

## One-Dimensional Transport in Polymer Nanofibers

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We report our transport studies in quasi-one-dimensional (1D) conductors—helical polyacetylene fibers doped with iodine—and the data analysis for other polymer single fibers and tubes. We found that at  $30\text{ K} < T < 300\text{ K}$ , the conductance and the current-voltage characteristics follow the power law  $G(T) \propto T^\alpha$  with  $\alpha \sim 2.2\text{--}7.2$  and  $I(V) \propto V^\beta$  with  $\beta \sim 2\text{--}5.7$ . Both  $G(T)$  and  $I(V)$  show the features characteristic of 1D systems such as a Luttinger liquid or Wigner crystal. The relationship between our results and theories for tunneling in 1D systems is discussed.

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The transport properties of one-dimensional (1D) conductors are a subject of intense interest because of the recent development of semiconductor nanotechnology [1]. Electron-electron interactions (EEI) are strongly affecting the transport in 1D systems by leading to phases different from conventional Fermi liquid. The repulsive short-range electron-electron interactions result in Luttinger liquids (LL) [2], while long-range Coulomb interactions (LRCI) cause a Wigner crystal (WC) [3]. The characteristic feature of 1D systems is the power-law behavior of the tunneling density of states near the Fermi level, which manifests itself in the power-law temperature dependencies of the conductance,  $G(T)$ , and the current-voltage ( $I$ - $V$ ) characteristics,  $I(V)$ . This behavior has been observed recently in 1D systems, such as single-wall and multiwall carbon nanotubes (SWNT and MWNT) [4,5], doped semiconductor nanowires [6,7], and in fractional quantum Hall edge states [8]. The LL, WC, or Environmental Coulomb blockade (ECB) [5] models are currently debated in order to explain the above-mentioned power-law behavior in 1D systems. Nanofibers that are made of conjugated polymers are another example of initially 1D systems. Polyacetylene (PA) nanofibers are of particular interest because of the unique chemical structure of this polymer. PA has the band gap of  $E_g \sim 1.5\text{ eV}$ , and consists of linear chains of CH units with alternating single and double bonds. Their conductivity greatly increases upon doping [9]. Both of these features make PA fibers promising for nanotransport studies. The low temperature transport in doped single PA fibers and polypyrrole (PPy) nanotubes has been studied recently [10,11]; the tunneling transport mechanism has also been considered [12]. The electrical transport in doped helical PA has been thoroughly studied for 3D films [13]. However, the complete understanding of the transport mechanism and the applicability of theories for tunneling in 1D systems for a single helical PA fiber is still lacking. In this Letter

we report our transport studies of helical PA fibers doped with iodine. Analysis of early experimental data for a single PA fibers and polymer tubes is included in order to examine the relationships between various theoretical models for 1D conductors.

Helical PA (hel PA) is synthesized using chiral nematic liquid crystal as a solvent of Ziegler-Natta catalyst by Akagi *et al.*, following the procedure presented elsewhere [14]. Helical PA is polycrystalline and can be produced with either *R*- (counterclockwise) or *S*- (clockwise) type helicity. The typical length of helical PA fibers is of the order of  $10\ \mu\text{m}$ —much longer than that of the traditional PA. A single fiber has a cross section, typically  $40\text{--}65\text{ nm}$  (wide) and  $130\text{--}300\text{ nm}$  (high). *R*-helical PA fibers are deposited on a Si substrate with a  $\text{SiO}_2$  layer and gold or platinum electrodes thermally evaporated on the top,  $2\ \mu\text{m}$  apart. The fiber doped with iodine from vapor phase up to the saturation level ( $1\text{--}2\text{ wt}\%$ ) [15]. The transport measurements are performed in the two-probe geometry in a vacuum at  $\sim 10^{-5}$  Torr, using dispex-osp cryogenic system with a Keithley 6517A electrometer. The conductance of the sample is determined from the Ohmic regime of the  $I$ - $V$  at each temperature. The conductance measurements for the same sample at  $300\text{ K}$  showed the values of the same order of magnitude in both two-probe and four-probe geometry.

