

Long Phase Coherence Time and Number Squeezing of Two Bose-Einstein Condensates on an Atom Chip

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We measure the relative phase of two Bose-Einstein condensates confined in a radio frequency induced double-well potential on an atom chip. We observe phase coherence between the separated condensates for times up to ~ 200 ms after splitting, a factor of 10 longer than the phase diffusion time expected for a coherent state for our experimental conditions. The enhanced coherence time is attributed to number squeezing of the initial state by a factor of 10. In addition, we demonstrate a rotationally sensitive (Sagnac) geometry for a guided atom interferometer by propagating the split condensates.

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Precision measurements in atomic physics are usually done at low atomic densities to avoid collisional shifts and dephasing. This applies to both atomic clocks and atom interferometers. At high density, the atomic interaction energy results in so-called clock shifts [1], and leads to phase diffusion in Bose-Einstein condensates (BECs) [2–7]. Most precision measurements with neutral atoms are performed with free-falling atoms in atomic beams [8,9] or in fountain geometries [10]. Major efforts are currently directed towards atom interferometry using confined geometries, such as atom traps or waveguides, often realized by using atom chips [11]. These geometries are promising in terms of compactness and portability, and also offer the prospect of extending interrogation times beyond the typical 0.5 s achievable in the atomic fountains [10].

However, given the deleterious effects of high atomic density, those devices were thought to be able to operate only at low density and therefore at small flux, seriously limiting the achievable signal-to-noise ratio and sensitivity. Here we show that we can operate BEC interferometer at high density, with mean field energies exceeding $h \times 6$ kHz, where h is Planck's constant. Using a radio frequency (rf) induced beam splitter [12–14], we demonstrate that condensates can be split reproducibly, so that even after 200 ms, or more than 1000 cycles of the mean field evolution, the two condensates still have a controlled phase. The observed coherence time of 200 ms is 10 times longer than the phase diffusion time for a coherent state. Therefore, repulsive interactions during the beam splitting process [15] have created a nonclassical squeezed state with relative number fluctuations 10 times smaller than for a Poissonian distribution.

Our work is a major advance in the coherence time of confined atom interferometers, which have operated at interrogation times below ~ 50 ms [13,16,17] due to tech-

nical limitations. Our work also advances the preparation of number squeezed states to much higher atom numbers. Previous experiments in optical lattices [18,19] and in an optical trap [20] were limited to very small populations (~ 1 –1000 atoms). In addition, the fact that the clouds could be prepared on an atom chip with dc and rf electric currents, but without any laser beams, is promising for future applications. Finally, operating the rf-induced beam splitter on propagating condensates, we realized an on-chip Sagnac interferometer.

For two separated Bose-Einstein condensates, a state of well-defined relative phase (phase-coherent state), $|\phi\rangle$, is a superposition state of many relative number states, $|N_r = N_1 - N_2\rangle$, where N_1 and N_2 are the occupation of each well for $N = N_1 + N_2$ atoms. Because of atom-atom interactions in the condensates, the energy of number states, $E(N_1, N_2)$, have quadratic dependence on the atom numbers N_1 and N_2 so that the different relative number states have different phase evolution rates [2,5]. A superposition state will therefore have a spread of evolution rates, causing “phase diffusion” or “decoherence” of the relative phase with time. In contrast to normal diffusion processes, the phase uncertainty, $\Delta\phi$, increases here linearly. The phase diffusion rate, R , is proportional to the derivative of the chemical potential of condensates, $\mu(N_i)$ ($i = 1, 2$), with respect to the atom number and the standard deviation of the relative atom number, ΔN_r : $R = (2\pi/h)(d\mu/dN_i)_{N_i=N/2}\Delta N_r$ [2–7]. A number squeezed state with sub-Poissonian number fluctuations ($\Delta N_r = \sqrt{N}/s$), where $s > 1$ is the squeezing factor, will exhibit a reduced phase diffusion rate relative to a phase-coherent state with $\Delta N_r = \sqrt{N}$.

Bose-Einstein condensates of $\sim 4 \times 10^5$ ^{23}Na atoms in the $|F = 1, m_F = -1\rangle$ state were transferred into a mag-

netic trap generated by the trapping wire on an atom chip and external bias field [21]. A double-well potential in the horizontal plane was formed using adiabatic rf-induced splitting as described in Fig. 1(a) [12–14]. Typically, the separation of the two wells was $d \sim 8.7 \mu\text{m}$, the height of the trap barrier was $U \sim h \times 30 \text{ kHz}$, and the chemical potential of the condensates, measured from the trap bottom, was $\mu \sim h \times 6 \text{ kHz}$ [Fig. 1(b)]. The lifetime of the atoms at the splitting position was $\sim 1.8 \text{ s}$, significantly longer than in our previously demonstrated two-wire splitting method [21,22]. rf-induced splitting has several advantages over two-wire schemes: no loss channel (open port) during splitting, less sensitivity to magnetic bias fields, and realization of high trap frequencies far from a surface [23]. Atoms were held in the double well for varying hold times, released by turning off the trapping potential within $30 \mu\text{s}$ at a known phase of the rf field [24], overlapped, and interfered in time of flight [Fig. 1(c)]. The relative phase of the two condensates was measured as the spatial phase of the interference pattern [16,21].

