## A haronov-Bohm Signature for Neutral Polarized Excitons in Type-II Quantum Dot Ensembles

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The Aharonov-Bohm effect is commonly believed to be a typical feature of the motion of a charged particle interacting with the electromagnetic vector potential. Here we present a magnetophotoluminescence study of type-II InP/GaAs self-assembled quantum dots, revealing the Aharonov-Bohm-type oscillations for neutral excitons when the hole ground state changes its angular momentum from  $\ell_h = 0$ to  $\ell_h = 1, 2$ , and 3. The hole-ring parameters derived from a simple model are in excellent agreement with the structural parameters for this system.

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In 1959, Aharonov and Bohm proposed an experiment to assess the manifestations of the electromagnetic potentials in the quantum domain [1]. By allowing a charged particle to circulate a confined magnetic field flux region, they showed that, surprisingly, there exist effects of the vector potential on the charged particles moving outside. After the circulation, the particle wave function acquires a phase that is proportional to the magnetic flux contained within the closed path [2]. Therefore, all observable phenomena depend upon the flux  $\Phi$  through the excluded region, and are shown to be periodic with period  $\Phi_0 = hc/e$  [3–5]. This oscillatory characteristic is the signature of the Aharonov-Bohm (AB) effect [1,6].

The definite measurement of the original AB effect was performed by Tonomura et al. in a very clever experiment [6,7]. Investigation and applications of the AB concepts in condensed matter have been carried out in metals [8] and superconductors [3,4,9]. With the advance of lithography and semiconductor growth techniques, it was possible to devise mesoscopic [10,11] and nanoscopic [12,13] devices where many theoretically predicted signatures evidencing ringlike electronic properties [14–16] have been observed by transport experiments. For the case of few electrons, self-assembled quantum rings [17] were used for the observation of the characteristic spectra including excitations of states of different angular momentum [17]. Because of the small sizes of these structures, it was possible for the carriers to maintain the coherence of their wave functions during their motion (at sufficiently low temperatures), thus allowing the observation of relative quantum phase effects (AB-like).

It was proposed that a neutral excitation could also exhibit such an AB oscillatory behavior [18,19]. Electronhole pairs created by optical excitation and bound together via Coulomb interaction (excitons) are a good candidate when either one or both carriers are confined to a ringlike geometry. The existence of the AB oscillations for neutral excitons in semiconductor quantum rings, where both carriers are confined in the rings, has been a matter of controversy in recent years [18,20-24] since some of the work predicted that the AB oscillations might be very weak because of exponentially small electron-tohole tunnel amplitude [18,19] or would vanish for a finite width ring [21,22]. Recently, the AB effect was observed in optical experiments by Bayer et al. on quantum rings fabricated by lithographical methods [25]. They recorded AB oscillations for charged excitons. Perhaps due to the aforementioned reasons, the AB effect was not found in the spectra of *neutral* excitons. The second possibility for observing AB-like oscillations in the optical spectra of a neutral excitation is the case of type-II quantum dots (QD) [19,23,26,27], where the confinement of one carrier inside the QD and the other carrier in the barrier naturally creates a ringlike structure (see Fig. 1). In such a structure, the carrier outside the OD would be bound to



FIG. 1. Sketches of the type-II InP/GaAs QDs: (a) conduction and valence band profiles, indicating the spatial separation of electrons and holes; (b) top view of the QD plane, indicating the holes confined to a ring around the OD due to the Coulomb interaction with the electron trapped into the dot.

that confined in the QD via Coulomb attraction. This spatial charge separation produces a polarization of the exciton and, thus, AB oscillations could be observed in the energy of those carriers that are confined in the ringshaped orbit around the QD. Moreover, the AB effect with a *polarized* exciton may not involve an electron-to-hole tunnel amplitude [19,23]. There are several selfassembled quantum dot systems where a type-II heterojunction is expected; for instance, GaSb on GaAs [28] and Ge on Si [29] provide a three-dimensional confinement for the holes, thereby creating a ringlike potential for the electrons. Alternatively, InP on InGaP [30] and InP on GaAs [31] provide the localization of the electrons in the OD, and consequently a ringlike hole wave function. Figure 1 sketches the valence band potential in a very simplified way, not taking into account the contribution of the strain. It is known that the QD strains the GaAs substrate and cap layer, and that in turn changes the potential landscape in the GaAs, creating an additional ringlike potential around the QD for heavy-hole confinement [32]. The light hole may have a well-like strain-induced potential below the QD [32], however being shallower than the heavy-hole ring potential. InP QDs are particularly suitable for observing oscillatory behavior with AB period  $\Phi_0$ . With diameters of the order of 35 nm, one obtains a period of few Tesla for the AB effect.

