and optical-absorption measurements with density functional theory calculations. We have found evidence of a pressure-induced phase transition near 15 GPa. Experiments and calculations agree in assigning the high-pressure phase to a monoclinic fergusonite-type structure. The reported results are consistent with previous powder x-ray-diffraction experiments, but are in contradiction with the conclusions obtained from earlier Raman measurements, which support the existence of more than one phase transition in the pressure range covered by our studies. The observed scheelite-fergusonite transition induces significant changes in the electronic band gap and phonon spectrum of CaMoO₄. We have determined the pressure evolution of the band gap for the low- and high-pressure phases as well as the frequencies and pressure dependencies of the Raman-active and infrared-active modes. In addition, based on calculations of the phonon dispersion of the scheelite phase, carried out at a pressure higher than the transition pressure, we propose a possible mechanism for the reported phase transition. Furthermore, from the calculations we determined the pressure dependence of the unit-cell parameters and atomic positions of the different phases and their room-temperature equations of state. These results are compared with previous experiments showing a very good agreement. Finally, information on bond compressibility is reported and correlated with the macroscopic compressibility of CaMoO₄. The reported results are of interest for the many technological applications of this oxide.

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I. INTRODUCTION

In recent years, scheelite-structured orthomolybdates have gotten broad attention because of the many applications in which they can be used. These applications run from scintillating detectors to solid state lasers and include fluorescent lamps and catalytic materials, among others [1]. Currently, calcium molybdate (CaMoO₄), due to its unique thermal, chemical, and luminescence properties, is considered one of the most suitable materials for the above described technological functions. As a consequence, during the last years, the electronic and optical properties of CaMoO₄ have been extensively studied at ambient pressure [1-8]. This compound has a tetragonal crystal structure, which is isomorphic to the scheelite structure and can be described by space group $I4_1/a$ [9]. In this structure, shown in Fig. 1, each molybdenum (Mo) atom is surrounded by four oxygen (O) atoms forming a regular MoO₄ tetrahedron and each calcium (Ca) atom is coordinated by eight O atoms forming a CaO₈ dodecahedron. Notice that CaMoO₄ can be synthetically prepared but it is also found in nature, its mineral name being powellite.

High-pressure (HP) research has proven to be a useful tool for improving the understanding of the physical properties of scheelite CaWO₄ [9–22]. In particular, the conclusions extracted from Raman [13,21], x-ray diffraction (XRD)

[12,17–20], and *ab initio* calculations [13,17,22] support that compression triggers a phase transition from the scheelite to the monoclinic fergusonite-type structure (space group I2/a also described by space group C2/c). The combination of theory and experiments has allowed us also to obtain an accurate description of the pressure dependence of many physical parameters of CaWO₄. In particular, it has helped us to understand that the large band-gap reduction at the phase transition is due to the changes in the interatomic distances associated with the structural changes at the phase transition [15]. The existence of a second phase transition in CaWO₄ beyond 33.4 GPa has been also recently reported [12].

In contrast with CaWO₄, the HP behavior of CaMoO₄ is not so well understood and there are contradictions among the results reported in the literature. The first HP study on CaMoO₄ was carried out by Nicol and Durana nearly half a century ago [23]. Using Raman spectroscopy, they found evidence of a phase transition below 4 GPa. However, their experiments were carried out using NaCl as pressure medium, which generated nonhydrostatic conditions [24]. On the other hand, in the 1980s it was shown by single-crystal XRD experiments carried out under quasihydrostatic conditions (a 4:1 methanol-ethanol mixture was used as pressure medium) that there was no phase transition in CaMoO₄ up to 5.8 GPa [9]. Subsequent Raman studies carried out in the 1990s under similar experimental conditions [25] reported pressure-induced changes in the Raman spectra which were attributed to two phase transitions observed around 8.2 and 15 GPa. These conclusions have been

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FIG. 1. Schematic view of the low-pressure and high-pressure polymorphs of CaMoO₄. Ca atoms: blue. Mo atoms: purple. Oxygen atoms: red. The coordination polyhedra of Ca and Mo are also shown.

challenged by more recent powder XRD measurements [26] in which only one phase transition from the scheelite to the fergusonite phase (isomorphic to the HP phase of CaWO₄) was observed at 15 GPa. However, posterior Raman experiments observed this phase transition at 10 GPa [27]. More recently, the luminescence of CaMoO₄:Pr³⁺ was investigated as a function of the pressure [28], with reports that the most intense lines in the luminescence spectrum progressively vanish from 10.6 to 17.5 GPa. Similar conclusions were obtained from luminescence measurements of CaMoO₄:Tb³⁺ [29]. These observations cannot be fully explained by conclusions extracted from previous XRD and Raman studies.

All the facts described above suggest that the performance of additional HP studies on CaMoO₄ is needed to properly understand the HP behavior of this technologically important material. Here we will report a combined experimental and theoretical study of CaMoO₄ under compression. Raman spectroscopy and optical-absorption experiments have been carried out up to 28 GPa, which are complemented by ab initio calculations performed up to 29 GPa. This approach has allowed researchers in the past to accurately understand the HP behavior of scheelite-type $SrMoO_4$ [30]. In the case of CaMoO₄, our results are fully compatible with previous XRD experiments [26]. Only one phase transition occurs in CaMoO₄ below 29 GPa. The transition has important consequences for the physical properties of CaMoO₄, which will be discussed in detail. In particular, the pressure dependencies of unit-cell parameters, Raman and infrared (IR) modes, and the electronic band gap will be also reported for the different phases. Possible explanations for the inconsistencies among previous HP studies of $CaMoO_4$ will be proposed. The reported studies have enabled us to improve the understanding of the HP properties of $CaMoO_4$ and related compounds.

