## **Coexistence of Strongly Mixed-Valence and Heavy-Fermion Character** in SmOs<sub>4</sub>Sb<sub>12</sub> Studied by Soft- and Hard-X-Ray Spectroscopy

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Sm-based heavy-fermion compound SmOs<sub>4</sub>Sb<sub>12</sub> has been investigated by soft x-ray ( $h\nu =$ 1070–1600 eV) and hard x-ray (HX;  $h\nu = 7932$  eV) spectroscopy. The HX photoemission spectroscopy clearly demonstrates that the strongly mixed-valence state and the heavy-fermion state coexist in the bulk. It is found that the Sm valence decreases below 100 K, indicating that the Kondo coherence develops with approaching the proposed Kondo temperature. Our theoretical analyses suggest that the origin of the coexistence in  $SmOs_4Sb_{12}$  is the coincidence of two conditions, namely, (i) the energy difference between Sm divalent and trivalent states is very small and (ii) the hybridization between Sm 4f and conduction electrons is weak.

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Recently, many heavy-fermion (HF) compounds with multiple f electrons (or holes) have been discovered in the lanthanide system [1-4]. Sm-based filled skutterudites have attracted much attention due to exotic behaviors, such as Kondo anomaly, weak ferromagnetism, and heavy electron mass [3-7]. Among them, SmOs<sub>4</sub>Sb<sub>12</sub> has been discovered to show the HF character [3,4]. It is found that  $A/\gamma^2$  (A is the coefficient of  $T^2$  in  $\rho - T$ , where  $\rho$  is the resistivity;  $\gamma$  is the electronic specific heat coefficient) in SmOs<sub>4</sub>Sb<sub>12</sub> follows the "grand Kadowaki Woods relation" [8], suggesting that this compound falls into the same category as other so-far-reported HF compounds and the orbital degeneracy in Sm 4f electron plays a key role in realizing the HF state. However, the crystalline-electricfield ground state of  $\text{Sm}^{3+}$  (J = 5/2) in  $\text{SmOs}_4\text{Sb}_{12}$ , which determines the degeneracy, is still in controversy [3,4]. Even the valence of Sm ions has not been clarified yet.

In general,  $RFe_4P_{12}$  (*R* denotes a rare-earth-metal atom) has a larger energy scale than  $ROs_4Sb_{12}$  as represented by higher superconducting transition temperature for La system [9,10], larger hybridization gap for Ce system [11,12], and higher Curie temperature  $(T_C)$  for Nd and Eu systems [13–15]. These results suggest that the hybridization between conduction and 4f electrons (c-f) and/or the direct exchange interaction between R atoms in  $ROs_4Sb_{12}$ are weaker than in RFe<sub>4</sub>P<sub>12</sub> due to the larger lattice constant. However,  $T_C$  and  $\gamma$  in SmOs<sub>4</sub>Sb<sub>12</sub> (2–3 K and 820–880 mJ/(mol K<sup>2</sup>)) are larger than those of SmFe<sub>4</sub>P<sub>12</sub>  $(1.6 \text{ K and } 370 \text{ mJ}/(\text{mol } \text{K}^2))$  [3–6]. These unusual tendencies must be originating from the specific nature of the Sm atom.

In order to reveal the bulk nature of Sm compounds, bulk-sensitive photoemission spectroscopy (PES) with soft and hard x rays (SXPES and HAXPES) is a very powerful tool since the Sm valence and electronic structures on the surface are often different from those in the bulk [16-18]. It has been demonstrated that the high-resolution bulksensitive SXPES can reveal bulk electronic states [19-21]. The bulk sensitivity arises from the long inelastic mean free path (IMFP) of the high-energy photoelectrons excited by soft x ray (SX). HAXPES is attracting much more attention for investigating the bulk electronic structures of rare-earth compounds [22-24] because it provides a longer probing depth than the SXPES due to the increase of the IMFP. The longer probing depth makes the measurement insensitive to surface contamination.

