

**Łodziana and Vegge Reply:** In the Comment to our Letter [1], Zarkevich and Johnson argue [2] that our methodology cannot be used to study  $\text{LiBH}_4$  at high temperatures. We show that the claims in [2] are not physically justified.

In agreement with our findings and those of others [3], Zarkevich and Johnson present data showing (Fig. 1 in [2]) that  $\text{LiBH}_4$  is not stable in the experimentally proposed  $P6_3mc$  symmetry [4]. Unfortunately, no information about a stable symmetry of  $\text{LiBH}_4$  at high temperatures is presented in [2]. The statement “hexagonal structure with rotational modes” is unclear to us, since all molecular structures like  $\text{LiBH}_4$  intrinsically possess translational, rotational (“librational” in [1]), and stretching modes.

Every ordered nonmagnetic crystal system belongs to exactly one of 230 space groups, which are unequivocally defined via their point and lattice symmetry operations [5]. The (quasi) harmonic approximation assumes harmonicity of the potential energy at equilibrium (the free energy minimum). A system which is unstable within the harmonic approach can be stabilized by entropy, in which case it must possess more than dynamical disorder. With additional configurational disorder, the equilibrium symmetry is different (perhaps lower, as we show [1]) and the definition of the space group would require designation of site occupancy.

Figure 1 in [2] presents the calculated energies for  $0^\circ$ ,  $30^\circ$ , and  $60^\circ$  rotations of  $\text{BH}_4$  around  $[0001]$  ( $C_3$  here) connected by a periodic potential displaying a puzzling sixfold symmetry, which is absent for any site in  $P6_3mc$ —in particular for the  $3m$  symmetry of the “ $b$ ” site of B and H. Accurate calculation of the rotation of individual  $\text{BH}_4$  units requires large systems ( $\geq 96$  atoms), whereas a 12 atom supercell (used in [2]) corresponds to a speculative unison rotation. In fact, no barrier for rotation is found in [2], but a lower energy configuration where half of the  $\text{BH}_4$  units are rotated  $30^\circ$ .

In [1], we specifically addressed the instability of the  $P6_3mc$  structure, however for clarity, the calculated  $\text{BH}_4$  rotational barriers for the  $P6_3mc$  structure are presented here in Fig. 1. The large barriers along  $C_3$  possess proper symmetry and they exclude free rotation of  $\text{BH}_4$  around this axis, which was originally proposed in [4] and restated in [2]. Rotations of the  $\text{BH}_4$  tetrahedron around various axes possess minima other than the equilibrium orientation of  $\text{BH}_4$  in the  $P6_3mc$  symmetry, see Fig. 1(b). There are actually more modes with this property [1], not only one as investigated in [2], many of which have translation-rotation coupling. In that sense, the harmonic approximation is not justified to study thermodynamics of  $\text{LiBH}_4$  in the  $P6_3mc$  symmetry, which is why no conclusions are drawn in [1] about the  $P6_3mc$  structure from the harmonic approximation, except the fully justified conclusion that it is unstable. A simple analysis gives different alignments of  $\text{BH}_4$  which are slanted from their orientation along  $[0001]$  and the resulting symmetry is  $P2_1$ ; mode coupling results in the  $Cmc2_1$  and  $Cc$  symmetry.

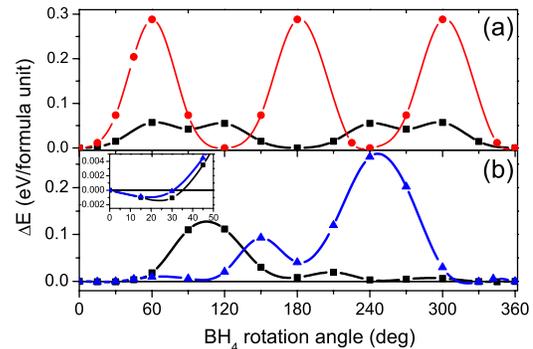


FIG. 1 (color online). (a) Adiabatic rotational barriers for  $\text{BH}_4$  rotation around the  $C_3$  (red circles) and  $C_2$  (black squares) axes in the  $P6_3mc$  structure of  $\text{LiBH}_4$ . (b) Barriers for  $\text{BH}_4$  rotation around the  $[0100]$  (black squares), and  $[1100]$  (blue triangles) directions; the inset shows local minima for the  $\text{BH}_4$  orientation. Lines are guides to the eye.

At least two structures of  $\text{LiBH}_4$  at high temperatures have been proposed experimentally, i.e., a tetragonal [6] and a hexagonal [4]. The x-ray diffraction pattern of the  $Cc$  structure in [1] is slightly different from the experimentally ascribed  $P6_3mc$  hexagonal structure. However, when considering anisotropic temperature effects (cannot be handled within the quasiharmonic approximation) the fit of the preserved  $Cc$  structure to the experimental pattern is reasonable. An anisotropic thermal expansion can shift the four asymmetric peaks at  $T = 0$  K (Fig. 3 in [1]) to three symmetric peaks of the  $Cc$  phase (as found for  $P6_3mc$ ) with only a minor features at higher angles.

We fully acknowledge the limitations of both density functional theory and diffraction experiments with respect to the determination of hydrogen positions at finite temperatures, however, no physically justifiable new insight is presented in the preceding Comment [2].

Zbigniew Łodziana<sup>1</sup> and Tejs Vegge<sup>2</sup>

<sup>1</sup>Institute of Nuclear Physics, ul. Radzikowskiego 152  
PL-31-342 Krakow, Poland

<sup>2</sup>Materials Research Department  
Risø National Laboratory  
DK-4000 Roskilde, Denmark

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