## How the Liquid-Liquid Transition Affects Hydrophobic Hydration in Deeply Supercooled Water

## Dietmar Paschek\*

Physikalische Chemie, Universität Dortmund, Otto-Hahn-Strasse 6, D-44221 Dortmund, Germany (Received 3 December 2004; published 2 June 2005)

We determine the phase diagram of liquid supercooled water by extensive computer simulations using the TIP5P-E model [J. Chem. Phys. **120**, 6085 (2004)]. We find that the transformation of water into a low density liquid in the supercooled range strongly enhances the solubility of hydrophobic particles. The transformation of water into a tetrahedrally structured liquid is accompanied by a minimum in the hydration entropy and enthalpy. The corresponding change in sign of the solvation heat capacity indicates a loss of one characteristic signature of hydrophobic hydration. The observed behavior is found to be qualitatively in accordance with the predictions of the information theory model of Garde *et al.* [Phys. Rev. Lett. **77**, 4966 (1996)].

DOI: 10.1103/PhysRevLett.94.217802 PACS numbers: 61.20.Ja, 02.70.Ns, 07.05.Tp, 64.70.Ja

The thermodynamical anomalies of liquid water are considered to be caused by a transformation between two different liquid forms of water buried in the deeply supercooled region [1]. The two different dense liquids have well characterized counterparts in the glassy state: the (very) high density and low density amorphous ice forms [2,3]. Computer simulation studies have furnished a picture of a first order liquid-liquid phase transition between two liquids ending up in a metastable critical point [4,5]. Although singularity-free scenarios might explain as well the properties of supercooled water [1], there is experimental support for the liquid-liquid critical point hypothesis from the changing slope of the metastable melting curves observed for different ice polymorphs [6,7]. To make the situation even more puzzling, recent computer simulations provide evidence that there might be even more than one liquid-liquid transition [8].

One prominent anomaly of liquid water is the increasing solubility of hydrophobic gases with decreasing temperature [9]. This behavior is the consequence of a negative solvation entropy of small hydrophobic particles [10]. Since the corresponding solvation enthalpy is also negative, the observed low solubility (the large positive solvation free energy) of small hydrophobic particles is due to a dominating entropy effect. The origin of the negative hydration entropy is widely regarded as being due to the bias in the hydration water orientational space, as the water molecules are trying to preserve their hydrogen bond network [11]. Entropy and enthalpy effects have been shown to be determined by the water in the first hydration shell [12]. In addition, the broken hydrogen bond states, with hydrogen bond donors or acceptors pointing towards the hydrophobic particles, are increasingly populated with increasing temperature [11]. Hence, the positive solvation heat capacity of hydrophobic particles is considered to be one of the key signatures for hydrophobic hydration [13]. A recent experimental study of Souda [14], investigating alkane layers adsorbed on an amorphous solid water substrate, shows that the alkane phase gets soaked into the water phase in the temperature region close to the suspected glass transition temperature [15]. One possible explanation (among others) might be that the highly viscous low density liquid form of water provides a significantly increased solubility for hydrophobic molecules. The scope of the present contribution is to monitor the hydration of a small hydrophobic particle as we penetrate the deeply supercooled region. Our particular interest is to elucidate how the transformation into a highly tetrahedrally ordered low density liquid (LDL) phase [16] affects hydrophobic hydration.

An important problem regarding simulations of highly viscous liquids close to the glass transition is to provide proper sampling. To overcome this problem we perform parallel tempering simulations of an extended ensemble of states [17] using the technique of the volume-temperature exchange molecular dynamics simulation (VTREMD) [18]. To represent liquid supercooled water, we employ the recently proposed TIP5P-E model for water, which was fitted to reproduce water density maximum and related thermodynamical anomalies while treating the Coulomb interactions with the Ewald sum [19]. For the VTREMD simulation [20] we consider a grid of 440 (V, T) states [21]. Starting from a set of equilibrated initial configurations obtained at ambient conditions, the VTREMD simulation [22] was conducted for 20 ns, providing a total of 8.8  $\mu$ s worth of trajectory data. The average time interval between two successful state exchanges was obtained to be about 3 ps. During the entire course of the simulation each replica crossed the whole temperature and density interval several times. After an initial equilibration period of about 4 ns, the average pressure and potential energies show convergence even for the lowest temperatures and the remaining 16 ns are used for