In this Letter, we report on detailed spectroscopic measurements with SX and hard x ray (HX) for Sm-based filled skutterudite  $SmOs_4Sb_{12}$ . It is demonstrated that the above mentioned HF character is accompanied by the strongly mixed-valence state. With the aid of the theoretical calculation based on the impurity Anderson model with configuration interaction, we have estimated the mean valence of bulk Sm ions. The mean valence is revealed to depend on temperature below 100 K, which is consistent with the development of Kondo coherence in SmOs<sub>4</sub>Sb<sub>12</sub>. Significant intensity at Fermi level  $(E_F)$  was observed in Sm 3d-4f resonant photoemission spectroscopy (RPES), indicating that Sm 4f electrons contribute directly to form the HF state.

SXPES and Sm 3d-4f x-ray absorption spectroscopy (XAS) were carried out at the twin-helical undulator SX beam line BL25SU in SPring-8 using GAMMADATA-SCIENTA SES-200 spectrometer [25]. The total energy resolution ( $\Delta E$ ) of the SXRPES was set to  $h\nu/\Delta E =$ 4000–6700. The XAS spectra were measured by the total

electron yield method. HAXPES was performed at the state-of-the-art beam line BL19LXU in SPring-8 with MB Scientific A1-HE spectrometer. The linearly polarized light was delivered from an in-vacuum 27 m long undulator [26]. The highest  $\Delta E$  of the HAXPES (for the energy calibration using Au thin films) was set to 70 meV at  $h\nu =$  7932 eV.

For measurements, single crystals of SmOs<sub>4</sub>Sb<sub>12</sub> were employed. They were grown by the Sb-self flux method using high-purity raw materials [27]. Clean surfaces were obtained by fracturing samples *in situ* in UHV ( $\sim 2 \times 10^{-8}$ and  $\sim 7 \times 10^{-8}$  Pa for SXPES and HAXPES) at measuring temperature ( $T \approx 20$  K) except for temperaturedependent measurements. Configurations of the apparatus were set so as to collect the normal emission of photoelectrons from samples.

Figure 1(a) shows the Sm 3d-4f XAS spectrum of SmOs<sub>4</sub>Sb<sub>12</sub>. The spectrum has a prominent shoulder structure at  $h\nu \approx 1076.5$  eV as indicated by the arrow labeled B. At this photon energy, one of the multiplet components of a pure-trivalent Sm ( $4f^5$ ) ion is predicted from the atomic multiplet calculation [28]. The intensity of this shoulder is, however, suppressed in the spectrum of Sm<sub>4</sub>As<sub>3</sub>, which is known to have a well localized  $4f^5$  ground state in the bulk [24]. In some Sm compounds, one can see the Sm divalent state on the lower photon energy side of the Sm trivalent state in the XAS spectrum

[29]. The observation of the prominent intensity at this photon energy indicates the existence of the Sm divalent state together with the trivalent one. Therefore, we conclude that a mixed-valence state is realized in  $SmOs_4Sb_{12}$ .

By means of the Sm 3d core-level PES, one can investigate the Sm valence and 4f states through the interaction between the 4f electrons and the 3d core hole. In Fig. 2(a), Sm 3*d* core-level PES spectra of  $SmOs_4Sb_{12}$  at two different photon energies are compared. At  $h\nu = 7932$  eV, one can obtain the nearly true bulk spectrum for the Sm 3dcore-level PES since the IMFP reaches into 87 Å in contrast to 12 Å at  $h\nu = 1600$  eV [30]. The spectra have two components in this binding energy  $(E_B)$  range, that is, Sm<sup>3+</sup> (the  $|3d^94f^5\rangle$  final state) and Sm<sup>2+</sup> (the  $|3d^94f^6\rangle$ final state) components. The Sm2+ spectral weight increases with the photon energy, in contrast to the case of  $Sm_4As_3$  where the surface  $Sm^{2+}$  component is reduced by increasing the photon energy [24]. This suggests that in SmOs<sub>4</sub>Sb<sub>12</sub> there are much more divalent Sm ions in the bulk than on the surface. In other words,  $SmOs_4Sb_{12}$  has the trivalent dominant state on the surface, although the valence of Sm ions often prefers to have the divalent state on the surface [17,24].