Here we present data on InP/GaAs self-assembled quantum dot ensembles where the confined magnetoexcitons trap fluxes in the range of 0-3 flux quanta, corresponding to a magnetic field span of 0-12 T. Samples were grown at different rates and PH<sub>3</sub> fluxes by metalorganic chemical vapor deposition in a commercial reactor on nominally flat semi-insulating Cr-doped GaAs [001] substrates at 550 °C [31]. The structures consisted of a 300 nm undoped GaAs grown at 600 °C buffer layer followed by the QD layer. The islands were then capped with a 50 nm undoped GaAs cap. For this work, the sample with the narrowest luminescence line width (~35 meV) was chosen, representing an ensemble of 3  $\times$  $10^{10}$  QDs/cm<sup>2</sup> [31] with small size dispersion. The dimensions of the QDs were determined by cross-section transmission electron microscopy (TEM) [33], and were found to be  $(32 \pm 6)$  nm and  $(4 \pm 2)$  nm in average diameter and height. The InP QDs are not cylindrically symmetric, being elongated in the [110] direction. The photoluminescence (PL) experiments were performed at 2 K, with magnetic fields up to 12 T (in 0.2 T steps), and using an Ar laser with  $2 \text{ W/cm}^2$  as excitation source. These conditions guaranteed the filling of only the system ground state, allowing the assessment of single particle energies. For higher excitation power, a line broadening and luminescence shift [34] takes place, indicating excited state population, which would complicate our analysis.

Figure 2 shows the InP QDs PL spectra for B = 0 (circles) and B = 12 T (triangles). The total energy shift 126402-2



FIG. 2. PL spectra of the InP QDs for B = 0 (circles) and B = 12 T (triangles). Solid lines are Gaussian fits to the data. The total energy shift is 4.5 meV for 12 T.

within this field range was 4.5 meV. The PL peak intensity increased about 50% from 0 to 12 T, indicating an enhancement of the electron and hole wave function overlap. The spectra for all the field values were fit with a single Gaussian line shape in order to extract the evolution of the PL peak position of the InP QDs as a function of the applied magnetic field,  $E_{PL}(B)$ , which is plotted in Fig. 3(a). There one can see that, instead of the typical monotonic diamagnetic energy shift characteristics of type-I QD [35], the InP QD PL shows an oscillatory behavior in the  $E_{PL}(B)$  curve, very similar to what has been predicted by Kalameitsev and collaborators [19]. In that work, it was expected that the maxima of oscillating part in  $E_{PL}(B)$  would develop every time that the lowerlying carrier state changed its angular momentum from  $\ell_e = 0$  to  $\ell_e = -1$  and so forth. These transitions were seen to occur when  $R^2/l_B^2 \sim |\ell_e|$  [19], with *R* being the ring radius,  $l_B^2 = \hbar/eB$  the magnetic length, and  $\ell_e$  the electron state angular momentum. Rewriting this expression for the holes in InP QDs,  $R \sim (\hbar \ell_h / eB)^{1/2}$  and then by inserting the experimental values of B for the observed plateaulike regions [Fig. 3(a)], an estimate for the hole-ring radius can be obtained. Averaging the results for the three plateaux, a radius of  $R = (16 \pm 1)$  nm is obtained, in agreement to what has been measured by TEM [33].

Nevertheless, it is possible to further elaborate the analysis of the data. The electron ground state of InP/GaAs QDs has been investigated by capacitance spectroscopy (CV) [36]. It has already been established [35] that the lateral confinement for the self-assembled quantum dot can be reasonably modeled by a parabolic potential. The diamagnetic shift of the electron ground state can be described by  $E_e = [(\hbar\omega_0)^2 + (\hbar\omega_c)^2/4]^{1/2}$ [37], with  $\omega_c$  being the cyclotron frequency. For InP/GaAs QDs grown under identical nominal conditions, a



