¹⁵C⁻¹⁵F Charge Symmetry and the ¹⁴C (n, γ) ¹⁵C Reaction Puzzle

N. K. Timofeyuk,¹ D. Baye,² P. Descouvemont,² R. Kamouni,² and I. J. Thompson¹

¹Department of Physics, University of Surrey, Guildford, Surrey GU2 7XH, United Kingdom
²PNTPM CP220 Université Libre de Bruxelles, B1050 Brussels, Belgium

PNTPM CP229, Universite´ Libre de Bruxelles, B1050 Brussels, Belgium

(Received 8 November 2005; published 27 April 2006)

The low-energy reaction $^{14}C(n, \gamma)^{15}C$ provides a rare opportunity to test indirect methods for the determination of neutron capture cross sections by radioactive isotopes versus direct measurements. It is also important for various astrophysical scenarios. Currently, puzzling disagreements exist between the ${}^{14}C(n, \gamma) {}^{15}C$ cross sections measured directly, determined indirectly, and calculated theoretically. To solve this puzzle, we offer a strong test based on a novel idea that the amplitudes for the virtual ¹⁵C \rightarrow ¹⁴C + *n* and the real ${}^{15}F \rightarrow {}^{14}O + p$ decays are related. Our study of this relation, performed in a microscopic model, shows that existing direct and some indirect measurements strongly contradict charge symmetry in the ${}^{15}C$ and ${}^{15}F$ mirror pair. This brings into question the experimental determinations of the astrophysically important (n, γ) cross sections for short-lived radioactive targets.

DOI: [10.1103/PhysRevLett.96.162501](http://dx.doi.org/10.1103/PhysRevLett.96.162501) PACS numbers: 25.40.Lw, 21.60.Gx, 27.20.+n

Many nuclear reactions in stellar interiors involve radioactive nuclei. Construction of radioactive beam facilities all around the world provided the opportunity to study some of these reactions directly. However, a large class of nuclear reactions, namely, neutron capture by shortlived radioactive isotopes, cannot be studied directly due to the nonexistence of neutron targets and the short neutron lifetime. Nevertheless, since the knowledge of these reactions is important for predictions of chemical evolution of the Universe they are studied indirectly, for example, using inverse dissociation reactions, and will be done so for a long time in the future. Therefore, the consistency between direct and indirect methods must be achieved.

The neutron capture on a long-lived radioactive target 14 C provides one of the few possible test cases where a comparison between direct and indirect methods is possible. On the other hand, the ¹⁴C(*n*, γ)¹⁵C reaction is interesting on its own because of its important astrophysical applications. First, the knowledge of this reaction rate is necessary for making quantitative predictions for primordial abundances of heavy chemical elements in a nonstandard inhomogeneous big bang model. According to this model, neutron- and proton-rich zones may appear in the early Universe with different sequences of nuclear reactions in them. In neutron-rich zones, reaction chains composed of (n, γ) , (t, n) , and (α, n) reactions allow bypassing of the $A = 8$ mass gap and the production of beryllium, boron, and carbon isotopes including stable ones on the time scale of the big bang isotope ^{14}C [1]. Further nucleosynthesis depends on reactions that destroy ¹⁴C, the most important of which is ¹⁴C(*n*, γ)¹⁵C. Second, ¹⁴C(*n*, γ)¹⁵C is a part of the neutron induced CNO cycles in the helium burning layer of asymptotic giant branch stars, in the core helium burning of massive stars, and in subsequent carbon burning [2]. Such cycles may cause a depletion in the CNO abundances. The ¹⁴C(*n*, γ)¹⁵C reaction is the slowest of both of these cycles and, therefore the knowledge of its rate is important to predict the ${}^{14}C$ abundances over the period of high neutron flux [2]. Finally, the ¹⁴C(*n*, γ)¹⁵C reaction triggers synthesis of heavy carbon and oxygen isotopes in the hot-bubble scenario of gravitational core-collapse Type II supernovae explosions with neutrino driven winds [3].