Presented experimental results clearly demonstrate that the mixed-valence state is realized in the bulk of  $SmOs_4Sb_{12}$ . In order to estimate the valence of Sm ions in  $SmOs_4Sb_{12}$ , we have calculated the Sm 3d-4f XAS and





FIG. 1 (color online). Sm 3d-4f XAS spectrum of SmOs<sub>4</sub>Sb<sub>12</sub> at the  $M_5$  edge. The spectrum of Sm<sub>4</sub>As<sub>3</sub> is also shown as a reference by a dashed line in (a). The solid line in the bottom of (a) is the calculated spectrum of a pure-trivalent Sm ion. Arrows indicate the photon energies employed in RPES measurements. (b) Calculated Sm 3d-4f XAS spectrum (solid line). The lower solid line is the calculated spectrum before Gaussian and Lorentzian broadening ( $\Gamma_G = 100 \text{ meV}$  and  $\Gamma_L = 1.0 \text{ eV}$ ). Dots are the experimental spectrum of SmOs<sub>4</sub>Sb<sub>12</sub>. Inset shows the overall Sm 3d-4f XAS spectra.

FIG. 2 (color online). Sm 3*d* core-level PES spectra of SmOs<sub>4</sub>Sb<sub>12</sub>. (a) Photon-energy dependence of the spectrum. (b) Calculated Sm 3*d* core-level PES spectrum ( $\Gamma_G = 1.0 \text{ eV}$ ,  $\Gamma_L(E_B \ge 1072.6 \text{ eV}) = 1.4 \text{ eV}$ , and  $\Gamma_L(E_B < 1072.6 \text{ eV}) = 0.6 \text{ eV}$  [49]). Open circles show the experimental spectrum. Inset shows the overall Sm 3*d* core-level PES spectra. Dashed lines and dotted lines are the plasmon contribution and the Shirley-type background [51], respectively. (c) Temperature dependence of the Sm<sup>2+</sup> component in the Sm 3*d* core-level PES spectrum at  $h\nu = 7932 \text{ eV}$ .

TABLE I. Best-fit values for the effective charge transfer energy ( $\Delta_{eff}$ ), effective hybridization strength ( $V_{eff}$ ), and core-hole potential ( $U_{fc}$ ) in CI model calculations for SmOs<sub>4</sub>Sb<sub>12</sub>. Estimated Sm valences are also given.

	$\Delta_{eff}$ (meV)	$V_{\rm eff}~({\rm meV})$	$U_{fc}$ (eV)	Valence
Sm 3 <i>d</i> -4 <i>f</i> XAS	65	178	11.0	2.807 ( $T \simeq 20$ K)
Sm 3 <i>d</i> core-level PES	65	$310 \pm 15$	9.48	$2.726 \pm 0.006 \ (T = 18 \text{ K})$
	65	237 ± 15	9.48	$2.763 \pm 0.006 \ (T = 100 \text{ K})$

