## Spin-Orbit Coupling and Anisotropy of Spin Splitting in Quantum Dots

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In lateral quantum dots, the combined effect of both Dresselhaus and Bychkov-Rashba spin-orbit coupling is equivalent to an effective magnetic field  $\pm B_{\rm SO}$  which has the opposite sign for  $s_z=\pm 1/2$  spin electrons. When the external magnetic field is perpendicular to the planar structure, the field  $B_{\rm SO}$  generates an additional splitting for electron states as compared to the spin splitting in the in-plane field orientation. The anisotropy of spin splitting has been measured and then analyzed in terms of spin-orbit coupling in several AlGaAs/GaAs quantum dots by means of resonant tunneling spectroscopy. From the measured values and sign of the anisotropy we are able to determine the dominating spin-orbit coupling mechanism.

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A better understanding of the spin-orbit (SO) effects is crucial for the implementation of the coherent manipulation of the electron spin [1,2] in quantum dots and wires. SO coupling in III-V semiconductor structures is usually composed of two interplaying contributions of different symmetries,

$$\mathcal{H}_{SO} = \varrho_{D}(p_{x}s_{x} - p_{y}s_{y}) + \varrho_{BR}(p_{y}s_{x} - p_{x}s_{y}). \tag{1}$$

The first term is reminiscent of the Dresselhaus SO coupling in zinc blende bulk semiconductors [3,4] (it reflects the inversion asymmetry of GaAs). The second term in Eq. (1) is the interface-induced coupling of the Bychkov-Rashba type [5]. It is difficult to separate the effects of the two SO coupling mechanisms in quantum transport measurements and spin relaxation [6–11] (except for optical experiments [12,13]), and even to determine which one is dominant. At the same time coherent spin manipulation as well as the spin-Hall effect [2,14,15] depend on the balance between the two mechanisms.

Here, we show that the relative strength of the Dresselhaus and Bychkov-Rashba SO coupling mechanisms in a device can be determined from the anisotropy of the spin splitting. We exploit single-electron resonant tunneling spectroscopy [16] to observe the difference  $\Delta_\perp - \Delta_\parallel$  in spin splitting in a double-barrier structure subjected to a magnetic field perpendicular  $(\Delta_\perp)$  and parallel  $(\Delta_\parallel)$  to the plane of the quantum well. We analyze this anisotropy within the framework of the theory of SO coupling in lateral quantum dots [8,9]. It is shown below that the two mechanisms cause anisotropy of opposite signs, and that

$$\Delta_{\perp} - \Delta_{\parallel} \propto (-g/|g|)(\varrho_{\rm BR}^2 - \varrho_{\rm D}^2),$$
 (2)

where g is the quantum well electron Lande g factor in the in-plane magnetic field.

The experiment was performed with two highly asymmetric double-barrier resonant tunneling devices with an undoped 10 nm wide GaAs quantum well being sandwiched between 5 and 8 nm thick Al<sub>0.3</sub>Ga<sub>0.7</sub>As tunneling barriers separated from the highly doped GaAs contacts (Si doped with  $n_S = 4 \times 10^{17} \text{ cm}^{-3}$ ) by 7 nm thick undoped GaAs spacer layers. The samples were fabricated as pillars of 2  $\mu$ m (sample A) and 40  $\mu$ m diameter (sample B). dc measurements of the I-V characteristics were performed in a dilution refrigerator at 20 mK base temperature for two different orientations of the magnetic field, see Fig. 1(a). The studied GaAs quantum well embedded between two AlGaAs barriers can be viewed as a two-dimensional system with the edges and residual impurities confining the lateral electron motion and thus forming dots. Tunneling through the lowest state of the dot, at the energy  $E_0$  and with lateral extent  $\lambda$ , produces the lowest resonance peak in the differential conductance, whereas its excited states are responsible for additional peaks in dI/dV, which all move in a magnetic field  $B_z$  perpendicular to the quantum well, as shown in Figs. 2 and 3. The magnetic field dependence of energy levels can be illustrated using the model of parabolic confinement,  $V(\mathbf{r}) = \frac{1}{2}m\omega^2\mathbf{r}^2$ , with the extension of the wave function  $\lambda \sim \sqrt{\hbar/\omega m}$ , where the

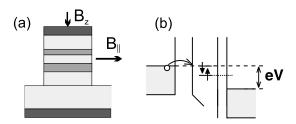


FIG. 1. Schematic picture (a) and energy diagram (b) of the studied device under finite bias and finite magnetic field.