II. EXPERIMENTAL DETAILS

CaMoO₄ single crystals were grown by means of a fluxgrowth method [31]. The composition of the starting mixture was CaO 7%, Na2CO3 18%, MoO3 75% (in wt %). The mixture was careful mixed, put in a platinum crucible, and slowly heated to 1350 °C in a horizontal furnace. After a 12 h soaking time the temperature was lowered to 600 °C at a rate of 5 °C/hour. Transparent crystals up to $3 \times 2 \times 1 \text{ mm}^3$ were separated from the flux using hot diluted HCl. The crystal structure and purity of the crystals were determined by powder XRD at the BL11 beamline of the INDUS2 synchrotron source [32] using monochromatic x rays of wavelength 0.62406 Å. CaMoO₄ crystallizes in the tetragonal scheelite structure with space group $I4_1/a$ and the unit cell parameters are a = 5.224(1) Å and c = 11.427(2) Å. The atomic positions are summarized in Table I. The crystal structure obtained for CaMoO₄ agrees very well with that determined from single-crystal XRD [9] and neutron diffraction [33].

For both HP Raman and optical-absorption measurements samples were obtained from the above described single crystals. In the optical experiments thin platelets $(100 \,\mu\text{m} \times 100 \,\mu\text{m} \times 10 \,\mu\text{m})$ were cleaved from the single crystals of CaMoO₄ along the $\{101\}$ natural cleavage plane [34]. The samples were loaded in a diamond-anvil cell (DAC) with diamond anvils with a culet size of $400 \,\mu$ m. Tungsten or Inconel were used as the gasket material. The gasket was pre-indented to a thickness of $50\,\mu\text{m}$ and a hole with a diameter of 120 μ m was drilled in its center to form a pressure chamber. Special caution was taken during the sample loading to avoid sample bridging between the diamond anvils [35,36]. Pressure was determined using the ruby scale [37]. A 4:1 methanol-ethanol mixture was used as a pressure-transmitting medium [38]. In the pressure range covered by the experiments (20 GPa for optical absorption and 28 GPa for Raman) we found that the ruby lines showed a full width at half maximum smaller than 0.4 nm. This observation indicates than even beyond the hydrostatic limit of the PTM (≈ 10 GPa) [38] the uniaxial stresses applied to the sample were small.

Raman spectra were collected using a 488 nm argon-ion laser in Jobin-Yvon triple Raman spectrometer T64000. The instrument was calibrated using the well-known phonon modes of silicon. In the measurements a laser power of less than

TABLE I. Structural parameters of the scheelite structure $(I4_1/a)$ at ambient pressure. Experiment: a = 5.224(1) Å, c = 11.427(2) Å. Theory: a = 5.21600 Å, c = 11.32075 Å.

		Theory			Experiment		
Atom	Site	x	у	Z	x	у	z
Ca	4e	0	0.25	0.625	0	0.25	0.625
Мо	4e	0	0.25	0.125	0	0.25	0.125
0	4e	0.15296	0.00575	0.21114	0.1503(5)	0.0062(5)	0.2089(5)

20 mW before the DAC was used to avoid sample heating. The spectral resolution of the system is below 1 cm^{-1} . Optical-absorption measurements in the ultraviolet-visiblenear-infrared (UV-VIS-NIR) range were carried out using a confocal setup. This system was built using an Ocean Optics DH-2000 light source, two Cassegrain objectives, and a USB2000 UV-VIS-NIR spectrometer from Ocean Optics [39,40]. The absorption spectra were obtained at selected pressures from the recorded transmittance spectra. These spectra were acquired using the sample-in sample-out method [41,42].

III. COMPUTATIONAL DETAILS

Ab initio simulations of CaMoO₄ under pressure up to 29 GPa were performed using density functional theory (DFT) [43]. The calculations were carried out with the Vienna ab *initio* simulation package (VASP) [44] employing pseudopotentials with the projector augmented wave scheme (PAW) [45]. With the aim of obtaining precise results, the set of plane waves was expanded up to a kinetic-energy cut off of 520 eV. On the other hand, the generalized-gradient approach (GGA) was used for describing the exchange-correlation energy. In particular, the Perdew-Burke-Ernzenhof prescription for solids (PBEsol) [46], which accurately describes the properties of densely packed solids, was employed. Integrations over the Brillouin zone (BZ) were performed using dense meshes of Monkhorst-Pack special k points [47] which guarantee a convergence in energy better than 1 meV per formula unit. For the crystal structures considered, all the structural parameters were optimized, at selected volumes, minimizing the forces on atoms (forces $< 0.004 \text{ eV}/\text{\AA}$) and the stress tensor (diagonal stresses differences <0.05 GPa). From the computer simulations, total energy (E), volume (V), and pressure (P)data sets were obtained (pressure like other energy derivatives is obtained from the calculated stress tensor). The enthalpy (H)was calculated as a function of P. The thermodynamic stability of the different phases was determined from the analysis of the H-P plots. The Raman and IR phonons were studied with the direct force-constant method [48]. The lattice-dynamic calculations were performed at the zone center (Γ point) of the BZ. The phonon dispersion of the scheelite structure as a function of pressure was calculated with the supercell method in order to determine possible mechanisms of the observed phase transition [49]. Finally, the electronic density of states of both phases of CaMoO₄ and the band structure were calculated following standard procedures [50].