Sm 3d core-level PES spectra by the single-impurity Anderson model considering atomic multiplets with configuration interaction (CI) [34–36]. The periodic Anderson model (PAM) is known to be an appropriate model for the dense Kondo system [37,38]. At present, however, one cannot calculate the full multiplet structures of Sm atoms in the case of the PAM. Multiplet calculations of the spectra were performed using the XTLS 8.0 program [39]. The values of Slater integrals were reduced to 82% of their Cowan's Hartree-Fock values [40] in order to fit the experimental spectra [41]. We have considered the basis state consisting of two configurations, that is, the major  $|4f^5\rangle$ state and the minor  $|4f^6\underline{L}\rangle$  state arising from the *c*-*f* hybridization in the initial state, where L denotes an additional hole in the conduction band. The effective charge transfer energy  $\Delta_{\rm eff}$  is defined as  $\Delta_{\rm eff} \equiv E[4f^6\underline{L}]_{\rm gs} E[4f^5]_{gs}$ , where  $E[4f^6\underline{L}]_{gs}$  and  $E[4f^5]_{gs}$  represent energies of  $|4f^6L\rangle$  and  $|4f^5\rangle$  ground states, respectively.

The solid curves in Fig. 1(b) show the calculated Sm 3d-4f XAS spectra which are broadened by Gaussian and Lorentzian functions representing the experimental resolution and the lifetime broadening. The calculated Sm 3dcore-level PES spectra are shown in Fig. 2(b). Both calculated spectra in Figs. 1(b) and 2(b) well reproduce the experimental spectra of SmOs<sub>4</sub>Sb<sub>12</sub>. In Table I, the bestfit parameters are summarized. The valences of the Sm ions estimated from fitting of the XAS and PES spectra are 2.807 and 2.726 at  $T \simeq 20$  K, respectively. Both  $\Delta_{\rm eff}$  and  $V_{\rm eff}$  are much smaller than those previously obtained for  $PrFe_4P_{12} \Delta_{eff} (= E[4f^3\underline{L}]_{gs} - E[4f^2]_{gs}) = 2.3 \text{ eV}, V_{eff} =$ 1.2 eV] [42]. The small  $\Delta_{eff}$  is an essential requirement for SmOs<sub>4</sub>Sb<sub>12</sub> to realize the strongly mixed-valence state in spite of the very weak c-f hybridization. The difference in the best-fitted  $U_{fc}$  and  $V_{eff}$  between XAS and PES calculations, which may originate from incompleteness in the present model, is not a vital issue for the scenario of the weakly hybridized mixed-valence state.

The temperature dependence of the Sm 3*d* core-level PES spectrum at  $h\nu = 7932$  eV is shown in Fig. 2(c). The relative spectral weight of the Sm divalent component to the trivalent one  $(W_{2+}/W_{3+})$  does not change above T = 100 K. However, it is found that  $W_{2+}/W_{3+}$  increases by about 15% at T = 18 K, which is close to the proposed Kondo temperature  $T_K$  ( $\approx 20$  K), suggesting that the Kondo coherence develops with lowering temperature toward  $T \sim T_K$ . In fact, the fitted  $V_{\text{eff}}$  for the spectrum at T = 18 K is enhanced. Development of the Kondo coherence at few

tens of Kelvin favors the HF formation. The temperature dependence of the Sm valence has also been seen in the Sm *L*-edge XAS measurement [43].

In filled skutterudites  $CeRu_4Sb_{12}$  and  $YbFe_4Sb_{12}$ , mixed valence and electron mass enhancement ( $\gamma \approx$  140 mJ/(mol K<sup>2</sup>)) were also reported [44,45]. At low temperatures, the hybridization gap opens in both compounds [46]. For SmOs<sub>4</sub>Sb<sub>12</sub>, however, there has been no experimental evidence which implies (pseudo) gap opening. This suggests that the *c*-*f* hybridization in SmOs<sub>4</sub>Sb<sub>12</sub> is weaker than those in CeRu<sub>4</sub>Sb<sub>12</sub> and YbFe<sub>4</sub>Sb<sub>12</sub>, consistent with our results and the observation of the larger  $\gamma$ in SmOs<sub>4</sub>Sb<sub>12</sub>.