Currently, a puzzling disagreement exists between the cross sections $\sigma_{n,\gamma}$ of ¹⁴C(*n*, γ)¹⁵C measured directly, determined indirectly, and calculated theoretically. The first direct measurements in Ref. [4] provided $\sigma_{n,v} = 1.1 \pm$ $0.28 \mu b$ which is about 5 times smaller than the theoretical value of $5.1 \mu b$ predicted earlier in Ref. [5] within a potential model. The subsequent folding model calculations [6] and microscopic cluster model calculations [7] have confirmed the large value of Ref. [5]. Recently, the ¹⁴C(*n*, γ)¹⁵C cross sections have been determined indirectly in three dissociation experiments of ${}^{15}C$ [8–10]. In these works, $\sigma_{n,\gamma}$ (23.3 keV) has been obtained from the fit to the data at higher energies providing $2.6 \pm 0.9 \mu b$ [8], 4.4 \pm 0.6 μ b [9], and 4.1 \pm 0.4 μ b [10]. Last year, new direct measurements of $\sigma_{n,\gamma}$ have been reported in Ref. [11]. They suggest that $\sigma_{n,\gamma}(23.3 \text{ keV}) = 2.7 \pm 0.2 \text{ }\mu\text{b, which}$ is twice the value from the first direct measurements.

In this Letter, we propose to use charge symmetry between ¹⁵C($\frac{1}{2}$ ⁺) and its isobar analog ¹⁵F($\frac{1}{2}$ ⁺) as a strong and model-independent tool to discriminate between different determinations and predictions for the ${}^{14}C(n, \gamma) {}^{15}C$ cross sections.

Let us notice first that the main contribution to the ¹⁴C(*n*, γ)¹⁵C reaction rate comes from the direct *E*1 capture from the initial *p* wave to the relatively weakly bound $\frac{1}{2}$ ⁺ ground state of ¹⁵C. This capture occurs well outside the 24 C interior, which we demonstrate in Fig. 1 by plotting the integrand of the *E*1 amplitude $M_{n,\gamma}^{(E1)}$ for the (n, γ) reaction

$$
M_{n,\gamma}^{(E1)} \sim \int_0^\infty dr r^3 \varphi_{\rm sc}(r) I(r) \tag{1}
$$

as a function of the distance r between n and ¹⁴C. In

FIG. 1. Integrand for the *E*1 amplitude of the ¹⁴C(*n*, γ)¹⁵C reaction times $E^{-1/2}$ for various incident neutron energies *E*. $\varphi_{\rm sc}(r)$ and *I*(*r*) have been calculated using the potential model parameters from Ref. [5].

Eq. (1), $\varphi_{\rm sc}(r)$ is the neutron scattering wave function in the entrance channel and $I(r)$ is the radial part of the overlap integral $\langle {}^{14}C | {}^{15}C \rangle$. In this case, $M_{n,\gamma}^{(E1)}$ is mostly determined by the $I(r)$ tail that behaves as

$$
\sqrt{15}I(r) \approx C_n e^{-\kappa_n r}/r, \qquad r \to \infty.
$$
 (2)

Here C_n is the neutron asymptotic normalization coeffi-Here C_n is the neutron asymptotic normalization coefficient (ANC), $\kappa_n = \sqrt{2\mu \epsilon_n}/\hbar$, ϵ_n is the neutron separation energy in ¹⁵C and μ is the n + ¹⁴C reduced mass. The energy in \degree C and μ is the n + \degree C reduced mass. The factor $\sqrt{15}$ accounts for antisymmetrization. The (n, γ) cross sections are therefore determined by the ANC squared C_n^2 and all theoretical models using the same C_n^2 should provide approximately the same $\sigma_{n,\gamma}$.