IV. RESULTS AND DISCUSSION

A. Optical-absorption experiments

A selection of the spectra collected in the optical-absorption measurements at different pressures in CaMoO₄ is shown in Fig. 2. The spectrum measured at ambient pressure (10^{-4} GPa) is very similar to those reported by Lukanin *et al.* and Fujita *et al.* [51,52] and resembles the absorption spectrum of other scheelite-structured molybdates [30]. The steep increase of the absorption coefficient α with respect to the photon energy is consistent with a direct nature for the fundamental band gap. This is agreement with the conclusions of Zhang *et al.*



FIG. 2. Optical-absorption edges of $CaMoO_4$ at selected pressures. The abrupt change found from 13.9 to 14.5 GPa is indicative of the phase transition.

[53]. In order to determine the value of the band-gap energy (E_{gap}) at all pressures, we followed the procedure described in Ref. [54]. We obtained at ambient pressure $E_{gap} = 4.50(5) \text{ eV}$, in agreement with the value determined from luminescence measurements by Hemphill et al. [55]. In Fig. 2 it can be seen that under pressure the absorption edge gradually redshifts up to 13.9 GPa. A similar behavior was previously observed in scheelite-type CaWO₄ [15] and SrMoO₄ [30]. In a subsequent compression step, at 14.5 GPa we have detected a sudden shift towards low energy in the absorption edge. Such change is typical of the scheelite-fergusonite transition [15] found in XRD measurements [26]. Since the main change in the absorption spectrum is the shift in energy, without major changes in its shape, it can be assumed that the HP phase also is a direct bandgap material. Under further compression, in the HP phase, the absorption edge again continuously redshifts, but faster than in the low-pressure phase (see Fig. 2). This indicates that only one phase transition takes place in CaMoO₄ up to 20 GPa. This result confirms the conclusions of Crichton and Grzechnik [26] who reported a phase transition at 15 GPa and casts doubts on the existence of two phase transitions, one at 8.2 and the other at 15 GPa, as proposed from Raman spectroscopy measurements [25]. We will discuss in detail this issue after reporting the Raman experiments and *ab initio* calculations.

In Fig. 3 we present the value determined for E_{gap} at different pressures for the two phases of CaMoO₄. In the low-pressure scheelite phase E_{gap} decreases from 4.50(5) eV at ambient pressure to 4.42(5) eV at 13.9 GPa. The pressure dependence of the band-gap energy can be well described by a quadratic function: $E_{gap}(eV) =$ $4.50-8\times10^{-3}P + 1.9\times10^{-4}P^2$, where the pressure is in GPa. After the phase transition, at 14.5 GPa we determined $E_{gap} =$ 3.95(5) eV. The decrease of the band gap at the transition is approximately 0.5 eV. In the HP phase E_{gap} is more sensitive to pressure than in the low-pressure phase. From 14.5 to 20.5 GPa, E_{gap} is reduced approximately 0.6 eV. In the HP



FIG. 3. Pressure dependence of E_{gap} in the low- and high-pressure phases. Symbols correspond to experimental results. Solid lines are a quadratic fit to the experiments. The dashed red lines are the theoretical results. The theoretical results have been shifted up by 1 eV to facilitate comparison.

phase the band-gap energy as a function of pressure is given by $E_{gap} = 5.50 - 11 \times 10^{-1}P + 2.5 \times 10^{-4}P^2$. The pressure dependence of E_{gap} obtained for CaMoO₄ is qualitatively similar to that previously reported for CaWO₄ (compare Fig. 3 with Fig. 2 in Ref. [15]).

B. Raman spectroscopy

In previous Raman experiments [25] changes in the Raman spectrum that were attributed to a phase transition were observed at 8.2 GPa. A second transition was found at 15 GPa. However, our optical experiments and previous XRD experiments [26] only found evidence of the second transition. In order to understand this apparent discrepancy, we have carried out Raman experiments up to 28 GPa. A selection of Raman spectra is shown in Fig. 4. We found a broadening of Raman peaks at 12 GPa, which is consistent with the hydrostatic limit of the pressure medium used in the experiments. However, all Raman spectra can be undoubtedly identified with the scheelite structure up to 13.5 GPa. The thirteen Raman-active modes ($\Gamma = 3A_g + 5B_g + 5E_g$) [56] have been measured from ambient pressure up to 13.5 GPa. It can be seen from Fig. 4 that with pressure, apart from a separation of two overlapping modes A_g and B_g at $\sim 300 \,\mathrm{cm}^{-1}$, no other mode is suggestive of a phase transition at low pressures. We would like to mention here that this mode separation is due to a different pressure dependence of both these modes as is apparent from Table II and Fig. 5. Upon further compression clear changes occur in the Raman spectrum at 17 GPa. In particular, the appearance of new modes can be detected. These changes are evidence of the



FIG. 4. Raman spectra measured at different pressures. The red ticks indicate the position of Raman modes in scheelite at ambient pressure and in fergusonite at 17 GPa.

phase transition detected by the other two techniques near 15 GPa. The Raman spectra of the HP phase resemble that of the fergusonite structure of related compounds. In particular, the presence of four modes in the high-frequency region and the increase of the total number of modes to eighteen $(\Gamma = 8A_g + 10B_g)$ [56] is consistent with the identification of the HP phase as fergusonite made by XRD [26]. As we will show next, ab initio calculations fully support this conclusion. We think that the previous identification of a phase transition at 8.2 GPa could be caused by nonhydrostatic conditions [24,30,36]. Such conditions usually enhance kinetic barriers, reduce the transition pressure, and favor phase coexistence in a large pressure range. As a consequence, the pressure region from 8.2 to 15 GPa of the previous Raman experiments [25] could be in fact a coexistence region between the low-pressure scheelite phase and the high-pressure fergusonite phase, the onset of the transition being at 8.2 GPa but being completed only at 15 GPa (the transition pressure of the rest of the experiments). Indeed, the Raman spectrum reported by Christofilos et al. at 22 GPa [25] is very similar to the Raman spectrum we measured at the same pressure for fergusonite-type CaMoO₄. Our interpretation fully reconciles

TABLE II. Frequencies and pressure coefficients of Raman modes determined for scheelite-type CaMoO₄ at ambient pressure. Experimental and theoretical results are shown. For the experiments the Grüneisen parameters are also given. They have been calculated assuming $B_0 = 82$ GPa [26].

