

## Role of N Defects on Thermally Induced Atomic-Scale Structural Changes in Transition-Metal Nitrides

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Transition-metal nitrides (TMN) have exceptional stability, which underlies their use in various applications. Here, we study the role of N point defects on the stability of prototype TMNs using first-principles calculations. We find that distinct regimes for TMN changes relate to specific atomic-scale mechanisms, namely, diffusion of N interstitials ( $I_N$ ), of  $I_N$  pairs, and of N vacancies. The activation of these processes occurs sequentially as the temperature is raised in a range of several hundreds of degrees, accounting for observed TMN changes under widely different conditions.

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Transition-metal nitrides (TMN) form a class of compounds which has attracted sustained interest due to their exceptional physical properties [1–5]. Because of their hardness and corrosion resistance, they are used in a variety of applications. For example, TMN films are employed as diffusion barriers [3,4] in microelectronics, and as wear resistant coatings in devices, tools, and bullet proof vests. TiN is regarded as a prototype TMN system, and the structural, mechanical, electronic, and optical properties of bulk [6–8] and nanocrystalline [9] TiN, TiN surfaces [10,11], as well as TiN-based alloys [8,12] and heterostructures [13] have been the focus of several experimental and theoretical studies. TMN-based nanocomposites have emerged recently as candidates for superhard materials [14]. Interest in TiN extends to investigations of the isotopic composition of the sun, as inferred from TiN-based minerals in meteorites [15].

The most common crystalline form of TMNs is the rock salt structure, which is retained for a range of N stoichiometry  $x$ . The rock salt TiN phase ( $\delta$ -TiN), for example, is stable [16,17] for an intriguingly wide range of  $x$  ( $0.6 \leq x \leq 1.2$ ), and diffusion barriers and other sought properties can be tailored by selecting specific  $x$  values. The importance of point defects arises, therefore, naturally in TMN growth. N vacancies ( $V_N$ ) and interstitials ( $I_N$ ), in particular, are regarded as the primary TMN defects. Experimental [8,17–20] and theoretical [8,17,19,21] studies have linked changes in the electronic and mechanical properties of the host crystal to the presence of  $V_N$ 's. With respect to thermal stability, however, questions on the origin of specific defect-induced changes remain open. Experiments on TiN have identified pertinent activation energies ( $E_a$ ) of 1.23, 2.09, and 3.9 eV, and similar values have been obtained for other TMNs [1,3,22]. These values point to distinct processes being activated at drastically different temperatures, spanning a range of several hundreds of degrees. And yet, the same mechanisms have been

suggested as explanation for different  $E_a$ 's and different mechanisms have been put forward for the same  $E_a$ 's. In particular,  $V_N$  migration has been suggested for both the  $E_a$ 's of about 2.1 eV and those of about 3.9 eV [3], while the former value has also been attributed to  $I_N$  diffusion [1]. Moreover, the origin of the 1.23 eV value remains an open question, and the 3.9 eV  $E_a$  for TiN [22] has been disputed [23], even though  $E_a$ 's in the same range have been measured for ZrN, UN, and NbN [3]. The resolution of these conflicting suggestions is key for the understanding, control, and optimization of properties of TMN films grown with different techniques and on various substrates.

In this Letter, we use first-principles calculations to elucidate key atomic-scale mechanisms that affect the stability of TiN and ZrN and we resolve the puzzle on the origin of distinct  $E_a$ 's in TiN. These mechanisms relate to interactions and migration of point defects and they are indeed activated at drastically different temperatures. We first identify the structural properties and interactions among isolated point defects in TiN. We find that the interaction between neighboring  $V_N$ 's is slightly repulsive and  $V_N$  migration has a very high activation energy of 3.8 eV. The lowest energy  $I_N$  arrangements are those of split-configurations with stretched N-N bonds aligned along certain crystal directions. In contrast to  $V_N$ 's,  $I_N$  pairs have a substantial binding energy forming complexes in a number of stable configurations.  $I_N$  migration is relatively facile and the calculated diffusion barriers ( $E_d$ ) for isolated  $I_N$ 's and  $I_N$  pairs are 1.3 and 2.0 eV, respectively. We confirm that  $V_N$  diffusion is also responsible for the 3.9 eV  $E_a$  in the case of ZrN. We finally discuss the stability of Frenkel  $V_N$ - $I_N$  pairs. Overall these internally consistent assignments of activation energies provide a systematic account for key observations related to the stability of these materials.