Figure 1 shows the phase diagram of liquid supercooled water in terms of a contour plot of the  $P(\rho, T)$  data as obtained by the VTREMD simulations. The TIP5P-E phase diagram apparently exhibits a first order phase tran-

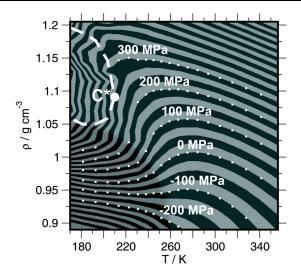


FIG. 1 (color online). Phase diagram for stable and supercooled liquid TIP5P-E water. The spacing between different contour colors corresponds to a pressure drop of 25 MPa. Selected isobars are indicated. The heavy dashed line denotes the high density/low density liquid (HDL/LDL) coexistence line. The HDL/LDL critical point is located at  $C^*$  with  $T^*=210$  K,  $P^*=310$  MPa, and  $\rho^*=1.09$  g cm<sup>-3</sup>. Darker shading indicates the LDL basin.

sition between two metastable liquid phases, ending in a second critical point  $C^*$ . The location of the coexistence line, estimated from a Maxwell construction using the subcritical isotherms shown in Fig. 2(d), has to be seen as a rough guess only, since the exact form of the van der Waals loops in the two phase region might depend on the system size. The location of  $C^*$  is close to the values reported by Yamada et al. for the original TIP5P model with  $T^* = 217$  K,  $P^* = 340$  MPa, and  $\rho^* = 1.13$  g cm<sup>-3</sup> [23]. Figure 2(a) compares experimental data [24] with several selected isobars according to a linear interpolation from the TIP5P-E  $P(\rho, T)$  data set. Although the location of the density maximum at normal pressure is close to the experimental values, the TIP5P-E model exhibits a considerably larger thermal expansivity as real water and is significantly more compressible. Figure 2(b) shows that the isobars derived from the VTREMD data set match exactly the data obtained from conventional NPT simulations. For comparison the isobar according to Rick's simulation is shown [19]. We denote small but significant differences. Since both simulations were using Ewald summation, their origin is not quite clear at present. We emphasize one particular detail of the low pressure isobars, indicated in Figs. 1 and 2(b): The density goes through a minimum after the transformation into the low density liquid has taken place. Apparently at low temperatures the expansivity seems to behave as it would be expected for a conventional liquid. Brovchenko et al. [8] and recently Poole et al. [25] made similar observations for the ST2 model. Figure 2(c) shows the evolution of the com-

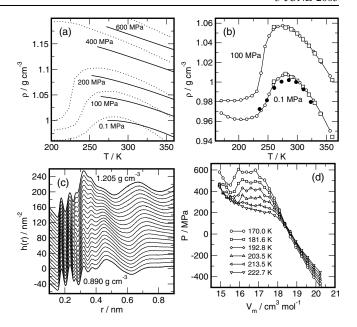


FIG. 2. (a) Selected isobars for TIP5P-E water (dotted lines) compared with experimental data [24]. (b) Two isobars for TIP5P-E. Open circles: Interpolated data from the VTREMD  $P(\rho,T)$  data set. Open squares: Constant temperature/pressure (NPT) MD simulations. Filled circles: Ref. [19]. (c)  $h(r) = 4\pi r(N/V)[0.092g_{OO}(r) + 0.486g_{HH}(r) + 0.422g_{OH}(r) - 1]$  functions for the 222.7 K isotherm. The functions are shifted by an increment of  $10 \text{ nm}^{-2}$ . (d) Near-critical and subcritical isotherms.

posite radial distribution function h(r) along the 222.7 K isotherm. The highlighted patterns obtained for the lowest and highest densities show a strong similarity with the functions determined experimentally by Bellissent-Funel et al. for high and low density amorphous ice [26]. The observed low density pattern has been shown to be related to a high tetrahedral order of water's first hydration shell [16]. Similarities between the local structure of LDA and ice Ih have also been demonstrated recently by Finney et al. from the analysis of neutron scattering experiments [27]. We do not observe indications for the presence of further liquid-liquid transitions for TIP5P-E, as suggested by Brovchenko et al. for the ST2 model [8]. However, further phase transitions might be present at even lower temperatures. Finally, no signs for crystallization are observed, as denoted by Yamada et al. [23]. Probably our smaller system size and the random walk of the replicas through state space, regularly reaching stable regions, prevents the systems from crystallizing.