In this Letter, we determine C_n^2 using a recently established relation between the neutron ANC of a bound state and the proton width Γ_p of its mirror analog resonance [12], which follows from the charge symmetry of onenucleon decay amplitudes. As shown in Ref. [12], the ratio

$$
\mathcal{R}_{\Gamma} = \Gamma_p / C_n^2,\tag{3}
$$

for narrow resonances can be approximated by a modelindependent analytical expression that contains the neutron separation energy, the energy E_R of the proton resonance, charge of the core, and the range of the strong interaction between the last neutron (or proton) and the core. However, this expression may not be accurate for the broad *s*-wave resonance ${}^{15}F(\frac{1}{2}^+)$. To predict \mathcal{R}_{Γ} more reliably in this case, more accurate model calculations should be performed. The only requirement for a model should be its ability to reproduce exactly the asymptotic behavior of the valence neutron in ¹⁵C given by Eq. (2) and its applicability to the elastic scattering calculations. The microscopic cluster model (MCM) of the type we used in [13] is well suited for such calculations. Previous study of some broad *s*-wave resonances within this model has shown that \mathcal{R}_{Γ} is not very sensitive to model assumptions even if C_n^2 and Γ_p strongly depend on them [13]. The theoretical uncertainty of \mathcal{R}_{Γ} is less than 10% [13]. A similar uncertainty in \mathcal{R}_{Γ} for the ¹⁵C-¹⁵F mirror pair would be sufficient to determine

 C_n^2 and, therefore, to predict $\sigma_{n,\gamma}$ accurately enough to reduce its uncertainty from the current factor of 5.

To calculate \mathcal{R}_{Γ} , we use the MCM from Ref. [14] where ¹⁵C (¹⁵F) is represented by the ¹⁴C + *n* (¹⁴O + *p*) configuration. The internal structure of ${}^{14}C$ (${}^{14}O$) is described by the 0*p* translation-invariant oscillator shell model. We performed both single-channel and multichannel calculations. In the latter case, we have taken into account the 0^+_2 , 1^+ , and $2^+_{1,2}$ core excitations. Each calculation has been performed with two values of the oscillator radius, 1.5 fm and 1.75 fm. We use effective nucleon-nucleon (NN) interactions well adapted for such calculations, the Volkov potential V2 [15] and the Minnesota (MN) potential [16]. The two-body spin-orbit force [17] with $S_0 = 30$ MeV fm⁵ and the Coulomb interaction are also included. Both V2 and MN have one adjustable parameter that gives the strength of the odd NN potentials V_{11} and V_{33} . We fit this parameter in each case to reproduce the experimental values for ϵ_n or E_R . Slightly different adjustable parameters in ¹⁵C and ¹⁵F, needed to reproduce ϵ_n and E_R , simulate charge symmetry breaking of the effective NN interactions.

First, we calculate \mathcal{R}_{Γ} assuming for E_R the value of 1.47 MeV obtained in Ref. [14] using an *R*-matrix analysis of the 14 O + p scattering measured in Ref. [18]. The resulting value of \mathcal{R}_{Γ} changes from 0.280 to 0.313 MeV \cdot fm with different model assumptions and NN potentials (see Table I). We adopt its average value $\mathcal{R}_{\Gamma} = 0.297 \pm$ 0.017 MeV · fm. Using the experimental value $\Gamma_p =$ 0*:*56 MeV from Ref. [14], we obtain from Eq. (3) for 15C the C_n^2 value equal to 1.89 \pm 0.11 fm⁻¹. Below, we refer to C_n^2 obtained using \mathcal{R}_{Γ} from the MCM calculations as C_{mir}^2 .