SXRPES can reveal the contribution of Sm 4*f* states to the PES intensity at  $E_F$ . The on-RPES spectrum of SmOs<sub>4</sub>Sb<sub>12</sub>, measured at the photon energy B in Fig. 1(a), is shown in Fig. 3 together with the off-RPES spectrum taken at the photon energy A. On- and off-RPES spectra are normalized by the photon flux. The Sm divalent state is strongly enhanced due to the resonance effect. Figure 3(b) shows the on-RPES spectrum near  $E_F$  with higher energy resolution ( $\Delta E \approx 160$  meV). Two peaks, clearly seen in the spectrum, are attributed to <sup>6</sup>H and <sup>6</sup>F multiplet terms [18,47,48]. We note that these structures



FIG. 3 (color online). Sm 3d-4f RPES spectra of SmOs<sub>4</sub>Sb<sub>12</sub>. On-RPES spectrum is taken at the photon energy B ( $h\nu \approx$  1076.5 eV) in Fig. 1(a). Off-RPES spectrum is taken at the photon energy A ( $h\nu \approx$  1070 eV) in Fig. 1(a). (b) High-resolution Sm 3d-4f RPES spectrum near  $E_F$ .

are not strongly influenced by the shape of the off-RPES spectrum, which originates dominantly from Os 5*d* states, because of the much smaller intensities of the off-RPES spectrum. It is found that the on-RPES spectrum has significant intensity at  $E_F$ . This indicates that the Sm 4*f* state contributes to the electronic states at  $E_F$  and is related to the formation of the HF state in SmOs<sub>4</sub>Sb<sub>12</sub>. Further discussion concerning the structures near  $E_F$  will be necessary within the framework of the PAM.

In conclusion, the soft and hard x-ray spectroscopy has revealed that the strongly mixed-valence state and the heavy-fermion state coexist in the bulk of SmOs<sub>4</sub>Sb<sub>12</sub>. Through theoretical analyses, the origin of the coexistence is found to be the coincidence of two conditions, namely, the small energy difference between the Sm divalent and trivalent states, and the weak *c*-*f* hybridization due to the Sm-centered large Sb cage in SmOs<sub>4</sub>Sb<sub>12</sub>. The estimated mean valence of bulk Sm ions is 2.7–2.8 and decreases with cooling down to  $T \sim T_K$  due to the Kondo effect.

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- [1] E.D. Bauer et al., Phys. Rev. B 65, 100506 (2002).
- [2] P.-C. Ho et al., Phys. Rev. B 72, 094410 (2005).
- [3] S. Sanada et al., J. Phys. Soc. Jpn. 74, 246 (2005).
- [4] W. M. Yuhasz et al., Phys. Rev. B 71, 104402 (2005).
- [5] H. Kotegawa et al., J. Phys. Soc. Jpn. 74, 2173 (2005).
- [6] N. Takeda and M. Ishikawa, J. Phys. Condens. Matter 15, L229 (2003).
- [7] K. Matsuhira et al., J. Phys. Soc. Jpn. 74, 1030 (2005).
- [8] N. Tsujii *et al.*, Phys. Rev. Lett. **94**, 057201 (2005).
- [9] H. Sato *et al.*, Phys. Rev. B **62**, 15125 (2000).
- [10] H. Sugawara et al., Phys. Rev. B 72, 014519 (2005).
- [11] G.P. Meisner et al., J. Appl. Phys. 57, 3073 (1985).
- [12] E.D. Bauer *et al.*, J. Phys. Condens. Matter **13**, 4495 (2001).
- [13] G.P. Meisner, Physica (Amsterdam) **108B&C**, 763 (1981).
- [14] A. Gerard et al., J. Phys. C 16, 2797 (1983).