The hydrophobic hydration of a Lennard-Jones argon particle ( $\sigma_{\text{Ar-O}} = 0.3256$  nm and  $\epsilon_{\text{Ar-O}}/k = 105.8$  K) [28] is given as excess chemical potential  $\mu_{\text{ex}} = -\beta^{-1} \ln \gamma$  for infinite dilution, where  $\gamma$  is the solubility and  $\beta = 1/kT$ . We employ the Widom particle insertion method [17] with  $\mu_{\text{ex}} = -\beta^{-1} \ln \langle \exp(-\beta \Phi) \rangle$ , where  $\Phi$  is the energy of an inserted test particle. The brackets  $\langle \cdot \cdot \cdot \rangle$  indicate canonical

sampling. Details about the calculation are given elsewhere [28]. Figure 3 shows the excess chemical potential for argon dissolved in TIP5P-E water for all simulated state points. First of all, we emphasize that the solubility increases strongly when penetrating the deeply supercooled region with  $\mu_{\rm ex}$  becoming even negative. The inset of Fig. 3 compares the experimental data of Kennan and Pollack [29] with data from our simulation. The pressure dependence is expressed by a positive partial molar volume of 30 cm<sup>3</sup> mol<sup>-1</sup>, close to the experimental value of 25 cm<sup>3</sup> mol<sup>-1</sup> [30]. The decreasing solubility upon density increase basically reflects the loss of available free volume. A larger partial molar volume in the simulation is hence in line with the increased isothermal compressibility observed for the TIP5P-E model, indicated by Fig. 2(a). Two regimes of small and strong pressure dependence are denoted, obviously related to the transformation between the high and low density liquid forms of water. We point out that we find an increase of the partial molar volume for Ar around normal pressure for the 260–255 K isotherms. Kennan and Pollack made a similar observation for xenon around 298 K. If and how these two observations are related has to be further investigated. Figure 4 shows the temperature dependence of  $\mu_{\rm ex}$  for several selected isobars ranging from -200 MPa to the supercritical 350 MPa. The experimental 0.1 MPa isobar [31] is given for comparison. From computer simulations of water, Garde et al. derived an information theory (IT) model

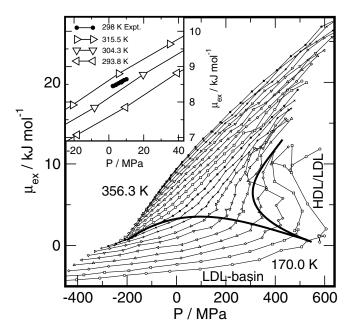


FIG. 3. Excess chemical potential of Ar dissolved in TIP5P-E water as a function of P and T. Thin lines indicate all calculated isotherms ranging from 170 to 356.3 K. The inset shows experimental data for 298 K [29] and simulated isotherms close-by. Thick lines indicate the LDL basin and the HDL/LDL coexistence region (see Fig. 1).

[32,33], giving simple analytic expressions for the hydrophobic hydration as a function of temperature and density. The leading term in the IT model strongly suggests a quadratic relation between the excess chemical potential and the water number density according to  $\mu_{\rm ex}/k \approx$  $ho^2 T v^2 / 2 \sigma_n^2$  [33], where v denotes the volume of a hydrophobic hard sphere particle, while  $\sigma_n^2 = \langle n^2 \rangle - \langle n \rangle^2$  indicates the variance of the number of water molecules in a sphere of volume v. The lines in Fig. 4 indicate a temperature dependence as suggested by the IT model, assuming the term  $v^2/2\sigma_n^2$  to be constant and shifting the isobars by a constant offset to account for attractive interactions. Well reproduced is the change in slope when passing the transformation into the low density liquid, qualitatively correct even for the supercritical isotherm at 350 MPa, suggesting a discontinuity of  $\mu_{ex}$ . Hence an important conclusion is that the weak monotonous temperature and density dependence of  $\mu_{ex}$ , as proposed by the IT model, and confirmed for the high temperature regime [32], is apparently also valid for the deeply supercooled region. This seems to be in line with the continuous structural transformation of water as a function of density [Fig. 2(c)] and temperature (not shown). The thermodynamics of hydrophobic hydration of small solutes is therefore largely predetermined by the location of the water isobars in the  $\rho$ , T plane. As a consequence, also a waterlike liquid showing a continuous singularity-free transition might exhibit a quite similar  $\mu_{\rm ex}$  dependence (apart from the discontinuous behavior of  $\mu_{\rm ex}$  above  $P_c$ ). As shown in the inset of Fig. 4, the change in slope of  $\mu_{\rm ex}$  is related to extrema in the temperature dependence of the entropy and enthalpy contributions. The minimum in the enthalpy causes a change in sign of the corresponding heat capacity from positive at high temperatures to negative for the low density liquid.