Often, a two-body potential model is used to predict the \langle ¹⁴C|¹⁵C) overlap. For the magnitude of its tail to be determined by C_{mir} , the single-particle wave function should be multiplied by a spectroscopic amplitude $S_{\text{mir}}^{1/2}$ = $C_{\text{mir}}/b_{\text{s.p.}}$, where $b_{\text{s.p.}}$ is the single-particle ANC obtained in such a model. Table II shows S_{mir} for a range of the Woods-Saxon potentials used in earlier work. S_{mir} from the first four lines agrees with the spectroscopic factors either determined or used in these works, *S*exp, within the error bars. The corresponding ANCs squared $C_{\text{exp}}^2 = S_{\text{exp}} b_{\text{sp}}^2$ also agree with C_{mir}^2 within the error bars. These C_{exp}^2 were used in the analysis of the ${}^{14}C(d, p) {}^{15}C$ reaction within the distorted wave Born approximation [19], direct (n, γ) calculations [5], time-dependent [20], and distorted

TABLE I. Ratio \mathcal{R}_{Γ} (in MeV · fm) calculated in the singlechannel and multichannel MCM with two different oscillator radii *b* and two different NN potentials.

	single-channel MCM		multichannel MCM		
		$b = 1.5$ fm $b = 1.75$ fm		$b = 1.5$ fm $b = 1.75$ fm	
V2	0.297	0.280	0.301	0.286	
MN	0.309	0.291	0.313	0.297	

TABLE II. The depth V_0 (in MeV), radius r_0 and diffuseness *a* (in fm) of the Woods-Saxon potentials, the single-particle ANC $b_{s,p}$ $(\text{in fm}^{-1/2})$, the spectroscopic factor S_{exp} for the works listed in the first column and the corresponding ANC squared $C_{\text{exp}}^2 = S_{\text{exp}} b_{\text{s.p.}}^2$ $(\text{in fm}^{-1/2})$. Also shown are the spectroscopic factor $S_{\text{mir}} = (C_{\text{mir}}/b_{\text{s.p.}})^2$, corresponding to $C_{\text{mir}}^2 = 1.89 \pm 0.11 \text{ fm}^{-1}$, the coefficients $S(0)$ (in 10²⁰ fm³ s⁻¹), s_1 (in MeV⁻¹) and s_2 (in MeV⁻²) in the Taylor expansion of $\sigma_{n,\gamma}$ [Eq. (4)] and the $\sigma_{n,\gamma}$ value at 23.3 keV (in μ b), calculated with the corresponding values of V_0 , r_0 , a , and S_{mir} .

Ref.	V_0	r_0	a	$b_{\rm s.p.}$	D_{exp}	C^2_{exp}	$S_{\rm mir}$	S(0)	S ₁	S_2	$\sigma_{n,v}$ (23.3 keV)
[5]	48.65	1.261	0.7	1.48	0.88	1.92	0.87 ± 0.05	11.4 ± 0.65	-0.843	0.540	5.35 ± 0.30
[19]	46.46	1.3	0.7	1.49	0.88	1.96	0.85 ± 0.05	11.3 ± 0.65	-0.846	0.541	5.33 ± 0.30
[20]	52.79	1.228	0.6	1.38	1.0	1.91	0.99 ± 0.06	11.3 ± 0.65	-0.872	0.607	5.32 ± 0.30
$\lceil 21 \rceil$	49.29	1.25	0.7	1.47	0.97 ± 0.08	2.10 ± 0.15	0.87 ± 0.07	11.3 ± 0.65	-0.842	0.539	5.32 ± 0.30
[21]	44.29	1.25	0.7	1.47	0.73 ± 0.05	1.58 ± 0.11	0.87 ± 0.07	11.3 ± 0.65	-0.842	0.539	5.32 ± 0.30
$\lceil 21 \rceil$	61.17	1.15	0.5	1.28	0.92 ± 0.07	1.50 ± 0.08	1.16 ± 0.06	11.3 ± 0.65	-0.882	0.637	5.32 ± 0.30
[22]	55.36	1.223	0.5	1.30	0.90	1.53	1.11 ± 0.07	11.2 ± 0.65	-0.894	0.652	5.28 ± 0.30
[18]	54.15	1.17	0.71	1.45			0.90 ± 0.05	11.4 ± 0.65	-0.834	0.530	5.36 ± 0.30

wave [21] analysis of the ¹⁵C breakup. The C_{exp}^2 and S_{exp} values from the next three lines, obtained in the plane-wave analysis of the Coulomb breakup [21] and from knockout [22], are smaller than C_{mir}^2 and S_{mir} by \sim 25%.