The calculations were performed within density-functional theory (DFT), with a generalized-gradient cor-

rected (GGA) exchange-correlation functional [24], a plane wave basis set with an energy cutoff ( $E_c$ ) of 400 eV, and projector-augmented wave potentials [25], as implemented in the VASP code [26]. The supercells we used were  $2 \times 2 \times 2$ ,  $3 \times 3 \times 3$ ,  $4 \times 4 \times 4$  in terms of the conventional unit cell. The lattice constant was fixed at 4.2366 Å [6,9]. The results we present below are based on the  $3 \times 3 \times 3$  supercell with 108 Ti and 108 N atoms when no defects are present. We used a varying number of  $k$  points following the Mohnkorst-Pack scheme [27] for Brillouin zone sampling. In particular, we used  $2 \times 2 \times 2$  and  $3 \times 3 \times 3$  grids for the majority of the results on the above-mentioned large supercells. In the following we report only the  $3 \times 3 \times 3$  results, unless stated otherwise. Previous studies [28] showed the importance of  $k$ -point sampling for the calculation of TiN elastic constants. In the present case, we find by comparing to calculations with finer grids ( $6 \times 6 \times 6$ ) that the relevant quantities (relative stability of defects, defect binding energies, and barriers) are converged within about 0.1 eV. This accuracy is sufficient to decide on the role of the point defects discussed here on TMN thermal stability.  $E_d$ 's were calculated with the elastic band (EB) method [29] for minimum energy pathways (MEP), as described in previous studies [30] that obtained DFT-GGA  $E_a$ 's within 0.1–0.2 eV from the experimental values. The interaction energies  $E_i$  between defects were obtained combining the energy of the host crystal and the energies of supercells with isolated defects and with defect complexes.

In agreement with Jhi *et al.* [21], we found that a N vacancy induces a small outward relaxation in the surrounding TiN matrix. The distance between neighboring Ti atoms and the  $V_N$  site changes from the pristine 2.12 to 2.20 Å. The backbonds of these Ti atoms to Ti species of the second shell around the vacancy contract from 2.99 to 2.93 Å.

The outward relaxation is obtained only for the converged calculations with the larger  $3 \times 3 \times 3$  and  $4 \times 4 \times 4$  supercells. The calculation with the smaller  $2 \times 2 \times 2$  supercell and  $\Gamma$ -point sampling gives a slight inward relaxation for the Ti atoms around the N vacancy. In Fig. 1(a) we show the transition state (TS) of  $V_N$  diffusion. We started with an initial guess for the MEP with the vacancy migrating through the body centered position of the conventional cubic unit cell around the defect. This MEP relaxed with the EB calculation to a path that crosses one of the stretched Ti-Ti bonds around the  $V_N$  site, as shown in Fig. 1(a). The diffusion barrier is 3.8 eV, in excellent agreement with one of the reported [22] experimental  $E_a$ 's. The  $E_d$  value is sensitive to the calculational parameters. For an energy cutoff  $E_c$  of 300 eV the computed  $E_d$  was 3.88 eV, and for  $\Gamma$ -point sampling the value was significantly lower, 3.43 eV. Calculations with an  $E_c$  of 400 eV and a  $2 \times 2 \times 2$   $k$  grid give an  $E_a$  of 3.95 eV. Use of a finer grid ( $6 \times 6 \times 6$ ) for the total energies of configura-

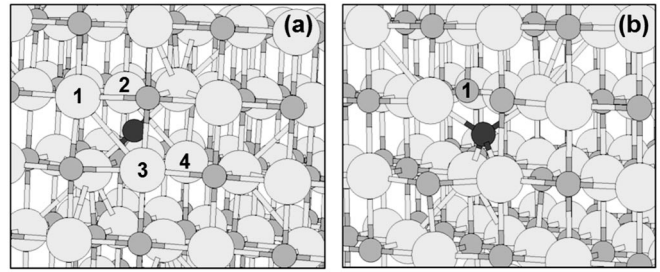


FIG. 1. Transition states for point defect migration in TiN: (a)  $V_N$  diffusing ( $E_d = 3.8$  eV) between the midpoints of 1–2 and 3–4 Ti-Ti bonds. (b)  $I_N$  migration ( $E_d = 1.08$  eV) between the split  $I_N$  configurations of Fig. 2(a) ( $I_N$  bonds to N atom 1) and Fig. 2(c). The diffusion barrier between the lowest energy configurations of Fig. 2(b) is 1.28 eV. (Ti: light gray, N: gray, interstitial N: dark gray spheres.)

tions obtained with  $3 \times 3 \times 3$  sampling gives an  $E_a$  of at least 3.76 eV, confirming the convergence of results.