	Theory (this work)			Experimer	Experiment (Ref. [25])		
Raman Mode Symmetry	ω_0 (cm ⁻¹)	$\frac{d\omega}{dP}$ (cm ⁻¹ /GPa)	ω_0 (cm ⁻¹)	$\frac{d\omega}{dP}$ (cm ⁻¹ /GPa)	Mode Grüneisen Parameter γ	ω_0 (cm ⁻¹)	$\frac{\frac{d\omega}{dP}}{(\mathrm{cm}^{-1}/\mathrm{GPa})}$
$\overline{B_g}$	105	-0.42	110	-0.34	-0.25	113	-0.15
$\tilde{E_g}$	142	1.72	142	1.63	0.95	145	1.9
E_{g}°	186	3.69	188	3.68	1.61	193	4.0
A _g	204	3.56	203	3.32	1.34	206	3.7
B_{g}°	211	4.58	215	4.59	1.75	220	5.1
$\vec{E_g}$	264	6.17	265	6.11	1.89	270	6.5
A _g	309	2.41	320	2.39	0.61	324	2.5
B_{g}°	318	3.99	325	3.98	1.01	330	4.2
B_{g}	378	3.83	390	3.6	0.76	392	4.8
$\vec{E_g}$	389	4.13	401	4.03	0.82	402	4.6
Ĕ _g	792	2.77	792	2.73	0.28	796	3.0
B_{g}°	836	1.73	846	1.61	0.16	850	2.1
A _g	871	2.01	877	1.99	0.19	882	2.1

all HP experiments carried out for CaMoO₄. It will explain also why in the highly nonhydrostatic experiments carried out nearly half a century ago [23] the phase transition was



FIG. 5. Pressure dependence of Raman modes. Symbols represent experiments and lines calculations. We use circles (squares) for scheelite (fergusonite) and different colors for A_g , B_g , and E_g modes as indicated in the inset.

detected at 4 GPa. Notice that the influence of deviatoric stresses in the HP structural sequence of molybdates is not an unknown phenomenon. In $SrMoO_4$ it has been also observed [30,57].

From our experiments we determined the frequency of the Raman modes of the low- and high-pressure phases. For those modes that partially overlap a Lorentzian multipeak fitting analysis was used for the deconvolution of the different modes. The results are summarized in Tables II and III. The mode assignment has been made based on the literature [25] and present ab initio calculations. The pressure dependence of the different modes is represented in Fig. 5. For the scheelite phase the dependence is nearly linear up to 13.5 GPa. For fergusonite, in the pressure range where this phase is detected by the experiments (>17 GPa), the pressure dependence is nearly linear too (however, when discussing the calculations, we will describe that a nonlinear behavior occurs from the transition pressure to 17 GPa). The obtained pressure coefficients are included in Tables II and III. In the tables we compare our results with earlier results [25]. For the scheelite phase, at ambient pressure the agreement is quite good, in particular with the Raman frequencies measured by Porto and Scott [58]. As mentioned before, for the scheelite phase we have measured the thirteen Raman modes and for the HP phase we have measured eighteen modes. Their frequencies agree quite well with the calculated frequencies (see Table III). Some of the fergusonite modes coincide very well with the modes identified as HP phase II previously [25]. This fact supports the hypothesis that there are no HP phases I and II and that the transition occurs directly at 15 GPa from scheelite to the HP phase assigned by XRD to the fergusonite phase (which corresponds to the previously named HP phase II). The main distinguishable feature of the Raman spectrum of scheelite CaMoO₄ is the existence of a low-frequency B_g mode with a negative pressure coefficient (see Table II), which is typical of scheelites [56]. This mode continues to have a negative pressure coefficient till 13.5 GPa unlike in earlier studies [25] where it showed a positive pressure coefficient beyond

TABLE III. Frequencies and pressure coefficients of Raman modes determined for fergusonite-type CaMoO₄. Experimental (17 GPa) and theoretical (17.6 GPa) results are shown and compared with previous experimental results [25]. For the present experiments the Grüneisen parameters are also given. They have been calculated assuming $B_0 = 86.7$ GPa (present calculations).