FIG. 3. (a) The PL peak position as a function of the applied magnetic field (solid circles). Three plateaulike structures are clearly observed. The error bars are smaller than the solid circles. (b) Hole energy dependence on the magnetic field (open squares), showing the Aharonov-Bohm oscillations with period  $\phi_0$ . The error bars are the uncertainties on the peak position after the Gaussian fits. The dashed curves are parabolas following Eq. (2) shifted upward by arbitrary energy. Calculated  $E_h$  [Eq. (2)] for a QD ensemble described by a Gaussian size distribution for R, with  $R_{\text{peak}} = 19.1$  nm and full width at half maximum of  $2\Delta R_{\text{CV}} = 1.6$  nm is shown by the solid curve. Note the progressive offsets of the parabola minima for increasing  $\ell_h$ .

characteristic energy of  $\hbar\omega_0 = (5.6 \pm 0.9)$  meV was inferred [36]. Bearing this information in mind, an expression for  $E_{\rm PL}(B)$  can be written, consisting of three terms: a constant contribution, related to the energy gap of the material and the exciton binding energy; the diamagnetic energy shift for the electrons, discussed above; and the variation of the hole energy with the magnetic field [24,26]:

$$E_{\rm PL}(R,B) = E_g + \sqrt{(\hbar\omega_0)^2 + \left(\frac{\hbar\omega_c}{2}\right)^2 + \frac{\hbar^2}{2m_h^*R^2} \left(\ell_h - \frac{\Phi}{\Phi_0}\right)^2},$$
(1)

where  $m_h^*$  is the hole effective mass,  $\Phi_0 = hc/e$  is the flux quantum, and  $\Phi = \pi R^2 B$  is the total magnetic flux through the ring of radius *R*. Using the above result for  $\hbar\omega_0$ , both the constant and the electron contributions in the experimental data [see solid curve in Fig. 3(a)] can be subtracted. The result is shown in Fig. 3(b), where

$$E_h(R, B) = E_{\rm PL}(R, B) - E_g - E_e = \frac{\hbar^2}{2m_h^* R^2} \left(\ell_h - \frac{\Phi}{\Phi_0}\right)^2.$$
(2)

As shown in Fig. 3(b),  $E_h$  (open squares) clearly oscillates as a function of the magnetic field, indicating phase coherence for the hole wave functions. Since  $\Phi_0$  is a 126402-3

constant (the Aharonov-Bohm period of the excitonic energy oscillations [1,6,15]), the experimental data were fit with the parabolas given by Eq. (2), one for each value of  $\ell_h = 0$ , 1, 2, and 3, indicating the number of flux quanta enclosed by the hole ring. The result is shown by the dashed curves in the upper part of Fig. 3(b), from which  $R = (19.1 \pm 0.4)$  nm and  $\Phi_0 = 3.61$  T were obtained. One should keep in mind that the hole ring must have a radius slightly larger than the QD diameter (Fig. 1), and therefore the obtained values are in excellent agreement with the structural and electronic results discussed above [33].

It is worth noting that an ensemble of islands and not a single OD was probed. Nevertheless, the size dispersion did not suppress the AB oscillations. Some considerations can be done on the influence of the size dispersion  $\Delta R$  on the experimental results. From CV experiments [36], an effective size distribution of  $\Delta R_{\rm CV} = 0.8$  nm was inferred for the electron-confining potential. This CV estimate for  $\Delta R$  would be a lower bound for the experimentally probed size dispersion. In order to model in a more quantitative fashion the effect of the QD ensemble on the hole-ring energy oscillations,  $E_h(R, B)$  [Eq. (2)] was calculated and weighted by a Gaussian size distribution function, where R determined in Fig. 3(b) is the central peak radius and  $2\Delta R_{CV}$  is its full width at half maximum. The result is plotted in Fig. 3(b) (solid curve). It can be seen that the main effect of the size dispersion on  $E_h$  is a progressive attenuation of the oscillation intensity, as one would expect, and it is consistent with the decrease in the amplitude of the data in Fig. 3(b). By comparing the data and the solid curve in Fig. 3(b), one can see that the experimental data of the hole ring are consistent with an effective size dispersion obtained from  $\Delta R_{\rm CV}$ .