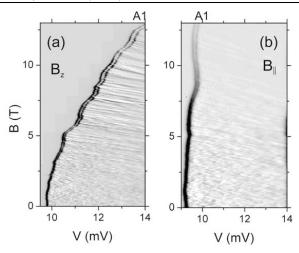


FIG. 2. Differential conductance as a gray-scale plot for sample A ( $\hbar\omega=31.2$  meV) as a function of bias voltage and magnetic field for (a)  $B_z$  being perpendicular to the quantum well plane, and (b)  $B_{\parallel}$ , T=20 mK.

spectrum of quantum dot states  $|n_+ n_-\rangle$ ,  $n_{\pm} = 0, 1, 2, ...$  is described by

$$E_{n_{+}n_{-}} = E_{0} + \hbar\sqrt{\omega^{2} + (\omega_{c}/2)^{2}} - \hbar\omega + \sum_{\pm} n_{\pm}\hbar\omega_{\pm}$$

$$\omega_{\pm} = \sqrt{\omega^{2} + (\omega_{c}/2)^{2}} \pm \frac{1}{2}\omega_{c}, \qquad \omega_{c} = eB/m.$$
(3)

For a strongly bound state or at low fields, such that  $\omega > \omega_c$  (also  $\lambda < \lambda_B$ , where  $\lambda_B = \sqrt{\hbar/eB_z}$ ), the first tunneling

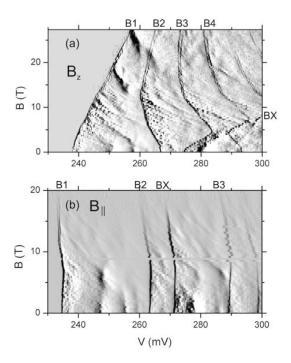


FIG. 3. Differential conductance as a gray-scale plot for sample B ( $\hbar\omega=13.8$  meV) as a function of bias voltage and magnetic field for (a)  $B_z$  being perpendicular to the quantum well plane, and (b)  $B_{\parallel}$ , T=20 mK.

resonance experiences a diamagnetic shift  $E_{00} \approx E_0 + \hbar \omega_c^2/8\omega$ , which is quadratic in  $B_z$ . For  $\omega \ll \omega_c$  at high fields,  $\omega_+ \approx \omega_c$  and  $\omega_- \approx \omega^2/\omega_c \ll \omega_c$ , the diamagnetic shift of several low-energy states in a dot follows approximately the energy of the lowest 2D Landau level,  $E_{0n_-} \approx [E_0 - \hbar \omega + (n_- + 1)\hbar \omega^2/\omega_c] + 1/2\hbar \omega_c(B_z)$ . In the structures studied, both weakly and strongly bound states have been seen.

Figure 2(a) shows the differential conductance peak A1 found in sample A and attributed to a strongly bound state  $(\hbar\omega = 31.2 \text{ meV})$  extracted from the diamagnetic shift using an energy-voltage conversion factor of  $\alpha = 0.5$  [17]), presumably formed by a growth-induced local potential minimum. Several differential conductance peaks, B1-B4 and BX, were observed in sample B. The magnetic field dependence of their positions shown in Fig. 3(a) complies with the magnetospectrum in a parabolic potential with  $\hbar\omega = 13.8 \text{ meV}$  [18]. We attribute the large voltage onset of around 240 mV in sample B to strong serial resistances due to partly compensated regions in emitter and collector [19]. The data shown in Fig. 2(b) and 3(b) taken on the same structures subjected to an in-plane magnetic field do not display a diamagnetic shift and confirm the 2D nature of the dots.