	Theory (this work)			Experimer	Experiment (Ref. [25])		
Raman Mode Symmetry	ω_0 (cm ⁻¹)	$\frac{\frac{d\omega}{dP}}{(\mathrm{cm}^{-1}/\mathrm{GPa})}$	ω_0 (cm ⁻¹)	$\frac{d\omega}{dP}$ (cm ⁻¹ /GPa)	Mode Grüneisen Parameter γ	ω_0 (cm ⁻¹)	$\frac{d\omega}{dP}$ (cm ⁻¹ /GPa)
$\overline{A_g}$	122	2.73	114	2.76	2.09	116	1.4
B_g	160	1.65	161	0.64	0.34		
B_g	193	1.10	187	1.10	0.51		
B_{g}	233	1.75	231	0.91	0.34		
B_g	258	2.87	254	3.00	1.02		
A _g	261	1.45	261	1.36	0.45	258	1.9
A _g	280	1.14	286	0.91	0.27	280	2.1
A _g	355	2.43	343	1.64	0.41		
B_{g}	360	2.92	365	2.45	0.58	355	2.8
A _g	382	1.41	380	1.82	0.41		
B_{g}	392	4.05	392	2.95	0.65	390	3.1
B_{g}°	454	2.15	453	1.55	0.29	449	5.4
Å _g	460	4.12	462	2.55	0.47	460	5.0
B_{g}	473	3.07	478	2.64	0.47		
B_{g}°	805	0.65	812	1.09	0.11		
Å,	835	-0.64	840	-0.72	-0.07	868	-2.5
B_{g}°	854	2.43	860	2.63	0.26		
Åg	915	2.10	915	2.27	0.21	905	2.3

8.2 GPa. The similarities between the phonon distribution in the low- and high-pressure phases and the presence of four high-frequency modes in the HP phase that can be assigned to internal vibration of the MoO_4 tetrahedron are consistent with the identification of the HP phase as fergusonite. In this phase there is also one Raman mode that has a negative pressure coefficient (see Table III). The discussion on lattice vibrations will be extended in the next section when presenting the results of the calculations.

C. Calculations

In addition to the experiments we have carried out ab initio calculations to definitively clarify the HP behavior of CaMoO₄. We have found that at ambient conditions scheelite is the structure with the lower enthalpy and therefore the stable structure. The details of the structure calculated at ambient pressure are given in Table I. Phonon calculations have also shown that the scheelite structure is dynamically stable with no imaginary branches. Under compression, the scheelite structure is found to be the most stable structure up to 13.5 GPa. In particular, up to this pressure when calculations are carried out for the fergusonite structure we found that after the optimization of the structural parameters, fergusonite is reduced to scheelite. Above 13.5 GPa, we found that the enthalpy fergusonite becomes slightly smaller than that of scheelite; however, the difference in enthalpy between both structures is smaller than 7 meV per formula unit (1.166 meV per atom), which is comparable with the accuracy of calculations. The difference in the enthalpy of the two phases increases gradually beyond 13.5 GPa up to 29 GPa (the maximum pressure covered by the calculations). This fact supports the occurrence of the scheelite-fergusonite transition found in the experiments. More clear evidence of the destabilization of the scheelite structure comes from phonon calculations. We found that above 13.5 GPa there is a phonon branch that becomes imaginary in scheelite. This is illustrated in Fig. 6 by the phonon dispersion calculated for scheelite at 15.5 GPa. The softening of a phonon branch and the behavior of the lowest-frequency Raman mode of the scheelite phase support a phonon-driven nature of the scheelite-fergusonite transition. These observations are consistent with a displacive



FIG. 6. Phonon dispersion curve for scheelite-type CaMoO₄ at 15.5 GPa.

TABLE IV. Structural parameters of the fergusonite structure (I2/a) at 14.5 GPa (theory) and 15 GPa (experiments) [26]. Experiment: a = 5.0342 Å, b = 10.7683 Å, c = 5.1084 Å, $\beta = 90.957^{\circ}$. Theory: a = 5.0034 Å, b = 10.6847 Å, c = 5.0510 Å, $\beta = 90.725^{\circ}$.

		Theory			Experiment			
Atom	Site	x	у	z	x	у	z	
Ca	4e	0.25	0.62456	0	0.25	0.6117	0	
Mo	4e	0.25	0.12797	0	0.25	0.1216	0	
O_1	8f	0.91839	0.96559	0.24209	0.9060	0.9635	0.2120	
O ₂	8f	0.49267	0.21676	0.82478	0.5000	0.2178	0.8240	

transformation mechanism and the transition being characterized as ferroelastic [17,59,60].

From the phonon dispersion calculations, following the procedure proposed by Zurek and Grochala [61], the fergusonite structure is found from the full optimization of a monoclinic structure obtained from the distortion of scheelite. The structural parameters of the fergusonite structure optimized at 15 GPa are given in Table IV. They agree very well with those determined by Grzechnick et al. [26] from XRD. Thus calculations confirm that up to 29 GPa there is only one phase transition in CaMoO₄, which occurs at 15 GPa from the scheelite to the fergusonite structure. The fergusonite structure remains thermodynamically and dynamically stable up to 29 GPa. The fergusonite structure is represented in Fig. 1. There it can be seen that fergusonite is a distorted version of scheelite which implies a lowering of the point-group symmetry from 4/m to 2/m. In particular, in fergusonite the unit-cell parameters that correspond to the basal plane perpendicular to the long axis of the structure become slightly different and the β angle becomes slightly different from 90°. No volume change is detected at the transition which is consistent the fact that it has been found to be reversible in the experiments.