This discrepancy may originate due to either insufficient understanding of one-nucleon removal reactions, or to underestimating the \mathcal{R}_{Γ} . According to Ref. [13], \mathcal{R}_{Γ} can have large uncertainties either in components with small spectroscopic factors, or in the presence of strong core excitations. In ${}^{15}C$, the core excitations are not significant and the ${}^{14}C_{g,s}$ + *n* configuration dominates. Thus, there is no room for increasing \mathcal{R}_{Γ} by 25% unless we have fitted the theoretical position of the resonance at a wrong energy. To verify this, we repeat the MCM calculations using different values of E_R and Γ_p from the literature, as given in Table III. The predicted \mathcal{R}_{Γ} and C_{mir}^2 are shown in Table III. In general, the new C_{mir}^2 are larger than the one obtained with $E_R = 1.47$ MeV and $\Gamma_p = 0.56$ MeV. They may agree with C_{exp}^2 derived from the plane-wave analysis of the Coulomb breakup [21] and from neutron knockout [22] only if the largest values of E_R combined with the lowest Γ_p values from the intervals given in Refs. [24,26] are assumed.

Large C_{mir}^2 , obtained for E_R and Γ_p from Refs. [18,23– 27], give large spectroscopic factors $S_{\text{mir}} = (C_{\text{mir}}/b_{\text{s.p.}})^2$

(see Table III), which in most cases are larger than the prediction of $(15/14)^2 \approx 1.15$ from the simplest version of the translation-invariant shell model. This value follows from the Pauli principle applied to 15 nucleons occupying the lowest shell model states. Any other occupancy of energy levels decreases the spectroscopic factor. Therefore, the inequality $S_{\text{mir}} \leq 1.15$ can serve as a tool for identifying physically meaningful values of E_R and Γ_p . From this point of view, E_R and Γ_p from Ref. [25] can be discarded. The same concerns the values $E_R = 1.29$ MeV and $\Gamma_p = 0.7$ MeV from Ref. [18]. However, other intervals for E_R and Γ_p from Table III can be narrowed down to satisfy the $S_{\text{mir}} \leq 1.15$ condition. The values $E_R =$ 1.47 MeV and $\Gamma_p = 0.56$ MeV give the most reasonable range for S_{mir} . Therefore, we use the $C_{\text{mir}}^2 = 1.89 \pm$ 0.11 fm^{-1} value obtained with them to predict the ¹⁴C(*n*, γ)¹⁵C cross sections.

To calculate $\sigma_{n,\gamma}$, we use the new representation of the low-energy (n, γ) cross sections introduced in Ref. [28]. For *E*1 capture from a *p* wave it reads

$$
\sigma_{n,\gamma}(E) \approx \frac{\mu\sqrt{2\mu E}}{\hbar^2} S(0)(1 + s_1E + s_2E^2). \tag{4}
$$

In Eq. (4) the coefficient $S(0)$ is the analog of the astro-

TABLE III. The energy E_R and the width Γ_p of the ¹⁵ $F(\frac{1}{2}^+)$ resonance (in MeV) from the references in the first column, the MCM value of \mathcal{R}_{Γ} corresponding to E_R , the neutron ANC squared C_{mir}^2 in ¹⁵C (in fm^{-1/2}) and the spectroscopic factor $S_{\text{mir}} = (C_{\text{mir}}/b_{\text{sp.}})^2$ compatible with this ANC. S_{mir} has been calculated using all the $b_{\text{s.p.}}$ values from Table II.

