

Meson Supercurrent State in High-Density QCD

T. Schäfer

Department of Physics, North Carolina State University, Raleigh, North Carolina 27695, USA
(Received 31 August 2005; published 12 January 2006)

The ground state of three flavor quark matter at asymptotically large density is believed to be the color-flavor-locked (CFL) phase. At nonasymptotic density the effect of the nonzero strange quark mass cannot be neglected. If the strange quark mass exceeds $m_s \sim m_u^{1/3} \Delta^{2/3}$, the CFL state becomes unstable toward the formation of a neutral kaon condensate. Recently, several authors discovered that for $m_s \sim (2\Delta p_F)^{1/2}$ the CFL state contains gapless fermions, and that the gapless modes lead to an instability in current-current correlation functions. Using an effective theory of the CFL state, we demonstrate that this instability can be resolved by the formation of a meson supercurrent, analogous to Migdal's p -wave pion condensate. This state has a nonzero meson current that is canceled by a backflow of gapless fermions.

DOI: 10.1103/PhysRevLett.96.012305

PACS numbers: 12.38.Mh

Calculations based on weak coupling QCD show that the ground state of three flavor QCD at very high baryon density is the color-flavor-locked (CFL) phase [1–3]. During the past several years, a lot of effort has been devoted to the question of how the CFL state is modified in the presence of a nonzero strange quark mass. Using a BCS-type gap equation, it is easy to see that the most important parameter is $m_s^2/(p_F \Delta)$, where p_F is the Fermi momentum and Δ is the gap in the chiral limit [4].

Using effective field theory methods we showed that the CFL state is not modified if $m_s < m_s^{\text{crit}} \sim m_u^{1/3} \Delta^{2/3}$. At $m_s(\text{crit})$ the CFL phase undergoes a phase transition to a kaon condensed phase [5]. This transition is shifted to larger values of m_s if instanton effects are important, as is the case at moderate density [6]. For $m_s^2/(2p_F) \sim 2\Delta$ the effective field theory description breaks down, and we expect a phase transition to a less symmetric phase to occur. More recently, several groups observed that gapless fermion modes can appear in the spectrum of the CFL phase in the vicinity of the point $m_s^2/(2p_F) \sim \Delta$ [7,8]. Gapless modes also appear in the kaon condensed CFL phase, but the critical strange quark mass is shifted to somewhat larger values [9].

The problem is that gapless fermion modes in a weakly coupled (BCS) superfluid tend to cause instabilities in current-current correlation functions. These instabilities are quite generic and appear in a wide range of systems, including the 2SC phase, the CFL phase, and cold atomic gases [10–12]. The presence of an instability implies that the homogeneous superfluid is not the correct ground state [13–15]. One possibility is that the true ground state is an inhomogeneous superconductor of the type first considered by Larkin, Ovchinnikov, Fulde, and Ferrell (LOFF) [16] and generalized to QCD in [15,17]. In this work we study the possibility that the ground state has a nonzero meson current similar to the p -wave meson condensate suggested by Migdal, Sawyer, and Scalapino [18]. For this purpose we study the stability of the s -wave kaon condensate with

respect to the formation of a nonzero current. Our study is analogous to the calculations performed in chiral models of nuclear matter [19] and in effective theories of cold atoms [20].

Our starting point is the effective theory of the CFL phase derived in [9,21]

$$\begin{aligned} \mathcal{L} = & \frac{f_\pi^2}{4} \text{Tr}(\nabla_0 \Sigma \nabla_0 \Sigma^\dagger - v_\pi^2 \vec{\nabla} \Sigma \vec{\nabla} \Sigma) + a_3 [(\text{Tr}[M \Sigma])^2 \\ & - \text{Tr}[M \Sigma M \Sigma] + \text{H.c.}] + \text{Tr}(N^\dagger i v^\mu D_\mu N) \\ & - D \text{Tr}(N^\dagger v^\mu \gamma_5 \{\mathcal{A}_\mu, N\}) - F \text{Tr}(N^\dagger v^\mu \gamma_5 [\mathcal{A}_\mu, N]) \\ & + \frac{\Delta}{2} \{[\text{Tr}(NN) - [\text{Tr}(N)]^2] + \text{H.c.}\}. \end{aligned} \quad (1)$$