In both magnetic field directions, all peaks in dI/dV resolve into two at high enough field values, manifesting the spin splitting of each dot state. Spin splittings extracted from the data shown in Figs. 2 and 3 are gathered in Fig. 4: (a) shows the data for sample A averaged over a field

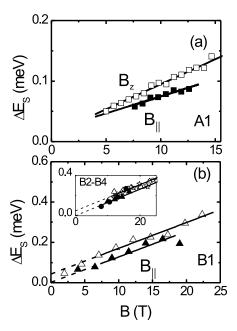


FIG. 4. (a) Spin splitting of the state A1 of sample A for both B-field configurations. (b) Spin splitting of the state B1 of sample B for both B-field configurations. Solid lines represent the result of a linear fit to the high-field part of the data. Inset shows the spin splitting of the states B2 (triangles), B3 (circles), and B4 (stars) for both B-field configurations.

interval of 0.33 T, whereas (b) shows the field dependence of splittings in sample *B* averaged over an interval of 3 T to eliminate the influence of fluctuations of the local density of states of the emitter [20]. In Fig. 4 a distinct anisotropy of the peak splitting is displayed, with the splitting caused by the out-of-plane field (open symbols) being systematically larger than what is created by the in-plane field (closed symbols).

The observed values of spin splitting anisotropy are much larger and have the opposite sign to what might be expected from the kinetic energy dependence, g = -0.44 + E(dg/dE) of the electron g factor across the conduction band in GaAs. Using  $dg/dE \sim +2 \text{ eV}^{-1}$  [21], we estimate that the diamagnetic shift (which increases the electron kinetic energy in a perpendicular magnetic field) would further reduce the value of g at higher fields by  $(\hbar \omega_c/2)(dg/dE)$ . The latter is less than the observed anisotropy in the peak B1. One may also notice that the anisotropy of spin splitting of the excited dot states B2-B4 shown in the inset to Fig. 4 is the same as of B1, despite a larger kinetic energy of an electron in them.

Although one may address the interpretation of this observation using a microscopic model of the quantum well based upon  $\mathbf{kp}$  theory, such as developed in Refs. [22], below we adopt an alternative phenomenological approach describing the SO coupling in a quantum well using the effective Hamiltonian in Eq. (1). This enables us to express the spin splitting anisotropy of the electron in a lateral quantum dot in terms of the effective magnetic field  $B_{\rm SO} = (\hbar m^2)/(2e)(\varrho_{\rm BR}^2 - \varrho_{\rm D}^2)$  recently discussed in relation to the geometrical Berry phase in quantum dots [8,9] and rings [23].

For a quantum well lying in the (001) crystallographic plane of GaAs it is convenient to choose coordinates along crystallographic directions  $\hat{\mathbf{e}}_1 = [110]$  and  $\hat{\mathbf{e}}_2 = [\bar{1}10]$ , and to study the effective 2D Hamiltonian in the form

$$\mathcal{H} = \frac{(-i\hbar\nabla - \mathbf{A} - \mathbf{a})^2}{2m} + \frac{g\epsilon_Z}{|g|^2}\mathbf{I}\sigma + \mathbf{V}(\mathbf{r}), \quad (4)$$

$$\mathbf{a} = \frac{\hbar \sigma_2 \hat{\mathbf{e}}_1}{2\lambda_1} - \frac{\hbar \sigma_1 \hat{\mathbf{e}}_2}{2\lambda_2},\tag{5}$$

where  $\mathbf{A} = \frac{e}{2}B_z[\mathbf{r} \times \hat{\mathbf{e}}_z]$ ,  $\mathbf{l} = \mathbf{B}/B$ ,  $\sigma = (\sigma_1, \sigma_2, \sigma_3)$  is the vector of Pauli matrices, and  $\epsilon_Z = |g\mu_B B|$  is the Zeeman energy (in a 10 nm wide GaAs/AlGaAs quantum well, g < 0 according to Snelling *et al.* [21]; and in the above expressions, we have already taken into account the negative sign of the electron charge, so that e > 0). The parameters  $\varrho_D$  and  $\varrho_{BR}$  of the SO coupling defined in Eq. (1) for a conventional choice of axes,  $\hat{\mathbf{x}} = [100]$  and  $\hat{\mathbf{y}} = [010]$ , appear in the uniform non-Abelian vector potential  $\mathbf{a}$  in Eq. (4) via the inverse of the SO coupling length  $\lambda_{1(2)}$  as  $\lambda_1^{-1} = (\varrho_D - \varrho_{BR})m$  and  $\lambda_2^{-1} = -(\varrho_{BR} + \varrho_D)m$ , where  $2\pi\lambda_{1(2)}$  characterizes the distance at which spin precession of a polarized electron moving along crystallographic direction  $\hat{\mathbf{e}}_{1(2)}$  undergoes one complete revolution.

