Muon Spin Relaxation Studies of Superconductivity in a Crystalline Array of Weakly Coupled Metal Nanoparticles

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We report muon-spin-relaxation studies in weak transverse fields of the superconductivity in the metal cluster compound, $Ga_{84}[N(SiMe_3)_2]_{20}$ -Li₆Br₂(thf)₂₀ · 2 toluene. The temperature and field dependence of the muon-spin-relaxation rate and Knight shift clearly evidence type II bulk superconductivity below $T_c \approx$ 7.8 K, with $B_{c1} \approx 0.06$ T, $B_{c2} \approx 0.26$ T, $\kappa \sim 2$, and weak flux pinning. The data are well described by the *s*-wave BCS model with weak electron-phonon coupling in the clean limit. A qualitative explanation for the conduction mechanism in this novel type of narrow-band superconductor is presented.

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The chemical synthesis of molecular metal cluster compounds presents an attractive bottom-up route for the generation of self-organized nanostructures composed of 3D ordered arrays of identical metal nanoparticles embedded in a dielectric matrix. Until recently, such cluster solids were always found electrically insulating. On the other hand, the strong similarity with (super)conducting molecular crystals, as the alkali-metal-doped fullerenes (C_{60}), suggests that, in principle, metal cluster compounds could also display metallic conductivity (and even superconductivity) due to intermolecular charge transfer. We have indeed recently obtained compelling evidence from ^{69,71}Ga-NMR [1] and magnetization measurements for the occurrence of *band-type conductivity* in crystalline ordered Ga₈₄ cluster compounds, composed of arrays of giant Ga₈₄ cluster molecules that display mixed-valence properties. In addition, bulk type II superconductivity was observed below a transition temperature $T_c \approx 7.5$ K, much higher in fact than known for bulk α -Ga metal ($T_c \approx 1$ K). This material may thus represent a first experimental realization of a theoretical model advanced by Friedel in 1992 [2], who predicted that for a *crystalline array of identical* metal nanoparticles, a very weak interparticle charge transfer can still yield superconductivity with a relatively high T_c value.

From the NMR study, a number of results were obtained. First, the field and temperature dependence of the Knight shift can be well fitted to BCS theory for weak electronphonon coupling, a rather surprising result since strong correlations would be expected for such narrow-band conductors as the present. Second, a very strong sample dependence of the second critical field B_{c2} was revealed. As compared to $B_{c2} \approx 13.8$ T reported previously [3], we found that for most of the samples the minimum field of about 2 T required for the NMR signal (due to signal-tonoise ratio) was already sufficient to suppress the superconductivity completely. Only in a few samples superconductivity could be detected by NMR up to about 5 T. By contrast, magnetization studies showed diamagnetic signals for all samples below similar values of $T_c = 7-8$ K, but with apparent B_{c2} values as low as 0.3 T. Although an explanation of this variation (by a factor of 50) in terms of lattice defects-associated with orientational disorder in the molecular crystal lattice-was proposed, definite proof for the occurrence of bulk superconductivity in the low B_{c2} samples seemed highly desirable. In order to check this assumption, muon-spin-relaxation (μ SR) experiments in small transverse fields $(B_{\rm TF})$ have therefore been performed. As discussed below, they provide unambiguous proof for bulk type II superconductivity, with a Ginzburg-Landau (GL) parameter $\kappa \sim 2$, and are likewise in agreement with weak-coupling BCS model predictions. A qualitative discussion of the nature of the conduction mechanism in terms of intermolecular charge fluctuations is presented at the end of the Letter.

The crystal structure of the giant molecular cluscompounds which short ter Ga_{84} , is for $Ga_{84}[N(SiMe_3)_2]_{20}\text{-}Li_6Br_2(thf)_{20}\cdot 2 \text{ toluene } (Me=CH_3$ and thf = $C_4H_8O_1$, is fully described in [4]. The μ SR experiments were performed on the sample labeled S3 in the previous work [1], which showed an excellent crystallinity in x-ray experiments [4], with typical dimensions of the (randomly oriented) crystallites of 0.1 mm. Magnetization measurements in a commercial SQUID magnetometer evidence a superconducting (SC) transition at $T_c = 7.75(5)$ K in zero external field. A T = 0 extrapolation yields an upper critical field $B_{c2} \approx 0.26$ T. Using the expression $B_{c2} \approx \Phi_0/2\pi\xi^2$, where Φ_0 is the flux quantum, gives a coherence length $\xi \sim 35$ nm much larger than the intercluster distance, of order 2 nm. The extrapolated thermodynamical critical field at T = 0 was found as $B_{c1} \approx 60$ mT. Using the general expression given by Brandt for an ideal triangular GL vortex lattice, relating B_{c2} , B_{c1} and the GL parameter κ [5], we find $\kappa \sim 2$ and a London penetration depth $\lambda \sim 70$ nm. This sample, which is consequently close to the "clean" SC limit, indeed

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displays the largest (super)conducting fraction reached so far in a Ga₈₄ sample (90%), as found in the ^{69,71}Ga NMR experiments performed on several batches [1].