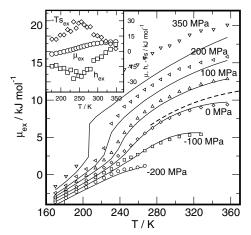


FIG. 4. The symbols indicate six isobars, interpolated from the  $\mu_{\rm ex}(\rho,T)$  TIP5P-E data set. The dashed line indicates experimental data for 0.1 MPa [31]. Full lines represent predictions for  $\mu_{\rm ex}=a\rho^2T+b$  with  $a=8\times10^{-2}$  kJ mol $^{-1}$  K $^{-1}$  cm $^6$  g $^{-2}$  and b=-16 kJ mol $^{-1}$ . The inset shows enthalpy  $(h_{\rm ex})$  and entropy  $(-Ts_{\rm ex})$  contributions to  $\mu_{\rm ex}$  for the 0 MPa isobar.

Apparently, a prominent signature of the "hydrophobic hydration" vanishes while passing the transition at about 250 K. In addition, an increasing slope of  $h_{\rm ex}$  upon approaching 250 K, as seen in the inset, and more prominently pronounced with increasing pressure (not shown), is consistent with the experimentally observed increase of the solvation heat capacity upon cooling [13]. Following the interpretation of the hydrophobic hydration according to Dill et al. [11], the change in sign of  $C_p$  is explained as follows: In the LDL regime, the water's coordination number approaches four, while the structure corresponds to a continuous random tetrahedral network. Because of the lack of additional possible hydrogen binding partners, the environment of a water molecule in the LDL bulk and in the hydrophobic hydration shell has greater similarity than in the "high density liquid" at ambient temperatures. This structural convergence in bulk and hydration shell in the LDL leads to a smaller entropy difference and hence to an increase in  $s_{ex}$ . Moreover, a larger hydrophobic particle in the LDL might even introduce disorder and hydrogen bond breaking into the (over)stretched hydrogen bond network and thus might even experience a positive hydration entropy. A further investigation into particle size dependence, hydrophobic aggregates, and hydrophobic interaction might reveal a behavior markedly different from that at ambient conditions.

This work was supported by the Deutsche Forschungsgemeinschaft (Forschergruppe 436). I thank Angel E. García, Ivan Brovchenko, and Alfons Geiger for valuable discussions.

- \*Electronic address: dietmar.paschek@udo.edu
- [1] P.G. Debenedetti, J. Phys. Condens. Matter **15**, R1669 (2003).
- [2] O. Mishima, L.D. Calvert, and E. Whalley, Nature (London) 310, 393 (1984).
- [3] T. Loerting, C. Salzmann, I. Kohl, E. Mayer, and A. Hallbrucker, Phys. Chem. Chem. Phys. 3, 5355 (2001).
- [4] P. H. Poole, F. Sciortino, U. Essmann, and H. E. Stanley, Nature (London) **360**, 324 (1992).
- [5] H. Tanaka, Nature (London) 380, 328 (1996).
- [6] O. Mishima and H. E. Stanley, Nature (London) 396, 329 (1998).
- [7] O. Mishima, Phys. Rev. Lett. 85, 334 (2000).
- [8] I. Brovchenko, A. Geiger, and A. Oleinikova, J. Chem. Phys. 118, 9473 (2003).
- [9] E. Wilhelm, R. Battino, and R. J. Wilcox, Chem. Rev. 77, 219 (1977).
- [10] L. R. Pratt, Annu. Rev. Phys. Chem. 53, 409 (2002).
- [11] N. T. Southall, K. A. Dill, and A. D. J. Haymet, J. Phys. Chem. B 106, 521 (2002).
- [12] D. Paschek, J. Chem. Phys. 120, 10605 (2004).
- [13] K. A. T. Silverstein, A. D. J. Haymet, and K. A. Dill, J. Am. Chem. Soc. 122, 8037 (2000).