Ref.	E_R		\mathcal{R}_{Γ}	$C_{\rm mir}^2$	$S_{\rm mir}$
$[23]$	1.6 ± 0.2	≥ 0.9	0.352 ± 0.111	≥ 1.94	≥ 0.87
$[24]$	1.37 ± 0.18	0.8 ± 0.3	0.250 ± 0.089	$3.20^{+3.59}_{-1.73}$	2.41 ± 1.75
$[25]$	1.51 ± 0.11	1.2	0.307 ± 0.067	4.10 ± 0.88	2.25 ± 0.81
$[26]$	1.41 ± 0.15	0.8 ± 0.3	0.260 ± 0.073	$3.08^{+2.83}_{-1.57}$	2.15 ± 1.48
$[18]$	$1.45_{-0.10}^{+0.16}$	0.7	0.295 ± 0.073	$2.37^{+0.78}_{-0.47}$	1.39 ± 0.54
$[18]$	$1.29_{-0.06}^{+0.08}$	0.7	0.212 ± 0.036	$3.30^{+0.70}_{-0.48}$	1.86 ± 0.60
$[14]$	1.47	0.56	0.297 ± 0.017	1.89 ± 0.11	1.01 ± 0.21
$[27]$	1.23 ± 0.05	0.67 ± 0.17	0.194 ± 0.029	$3.45^{+1.64}_{-1.22}$	2.06 ± 1.06

FIG. 2. Experimental (data points) and theoretical values of $\sigma_{n,\gamma}E^{-1/2}$. The dark shadowed area corresponds to $\sigma_{n,\gamma}$ derived from mirror symmetry assuming E_R and Γ_p from Ref. [14] while the light one corresponds to all other E_R and Γ_p consistent with $S_{\text{mir}} \leq 1.15$. The dot-dashed curve represents the MCM calculations from [7].

physical *S* factor for neutrons and is given by an integral (1) that contains the zero energy limit of $\varphi_{\rm sc}(r)$. Two other coefficients, s_1 and s_2 , contain first and second energy derivatives of $\varphi_{\rm sc}(r)$ at $E = 0$. The latter is calculated within a potential model using the same real central potential both in the entrance and exit channels. According to our calculations, different potential choices in these channels change $\sigma_{n,v}$ by only 1%. Absorption from the entrance channel is neglected because, according to our estimation within a coupled-channel model, they change $\sigma_{n,\gamma}$ at the astrophysical energies by no more than 0.5%.

The numerical values of $S(0)$, s_1 and s_2 are given in Table II, calculated with the parameters V_0 , r_0 , a, and S_{mir} from the same table. The main contribution to $S(0)$ comes from large *r* and it is almost entirely determined by C_n^2 . With fixed C_n^2 , the residual uncertainty in $S(0)$ due to different geometries of the potential well is only 1%. The other coefficients, s_1 and s_2 , are more sensitive to the potential choice: 3% and 10%, respectively. The resulting value of $\sigma_{n,\gamma}$ (23.3 keV) is 5.3 \pm 0.3 μ b, which is consistent with the first theoretical potential model calculations from Ref. [5].

Figure 2 shows $\sigma_{n,\gamma}E^{-1/2}$ derived from mirror symmetry by the dark shadowed area. The light shadowed area corresponds to calculations with all other E_R and Γ_p consistent with the condition $S_{\text{mir}} \leq 1.15$. Our $\sigma_{n,\gamma}$ are smaller than the previous MCM results of Ref. [7]. This is explained by the overestimation of C_n^2 in the MCM with the V2 forces, which is known for other nuclei. Our predictions agree with indirect determinations from Refs. [9,10] but they do not leave any room for small $\sigma_{n,\gamma}$. Reciprocally, small $\sigma_{n,\gamma}$ from Refs. [4,8,11] would correspond to smaller C_n^2 and, therefore, a smaller width of ¹⁵F($\frac{1}{2}$ ⁺), $\Gamma_p \sim$ 280 keV provided $E_R = 1.47$ MeV. The narrower width would make the experimental determination of E_R and Γ_p much easier and would have not caused the currently existing spread in their values.