Figure 1 shows the atomic-force microscopy (AFM) image of a *R*-hel PA fiber; the inset demonstrates the schematic of a two-probe device based on such a *R*-hel PA nanofiber. The cross section of this particular fiber is  $65\text{ nm} \times 290\text{ nm}$ , and its length is as long as  $10\ \mu\text{m}$ . Figure 2 presents the typical  $G(T)$  dependencies for *R*-hel PA nanofibers doped with iodine as well as the results of our analysis of early data for iodine doped single PA nanofiber (diameter  $\sim 20\text{ nm}$ ) and PPy nanotube (diameter  $\sim 15\text{ nm}$ ) available from Refs. [10,16]. As can be seen from Fig. 2, the conductance for all types of polymer fibers follows the power-law behavior  $G(T) \propto T^\alpha$

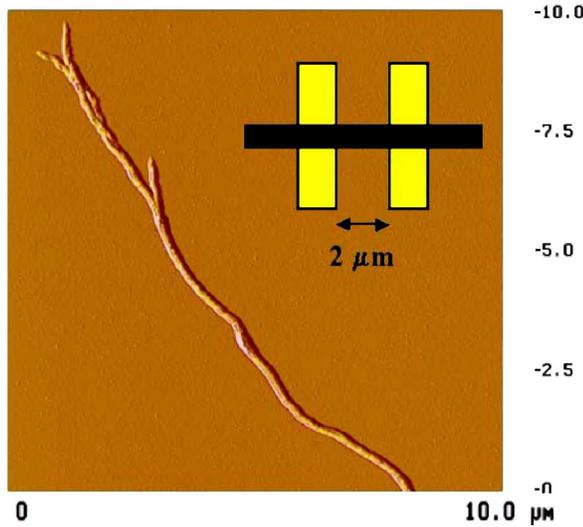


FIG. 1 (color online). AFM image of a R-hel PA fiber; the inset shows the schematic of a two-probe device based on such a R-hel PA fiber on top of Pt electrodes.

starting from room temperature and down to  $\sim 30$  K for the most conductive R-hel PA fiber (sample 1). The power exponent increases as the fiber diameter or its cross section (the amount of polymer chains) becomes smaller. The inset to Fig. 3 shows that the  $I$ - $V$  characteristics of a R-hel PA fiber (sample 1) at low temperature also follow the power law  $I(V) \propto V^\beta$  with  $\beta \sim 2.5$ . The same power-law variations for both  $G(T)$  and  $I(V)$  are found for all other polymer fibers and tubes with a variety of power exponents  $\alpha \sim 2.2$ – $7.2$  and  $\beta \sim 2$ – $5.7$ . The variation of  $\alpha$  and  $\beta$  from one fiber to another may result from the fiber cross-section scattering or doping level variation. The parameters for all polymer fibers and tubes under consid-

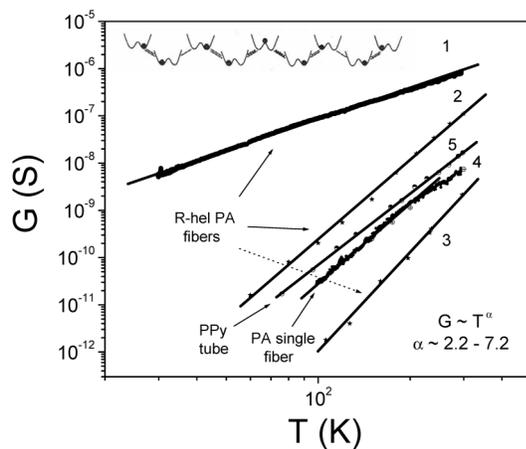


FIG. 2. Conductance vs  $T$  for iodine doped R-hel PA fibers, iodine doped single PA fiber (diameter  $\sim 20$  nm), and PPy nanotube (diameter  $\sim 15$  nm) (samples 1–5 from Table I). Inset shows the coupled double-well potentials with a conjugated defect in PA chain.