The large barrier indicates that  $V_N$  diffusion is activated only at very high temperatures. This fact is central in explaining the stability of  $TiN_x$ , and for other TMNs, since similar  $E_a$ 's of 3.4, 3.9, 4.1, and 4.8 eV have been measured for N diffusion in  $ZrN_{0.69}$ ,  $ZrN_{0.95}$ , UN, and NbN, respectively [3]. The accuracy of the experiments that obtained the 3.9 eV value for TiN, however, has been under debate [1,23]. We, therefore, studied also  $V_N$  migration in ZrN.  $V_N$  hopping in ZrN follows the same path as  $V_N$ 's in TiN, with a TS similar to the one shown in Fig. 1(a). The calculated barrier is 3.86 eV ( $2 \times 2 \times 2$   $k$  grid), in excellent agreement with the N  $E_d$  of 3.9 eV in near stoichiometric ZrN [3]. This agreement corroborates the result of 3.9 eV in TiN, and we therefore infer that  $V_N$  diffusion is indeed associated with the reported high  $E_a$ 's in TMNs.

N vacancies are believed to be the defects that control the stoichiometry of TiN films and their mutual interactions underlie the properties of  $TiN_x$  films. We studied the  $V_N$ - $V_N$  interactions for 3 N divacancy configurations: (i) both  $V_N$ 's were placed in the same (110) chain, (ii) the  $V_N$ 's were neighboring members of a (100) chain, and (iii) the two  $V_N$ 's were placed in a distance of 7.9 Å with respect to each other. The results are given through the interaction energies ( $E_i$ ). Positive (negative)  $E_i$ 's indicate repulsion (attraction) between defects. For the divacancies,  $E_i$ 's are slightly positive (about 0.15 eV) for neighboring  $V_N$ 's and they decrease to zero as the two defects move away from each other.

N interstitials is the second class of primary point defects in TMNs. Unlike N vacancies, which appear only in one configuration, a number of possibilities exist for  $I_N$ 's. One possibility is for an  $I_N$  to occupy a tetrahedral position, as shown in Fig. 2(c). Other possible arrangements are split interstitials for which  $I_N$  forms a stretched N-N bond of 1.33 Å with a N atom of the network. This stretched bond may be aligned along different directions. In particular, we found two stable configurations with the N-N dimer point-

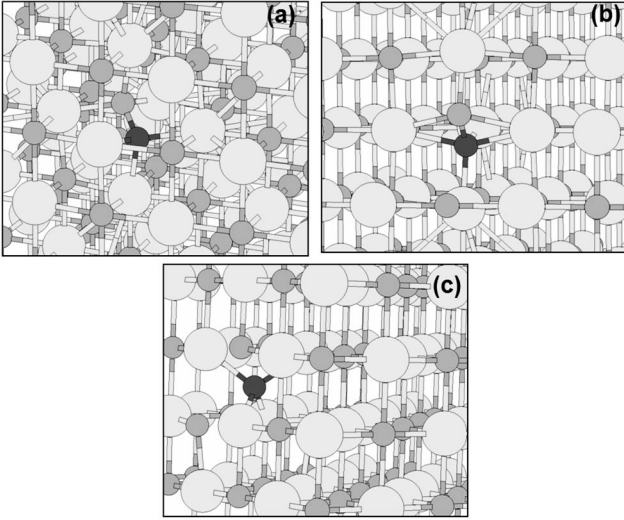


FIG. 2. (a) and (b) split  $I_N$ 's in TiN with N-N stretched bonds along (111) and  $(10\bar{1})$  directions, (c) tetrahedral  $I_N$ . Lowest energy  $I_N$  configuration is (b). Structures (a) and (c) are 0.20 and 0.86 eV higher in energy, respectively. (Ti: light gray, N: gray, interstitial N: dark gray spheres.)