The effective Lagrangian contains Goldstone boson fields Σ and baryon fields N . The meson fields arise from chiral symmetry breaking in the CFL phase [1] and the baryon fields originate from quark-hadron complementarity [22]. The chiral field is given by $\Sigma = \exp(i\phi^a \lambda^a / f_\pi)$ where f_π is the pion decay constant. M is the quark mass matrix. The chiral field and the mass matrix transform as $\Sigma \rightarrow L \Sigma R^\dagger$ and $M \rightarrow L M R^\dagger$ under chiral transformations $(L, R) \in \text{SU}(3)_L \times \text{SU}(3)_R$. The baryon field N transforms according to the adjoint representation of flavor $\text{SU}(3)$. We expand N in terms of the baryon nonet $(p, n, \Sigma^\pm, \Xi^\pm, \Xi^0, \Lambda^{8,0})$. $v^\mu = (1, \vec{v})$ is the Fermi velocity, and Δ is the superfluid gap. We have suppressed the singlet fields associated with the breaking of the exact $\text{U}(1)_V$ and approximate $\text{U}(1)_A$ symmetries.

The covariant derivative of the nucleon field is given by $D_\mu N = \partial_\mu N + i[\mathcal{V}_\mu, N]$. The vector and axial vector currents are

$$\begin{aligned} \mathcal{V}_\mu &= -\frac{i}{2} \{\xi \partial_\mu \xi^\dagger + \xi^\dagger \partial_\mu \xi\}, \\ \mathcal{A}_\mu &= -\frac{i}{2} \xi (\partial_\mu \Sigma^\dagger) \xi, \end{aligned} \quad (2)$$

where ξ is defined by $\xi^2 = \Sigma$. It follows that ξ transforms as $\xi \rightarrow L\xi U(x)^\dagger = U(x)\xi R^\dagger$ with $U(x) \in \text{SU}(3)_V$.

Symmetry arguments can be used to determine the leading mass terms in the effective Lagrangian. Bedaque and Schäfer observed that $X_L = MM^\dagger/(2p_F)$ and $X_R = M^\dagger M/(2p_F)$ enter the microscopic theory like the temporal components of left and right handed flavor gauge fields. We can make the effective Lagrangian invariant under this symmetry by introducing the covariant derivatives

$$D_0 N = \partial_0 N + i[\Gamma_0, N], \quad (3)$$

$$\nabla_0 \Sigma = \partial_0 \Sigma + iX_L \Sigma - i\Sigma X_R \quad (4)$$

with $\Gamma_0 = -\frac{i}{2}\{\xi(\partial_0 + iX_R)\xi^\dagger + \xi^\dagger(\partial_0 + iX_L)\xi\}$. If the density is very large and the QCD coupling is weak, then the low energy constants can be calculated in perturbation theory. The leading terms in the meson and baryon sector were calculated in [9,23]. The results are

$$f_\pi^2 = \frac{21 - 8 \log(2)}{18} \left(\frac{p_F^2}{2\pi^2} \right), \quad v_\pi^2 = \frac{1}{3}, \quad a_3 = \frac{3\Delta^2}{4\pi^2}, \quad (5)$$

and $D = F = 1/2$. The gap Δ can also be computed in perturbative QCD, but we will not make use of these results and treat Δ as a parameter.

The parameter that controls the effect of the strange quark mass is the effective chemical potential $\mu_s = m_s^2/(2p_F)$. When μ_s exceeds the mass of the kaon, the CFL ground state becomes unstable and a Bose condensate of kaons is formed. If isospin was an exact symmetry, the energy of the K^+ and K^0 mesons would be degenerate. Because of explicit isospin breaking, and because of the constraint of electric charge neutrality, a condensate of neutral kaons is favored. The K^0 condensed phase is characterized by

$$\xi_{K^0} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos(\alpha/2) & i \sin(\alpha/2) \\ 0 & i \sin(\alpha/2) & \cos(\alpha/2) \end{pmatrix}, \quad (6)$$

with $\cos(\alpha) = m_K^2/\mu_s^2$. From Eq. (5) we get $m_K^2 = 3m_u(m_d + m_s)\Delta^2/(\pi^2 f_\pi^2)$. For typical values of the parameters $\cos(\alpha) \sim (m_u/m_s)(\Delta/f_\pi)^2 \ll 1$. In the following we assume that $\cos(\alpha) = 0$ and the ground state is a maximal kaon condensate.