eration are summarized in Table I. From these data, it emerges that the power-law variations in  $G(T)$  and  $I(V)$  are a general feature of charge transport in polymer nanofibers and tubes. Note that the similar power-law variations are found for inorganic 1D systems including SWNT and MWNT, ( $\alpha, \beta \sim 0.36$ ) [4,5], InSb ( $\alpha \sim 2$ – $7$ ,  $\beta \sim 2$ – $6$ ) [6], and NbSe<sub>3</sub> ( $\alpha \sim 1$ – $3$ ,  $\beta \sim 1.7$ – $2.7$ ) [7] nanowires, and quantum Hall edge states in GaAs ( $\alpha, \beta \sim 1.4$ – $2.7$ ) [8]. It is evident that polymer fibers and tubes differ from 1D carbon nanotubes and semiconductor nanowires. Each R-hel PA fiber consists of a number of oriented 1D chains, which are for some extent coupled and disordered as a result of doping. Therefore, polymer fibers are in fact quasi-1D and the confinement effects are expected to be not significant. However, the remarkable similarities observed in  $G(T)$  and  $I(V)$  behavior, in particular, with inorganic 1D nanowires, brought us to examine various theoretical models for tunneling in 1D systems.

As a first step, we have fitted the  $G(T)$  curves to 1D variable-range hopping (VRH) [17] and fluctuation-induced tunneling (FIT) [18] models. The 1D VRH implies  $G(T) \propto \exp[-(T_0/T)^p]$  with  $p \sim 0.5$ – $0.75$  depends on the shape of a power-law density of states near the Fermi level. However, even fit with  $p \sim 0.25$  for 3D VRH is too strong to explain the  $G(T)$  for polymer fibers. The latter fluctuation-induced tunneling model reveals an unreasonable fitting parameter to get the power law in  $G(T)$ . Therefore, both of these models do not fit the data well. It is known that for 3D disordered systems in the critical regime of the metal-insulator transition, the temperature dependence of the resistivity,  $\rho(T)$ , follows an universal power law:  $\rho(T) \approx (e^2 p_F / \hbar^2) (k_B T / E_F)^{-1/\eta} \approx T^{-\gamma}$ , where  $p_F$  is the Fermi momentum and  $1 < \eta < 3$ , i.e.,  $0.33 < \gamma < 1$  [19]. This model with  $\gamma < 1$  can explain the transport in nonoriented 3D R-hel PA films at  $T > 30$  K

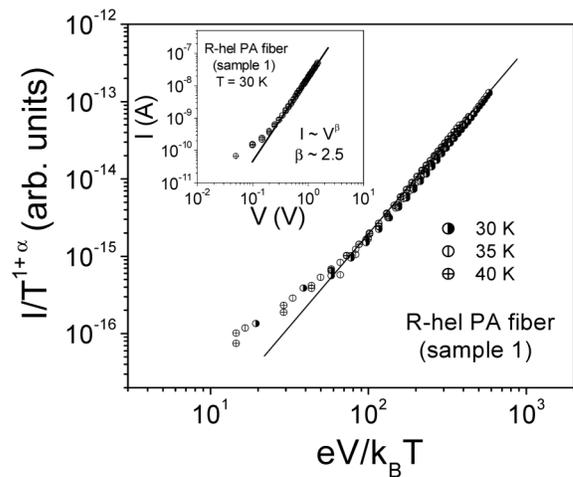


FIG. 3.  $I/T^{\alpha+1}$  vs  $eV/k_B T$  for R-hel PA fiber (sample 1) at different temperatures;  $\alpha \sim 2.8$  is the exponent in  $G(T) \propto T^\alpha$ . The inset shows  $I$ - $V$  curve for sample 1 at  $T = 30$  K.