Although describing the oscillation period and damping in a good agreement with independent structural/ electronic results, this simplified model fails to predict the energy offset of the last parabola (corresponding to  $\ell = 3$ ). The contributions for the offset might be (i) the experimental uncertainty in  $\hbar \omega_0$  obtained from the CV fit [solid curve in Fig. 3(a)]; (ii) a possible dependence of the exciton binding energy on the magnetic field; (iii) deviations from the parabolic lateral confinement due to the actual QD morphology. Deviations from the lateral parabolic potential assumption should be most prominent when  $\hbar \omega_c = 2\hbar \omega_0 \ (B \sim 8 \text{ T})$  and deviations on the exciton binding energy are relevant only for  $\hbar \omega_c > E_{\text{exc}}$  $(B \sim 6-8 \text{ T})$ . There is no quantitative evidence favoring either mechanism. Clearly, a more detailed and complete modeling of the system, including the points indicated above, is needed for understanding all the experimental features presented in Fig. 3(b), but such a task is beyond the scope of the present work. Nevertheless, the simple model used here consistently describes the main physical issues connected to the observation of the hole AB oscillations (Fig. 3).

In summary, we have presented clear evidence of Aharonov-Bohm oscillations in the spectrum of electrically neutral excitons confined in type-II InP/GaAs quantum dots. We have observed the trapping of up to three flux quanta inside the ring trajectory of the hole, for a reasonable span of magnetic fields. Despite the presence of a size dispersion, the AB oscillations were easily observable, evidencing the phase coherence for holes moving around QDs.

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- [1] Y. Aharonov and D. Bohm, Phys. Rev. 115, 485 (1959).
- [2] M.V. Berry, Proc. R. Soc. London, Ser. A 392, 45 (1984).
- [3] N. Byers and C. N. Yang, Phys. Rev. Lett. 7, 46 (1961).
- [4] F. Bloch, Phys. Rev. Lett. 21, 1241 (1968).
- [5] M. Büttiker, Y. Imry, and R. Landauer, Phys. Lett. 96A, 365 (1983).
- [6] For a review on the subject, see M. Peshkin and A. Tonomura, *The Aharonov-Bohm Effect*, in Lecture Notes in Physics Vol. 340 (Springer-Verlag, Berlin 1989).
- [7] A. Tonomura, N. Osakabe, T. Matsuda, T. Kawasaki, J. Endo, S. Yano, and H. Yamada, Phys. Rev. Lett. 56, 792 (1986).
- [8] R. A. Webb, S. Washburn, C. P. Umbach, and R. B. Laibowitz, Phys. Rev. Lett. 54, 2696 (1985); S. Washburn and R. A. Webb, Rep. Prog. Phys. 55, 1311 (1992).
- [9] R. D. Parks and W. A. Little, Phys. Rev. 133, A97 (1964).
- [10] G. Timp, A. M. Chang, J. E. Cunningham, T.Y. Chang, P. Mankiewich, R. Behringer, and R. E. Howard, Phys. Rev. Lett. 58, 2814 (1987).
- [11] C. J. B. Ford, T. J. Thornton, R. Newbury, M. Pepper, H. Ahmed, C. T. Foxon, J. J. Harris, and C. Roberts, J. Phys. C 21, L325 (1988).
- [12] A. Fuhrer, S. Lüscher, T. Ihn, T. Heinzel, K. Ensslin,
  W. Wegscheider, and M. Bichler, Nature (London) 413, 822 (2001); Microelectron. Eng. 63, 47 (2002).
- [13] J.-B. Yau, E. P. De Poortere, and M. Shayegan, Phys. Rev. Lett. 88, 146801 (2002).
- [14] B. L. Al'tshuler, A. G. Aronov, and B. Z. Spivak, Pis'ma Zh. Eksp. Teor. Fiz. 33, 101 (1981) [JETP Lett. 33, 94 (1981)].
- [15] M. Büttiker, Y. Imry, R. Landauer, and S. Pinhas, Phys. Rev. B **31**, 6207 (1985).
- [16] A. G. Aronov and Yu. V. Sharvin, Rev. Mod. Phys. 59, 755 (1987).
- [17] A. Lorke, R. J. Luyken, A. O. Govorov, J. P. Kotthaus, J. M. Garcia, and P. M. Petroff, Phys. Rev. Lett. 84, 2223 (2000).