To analyze the case of a weak SO coupling for electrons bound in a quantum dot,  $\lambda_{1,2} \gg \lambda$ , we follow Refs. [8,9] and perform a nonuniform unitary transformation to the electron wave function,  $\psi(\mathbf{r}) = U(\mathbf{r})\tilde{\psi}(\mathbf{r})$  and the Hamiltonian in Eq. (4),

$$U = \exp\{\frac{i}{2}[\lambda_1^{-1}x_1\sigma_2 - \lambda_2^{-1}x_2\sigma_1]\}, \qquad \tilde{\mathcal{H}} = U^{\dagger}\mathcal{H}U.$$

This transformation rotates locally the spin space by the angle  $R = \sqrt{(x_1/\lambda_1)^2 + (x_2/\lambda_2)^2}$  around the unit vector  $\hat{\mathbf{n}} = (\lambda_1^{-1} x_1 \hat{\mathbf{e}}_2 - \lambda_2^{-1} x_2 \hat{\mathbf{e}}_1)/R$ . As a result, the coordinate frame for the electron spin set in the center of the dot,  $x_{1,2} = 0$ , gets adjusted to the local orientation determined by the SO-induced spin precession upon its displacement along the radius vector  $\mathbf{r}$ . The energy spectrum can be found from the transformed Hamiltonian

$$\tilde{\mathcal{H}} = \frac{1}{2m} (-i\hbar \nabla - \mathbf{A} - \tilde{\mathbf{a}})^2 + \frac{1}{2} \epsilon_{\mathbf{Z}} \tilde{\mathbf{I}} \sigma + V(\mathbf{r}),$$

where  $\tilde{\mathbf{a}} = U^{\dagger} \mathbf{a} U + i\hbar U^{\dagger} \nabla U$  and  $\tilde{\mathbf{l}}(\mathbf{r}) = (\mathbf{l} \cdot \hat{\mathbf{n}}) \hat{\mathbf{n}} + \hat{\mathbf{n}} \times [\mathbf{l} \times \hat{\mathbf{n}}] \cos R - [\mathbf{l} \times \hat{\mathbf{n}}] \sin R$ . The transformation  $U(\mathbf{r})$  aims to gauge out [8,9,24,25] spin-orbit coupling, which appears in Eq. (4) in the form of uniform spin-dependent vector potential in Eq. (5). The latter goal cannot be achieved in full, since Pauli matrices do not commute with each other. However, for a weak SO coupling  $[\lambda_{1,2} \gg \lambda]$  and small rotation angles  $R \ll 1$ , the residual  $\tilde{\mathbf{a}}$ , [9]

$$\tilde{\mathbf{a}} = -\frac{[\mathbf{r} \times \hat{\mathbf{e}}_3]}{4\lambda_1 \lambda_2} \hbar \sigma_3 + \hbar \lambda_{1,2}^{-1} \mathcal{O}[R^2], \tag{6}$$

is dominated by the "vector potential" of an effective magnetic field which has the opposite sign for spin "up" and "down" electrons in the quantum dot, [8,9]

$$B_{\rm eff} = B_z - \sigma_3 B_{\rm SO}. \tag{7}$$

It is this difference in the effective magnetic field seen by an electron in the adjusted spin frame that causes the spin splitting anisotropy. For the in-plane magnetic field orientation ( $B_z=0$ ), the effective field  $B_{\rm eff}=\pm B_{\rm SO}$  produces the same negligibly small "diamagnetic" shift  $\sim\!B_{\rm SO}^2$  in the orbital motion energy of both spin components. Accordingly it does not alter the value of the quantum well Zeeman splitting,  $\Delta_{\parallel}=\epsilon_{\rm Z}$ .