Transverse field μ SR is a powerful technique to probe type II superconductivity locally [6], and can be performed in any arbitrary field close to zero, contrary to NMR. By implanting 100% spin polarized muons (μ^+) in the material, the local field they experience can be measured through their decay into, among others, a positron, in a typical time window of 0.1–10 μ s. We performed our experiments on the π M3 beam line on the GPS spectrometer in PSI, Villigen, Switzerland, in the temperature range 2 K \leq T \leq 10 K, using magnetic fields 0 \leq $B_{\text{TF}} \leq$ 0.4 T. The Ga₈₄ sample (30 mg) is extremely air sensitive and must be kept in a toluene solution with a sample/toluene mass ratio of order $80/20(\pm 10)$ to avoid loss of crystal solvent. We therefore sealed it in an Al sample holder [7], using an Al thickness of 0.35 mm between the incident μ^+ beam and the sample as a moderator for the muons. From the geometry of our sample, a pellet of thickness 0.55 mm and diameter 7 mm, and the calibrated beam distribution, the μ^+ fraction stopped in the Al sample holder (plus the nonconducting fraction of Ga₈₄) called "background" in the following, is of order 25%. This will appear as a temperature- and field-independent signal in the whole temperature range. The μ^+ fraction stopped in toluene is of order 17% and does not contribute to the measured signal, as seen experimentally by a reduction of the expected intensity by this amount. We attribute this reduction to the formation of muonium in this solvent. Given the large fraction of muons stopping outside the superconducting Ga₈₄ sample ($\sim 42\%$) we took data with good statistics, with typically $40 \times 10^6 \mu^+$ per point.

Figure 1 shows the time dependence of the μ^+ polarization P(t) along the polarization axis, perpendicular to $B_{\rm TF}$, for two temperatures and $B_{\rm TF} = 60 \text{ mT} \ge B_{c1}$, in a field cooled (FC) experiment. A clear difference can be seen between the data measured at $T = 10 \text{ K} > T_c$ and $T = 2 \text{ K} \ll T_c$. Above T_c , the local field (B_{μ}) distribution is small and only due to nuclear dipoles. It yields a usual slow Gaussian depolarization and a precession frequency centered at the suited Larmor frequency $\gamma B_{\mu}/2\pi$, where γ is the μ^+ gyromagnetic ratio. Below T_c , a flux line lattice (FLL) is created in the mixed state, resulting in a larger distribution of B_{μ} , i.e, a faster relaxation of P(t).

In order to get a first *qualitative* impression of the behavior of the various relevant parameters, a single damped cosine was fitted to the raw data. This model-independent analysis already clearly shows a transition at $T_c \approx 6.4$ and 5.9 K, for $B_{\rm TF} = 60$ and 90 mT (corresponding to B_{c2} found in magnetization measurements at these temperatures), in a FC experiment, in both the relaxation rate (not shown) and the precession frequency, $\nu_{\rm tot}$ [Fig. 2(inset)]. In a second step, the background contribution has to be evaluated to get more *quantitative* information. To fit the μ^+ polarization, we used the phenomeno-



FIG. 1 (color online). Polarization P(t) of the μ^+ spins, in a FC experiment ($B_{\rm TF} = 60$ mT). For clarity, only one of the two parts (imaginary or real) is presented for each *T*, in a rotating frame at a frequency $\gamma \times 55$ mT. The continuous lines are fits with Eq. (1). The dotted and dashed lines represent the envelope of the background and the total signal, respectively.

logical function

$$P(t) = x \exp(-[\sigma_{Ga}t]^{\alpha} - \sigma_{nd}^{2}t^{2})\cos(\omega_{Ga}t + \phi)$$
$$+ (1 - x)\exp(-\sigma_{bgd}^{2}t^{2})\cos(\omega_{bgd}t + \phi). \quad (1)$$

The first term accounts for the Ga₈₄ signal. The second term represents the background. The relaxation rates σ_{nd} and σ_{bgd} are due to the nuclear dipolar fields on the respective sites [6]. A global fit was used, sharing the *T*- and B_{TF} -independent parameters in order to limit the number of free parameters and to avoid unrealistic values. It yields a fraction $x \approx 0.7$ of μ^+ stopping in Ga₈₄, $\sigma_{nd} \approx 0.06 \ \mu s^{-1}$ and $\sigma_{bgd} \approx 0.04 \ \mu s^{-1}$, which are typical values for nuclear relaxation rates [6,8,9]. Although a rough approximation, a Gaussian ($\alpha = 2$) is usually suited to fit