We have calculated the pressure dependence of the unit-cell parameters in the low- and high-pressure structures. The results are shown in Fig. 7. In the figure, it can be seen how scheelite is gradually distorted into fergusonite above 13.5 GPa. There, it can be also seen that there is no volume discontinuity at the transition. The most remarkable features of the phase transition are the splitting of the unit-cell parameter a of scheelite (which becomes a and c in fergusonite) and the fact that the β angle gradually becomes different from 90°. Indeed, this parameter is the one that most clearly shows the symmetry breaking of scheelite and its transformation into fergusonite. The structural changes associated with the phase transition becomes detectable for experiments at 15 GPa, a pressure at which according to calculations the distortion of the scheelite structure will cause changes detectable by XRD. In Fig. 7 it can be appreciated that in the range where comparison is possible the computer simulations agree well with the experiments [9]. In the range of stability of the scheelite phase, we found that the c axis is more compressible than the a axis, which is agreement with the experiments. In the fergusonite phase we also found that compression is anisotropic. In particular, one notices the nonlinear behavior of the β angle. The *a* and *c* axes also behave nonlinearly from the transition pressure up to



FIG. 7. Pressure dependence of the unit-cell volume and lattice parameters. Lines represent our calculations. Symbols are from the literature [9,26]. Open symbols: fergusonite. Solid symbols: scheelite.

nearly 17 GPa. The behavior of the unit-cell parameters of both phases of CaMoO₄ is comparable to that of other tungstates and molybdates [9,12,17,18,57,62,63].

Regarding the pressure dependence of the volume, we found that in both phases, it can be well described by a third-order Birch-Murnaghan equation of state (EOS) [64]. The fit of the EOS was carried out using EosFit-7c [65]. The unit-cell volume at ambient pressure (V_0), bulk modulus (B_0), and its pressure derivative (B'_0) are given in Table V. The

TABLE V. EOS parameters and components of the compressibility tensor determined for scheelite (ambient pressure) and fergusonite (18 GPa) CaMoO₄.

	Scheelite	Fergusonite
$\overline{V_0(\text{\AA}^3)}$	308.0	307.1
B_0 (GPa)	82.1	86.7
B'_0	4.1	4.1
β_{11} (10 ⁻³ GPa ⁻¹)	3.53	3.73
$\beta_{22} (10^{-3} \mathrm{GPa^{-1}})$	3.53	4.92
$\beta_{33} (10^{-3} \mathrm{GPa}^{-1})$	4.75	3.79
$\beta_{13} (10^{-3} \mathrm{GPa}^{-1})$	0	0.57

choice of a third-order EOS was indicated by the dependence of the normalized pressure on the Eulerian strain [66]. The bulk modulus determined for the scheelite phase agrees with experiments [9,26]. The bulk modulus of the fergusonite phase is 6% larger than in the low-pressure phase.

From the pressure dependence of the lattice parameters we determined the compressibility tensor. In a monoclinic structure, it has four independent components, β_{11} , β_{22} , β_{33} , and β_{13} [67]. In fergusonite, when described by space group I2/a (b being the unique crystallographic axis) β_{22} and β_{33} describe the compressibility of the b and c axes, β_{11} gives the compressibility of the direction perpendicular to the *b*-*c* plane, and β_{13} expresses the change of the shape of the plane perpendicular to the b axis. In the case of the scheelite structure, $\beta_{11} = \beta_{22}$ and $\beta_{13} = 0$ for obvious reasons. Notice that the c axis of scheelite corresponds to the b axis of fergusonite. The values obtained for the components of the compressibility tensor are summarized in Table V. For scheelite we calculate the tensor at ambient pressure and for fergusonite at 18 GPa, a pressure where the pressure dependence of a, b, and c is nearly linear. The values of the component of the tensor confirm that c is the most compressible axis of scheelite, and b is the most compressible axis of fergusonite. This is consistent with the fact they correspond to the same direction within the crystal (see Fig. 1). On the other, the value of β_{13} indicates a gradually increase of the monoclinic distortion of the fergusonite structure under compression.

From our calculations we have obtained the pressure dependence of bond distances for low- and high-pressure phases. This information is relevant to understand the structural behavior of oxides under compression [68,69]. The results are shown in Fig. 8. There it can be seen that in the pressure range where single-crystal XRD experiment have been carried out [9], the calculations reproduce well the results of the experiments. Therefore, calculations can be used to extrapolate the behavior of interatomic bonds in the scheelite structure up to the transition pressure. In Fig. 8 it can be seen than the Ca-O bonds are much more compressible than the Mo-O bonds. Among the Ca-O bonds the long bonds are more compressible than the short bonds. Consequently, the CaO_8 dodecahedron becomes more regular as pressure increases. In particular, the distortion index, defined by Robinson [70–72], is reduced from 6.70×10^{-4} at ambient pressure to 6.32×10^{-4} at 13.5 GPa. The fact that Ca-O bonds are considerably more compressible than Mo-O bonds confirms the hypothesis that the MoO₄ tetrahedron is basically a rigid unit that change little under compression [9]. In our case, the polyhedral bulk modulus of MoO₄ is 435 GPa and the polyhedral bulk modulus of CaO₈ is 81 GPa. Thus, the dodecahedron accounts for most of the volume reduction of scheelite-type CaMoO₄ under compression. Accordingly, the macroscopic bulk modulus of the scheelite-type CaMoO₄ can be explained using the model developed by Recio et al. [73]. According to it, we determine a bulk modulus of 83 GPa using the above given polyhedral bulk moduli, which is in good agreement with the value determined from the EOS described before.