Properties of the kaon condensed state were studied in [5,9]. We showed, in particular, that the kaon condensed CFL phase has a gapless fermion mode that appears at $\mu_s = 4\Delta/3$. For comparison, in the ordinary CFL phase gapless modes appear at $\mu_s = \Delta$ [7]. Recently, several groups have shown that gapless fermion modes lead to instabilities in the current-current correlation function [11,12]. Motivated by these results, we examine the stability of the kaon condensed phase against the formation of a nonzero current.

Consider a spatially varying $U(1)_Y$ rotation of the maximal kaon condensate

$$U(x)\xi_{K^0}U^\dagger(x) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1/\sqrt{2} & ie^{i\phi_K(x)}/\sqrt{2} \\ 0 & ie^{-i\phi_K(x)}/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}. \quad (7)$$

This state is characterized by nonzero currents

$$\vec{V} = \frac{1}{2}(\vec{\nabla}\phi_K) \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}, \quad (8)$$

$$\vec{A} = \frac{1}{2}(\vec{\nabla}\phi_K) \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -ie^{i\phi_K} \\ 0 & ie^{-i\phi_K} & 0 \end{pmatrix}. \quad (9)$$

In the following we compute the vacuum energy as a function of the kaon current $\vec{j}_K = \vec{\nabla}\phi_K$. The meson part of the effective Lagrangian gives a positive contribution

$$\mathcal{E} = \frac{1}{2}v_\pi^2 f_\pi^2 \vec{j}_K^2. \quad (10)$$

A negative contribution can arise from gapless fermions. In order to determine this contribution, we have to calculate the fermion spectrum in the presence of a nonzero current. The relevant part of the effective Lagrangian is

$$\mathcal{L} = \text{Tr}(N^\dagger i v^\mu D_\mu N) + \text{Tr}(N^\dagger \gamma_5 (\rho_A + \vec{v} \cdot \vec{A}) N) + \frac{\Delta}{2} \{ \text{Tr}(NN) - \text{Tr}(N)\text{Tr}(N) + \text{H.c.} \}, \quad (11)$$

where we have used $D = F = 1/2$. The covariant derivative is $D_0 N = \partial_0 N + i[\rho_V, N]$ and $D_i N = \partial_i N + i\vec{v} \cdot [\vec{V}, N]$ with \vec{V}, \vec{A} given in Eq. (8) and

$$\rho_{V,A} = \frac{1}{2} \left\{ \xi \frac{M^\dagger M}{2p_F} \xi^\dagger \pm \xi^\dagger \frac{M M^\dagger}{2p_F} \xi \right\}. \quad (12)$$

The vector potential ρ_V and the vector current \vec{V} are diagonal in flavor space while the vector potential ρ_A and the axial current \vec{A} lead to mixing. In order to exhibit the mechanism for the instability, we first discuss the simple case of vanishing axial vector couplings $F = D = 0$. We then study the realistic case $D = F = 1/2$.

We can determine the spectrum by decomposing ρ_V and \vec{V} into isospin and hypercharge components. We find

$$\rho_V = -\frac{\mu_s}{2} \hat{I}_3 - \frac{\mu_s}{4} \hat{Y}, \quad \vec{V} = -\frac{\vec{j}_K}{2} \hat{I}_3 + \frac{3\vec{j}_K}{4} \hat{Y}, \quad (13)$$

where $\hat{I}_3 = \lambda_3/2$ and $\hat{Y} = \lambda_8/\sqrt{3}$ are the isospin and hypercharge generators. The dispersion relations can now be obtained from the (I_3, Y) quantum numbers of the baryon nonet. The result is

$$\begin{aligned}\omega_{n,\Xi^0} &= \sqrt{\Delta^2 + l^2} \pm \vec{v} \cdot \vec{J}_K, \\ \omega_{\Sigma^+, \Sigma^-} &= \sqrt{\Delta^2 + l^2} \pm \frac{1}{2}(\mu_s + \vec{v} \cdot \vec{J}_K), \\ \omega_{p, \Xi^-} &= \sqrt{\Delta^2 + l^2} \pm \frac{1}{2}(\mu_s - \vec{v} \cdot \vec{J}_K),\end{aligned}\quad (14)$$