ing along the (111) and  $(10\bar{1})$  directions. They are depicted in Figs. 2(a) and 2(b), respectively.  $I_N^b$  is the most stable.  $I_N^a$  is higher in energy, by 0.20 eV, and the tetrahedral  $I_N^c$  is considerably less stable by 0.86 eV. Diffusion between the lowest energy  $I_N^b$  configurations proceeds with hopping through  $I_N^a$  and  $I_N^c$ . The TS for a migration step between  $I_N^a$  and  $I_N^c$  is shown in Fig. 1(b). The barrier is 1.08 eV. We also computed the MEP for the transformation between  $I_N^a$  and  $I_N^b$  configurations at the same site. This latter MEP has a very small barrier, less than 0.2 eV. Combining the results of both MEPs and the relative stability of  $I_N$ 's, the effective  $I_N$  diffusion barrier is 1.28 eV. This relatively low value indicates that  $I_N$  migration is activated at dramatically lower temperatures than N vacancies.

In contrast to  $V_N$ , the interaction among  $I_N$ 's can be strongly attractive for a number of configurations. Two neighboring split interstitials, prepared with their N-N stretched bonds aligned in parallel, relax to a herringbone configuration with the N-N bonds perpendicular to each other. The most stable structure is the one with both interstitials in the  $I_N^b$  configuration of Fig. 2(b). The binding energy of this  $I_N^b$ - $I_N^b$  complex, shown in Fig. 3(a), is considerable and equal to 0.55 eV. When one of the  $I_N$ 's switches to a vicinal  $I_N^a$  or  $I_N^c$  configuration the energy increases by 0.14 and 1.33 eV, respectively. The latter  $I_N^b$ - $I_N^c$  complex, which is depicted in Fig. 3(b), is encountered as an intermediate configuration during the diffusion of an  $I_N$ - $I_N$  pair. A second intermediate structure is shown in Fig. 3(c) with two  $I_N^b$  interstitials bound by 0.44 eV in second nearest neighbor distance to each other. The activation energy for the transformation between the structures of Figs. 3(a)–3(c) is 1.97 eV, obtained as the difference between the energies of the  $I_N^b$ - $I_N^b$  complex and the TS of

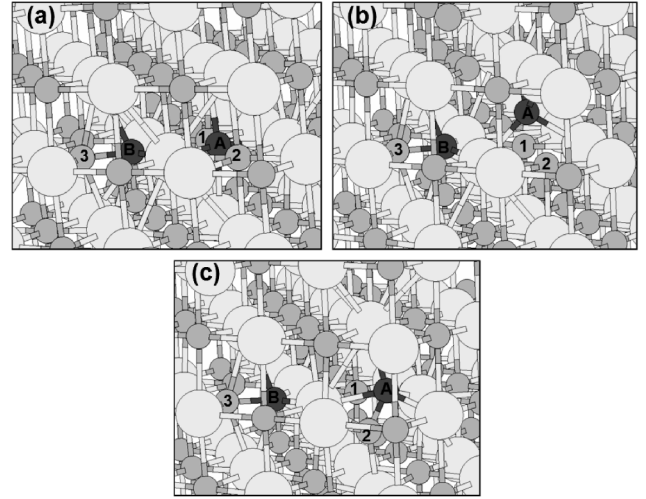


FIG. 3. Pairs of  $I_N$ 's shown in Fig. 2: (a) vicinal  $I_N^b$ - $I_N^b$  pair bound by 0.55 eV, (b) vicinal  $I_N^b$ - $I_N^c$ , and (c) two  $I_N^b$ 's in a second nearest neighbor distance and bound by 0.44 eV. N atoms 3-B form one  $I_N^b$  complex. N atom A moves from the 1-A  $I_N^b$  in (a), to tetrahedral position in (b), and connects to 2-A  $I_N^b$  in (b). The (a)–(c)  $E_d$  of 1.97 eV is the diffusion  $E_a$  for a  $I_N$ - $I_N$  pair in TiN. (Ti: light gray, N: gray, interstitial N: dark gray spheres.)

the Fig. 3(b) and 3(c) hopping. After one of the  $I_N$ 's hops so that the complex changes from the initial to the final configuration of Fig. 3, the other  $I_N$  atom can perform similar steps. As a result, a migration step for the  $I_N^b$ - $I_N^b$  complex can be completed. Therefore, the 1.97 value is the calculated diffusion barrier for the stable  $I_N$ - $I_N$  complex in TiN.