From the calculations we also obtain the pressure dependence of the bond distances in the fergusonite phase. The first thing than can be noticed in Fig. 8 is the modification at the



FIG. 8. Bond distances versus pressure. Solid (dashed lines): scheelite (fergusonite). Symbols are taken from experiments carried out in scheelite [9].

transition of the MoO₄ tetrahedron and CaO₈ dodecahedron. The first unit has two different distances in fergsuonite and the other has four different distances. Consequently, the distortion of the dodecahedron is enhanced and the tetrahedron becomes asymmetric. In particular, the behavior of all the bonds is nonlinear from the transition pressure up to approximately 17 GPa and then becomes linear. The distortion index of the tetrahedron is 8.35×10^{-3} at 16.5 GPa and 11.1×10^{-3} at 21.5 GPa. In the dodecahedron, the same parameter changes from 1.15×10^{-3} at 16.5 GPa to 3.35×10^{-3} at 21.5 GPa. So, after the transition, the distortion of the polyhedral units is additionally increased as pressure increases. Again, as in the low-pressure phase, in fergusonite CaMoO₄, the Ca-O bonds are much more compressible than the Mo-O bonds (see Fig. 8), accounting for most of the compressibility of the crystal.

In addition to the structural calculations, we have also carried out band-structure calculations which helped us to interpret the optical-absorption measurements. The band structures of the two phases of CaMoO₄ are shown in Fig. 9. The electronic densities of states are shown in Fig. 10. According to our calculations, scheelite-type CaMoO₄ is a direct band-gap material with the bottom of the conduction band and top of the valence band at the Γ point of the BZ. We also found that the upper part of the valence band is dominated mainly by O 2*p* states. On the other hand, the lower part of the conduction band



FIG. 9. Band structure for scheelite-type (top) and fergusonitetype (bottom) CaMoO₄ at ambient pressure and 15 GPa, respectively.

is composed primarily of electronic states associated with the Mo 4*d* states and O 2*p* states. The calculated value of E_{gap} is 3.5 eV. This value is similar to that obtained by Zhang *et al.* [53]. It underestimates E_{gap} (by 1 eV) as usually occurs in DFT calculations. However, calculations very accurately describe the redshift observed in the gap under high pressure in the scheelite structure. Indeed, if the calculated E_{gap} is shifted up by 1 eV the agreement between experiments and calculations is excellent as shown in Fig. 3. We found that the reduction of the band gap in scheelite-type CaMoO₄ is a consequence of the increase of the contribution of Ca 4*s* states to the bottom of the conduction band. A similar effect has been previously found for CaWO₄ [15].

Regarding the HP fergusonite-type phase, we also found that its band gap is direct and located at the Γ point. The band structure of fergusonite looks like that of scheelite, which is expected given the structural similarities between fergusonite and scheelite; however, the band structure of fergusonite is slightly more dispersive. The main change in the band structure is the closing of E_{gap} by approximately 0.5 eV, exactly as found in the experiments. The drop of the band gap is mainly related to structural changes caused by the phase transition, in particular to the distortion of the MoO₄ tetrahedron. Basically, the phase transition causes an enhancement of the crystal field acting on Mo 4d and O 2p states, those that dominate the bottom of the conduction band and top of the valence band, which leads to the observed decrease of E_{gap} .



FIG. 10. Density of states for scheelite-type (top) and fergusonite-type (bottom) CaMoO₄ at ambient pressure and 15 GPa, respectively.

Calculations also explain why under compression the band gap of fergusonite redshifts faster than the band gap of scheelite. This is a consequence of the pressure-induced increase of hybridization between Mo 4*d* states and O 2*p* states and with the small increase of the contribution of Ca 3*p* and 4*s*

TABLE VI. Theoretical pressure (*P*) dependence of the frequency (ω) of the Raman modes of fergusonite-type CaMoO₄ assuming a quadratic pressure dependence using calculations from 15.5 to 29.3 GPa. ω is given in cm⁻¹ and *P* in GPa.

Mode	$\omega(P)$
$\begin{array}{c} Mode \\ & A_g \\ & B_g \\ & B_g \\ & B_g \\ & A_g \\ & A_g \\ & A_g \\ & B_g \\ & B_g \\ & B_g \\ & A_g \\ & B_g \\ & B_g$	$\omega(P)$ 65.5 + 2.49 <i>P</i> + 0.0307 <i>P</i> ² 91.7 + 8.19 <i>P</i> - 0.1499 <i>P</i> ² 166.7 + 6.46 <i>P</i> - 0.0788 <i>P</i> ² 177.7 - 3.12 <i>P</i> + 0.1208 <i>P</i> ² 210.7 + 3.55 <i>P</i> - 0.0386 <i>P</i> ² 217.2 + 5.11 <i>P</i> - 0.0872 <i>P</i> ² 218.3 + 0.61 <i>P</i> + 0.0178 <i>P</i> ² 220.9 + 12.34 <i>P</i> - 0.1607 <i>P</i> ² 279.5 + 5.50 <i>P</i> - 0.0483 <i>P</i> ² 301.2 + 3.06 <i>P</i> - 0.0024 <i>P</i> ² 326.3 + 4.06 <i>P</i> - 0.0479 <i>P</i> ² 245.9 + 7.05 <i>P</i> - 0.0479 <i>P</i> ²
B_{g} B_{g} B_{g} A_{g} B_{g} A_{g}	$303.8 + 7.96P - 0.1079P$ $404.8 + 2.97P - 0.0049P^{2}$ $762.5 + 6.50P - 0.0810P^{2}$ $833.6 + 5.34P - 0.0510P^{2}$ $862.0 - 4.96P + 0.1123P^{2}$ $918.9 - 6.31P + 0.1058P^{2}$

states to the bottom of the conduction band. Noticeably, the calculated pressure dependence is extremely similar to that experimentally determined as can be seen in Fig. 3.