where $l = \vec{v} \cdot \vec{p} - p_F$ is the residual momentum. The neutral modes ($\Sigma_0, \Lambda_0, \Lambda_8$) are not affected by the current or the vector potential. Equation (14) shows that there are gapless fermion modes as μ_s approaches 2Δ , and that gapless modes occur earlier if there is a nonzero current. The contribution to the vacuum energy from gapless modes is

$$\mathcal{E} = 4 \frac{\mu^2}{2\pi^2} \int dl \int \frac{d\Omega}{4\pi} \omega_l \theta(-\omega_l), \quad (15)$$

where the factor 4 is a degeneracy factor and $d\Omega$ is an integral over the Fermi surface. Near the Fermi surface we can approximate

$$\omega_l = \Delta + \frac{l^2}{2\Delta} - \frac{1}{2}(\mu_s + \vec{v} \cdot \vec{J}_K). \quad (16)$$

The integral in Eq. (15) receives contributions from one of the pole caps on the Fermi surface. The result has exactly the same structure as the energy functional of a nonrelativistic two-component Fermi liquid with nonzero polarization, which was recently analyzed by Son and Stephanov [20]. Introducing dimensionless variables

$$x = \frac{J_K}{a\Delta}, \quad h = \frac{\mu_s - 2\Delta}{a\Delta}, \quad (17)$$

we can write $\mathcal{E} = c \mathcal{N} f_h(x)$ with

$$f_h(x) = x^2 - \frac{1}{x} [(h+x)^{5/2} \Theta(h+x) - (h-x)^{5/2} \Theta(h-x)]. \quad (18)$$

We have defined the constants

$$c = \frac{8^4}{2 \times 15^4 c_\pi^3 v_\pi^6}, \quad \mathcal{N} = \frac{\mu^2 \Delta^2}{\pi^2}, \quad a = \frac{8^2}{15^2 c_\pi^2 v_\pi^4}, \quad (19)$$

where $c_\pi = [21 - 8 \log(2)]/36$ is the numerical coefficient that appears in the weak coupling result for f_π . According to the analysis in [20], the function $f_h(x)$ develops a nontrivial minimum if $h_1 < h < h_2$ with $h_1 \simeq -0.067$ and $h_2 \simeq 0.502$. In perturbation theory we find $a = 13.9$ and the kaon condensed ground state becomes unstable for $(\Delta - \mu_s/2) < 0.46\Delta$.

We see that the instability is weaker if the axial coupling is taken into account. The axial vector potential and the axial vector current can be written as

$$\rho_A + \vec{v} \cdot \vec{\mathcal{A}} = \frac{i}{2}(\mu_s + \vec{v} \cdot \vec{J}_K)(e^{i\phi_K} \hat{u}^+ - e^{-i\phi_K} \hat{u}^-), \quad (20)$$

where $\hat{u}^\pm = (\lambda_6 \pm i\lambda_7)/2$ are the u -spin raising and lowering operators. The axial vector coupling leads to mixing among the charged (p, Ξ^-, Σ^\pm) and neutral ($n, \Xi^0, \Sigma^0, \Lambda^{0,8}$) baryons. Gapless fermions occur in the charged sector. The mixing in the charged sector is

$$\mathcal{L} = \frac{i}{2}(\mu_s + \vec{v} \cdot \vec{J}_K)\{e^{i\phi_K}(\Xi \Sigma^-) - e^{-i\phi_K}(\bar{\Sigma} \Xi^-)\}. \quad (21)$$

The dispersion relation of the lowest mode is given by

$$\omega_l = \Delta + \frac{(l - l_0)^2}{2\Delta} - \frac{3}{4}\mu_s - \frac{1}{4}\vec{v} \cdot \vec{J}_K, \quad (22)$$

where $l_0 = (\mu_s + \vec{v} \cdot \vec{J}_K)/4$. The calculation of the energy density is completely analogous to the one we performed in the previous section. The only differences are that the number of gapless modes is reduced and that the effect of the current on the energy of the fermion is smaller. The energy functional is $\mathcal{E} = c \mathcal{N} f_h(x)$ with x defined in Eq. (19) and $h = (3\mu_s - 4\Delta)/(a\Delta)$. The numerical coefficients are $c = 2/(15^4 c_\pi^3 v_\pi^6)$ and $a = 2/(15^2 c_\pi^2 v_\pi^4)$.