An atom interferometer requires two independent condensates without any weak link which may lock the phase [16,21]. To demonstrate this independence, we monitored the relative phase over short intervals right after and after up to 190 ms delay time. During each of these intervals, the

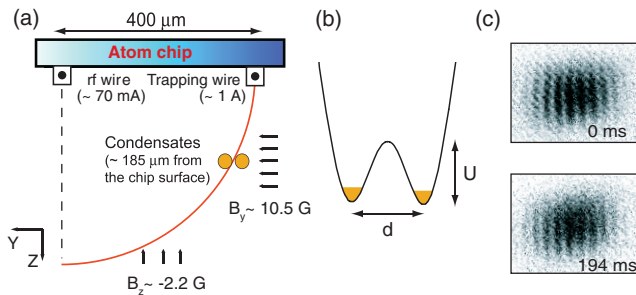


FIG. 1 (color online). Schematic of the atom chip interferometer. (a) Atoms were confined radially by the combined magnetic potential of a current-carrying wire and external bias field. Axial confinement in the x direction was provided by a pair of end cap wires (not shown) [21]. By dressing the atoms with an oscillating rf field from a second wire, the single minimum in the magnetic trapping potential was deformed into a double well [13]. If the trapping position lies on the circle containing the trapping wire and centered on the rf wire, the splitting occurs in the horizontal plane. Condensates were placed $185 \mu\text{m}$ away from the chip surface. For the single well, the radial (axial) trap frequency was $f_r = 2.1 \text{ kHz}$ ($f_z = 9 \text{ Hz}$) and the Larmor frequency at the trap center was $\approx 190 \text{ kHz}$ ($B_x \approx 0.27 \text{ G}$). Splitting was performed over 75 ms by linearly ramping the frequency of the rf field from 143 to 225 kHz . Gravity points in the $+z$ direction. (b) Double-well potential. The separation d between the two wells and the barrier height U were controlled by adjusting the frequency or amplitude of the rf field. (c) Matter wave interference. For various hold times after splitting, absorption images of condensates released from the double-well potential were taken after 10 ms time of flight. The field of view is $260 \times 200 \mu\text{m}$.

phase evolved linearly with time at $\sim 2\pi \times 200 \text{ Hz}$, the signature of independent condensates (Fig. 2). The non-vanishing phase evolution rates are attributed to small asymmetries in the two trapping potentials, which lead to slightly different chemical potential after the splitting process. The time variation of this rate is attributed to axial motion of the two separated condensates. Note that the observed drift of the phase evolution rate of $\sim 60 \text{ Hz}$ is only 1% of the condensates' chemical potential. In principle, the phase drift could be zeroed by a compensation field, but this has not been attempted.

To rule out the possibility that any weak link existed during the 200 ms time evolution and reset the relative phase, we demonstrated that an applied phase shift could be read out 200 ms after its appliance (Fig. 3). This proves that two independently evolving condensates have preserved phase coherence up to 200 ms , a factor of 10 longer than the phase diffusion time, $\tau_c = 1/R \approx 20 \text{ ms}$, for our parameters.

For the quantitative study of phase fluctuations, the standard deviation of the phase does not provide the best characterization because the phase is measured modulo 2π . In the limit of a large data set, a completely random distribution has a phase variance of $\sim (3\pi/5)^2$. Already for smaller variances, the overlap of the tails of the Gaussian distribution can cause ambiguities. As a more appropriate measure of correlation, we represent each measurement of the relative phase as a phasor with unit length and compare the length of the sum of N measured phasors with the expectation value of \sqrt{N} for N random phasors. The larger the difference, the smaller is the probability that the data set is compatible with a random phase distribution. This probability of uncorrelated phases is called randomness [26]. Uncorrelated data have an expected value of randomness near 0.5 , while strongly correlated data would have a small value, e.g., ten data points drawn from a distribution with variance $(\pi/5)^2$ have a probability of only 10^{-4} to be compatible with uncorrelated phases.