TABLE I. Polymer fibers and tubes used in transport experiments.

#	Sample	Diameter or Cross Section	$G_{300\text{ K}}$	$\alpha$	$\beta$	Reference
		nm	S		(at min T)	
1	<i>R</i> -hel PA fiber	$65 \times 90$	$8.4 \times 10^{-7}$	2.2	...	this work
				2.8	2.5 (30 K)	"
2	<i>R</i> -hel PA fiber	$60 \times 134$	$1.1 \times 10^{-7}$	5.5	4.8 (50 K)	"
3	<i>R</i> -hel PA fiber	$47 \times 312$	$2.1 \times 10^{-9}$	7.2	5.7 (95 K)	"
4	Single PA fiber	20	$7.3 \times 10^{-9}$	5.6	2.0 (94 K)	[10]
5	PPy tube	15	$1.7 \times 10^{-8}$	5.0	2.1 (56 K)	[16]
6	PPy tube	50	$2.8 \times 10^{-8}$	4.1	2.8 (50 K)	[16]

[13]. However, since  $\gamma > 1$  in the case of polymer fibers, this model is ruled out. The power law  $I(V) \propto V^\beta$ , with  $\beta \approx 2$  is known for the space-charge limited current (SCLC) transport in semiconductors [20]. The values  $\beta > 2$  observed for *R*-hel PA fibers and PPy tubes are inapplicable to the SCLC model. At last, as mentioned above, the power-law variations of  $G(T)$  and  $I(V)$  in inorganic 1D systems, such as SWNT, MWNT, doped semiconductor nanowires are discussed in terms of LL, WC, or ECB theories [4–8]. For a clean LL, a power-law variation  $G(T) \propto T^\alpha$  is predicted at small biases ( $eV \ll k_B T$ ), and  $I(V) \propto V^\beta$  at large biases ( $eV \gg k_B T$ ). The exponents of the power law depend on the number of 1D channels [21]; the LL state survives for a few 1D chains coupled by Coulomb interactions and can be stabilized in the presence of impurities for more than two coupled 1D chains [22]. According to the LL theory,  $I$ - $V$  curves taken at different temperatures should be fitted by the general equation [4,23]:

$$I = I_0 T^{\alpha+1} \sinh(eV/k_B T) |\Gamma(1 + \beta/2 + ieV/\pi k_B T)|^2, \quad (1)$$

where  $\Gamma$  is the Gamma function,  $I_0$  is a constant. The parameters  $\alpha$  and  $\beta$  correspond to the exponents estimated from  $G(T)$  and  $I(V)$  plots. It means that  $I$ - $V$  curves should collapse into a single curve if  $I/T^{\alpha+1}$  is plotted as a function of  $eV/k_B T$ . As can be seen from Fig. 3, all thus scaled  $I$ - $V$  curves for a *R*-hel PA fiber (sample 1) collapse into a single curve at low temperatures by plotting  $I/T^{\alpha+1}$  versus  $eV/k_B T$ , where  $\alpha \sim 2.8$  is the power-law exponent from the  $G(T)$  curve for the same sample. The similar scaled behavior is found for all other *R*-hel PA fibers as well as for a single PA fiber and PPy tubes. We conclude that the power-law variations in  $G(T)$  and  $I(V)$  and the scaled  $I$ - $V$  behavior are characteristic of such quasi-1D systems as polymer fibers and tubes. To a certain degree, this behavior correlates with a LL theory for transport in 1D systems, which implies that both tunneling along LLs through impurity barriers and tunneling between the chains with LLs provide the conduction of a set of coupled LLs. The LL model predicts the correlation between the exponents  $\beta = \alpha + 1$ , however, for all polymer fibers  $\beta \neq \alpha + 1$ , and, moreover,  $\beta$  is always less

than  $\alpha$ , which can not be explained in either LL or ECB theory [5]. Note that the same disagreement with the LL model is found earlier for inorganic 1D nanowires [6,7]. The LL model implies almost purely 1D transport, while the interchain hopping destroys the LL state. In view of the interchain hopping to be one of the main transport mechanisms in conducting polymers at low temperature [9], one can expect the manifestation of the LL state in polymer fibers at relatively high temperatures only. This correlates with our results obtained for *R*-hel PA nanofibers at  $T > 30$  K.

