Erratum: Complex Extension of Quantum Mechanics [Phys. Rev. Lett. 89, 270401 (2002)]

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This Erratum corrects an error concerning the condition for a linear operator to be an observable in \mathcal{PT} -symmetric quantum mechanics. The incorrect statement of this condition on line 2, p. 270401-4, reads that an observable is "one that commutes with $C\mathcal{PT}$." The correct statement is that "an observable \mathcal{A} satisfies $\tilde{A} = C\mathcal{PT} \ \mathcal{A} \ C\mathcal{PT}$, where $\tilde{}$ signifies transpose."(The transpose operation was inadvertently omitted.) This condition guarantees that the expectation value of \mathcal{A} is real and the condition is preserved under time evolution if $H = \tilde{H}$. In conventional quantum mechanics, where $C = \mathcal{P}$, this condition reduces to the usual Hermiticity condition $\tilde{A} = \mathcal{A}^*$. The symmetry requirement $H = \tilde{H}$ holds for all continuum \mathcal{PT} -symmetric models that we have discussed, but it requires that t = s in Eqs. (15) and (16). These corrections do not alter the conclusions of the Letter in any way.

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