Thermal stability depends also on the properties of Frenkel  $V_N$ - $I_N$  pairs. If there is a path that takes a remote  $I_N$  in the immediate vicinity of a  $V_N$  and this path does not include sites of high energy, then the mutual annihilation of  $V_N$ 's and  $I_N$ 's will be possible when the migration of one of the species is activated. We considered a number of  $V_N$  and  $I_N$  combinations. We created a  $V_N$  at one of the closest to a  $I_N^a$  N site (i) on the (110) line, (ii) on the  $(01\bar{1})$  line, and (iii) at a remote site in the same supercell. Likewise for  $I_N^b$ , we created a  $V_N$  (i) at one of the closest to the  $I_N$  N site on the same  $(10\bar{1})$  line, (ii) at one of the closest to the  $I_N$  N site, but on a neighboring  $(10\bar{1})$  line, and (iii) at a remote site in the same supercell. All these configurations, save for the ones with large  $I_N$ - $V_N$  distances, relax to an ideal TiN network as the  $I_N$  moves to the neighboring  $V_N$ . The FP configurations (i) and (ii) can be viewed as precursors before the mutual  $V$ - $I$  annihilation. Alternatively, they can be viewed as the first intermediate configurations after the FP creation and before its dissociation due to the migration of  $I_N$ . Because there is no barrier between these configurations and the ideal crystal, we conclude that  $I_N$  migration is the rate-limiting step for the annihilation or creation of FPs.

The results of this work are consistent with three regimes with distinct rate-limiting steps. Depending on



growth conditions, the thermal stability of a TMN film may fall in one particular regime, or a sequence of distinct processes may be encountered as the temperature is raised. It is believed that low-energy ion deposition creates  $I_N$ 's [3]. In this case, diffusion of isolated  $I_N$ 's with an  $E_a$  of 1.28 eV gives rise to defect-related changes, as excess N annihilates vacancies or gets trapped at surfaces and grain boundaries. The process is consistent with stress relaxation measurements [3] at relatively low ( $\approx 200$ – $500$  °C) temperatures. Alternatively, growth can lead to the formation of stable  $I_N$  pairs. Their calculated diffusion barrier, 1.97 eV, is in very good agreement with a measured [1]  $E_a$  of 2.09 eV. Hence,  $I_N$  pair migration can account for changes in TMN properties under annealing at higher temperatures ( $\approx 500$ – $800$  °C). We should note that indirect evidence for  $I_N$  migration is offered by the occasional formation of  $N_2$  bubbles in TiN [3]. Finally, an  $E_a$  of 3.8 eV, in agreement with experiments at even higher temperatures, is expected when  $V_N$ 's dominate a sample. Indeed, changes in properties such as color which can be attributed to  $V$  migration [18], occur only after prolonged annealing at temperatures above 900 °C.

Our findings have implications also for the stability and properties of TMNs away from the ideal 1:1 stoichiometry. The large  $V_N$  diffusion barrier underlies the stability of substoichiometric films. The suppression of  $V_N$  migration preserves the rock salt structure, and it is consistent with the random distribution of  $V_N$ 's, as observed [18]. An overstoichiometric  $TMN_x$  film is expected to be less stable in terms of atomic-scale structural changes, because  $I_N$  migration is much easier to activate. Let us also note that the selection of a particular substrate can play a decisive role for the thermal stability of TMN films. Changes in the lattice constants away from bulk values can give rise to considerable variations in the activation of the processes discussed above.

Finally, we should stress that other physical mechanisms may also be operative in TMN films, such as the nucleation and migration of extended defects like dislocations, or the formation of microvoids [3]. Other point defects (cation vacancies and interstitials, antisites, etc.), which are generally believed to be less mobile [3] may be present and affect physical properties. A comprehensive account of thermal stability also includes aspects such as phase separation and equilibrium, recrystallization, interfacial reactions, and oxidation [3]. The study of all these aspects, however, is beyond the scope of the present work; here, we have focused on the crucial role of N defects as the primary agents for atomic-scale structural stability. The results on the key processes of N defect migration are in agreement with experimental measurements and they settle long-

standing questions on the origin of observed changes during annealing.