- [15] E.D. Bauer *et al.*, J. Phys. Condens. Matter **16**, 5095 (2004).
- [16] G. K. Wertheim and G. Crecelius, Phys. Rev. Lett. 40, 813 (1978).
- [17] B. Johansson, Phys. Rev. B 19, 6615 (1979).
- [18] J.W. Allen et al., Phys. Rev. B 21, 1335 (1980).
- [19] E. Weschke et al., Phys. Rev. B 44, 8304 (1991).
- [20] A. Sekiyama *et al.*, Nature (London) **403**, 396 (2000);
   A. Sekiyama *et al.*, J. Phys. Soc. Jpn. **69**, 2771 (2000).
- [21] A. Yamasaki et al., Phys. Rev. B 70, 113103 (2004).
- [22] L. Braicovich et al., Phys. Rev. B 56, 15047 (1997).
- [23] C. Dallera *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A 547, 113 (2005).
- [24] A. Yamasaki et al., J. Phys. Soc. Jpn. 74, 2538 (2005).
- [25] Y. Saitoh et al., Rev. Sci. Instrum. 71, 3254 (2000).
- [26] M. Yabashi et al., Phys. Rev. Lett. 87, 140801 (2001).
- [27] H. Sugawara et al., Phys. Rev. B 66, 220504 (2002).
- [28] B.T. Thole et al., Phys. Rev. B 32, 5107 (1985).
- [29] S. Suga et al., Physica (Amsterdam) 186–188B, 59 (1993).
- [30] The IMFP of photoelectrons for  $\text{SmOs}_4\text{Sb}_{12}$  is obtained using the so-called TPP-2M formula [31]. Even though this empirical formula was developed from fits to calculated IMFPs for energies between 50 eV and 2 kV, it provides reasonable estimates for higher energy up to 30 keV [32]. We have adopted 101 for the total number of valence electrons per formula unit  $N_v$ , which consists of Sm  $5p^65d^16s^2$ , Os  $5d^66s^2$ , and Sb  $5s^25p^3$  electrons along the lines of recommended elemental values [33].
- [31] S. Tanuma et al., Surf. Interface Anal. 21, 165 (1994).
- [32] C.J. Powell (private communication).
- [33] S. Tanuma, C. J. Powell, and D. R. Penn (to be published).
- [34] A. Kotani and Y. Toyozawa, J. Phys. Soc. Jpn. 37, 912 (1974).
- [35] O. Gunnarsson and K. Schönhammer, Phys. Rev. B 28, 4315 (1983).
- [36] S. Imada and T. Jo, J. Phys. Soc. Jpn. 58, 2665 (1989).
- [37] A.J. Arko et al., Phys. Rev. B 56, R7041 (1997).
- [38] S. Suga et al., J. Phys. Soc. Jpn. 74, 2880 (2005).
- [39] A. Tanaka, T. Jo, and G. A. Sawatzky, J. Phys. Soc. Jpn. 61, 2636 (1992).
- [40] R. D. Cowan, *The Theory of Atomic Structure and Spectra* (University of California, Berkeley, 1981).
- [41] G. van der Laan and I.W. Kirkman, J. Phys. Condens. Matter 4, 4189 (1992).
- [42] A. Yamasaki *et al.* J. Electron Spectrosc. Relat. Phenom. 144–147, 621 (2005).
- [43] M. Mizumaki *et al.*, Physica (Amsterdam) **383B**, 144 (2006); M. Mizumaki *et al.* (to be published).
- [44] N.R. Dilley et al., Phys. Rev. B 58, 6287 (1998).
- [45] N. Takeda and M. Ishikawa, Physica (Amsterdam) 281– 282B, 388 (2000).
- [46] S. V. Dordevic et al., Phys. Rev. Lett. 86, 684 (2001).
- [47] M. Campagna et al., Phys. Rev. Lett. 33, 165 (1974).
- [48] S. Suga et al., Phys. Rev. B 51, 2061 (1995).
- [49] We have employed two different Lorentzian broadening widths to reproduce the whole spectral shape including the edge structure in the lowest  $E_B$  region considering the weak multiplet dependence of the core-hole lifetime [50].
- [50] H. Ogasawara et al., Phys. Rev. B 50, 12332 (1994).
- [51] D.A. Shirley, Phys. Rev. B 5, 4709 (1972).