To study phase diffusion in our system, we analyze the distribution of ten measurements of the relative phase at

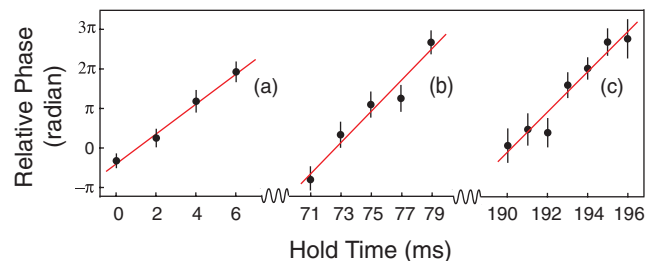


FIG. 2 (color online). Phase evolution of the relative phase during three different time intervals. The evolution rate of the relative phase are determined from the linear fit to be (a) 191 , (b) 198 , and (c) 255 Hz . The data points represent the average of ten measurements for (a) and (b), and 15 for (c).

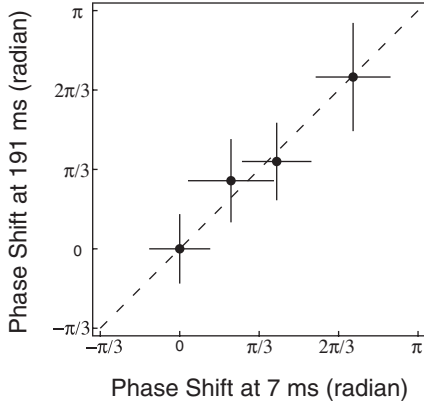


FIG. 3. Long phase coherence of two separated condensates. Applying various phase shifts to the condensates at 2 ms after splitting, the shifts of the relative phase were measured at 7 and 191 ms, showing strong correlation. The dotted line denotes the ideal case of perfect phase coherence. Phase shifts were applied by pulsing an additional magnetic field in the z direction for $50 \mu\text{s}$ with variable amplitude.

various times after splitting, as shown in Fig. 4. The data show a well-defined phase (with probability $>90\%$) for times shorter than ~ 200 ms. In contrast, the simulation for a coherent state in our experimental conditions, shown as a blue dotted line, predicts the same scatter of phase measurements already after ~ 20 ms. Fitting a phase diffusion model to the data points with randomness probability >0.1 , gives a phase diffusion time of 200 ms. The solid line is a fit which includes the initial variance $\Delta\phi_0^2$:

$$\Delta\phi(t)^2 = \Delta\phi_0^2 + (Rt)^2. \quad (1)$$

The variance of the initial state, $\Delta\phi_0^2 = (0.28\pi)^2$ is dominated by technical noise including fitting errors and non-ideal trap switch off. The contribution due to initial number fluctuations, $\Delta\phi_0^2 \approx (s/\Delta N_r)^2$, is $\sim (7.1 \times 10^{-4}\pi)^2$ for a coherent state ($s = 1$), and remains small unless the squeezing leads to number fluctuations on the order of a single atom, $s \sim \sqrt{N}$. The fitted value for the phase diffusion rate of $R = 5 \text{ s}^{-1}$ includes technical shot-to-shot variations in the relative atom number of two condensates after splitting and thermal fluctuation. Therefore, the inferred squeezing factor $s = 10$ represents a lower bound. It implies that our relative atom number fluctuations were smaller than $\pm 0.03\%$ corresponding to ± 50 atoms.

Locally the interference pattern of two pure condensates should always have 100% contrast, where contrast is defined as the density amplitude of the interference fringes over the mean density. Since in our experiment the contrast is derived from interference pattern integrated along the line of sight, it decreased gradually with time and exhibited fluctuations most likely due to asymmetric axial motion [Fig. 4(b)]. Except for small regions near 110 and 300 ms hold time, the contrast was above 10%, sufficient for accurate determination of the phase. The small windows