Now we will discuss the results of the phonon calculations. As can be seen in Fig. 5 the agreement with the experiments is very good for the two phases of CaMoO₄. This can be also seen in Tables II and III. The calculations have been quite helpful for the mode assignment especially for the HP phase. The pressure dependence of the Raman modes can be approximately described with a linear function. However, in the HP phase the behavior is highly nonlinear. This and the several phonon crossings found by calculations (in addition to nonhydrostatic conditions) could have contributed to mistakenly proposing the existence of two phase transitions in CaMoO₄ below 20 GPa [25]. Our calculations and experiments clearly contradict the existence of two phase transitions. In Table III the experimental and theoretical results are compared for pressures higher than 17 GPa, a pressure range where the pressure dependence can be assumed to be linear. In Table VI we give quadratic functions that describe the phonon behavior for all pressure where the fergusonite phase is found to be stable (including the nonlinear region). For the scheelite phase, we will only add here two comments: (a) calculations confirm the slight softening of the lowest-frequency mode and (b) the calculated pressure coefficients are more similar to those determined from present experiments than to those of previous experiments [25], suggesting that nonhydrostatic stresses could be larger in them, a fact that we already mentioned when discussing the structural sequence. Regarding the HP fergusonite structure, we would like to add here that it has eighteen Raman-active modes $(\Gamma = 8A_g + 10B_g)$. The A_g modes of fergusonite derive from the A_g and B_g modes of scheelite, and the B_g modes of fergusonite derive from the doubly degenerate E_g of scheelite [56]. The transformation of the modes of the low-pressure

TABLE VII. Theoretical pressure (*P*) dependence of the frequency (ω) of the infrared modes of scheelite-type CaMoO₄ assuming a quadratic pressure dependence using calculations from ambient pressure to 13.5 GPa. ω is given in cm⁻¹ and *P* in GPa.

Mode	$\omega(P)$	
E_u A_u E_u A_u E_u A_u A_u E_u	$139.9 - 1.16P + 0.0121P^{2}$ $187.7 + 1.54P - 0.1098P^{2}$ $198.8 + 5.67P - 0.1247P^{2}$ $231.7 + 2.20P + 0.0090P^{2}$ $298.9 + 4.54P + 0.0252P^{2}$ $414.3 + 5.24P - 0.0299P^{2}$ $769.8 + 1.93P - 0.0251P^{2}$ $789.4 + 2.19P - 0.0332P^{2}$	

phase into the modes of the HP phase can be clearly seen in Fig. 5. In particular, the splitting of each E_g mode of scheelite into two B_g modes of fergusonite near 15 GPa is quite obvious. Most Raman modes of fergusonite CaMoO₄ harden under compression. Only one of the high-frequency modes slightly soften with pressure (see Table III).

Finally, we would like to mention that from the calculations we have also obtained the IR-active modes which are reported for completeness. In the calculation of the IR frequencies the LO-TO splitting caused by the electron-phonon coupling has been neglected because CaMoO₄ is not a polar compound [75]. The frequencies of the calculated IR-active modes and their pressure dependencies for scheelite- and fergusonite-type CaMoO₄ are given in Tables VII and VIII. Their pressure dependencies are not linear. In both phases the IR modes have a frequency distribution similar to that of the Raman modes. In the literature there is very little information on IR modes of CaMoO₄. The only report where they have been measured was published more than a half a century ago [74]. The few modes there reported agree well with our calculations. We found that in both phases there are modes that show a weak softening

TABLE VIII. Theoretical pressure (*P*) dependence of the frequency (ω) of the infrared modes of fergusonite-type CaMoO₄ assuming a quadratic pressure dependence using calculations from 15.5 to 29 GPa. ω is given in cm⁻¹ and *P* in GPa.

Mode	$\omega(P)$	
B_u	$95.8 + 2.14P - 0.0002P^2$	
B_u	$126.7 - 1.16P + 0.1472P^2$	
A_u	$159.8 + 2.31P + 0.0102P^2$	
B_u	$193.9 + 5.38P - 0.0642P^2$	
B_u	$209.3 + 3.82P - 0.0527P^2$	
A_u	$237.2 + 2.67P - 0.0603P^2$	
A_{u}	$244.1 + 1.05P + 0.0613P^2$	
B_u	$265.7 + 9.07P - 0.1035P^2$	
B_u	$296.3 + 5.08P - 0.0101P^2$	
A_{u}	$387.8 + 9.73P - 0.1296P^2$	
A_{u}	$433.6 + 3.33P - 0.0103P^2$	
B_u	$762.4 + 5.36P - 0.0689P^2$	
A_{u}	$799.6 - 1.29P + 0.0379P^2$	
B_u	$876.8 - 7.23P + 0.1084P^2$	
A_u	$885.4 + 1.19P + 0.0103P^2$	

under compression. We hope our calculations will trigger IR studies of $CaMoO_4$ under HP which could be compared with our results.

V. SUMMARY

We have carried out HP Raman and optical-absorption experiments together with *ab initio* calculations on CaMoO₄. Changes in the crystal structure, lattice dynamics, and optical properties support the occurrence of only one phase transitions up to 29 GPa. Thus we have clarified contradictions found in the literature about the HP structural sequence of CaMoO₄. We have confirmed the existence of the scheelite-fergusonite transition near 15 GPa. The pressure dependence of unit-cell parameters, bond distances, Raman and IR modes, and bandgap energy is reported for the two phases of CaMoO₄. The effects of structural changes caused by the phase transition in the optical and vibrational properties have been discussed too. In particular, the influence of pressure in the band-structure and electronic density of states is discussed. The reported results contribute to improving the knowledge of the HP properties of scheelite-type oxides and related compounds. They will also help to improve the understanding of previous HP luminescent studies carried out in CaMoO₄ [28,29].

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