Using the weak coupling values for v_π and c_π , we find $a = 0.43$, and the kaon condensed ground state becomes unstable for $(\Delta - 3\mu_s/4) < 0.007\Delta$. In Fig. 1 we show the energy density as a function of the current J_K for several values of μ_s near the transition. We note that the mechanism for the instability is quite robust, but the value of the onset chemical potential depends sensitively on the values of the low energy constants. We also note that the homogeneous gapless kaon condensed phase becomes stable at even larger values of the effective chemical potential, $(\Delta - 3\mu_s/4) < -0.05$. This result may not be reliable, however, because the contribution from higher fermion modes has to be included.

We note that the ground state has no net current. This is clear from the fact that the ground state satisfies $\delta\mathcal{E}/\delta(\vec{\nabla}\phi_K) = 0$. As a consequence, the meson current is canceled by an equal but opposite contribution from gapless fermions. This is analogous to what happens in a p -wave pion condensate in nuclear matter [18,19,24] or in the LOFF phase [17]. We also expect that the ground state has no chromomagnetic instabilities. The effective Lagrangian given in Eq. (1) is formulated in terms of gauge

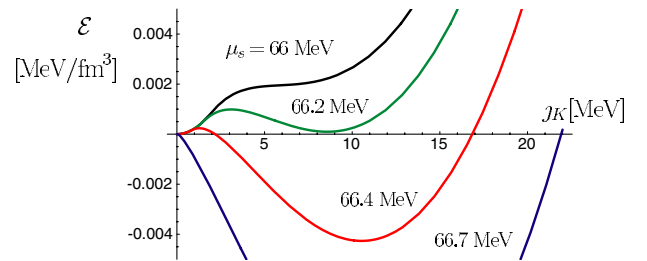


FIG. 1 (color online). Energy density as a function of the current J_K for several different values of $\mu_s = m_s^2/(2p_F)$ close to the phase transition.

invariant fields. Quark-hadron continuity implies that we should study the screening length of a $SU(3)_F$ gauge field. For diagonal gauge fields we find

$$m_V^2 = \left. \frac{\partial^2 \mathcal{E}}{\partial J_K^2} \right|_{JK=0} = v_\pi^2 f_\pi^2 \left(1 - \frac{5}{8\sqrt{h}} \theta(h) \right), \quad (23)$$

which shows the magnetic instability for $h > 0$ and has the characteristic square root singularity observed in microscopic calculations [11]. In this work we have calculated the energy functional for arbitrary values of JK , not just the second derivative at the origin. We find that the phase transition to a supercurrent state is first order and that the instability sets in for $h > h_c$ with $h_c < 0$. We also observe that the second derivative at the new minimum is positive and of the same order of magnitude as the screening mass at $h = 0$.

In summary, we have shown that for $\mu_s \sim 4\Delta/3$, which is the threshold for the appearance of gapless fermion modes, the CFL phase becomes unstable toward the formation of a meson supercurrent. This state is analogous to the p -wave pion condensate studied in low density nuclear matter. In that context the name p wave was motivated by the fact that the interaction that leads to the formation of a condensate is the $v \cdot D$ interaction between nucleons and pions that also determines the p -wave πN scattering amplitude. This is also true in our case. Supercurrent formation is driven by a $v \cdot D$ interaction between baryons and mesons.

Our result suggests that the series of phases encountered in three flavor QCD as the density is lowered starting from an asymptotically large value consists of the CFL phase, an s -wave kaon condensate, and a p -wave kaon condensate. There are many questions that remain to be addressed. In this work we established the presence of an instability but did not determine the exact nature of the new ground state. We have to consider additional currents, the role of other light fermions, and the effects of electric charge neutrality. Once the currents become large the effective field theory description breaks down and more microscopic approaches along the lines of [25,26] are necessary. These methods might also be useful in order to determine the fate of the meson supercurrent state as the density is lowered even further and μ_s approaches 2Δ . One possibility is that the supercurrent phase evolves into a LOFF-type state.

I thank A. Kryjevski for showing me a draft version of his closely related work [27]. This work is supported in part by the U.S. DOE Grant No. DE-FG-88ER40388.

- [1] M. Alford, K. Rajagopal, and F. Wilczek, Nucl. Phys. **B537**, 443 (1999).
[2] T. Schäfer, Nucl. Phys. **B575**, 269 (2000).