FIG. 2 (color online). *T* dependence of $K_{\text{Ga}} - K_{\text{Ga,n}}$, for two values of B_{TF} . Lines are BCS fits with a *s*-wave symmetry of the SC gap. Labels are weak (W) and strong (S) electron-phonon coupling, and clean (C) and dirty (D) limits. Insets: precession frequency ν_{tot} of the μ^+ spins obtained with a single damped cosine fit, for $B_{\text{TF}} = 60$ mT. The line shows the average value for $T > T_c$.

the FLL field distribution in powder samples [5,10]. This implies that the second moment of the field distribution, $\langle \Delta B_{\mu}^2 \rangle^{1/2}$, related to the penetration depth λ , is directly proportional to the μ^+ relaxation rate due to the FLL distribution (σ_{Ga}). In our case a Gaussian cannot account for the decay of the first P(t) oscillations at low-T (Fig. 1) and we find instead a T- and $B_{\rm TF}$ -independent $\alpha \approx 0.5$. This value is reminiscent of inhomogeneous field distribution cases as in spin glasses [11]. Given the fact that a strong sample dependence of B_{c2} is found in Ga₈₄ [1], a distribution of B_{c2} in this particular sample is also possible and would explain this result. A complication of this α value is that the corresponding average field distribution does not converge unless a cutoff (which could not be measured within the experimental resolution) is introduced in the spectrum. To proceed, we therefore assume the proportionality $\sigma_{\rm Ga}^2 \propto \langle \Delta B_{\mu}^2 \rangle$ to be still obeyed. We are then finally left with only two free parameters, σ_{Ga} and ν_{Ga} .

The *T* dependence of the average shift $K_{\text{Ga}} = (\omega_{\text{Ga}} - \gamma B_{\text{TF}})/\gamma B_{\text{TF}}$, is displayed in Fig. 2. This (muon) *Knight* shift is usually the sum of a *T*- and B_{TF} -independent orbital shift K_{orb} and a spin part K_S , proportional to the *s*-electron susceptibility [and to the electronic density of state at the Fermi level, $D(E_F)$]. In the normal state (n), we find a *T*- and B_{TF} -independent value (as expected in metals) of $K_{\text{Ga,n}} \sim K_{\text{bgd}} \sim -0.17\%$. The negative sign is due to the hyperfine coupling of the μ^+ with the carriers, which is known to be strongly sample dependent [12,13]. The present value is comparable to those found in several heavy fermion compounds [14,15].

Below T_c , the average precession frequency (inset of Fig. 2) is seen to increase continuously down to $T \rightarrow 0$ for both values of $B_{\rm TF}$. Since the Knight shift is negative, this implies a decrease of its absolute value. In the mixed state, a possible additional shift (K_d) due to the demagnetization and Lorentz fields would reduce the local field at the muon site. Therefore, it cannot account for an increase of $\nu_{\rm tot}$ and hence the variation of the shift can be attributed to a decrease of the spin part $|K_S|$ due to spin-singlet-pairing of the quasiparticles below T_c [16].

Figure 2 shows that $K_S(T)$ is well fitted by a BCS model with *s*-wave symmetry of the SC gap and weak electronphonon coupling (i.e., with a SC gap $\Delta_0 \approx 1.76k_{\rm B}T_c$) [17,18]. The decrease of the SC carrier density due to the increase of $B_{\rm TF}$ is directly observed through a nonzero shift at $T \rightarrow 0$. It is also clear that the reduction of $|K_S|$ is larger in the "low" field measurement, as expected from a larger fraction of Cooper pairs [19]. The strong electron-phonon coupling and the dirty limit cases (the latter being unlikely from the magnetization data) [20] are also presented in Fig. 2. Their steeper variation below T_c clearly does not agree with the data.

The *T* dependence of σ_{Ga} is presented in the inset of Fig. 3. The reduction of T_c and an increase of the internal field homogeneity (i.e., a decrease of σ_{Ga}), is clearly observed when B_{TF} is increased. In the extensively studied

cuprates and heavy fermions, the conditions $\kappa \gg 1$ and $B_{\rm TF} \ll B_{c2}$ imply that the ratio $\sigma_{\rm Ga}/\lambda^{-2}$ is roughly *T* and $B_{\rm TF}$ independent [6,9]. Here, the artificial reduction of $\sigma_{\rm Ga}$ due to the overlap of the vortices near B_{c2} has to be taken into account. In the framework of the GL theory, Brandt derived the quantity $\lambda^2 \langle \Delta B_{\mu}^2 \rangle^{1/2}$ as a function of κ and *b*, where *b* is the average internal field divided by $B_{c2}(T)$ [5]. Calling this quantity f(b), the function $\lambda^{-2} \propto f(b)\sigma_{\rm Ga}$ is presented in Fig. 3, taking $\kappa = 2$. The qualitative variation of $\lambda^{-2}(T)$ is very similar to the *T* dependence of K_S , as expected in the BCS model in small fields [17,18], and as shown by the fit with weak electron-phonon coupling in the clean limit (Fig. 3). This is quite rewarding concerning the validity of the analysis.