In summary, the charge symmetry of the ${}^{15}C \rightarrow {}^{14}C + n$ and ¹⁵F \rightarrow ¹⁴O + *p* decays offers a strong test for the direct $E1^{14}C(n, \gamma)^{15}C$ cross sections. It significantly reduces the uncertainty in the current knowledge of the ${}^{14}C(n, \gamma) {}^{15}C$ cross sections and favors the earlier theoretical predictions for this reaction from Ref. [5]. It also shows that directly and some indirectly measured cross sections in [4,8,11] strongly contradict charge symmetry in the ¹⁵C-¹⁵F mirror pair. This contradiction deserves thorough attention because it brings into question the determination of the astrophysically important (n, γ) cross sections for shortlived radioactive targets.

N. K. T. thanks T. Nakamura for communicating the $\sigma_{n,\gamma}$ (23.3 keV) value and T. Aumann for useful discussions. She also gratefully acknowledges support from the UK EPSRC via Grant No. GR/T28577.

- [1] T. Kajino, G. J. Matthews, and G. M. Fuller, Astrophys. J. **364**, 7 (1990).
- [2] M. Wiescher, J. Görres, and H. Schatz, J. Phys. G 25, R133 (1999).
- [3] T. Sasaqui *et al.*, Astrophys. J. **634**, 1173 (2005).
- [4] H. Beer *et al.*, Astrophys. J. **387**, 258 (1992).
- [5] M. Wiescher, J. Görres, and F. K. Thielemann, Astrophys. J. **363**, 340 (1990).
- [6] H. Herndl *et al.*, Phys. Rev. C **60**, 064614 (1999).
- [7] P. Descouvemont, Nucl. Phys. **A675**, 559 (2000).
- [8] A´ . Horva´th *et al.*, Astrophys. J. **570**, 926 (2002).
- [9] U. Datta Pramanik and (LAND-CB-FRS-Collaboration), Prog. Theor. Phys. Suppl. **146**, 427 (2002).
- [10] T. Nakamura *et al.*, Nucl. Phys. **A722**, C301 (2003); T. Nakamura (private communication).
- [11] R. Reifarth *et al.*, Nucl. Phys. **A758**, 787c (2005).
- [12] N.K. Timofeyuk, R.C. Johnson, and A.M. Mukhamedzhanov, Phys. Rev. Lett. **91**, 232501 (2003).
- [13] N. K. Timofeyuk and P. Descouvemont, Phys. Rev. C **72**, 064324 (2005).
- [14] D. Baye, P. Descouvemont, and F. Leo, Phys. Rev. C **72**, 024309 (2005).
- [15] A. B. Volkov, Nucl. Phys. **74**, 33 (1965).
- [16] D. R. Thompson, M. LeMere, and Y. C. Tang, Nucl. Phys. **A286**, 53 (1977).
- [17] D. Baye and N. Pecher, Bull. Cl. Sci., Acad. R. Belg. **67**, 835 (1981).
- [18] V. Z. Goldberg *et al.*, Phys. Rev. C **69**, 031302(R) (2004).
- [19] J. D. Goss *et al.*, Phys. Rev. C **12**, 1730 (1975).
- [20] P. Capel, D. Baye, and V. S. Melezhik, Phys. Rev. C **68**, 014612 (2003).
- [21] U. D. Pramanik *et al.*, Phys. Lett. **551B**, 63 (2003).
- [22] J. R. Terry *et al.*, Phys. Rev. C **69**, 054306 (2004).
- [23] W. Benenson *et al.*, Phys. Rev. C **17**, 1939 (1978).
- [24] G. J. KeKelis *et al.*, Phys. Rev. C **17**, 1929 (1978).
- [25] W. A. Peters *et al.*, Phys. Rev. C **68**, 034607 (2003).
- [26] A. Lepine-Szily *et al.*, Nucl. Phys. **A722**, C512 (2003).
- [27] F. Q. Guo *et al.*, Phys. Rev. C **72**, 034312 (2005).
- [28] D. Baye, Phys. Rev. C **70**, 015801 (2004).