- [18] A.V. Chaplik, Pis'ma Zh. Eksp. Teor. Fiz. 62, 885 (1995)[JETP Lett. 62, 900 (1995)].
- [19] A. B. Kalameitsev, V. M. Kovalev, and A. O. Govorov, Pis'ma Zh. Eksp. Teor. Fiz. 68, 634 (1998) [JETP Lett. 68, 669 (1998)].
- [20] R. A. Römer and M. E. Raikh, Phys. Rev. B 62, 7045 (2000).
- [21] J. Song and S. E. Ulloa, Phys. Rev. B 63, 125302 (2001).
- [22] H. Hu, J.-L. Zhu, D.-J. Li, and J.-J. Xiong, Phys. Rev. B 63, 195307 (2001).
- [23] A.O. Govorov, A.V. Kalameitsev, R. Warburton, K. Karrai, and S.E. Ulloa, Physica (Amsterdam) 13E, 297 (2002).
- [24] A.O. Govorov, S. E. Ulloa, K. Karrai, and R.J. Warburton, Phys. Rev. B 66, 081309 (2002); S.E. Ulloa, A.O. Govorov, A.V. Kalameitsev, R. Warburton, and K. Karrai, Physica (Amsterdam) 12E, 790 (2002); A.V. Maslov and D.S. Citrin, Phys. Rev. B 67, 121304 (2003).
- [25] M. Bayer, M. Korkusinski, P. Hawrylak, T. Gutbrod, M. Michel, and A. Forchel, Phys. Rev. Lett. 90, 186801 (2003).
- [26] K. L. Janssens, B. Partoens, and F. M. Peeters, Phys. Rev. B 64, 155324 (2001).
- [27] K. L. Janssens, B. Partoens, and F. M. Peeters, Phys. Rev. B 66, 075314 (2002).
- [28] F. Hatami, N. N. Ledentsov, M. Grundmann, J. Böhrer, F. Heinrichsdorff, M. Beer, D. Bimberg, S. S. Ruvimov, P. Werner, U. Gösele, J. Heydenreich, U. Richter, S. V. Ivanov, B. Ya. Meltser, P. S. Kop'ev, and Zh. I. Alferov, Appl. Phys. Lett. 67, 656 (1995).
- [29] P. Schittenhelm, M. Gail, J. Brunner, J. F. Nützel, and G. Abstreiter, Appl. Phys. Lett. 67, 1292 (1995); A. I. Yakimov, N. P. Stepina, A.V. Dvurechenskii, A. I. Nikiforov, and A.V. Nenashev, Phys. Rev. B 63, 045312 (2001).
- [30] M. Hayne, R. Provoost, M. K. Zundel, Y. M. Manz,
  K. Eberl, and V.V. Moshchalkov, Phys. Rev. B 62, 10324 (2000); M. Sugisaki, H.-W. Hen, S.V. Nair,
  K. Nishi, and Y. Masumoto, Phys. Rev. B 66, 235309 (2002).
- [31] E. Ribeiro, R. L. Maltez, W. Carvalho, Jr., D. Ugarte, and G. Medeiros-Ribeiro, Appl. Phys. Lett. 81, 2953 (2002).
- [32] Z. Xu and P. M. Petroff, J. Appl. Phys. 69, 6564 (1991).
- [33] R. L. Maltez, E. Ribeiro, W. Carvalho, Jr., D. Ugarte, and G. Medeiros-Ribeiro, J. Appl. Phys. 94, 3051 (2003).
- [34] M. K. K. Nakaema, F. Iikawa, M. J. S. P. Brasil, E. Ribeiro, G. Medeiros-Ribeiro, W. Carvalho, Jr., M. Z. Maialle, and M. H. Degani, Appl. Phys. Lett. 81, 2743 (2002).
- [35] P. D. Wang, J. L. Merz, S. Fafard, R. Leon, D. Leonard, G. Medeiros-Ribeiro, M. Oestreich, P. M. Petroff, K. Uchida, N. Miura, H. Akiyama, and H. Sakaki, Phys. Rev. B 53, 16458 (1996); L. R. Wilson, D. J. Mowbray, M. S. Skolnick, M. Morifuji, M. J. Steer, I. A. Larkin, and M. Hopkinson, Phys. Rev. B 57, 2073 (1998); M. Hayne, J. Maes, V.V. Moshchalkov, Y. M. Manz, O. G. Schmidt, and K. Eberl, Appl. Phys. Lett. 79, 45 (2001).
- [36] C.C.B. Bufon *et al.* (to be published).
- [37] V. Fock, Z. Phys. 47, 446 (1928).