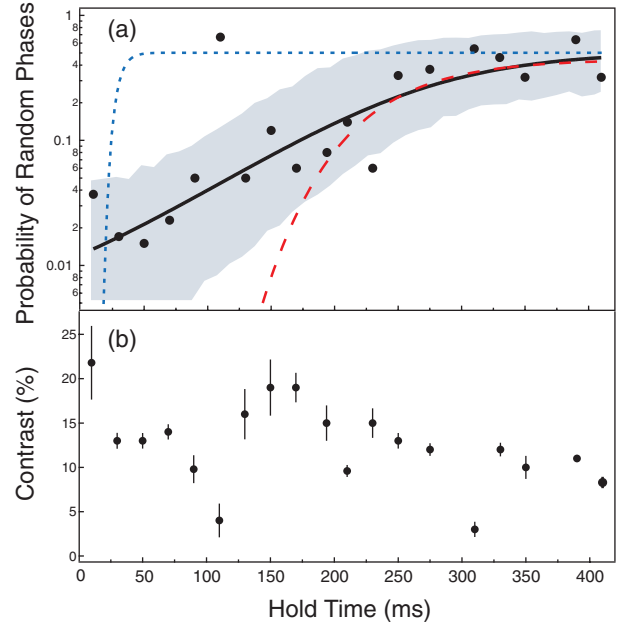


FIG. 4 (color online). Phase diffusion and number squeezing. (a) The randomness probability of ten measurements of the relative phase is displayed up to 400 ms after splitting. The blue dotted curve (red dashed curve) shows a simulation for a phase-coherent state (number squeezed state with $s = 10$), which have negligible initial phase uncertainty. The solid line includes an initial phase uncertainty of 0.28π (see text). The shaded region represents the window where ten data points from the sample with the given phase uncertainty would fall with 50% probability. (b) Contrast of the interference pattern. Since the end cap wires generate a field gradient $\frac{\partial B_z}{\partial x}$ as well as a field curvature $\frac{\partial^2 B_z}{\partial x^2}$ at the position of the condensates, the two wells are not parallel to the trapping wire and consequently have slightly different axial trapping potential. This difference induces relative axial motion of the two condensates, which periodically reduces the contrast.

with poor contrast have a large probability for random phases.

The observed long phase coherence time implies that the initial state is number squeezed. The probable origin of number squeezing during the splitting is repulsive atom-atom interactions [15]. The interactions make it energetically favorable for the two condensates to split with equal numbers in a symmetric double-well potential, whereas number fluctuations, such as in a coherent state, cost energy. Describing splitting dynamics by the Josephson Hamiltonian shows how the interplay of tunneling and interactions leads to an increase of squeezing as the barrier is increased [15,27]. Assuming that the squeezing can no longer increase when the Josephson frequency becomes slower than the inverse splitting time, we estimate a squeezing factor of ~ 13 for our experimental conditions [27]. For our elongated condensates, phase fluctuations are present for temperature above ~ 100 nK which is $\sim 1/10$ of the BEC transition temperature [28]. Since we cannot

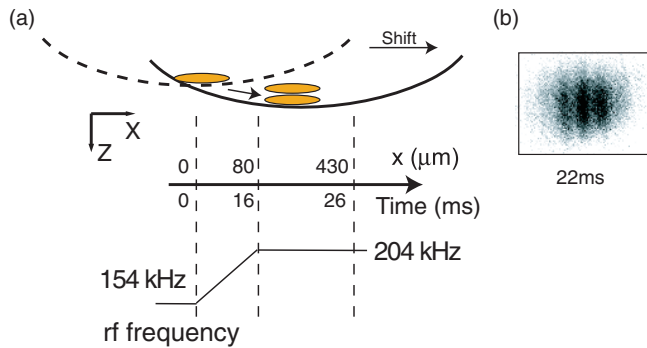


FIG. 5 (color online). Confined atom interferometry with enclosed area. (a) A single trapped condensate at rest was accelerated by shifting the trap center by $\sim 430 \mu\text{m}$ in the axial direction ($t = 0$ ms). The frequency of the rf field was linearly ramped from 154 to 204 kHz during 16 ms after launch, splitting the condensates and separating them by $5\text{--}6 \mu\text{m}$. (b) Phase measurements were done for up to 26 ms after the launch. The probability for random phases was determined for data sets of ten measurements. Until 16 ms, this probability was extremely low (less than 10^{-12}) and the relative phase was constant, implying that the two condensates were still connected. For $t > 16$ ms, the relative phase evolved (similar to Fig. 2), and the probability for a random phase distribution was smaller than 10%. This demonstrates that phase coherence was preserved after full splitting. The figure shows the interference pattern for $t = 22$ ms. The field of view is $260 \times 200 \mu\text{m}$.

measure the temperature of an almost pure condensate in time of flight, it is not clear whether the interfering condensates had correlated phase fluctuations or not.

The work presented so far, and also all previous work on interferometry of confined or guided atoms, featured geometries without any enclosed area between the two paths of the interferometer. An enclosed area is necessary for rotational sensitivity [8,9,29] and requires moving atoms. As described in Fig. 5, we were able to extend the coherent beam splitter to condensates moving on an atom chip. The observed coherence time (10 ms) and propagation distance after splitting ($\sim 350 \mu\text{m}$) were only limited by the chip geometry. This corresponds to an enclosed area of $\sim 1500 \mu\text{m}^2$, and a response factor $\frac{4\pi m A}{h} \sim 7.9 \times 10^{-5} \text{ rad}/\Omega_e$ for rotation sensing, where m is the probe particle mass and Ω_e the earth rotation rate [30].

In conclusion, the present work demonstrates a long phase coherence time of ~ 200 ms between two spatially separated condensates on an atom chip, rivaling the interrogation times in fountain-type interferometers [10]. Number squeezing by a factor ≥ 10 occurs during the preparation of the split state, providing a well-defined phase beyond the phase diffusion limit for a coherent state. Thus, interaction-induced squeezing reduces the phase diffusion caused by the same interactions [15]. These results show that it is both possible and promising to use

condensates at high density for interferometry on an atom chip.

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