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- [1] A. J. Perry, *J. Vac. Sci. Technol. A* **6**, 2140 (1988), and references therein.
  - [2] S. H. Jhi *et al.*, *Nature (London)* **399**, 132 (1999).
  - [3] L. Hultman, *Vacuum* **57**, 1 (2000), and references therein.
  - [4] F. Lévy *et al.*, *Surf. Coat. Technol.* **120–121**, 284 (1999).
  - [5] I. Pollini, A. Mosser, and J. C. Parlebas, *Phys. Rep.* **355**, 1 (2001).
  - [6] H. Höchst *et al.*, *Phys. Rev. B* **25**, 7183 (1982).
  - [7] Z. Dridi *et al.*, *J. Phys. Condens. Matter* **14**, 10237 (2002).
  - [8] M. Guemmaz *et al.*, *J. Phys. Condens. Matter* **9**, 8453 (1997); M. Guemmaz *et al.*, *J. Electron Spectrosc. Relat. Phenom.* **107**, 91 (2000); M. Guemmaz *et al.*, *Int. J. Inorg. Mater.* **3**, 1319 (2001).
  - [9] J. Hu *et al.*, *J. Am. Ceram. Soc.* **83**, 430 (2000).
  - [10] P. A. P. Lindberg *et al.*, *Phys. Rev. B* **36**, 939 (1987).
  - [11] B. W. Karr *et al.*, *Phys. Rev. B* **61**, 16137 (2000); S. Kodambaka *et al.*, *Surf. Sci.* **513**, 468 (2002); C. S. Shin *et al.*, *J. Appl. Phys.* **95**, 356 (2004).
  - [12] L. Calmels, C. Mirguet, and Y. Kihn, *Phys. Rev. B* **73**, 024207 (2006).
  - [13] P. Patsalas and S. Logothetidis, *J. Appl. Phys.* **93**, 989 (2003).
  - [14] S. Hao *et al.*, *Phys. Rev. Lett.* **97**, 086102 (2006).
  - [15] A. Meibom *et al.*, *Astrophys. J.* **656**, L33 (2007).
  - [16] J. H. Kang and K. J. Kim, *J. Appl. Phys.* **86**, 346 (1999).
  - [17] C. S. Shin *et al.*, *J. Appl. Phys.* **93**, 6025 (2003).
  - [18] J. P. Schaffer *et al.*, *J. Vac. Sci. Technol. A* **10**, 193 (1992).
  - [19] M. Tsujimoto *et al.*, *J. Electron Spectrosc. Relat. Phenom.* **143**, 159 (2005).
  - [20] T. Lee *et al.*, *Phys. Rev. B* **71**, 144106 (2005).
  - [21] S. H. Jhi *et al.*, *Phys. Rev. Lett.* **86**, 3348 (2001).
  - [22] V. S. Ereemeev, Y. M. Ivanov, and A. S. Panov, *Izv. Akad. Nauk SSSR Met.* **5**, 262 (1969).
  - [23] F. W. Wood and O. G. Paasche, *Thin Solid Films* **40**, 131 (1977).
  - [24] J. P. Perdew and Y. Wang, *Phys. Rev. B* **45**, 13244 (1992).
  - [25] P. E. Blöchl, *Phys. Rev. B* **50**, 17953 (1994).
  - [26] G. Kresse and J. Joubert, *Phys. Rev. B* **59**, 1758 (1999).
  - [27] D. J. Chadi, and M. L. Cohen, *Phys. Rev. B* **8**, 5747 (1973).
  - [28] S. Nagao, K. Nordlund, and R. Nowak, *Phys. Rev. B* **73**, 144113 (2006).
  - [29] G. Mills, H. Jónsson, and G. K. Schenter, *Surf. Sci.* **324**, 305 (1995).
  - [30] L. Tsetseris, S. W. Wang, and S. T. Pantelides, *Appl. Phys. Lett.* **88**, 051916 (2006); L. Tsetseris and S. T. Pantelides, *Phys. Rev. Lett.* **97**, 116101 (2006).