Next, we discuss the field dependence of σ_{Ga} at low T. We measured σ_{Ga} from the pure diamagnetic state up to the normal state by increasing the field from a zero field cooled (ZFC) condition at 2 K, from 0 up to $B_{\rm TF} > B_{c2}$. The results of the fits with Eq. (1) are presented in Fig. 4. For small fields ($B_{\rm TF} \leq B_{c1}$), $\sigma_{\rm Ga}$ continuously increases with $B_{\rm TF}$. A strong inhomogeneity of the electron density of state in Ga₈₄, as well as the powder nature of the sample as suggested in [10], may lead to some FLL bending around SC grains and an inhomogeneity responsible for a nonzero σ_{Ga} . When $B_{\text{TF}} \gtrsim B_{c1}$, σ_{Ga} reflects both the FLL organization [5] and the field dependence of λ^{-2} . For high fields $(B_{\rm TF} \gtrsim B_{c2} \sim 0.2 \text{ T} \text{ at } 2 \text{ K})$, the superconductivity is destroyed and an homogeneous field ($\sigma_{Ga} = 0$) is recovered. The ratio $\lambda/\lambda(0) \propto [f(b)\sigma_{Ga}]^{-2}$ is presented in the inset of Fig. 4 as a function of b. In a BCS model with s-wave symmetry, the penetration depth λ is expected to be weakly field dependent [21], with a roughly linear variation of σ_{Ga} . However, a linear variation of λ , quantitatively comparable to the type II superconductor NbSe₂ [6], is measured and is consistent with a *d*-wave symmetry of the SC gap (continuous lines) [6,22]. Moreover, the predicted σ_{Ga} variation, with a constant λ , does not fit the data (dashed line). The theoretical computations are usually performed in an equilibrium FLL, which does not really correspond to our case. Indeed, the pinning of the vortices increases the local



FIG. 3 (color online). T dependence of $f(b)\sigma_{Ga} \propto \lambda^{-2}$. The lines are BCS fits (WC). Inset: $\sigma_{Ga}(T)$ from Eq. (1).



FIG. 4 (color online). $B_{\rm TF}$ dependence of $\sigma_{\rm Ga}$, in ZFC and FC conditions. The pinning accounts for the difference. Inset: $\lambda(b)/\lambda(0)$. The lines are computations with $\kappa = 2$, a constant λ (*s* wave, dashed lines) and $\lambda/\lambda(0) \propto 1 + 3.1(5)b$ (*d* wave, solid lines). We note that b = 0 when $B_{\rm TF} \leq B_{\rm cl}$ [5].

field distribution, as seen by the usual [10,23] reduction of σ_{Ga} in the FC case (which also reduces the sensitivity of the experiment). However, the shape of the variation does not seem to be changed. We stress that these results should be taken with caution since the phenomenological function with $\alpha = 0.5$ could bias the results on σ_{Ga} , and λ . In any case the quantitative value for λ is uncertain.

Finally, we address the nature of the conduction mechanism in Ga₈₄. In the Friedel model, referred to in the introduction, conduction would occur in a narrow band originating from a molecular energy level near E_F of the Ga₈₄ cluster, with a width proportional to the intercluster, i.e., anion-anion charge transfer t. In view of the ligand shells around the Ga_{84} cluster cores, t is, however, expected to be quite small, of order 0.01 eV. In a Hubbard model approach, t would have to compete with the on-site Coulomb interaction (Hubbard-U) of the anion, estimated at about 0.5 eV (3 times smaller than for C_{60}). In such a narrow-band system, strong electron-electron correlations are expected whereas the NMR and μ SR experiments both indicate nearly free electron behavior (Korringa constants, Knight shifts). It appears relevant, therefore, to consider other possible charge fluctuations.

In analogy with the well-known models proposed for the transition metal compounds [24], one such possibility could be an electron transfer from the cluster anion to the Li cation, in combination with conduction in the cation band derived from the cation-cation overlap. Preliminary estimates, based on the cation ionization energy, the anion electron affinity, and the Madelung energies involved, indicate the anion-cation charge transfer process to be almost energetically neutral, i.e., it could in fact be quite small, smaller perhaps than the width of the cation band. The latter is difficult to estimate but could be larger than t. In this scenario the itinerant carriers would reside mainly in the cation band, which could explain why in the measured Ga-NMR spectra the different Ga sites in the cluster are clearly resolved, as in an insulating Ga compound. Clearly, more sophisticated calculations are needed to further elucidate the conduction processes in this exciting novel type of molecular (super)conductor.

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