- [14] R. Souda, J. Chem. Phys. 121, 8676 (2004).
- [15] O. Mishima, J. Chem. Phys. 121, 3161 (2004).
- [16] D. Paschek and A. Geiger, J. Phys. Chem. B 103, 4139 (1999).
- [17] D. Frenkel and B. Smit, *Understanding Molecular Simulation. From Algorithms to Applications* (Academic Press, San Diego, 2002), 2nd ed.
- [18] D. Paschek and A. E. García, Phys. Rev. Lett. 93, 238105 (2004).
- [19] S. W. Rick, J. Chem. Phys. 120, 6085 (2004).
- [20] State swapping moves between two states i and j are accepted with a probability  $P_{\text{acc}} \min(1, \exp\{\beta_i [U(\vec{s}_i^N; L_i) U(\vec{s}_j^N; L_i)] + \beta_j [U(\vec{s}_j^N; L_j) U(\vec{s}_i^N; L_j)]\}$ ). Here,  $\vec{s}_i^N$  represents the set of scaled coordinates  $\vec{s}_N = L^{-1} \vec{r}_N$  of the entire N-particle system belonging to state i.  $U(\vec{s}_i^N; L_i)$  denotes the potential energy of configuration  $\vec{s}_i^N$  at volume  $V_i = L_i^3$ , whereas  $U(\vec{s}_i^N; L_j)$  represents the configurational energy belonging to  $\vec{s}_i^N$  at volume  $V_j$ . Whether a state swapping move or an MD move is executed is chosen at random with a probability of 0.2 for selecting state swapping moves.
- [21] Temperatures at 170.0, 181.6, 192.8, 203.5, 213.5, 222.7, 230.8, 238.0, 244.8, 251.8, 259.1, 266.9, 275.2, 284.2, 293.8, 304.3, 315.5, 327.8, 341.3, and 356.3 K at densities between 0.890 and 1.205 g cm $^{-3}$  with an increment of 0.015 g cm $^{-3}$ .
- [22] Each replica represents a MD simulation of 256 molecules in the *NVT* ensemble. The electrostatic interactions are treated by Ewald summation [34] with a cutoff of 0.9 nm and a 18 × 18 × 18 mesh with 4th order interpolation. Lennard-Jones cutoff corrections for energy and pressure were considered. A 2 fs time step was used. The simulations were carried out with GROMACS 3.2 (www.gromacs. org), modified by us to allow *V*, *T*-state swapping. The temperature tiling has been chosen to maintain an acceptance ratio of about 0.2 for state swapping.
- [23] M. Yamada, S. Mossa, H.E. Stanley, and F. Sciortino, Phys. Rev. Lett. 88, 195701 (2002).
- [24] W. Wagner and A. Pruß, J. Phys. Chem. Ref. Data 31, 387 (2002).
- [25] P. H. Poole, I. Saika-Voivod, and F. Sciortino, cond-mat/ 0504574.
- [26] M. C. Bellissent-Funel, J. Teixeira, and L. Bosio, J. Chem. Phys. 87, 2231 (1987).
- [27] J. L. Finney, A. Hallbrucker, I. Kohl, A. K. Soper, and D. T. Bowron, Phys. Rev. Lett. 88, 225503 (2002).
- [28] D. Paschek, J. Chem. Phys. 120, 6674 (2004).
- [29] R. P. Kennan and G. L. Pollack, J. Chem. Phys. 93, 2724 (1990).
- [30] When fitting the  $\mu_{ex}$  data for argon of Ref. [29].
- [31] R. F. Prini and R. Crovetto, J. Phys. Chem. Ref. Data 18, 1231 (1989).
- [32] S. Garde, G. Hummer, A. E. García, M. E. Paulaitis, and L. R. Pratt, Phys. Rev. Lett. 77, 4966 (1996).
- [33] G. Hummer, S. Garde, A. E. García, and L. R. Pratt, Chem. Phys. 258, 349 (2000).
- [34] U. Essmann, L. Perera, M. L. Berkowitz, T. A. Darden, H. Lee, and L. G. Pedersen, J. Chem. Phys. 103, 8577 (1995).