For the perpendicular magnetic field orientation ( $\mathbf{B} = B\hat{\mathbf{e}}_z$ ), the difference in  $B_{\rm eff} = B_z \pm B_{\rm SO}$  generates the difference in the effective diamagnetic shift for two spin states and, therefore, an additional energy splitting. It results in the anisotropy of spin splitting in the lowest quantum dot state

$$\Delta_{\perp} - \Delta_{\parallel} = \frac{-g dE_{00}}{|g| dBz} 2B_{SO} = \frac{-g \frac{\omega_c e h}{2m} B_{SO}}{|g| \sqrt{\omega^2 + (\frac{1}{2} \omega_c)^2}}.$$
 (8)

Equation (8) is valid in both low and high magnetic field regimes. Its low-field asymptotic

$$\Delta_{\perp} - \Delta_{\parallel} \approx \left(\frac{-g}{|g|}\right) B \hbar e^2 B_{SO} / (2\omega m^2)$$
 (9)

TABLE I. Experimental parameters of the spin-orbit characteristics for sample A and B, as discussed in the text.

samples	A	В	
peak $\frac{e\hbar}{m}B_{\mathrm{SO}}$ $B_{\mathrm{SO}}$	$A1$ $32 \pm 2 \mu eV$ $19 mT$	$B1$ $43 \pm 10 \ \mu eV$	$B2-B4$ $44 \pm 16 \mu eV$ mT

for  $\omega_c < \omega$  also describes the situation of a strongly bound electron, such as the resonance level A1. The high-field asymptotic of the result in Eq. (8),

$$\Delta_{\perp} - \Delta_{\parallel} \approx \left(\frac{-g}{|g|}\right) \frac{e\hbar}{m} B_{\text{SO}} \quad \text{for } \omega_c \gg \omega, \tag{10}$$

simultaneously describes the anisotropy of the spin splitting of the few lowest quantum dot states  $E_{0n_-}$ . The anisotropy energy transforms into an offset with the sign dependent on the sign of  $B_{\rm SO} \propto (\varrho_{\rm BR}^2 - \varrho_{\rm D}^2)$  in Eq. (7) and on the sign of the electron g factor. Finally, we apply Eqs. (8)–(10) to analyze the peak splitting data shown in Fig. 4. Since in a 10 nm wide GaAs quantum well the bare value of the g factor is negative [21], larger values of spin splitting in a perpendicular field mean that  $B_{\rm SO} \propto (\varrho_{\rm BR}^2 - \varrho_{\rm D}^2) > 0$ , pointing at the dominance of the Bychkov-Rashba term in the SO coupling, presumably, due to the electron penetrating into the AlGaAs barrier which is enhanced in a narrow quantum well.

The fit to the experimentally observed anisotropy produces values of  $(e\hbar/m)B_{SO}$  which are shown in Table I and determine the effective field  $B_{SO}$  in each sample.  $B_{SO}$  =  $25 \pm 6$  mT was obtained using Eq. (10) for B1 and agrees well with the value of  $25 \pm 8$  mT for linear fitting of B2-B4. The strongly confined state observed in sample A [peak A1, Fig. 4(a)] was analyzed using Eq. (9), and we extracted  $B_{SO} = 19 \pm 1$  mT. The sign of SO coupling characteristics in  $B_{\rm SO} \propto (\varrho_{\rm BR}^2 - \varrho_{\rm D}^2)$  suggests that in a narrow quantum well Bychkov-Rashba coupling is dominant—in contrast to wide quantum wells investigated in Raman scattering [12]. The extracted SO coupling is also stronger than that estimated from the bulk Dresselhaus term,  $2\gamma \hbar^{-4} \sum_{ijk} \epsilon^{ijk} p_i^2 p_j s_j$ , (where  $\epsilon^{ijk}$  is the antisymmetric tensor) using  $\gamma = (26 \pm 5) \text{ eVÅ}^3$  collected from Refs. [7,12]. For the quantum well width w = 10 nm, the Dresselhaus mechanism alone would generate  $B_{SO}$ , which reduces the Zeeman splitting and is of much smaller absolute value,  $(\hbar^2 m/2)\varrho_D^2 \approx 2\pi^4 m(\gamma/w^2)^2 \approx 12 \mu eV$ . Using this estimate, we can deduce the strength of the Bychkov-Rashba coupling in quantum wells in the samples B(A) as, at least,  $(\hbar^2 m/2) \varrho_{BR}^2 \sim 54(44) \ \mu eV$ .

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