On the other hand, the consideration of repulsive long-range Coulomb interactions is believed to cause a WC, which is pinned by impurity [3,24]. WC occurs in solids with a low electronic density, i.e., with a large parameter  $r_S = a/2a_B$ , where  $a$  is the average distance between electrons and  $a_B$  is the effective Bohr radius. The WC transition has been shown to take place at  $r_S \sim 36$  [25]. Such a pinned WC can adjust its phase in the presence of disorder to optimize the pinning energy gain, similar to classical charge density wave systems. Polymer nanofibers and tubes are quasi-1D conductors with a low electronic density, where WC may occur. Because the molecular structure of PA consists of alternating single and double bonds in the CH chain, those result in the Peierls distortion. This creates the potential wells where the electrons can get trapped in and hence form the WC (see the inset to Fig. 2). At the modest doping level of the PA chain, the distance between impurities (iodine) is of the order 10 nm, so  $r_S$  is large enough to get WC in the PA fiber. When the localization length is larger than the distance between impurities, the tunneling density of states in WC follows a power law [3,24,26] with the exponents  $\sim 3$ -6, [27], similar to those found in  $G(T)$  for polymer nanofibers. However, the impurities in doped conjugated polymers are sited outside of the polymer chains and therefore they only supply charge carriers. This results in the polymer chain either not pinned or pinned weakly by conjugated defects. For a classical 1D WC pinned by impurities, one should expect the VRH regime at low temperature with an exponential  $G(T)$  [17,28]. The absence of effective pinning prevents the observation of VRH in polymer fibers at least at

$T > 30$  K and argues against the WC model; however, this regime may manifest itself at lower temperatures.

Therefore, all models under consideration, namely, VRH, LL, ECB, and WC, cannot describe precisely the power-law variations observed in  $G(T)$  and  $I(V)$  for polymer nanofibers despite the fact that some relationship with LL and WC models is found. We suppose that the real transport mechanism in quasi-1D polymer fibers obeys either the superposition of the above-mentioned models or the single LL-like model valid for the different parts of the metallic polymer fiber separated by intramolecular junctions. By analogy with the LL transport in bent metallic carbon nanotube [29], we suggest that the conductance across the intramolecular junction is much more temperature dependent than that of the two (or more) straight segments, but still obeys the power law  $G(T) \propto T^\alpha$ . In the case of SWNT for the end-to-end tunneling between two LLs separated with intramolecular junction (kink) the power exponent  $\alpha_{\text{end-end}} = (1/g - 1)/2 \sim 1.8$ , where the LL interaction parameter  $g \sim 0.22$ . It was found that for the SWNT with a single kink the exponent  $\alpha = 2.2$  [29], which is close to the calculated value and surprisingly close to the  $\alpha$  value for the most conductive  $R$ -hel PA fiber (sample 1). It is evident from the AFM image (Fig. 1) that  $R$ -hel PA fiber contains kinks at a distance between electrodes  $2 \mu\text{m}$ . In our opinion, each kink in the polymer fiber acts as the tunneling junction between the ends of two LLs. This results in stronger power-law variations in  $G(T)$  and  $I(V)$  with respect to those in a clean LL, and may have caused the above-mentioned contradictions with a pure LL model. In conclusion, we have found that at  $30 \text{ K} < T < 300 \text{ K}$ , the conductance and the current-voltage characteristics of iodine doped helical PA fibers and other conjugated polymer fibers and tubes follow the power laws characteristic of 1D systems, such as LL or WC. At the same time, there is a discrepancy between our results and theories for tunneling in 1D systems.

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