- [3] N. Evans, J. Hormuzdiar, S.D. Hsu, and M. Schwetz, Nucl. Phys. **B581**, 391 (2000).
[4] M. Alford, J. Berges, and K. Rajagopal, Nucl. Phys. **B558**, 219 (1999); T. Schäfer and F. Wilczek, Phys. Rev. D **60**, 074014 (1999); P. Bedaque, Nucl. Phys. **A697**, 569 (2002); A. W. Steiner, S. Reddy, and M. Prakash, Phys. Rev. D **66**, 094007 (2002); M. Alford and K. Rajagopal, J. High Energy Phys. **06** (2002) 031; F. Neumann, M. Buballa, and M. Oertel, Nucl. Phys. **A714**, 481 (2003).
[5] P.F. Bedaque and T. Schäfer, Nucl. Phys. **A697**, 802 (2002); D.B. Kaplan and S. Reddy, Phys. Rev. D **65**, 054042 (2002); A. Kryjevski, D.B. Kaplan, and T. Schäfer, Phys. Rev. D **71**, 034004 (2005).
[6] T. Schäfer, Phys. Rev. D **65**, 094033 (2002); C. Manuel and M.H.G. Tytgat, Phys. Lett. B **479**, 190 (2000).
[7] M. Alford, C. Kouvaris, and K. Rajagopal, Phys. Rev. Lett. **92**, 222001 (2004); M. Alford, C. Kouvaris, and K. Rajagopal, Phys. Rev. D **71**, 054009 (2005).
[8] S.B. Ruster, I.A. Shovkovy, and D.H. Rischke, Nucl. Phys. **A743**, 127 (2004).
[9] A. Kryjevski and T. Schäfer, Phys. Lett. B **606**, 52 (2005); A. Kryjevski and D. Yamada, Phys. Rev. D **71**, 014011 (2005).
[10] S.-T. Wu and S. Yip, Phys. Rev. A **67**, 053603 (2003).
[11] M. Huang and I.A. Shovkovy, Phys. Rev. D **70**, 051501 (2004).
[12] R. Casalbuoni, R. Gatto, M. Mannarelli, G. Nardulli, and M. Ruggieri, Phys. Lett. B **605**, 362 (2005); M. Alford and Q.H. Wang, J. Phys. G **31**, 719 (2005); K. Fukushima, Phys. Rev. D **72**, 074002 (2005); D.K. Hong, hep-ph/0506097.
[13] S. Reddy and G. Rupak, Phys. Rev. C **71**, 025201 (2005).
[14] I. Giannakis and H. C. Ren, Phys. Lett. B **611**, 137 (2005).
[15] R. Casalbuoni, R. Gatto, N. Ippolito, G. Nardulli, and M. Ruggieri, Phys. Lett. B **627**, 89 (2005).
[16] A.I. Larkin and Yu.N. Ovchinnikov, Sov. Phys. JETP **20**, 762 (1965); P. Fulde and A. Ferrell, Phys. Rev. **135**, A550 (1964).
[17] M. G. Alford, J. A. Bowers, and K. Rajagopal, Phys. Rev. D **63**, 074016 (2001); J.A. Bowers and K. Rajagopal, Phys. Rev. D **66**, 065002 (2002).
[18] A.B. Migdal, Sov. Phys. JETP **34**, 1184 (1972); R.F. Sawyer, Phys. Rev. Lett. **29**, 382 (1972); D.J. Scalapino, Phys. Rev. Lett. **29**, 386 (1972).
[19] G. Baym and D.K. Campbell, in *Mesons in Nuclei*, edited by M. Rho and D. Wilkinson (North-Holland, Amsterdam, 1979).
[20] D. T. Son and M. A. Stephanov, cond-mat/0507586.
[21] R. Casalbuoni and D. Gatto, Phys. Lett. B **464**, 111 (1999).
[22] T. Schäfer and F. Wilczek, Phys. Rev. Lett. **82**, 3956 (1999).
[23] D. T. Son and M. Stephanov, Phys. Rev. D **61**, 074012 (2000).
[24] G. Baym, Phys. Rev. Lett. **30**, 1340 (1973).
[25] M. Buballa, Phys. Lett. B **609**, 57 (2005).
[26] M. M. Forbes, Phys. Rev. D **72**, 094032 (2005).
[27] A. Kryjevski, hep-ph/0508180.