

## Resonance Peak in Sr<sub>2</sub>RuO<sub>4</sub>: Signature of Spin Triplet Pairing

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We study the dynamical spin susceptibility,  $\chi(\mathbf{q}, \omega)$ , in the normal and superconducting states of Sr<sub>2</sub>RuO<sub>4</sub>. In the normal state, we find a peak in the vicinity of  $\mathbf{Q}_T = (0.72\pi, 0.72\pi)$  in agreement with recent inelastic neutron scattering experiments. We predict that for spin triplet pairing in the superconducting state a *resonance peak* appears in the out-of-plane component of  $\chi$ , but is absent in the in-plane component. In contrast, no resonance peak is expected for spin singlet pairing.

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The superconducting (SC) state of Sr<sub>2</sub>RuO<sub>4</sub> has been the focus of intense experimental and theoretical research over the last few years. Sr<sub>2</sub>RuO<sub>4</sub> is isostructural with the high-temperature superconductor (HTSC) La<sub>2-x</sub>Sr<sub>x</sub>CuO<sub>4</sub> and is the only known layered perovskite which is superconducting in the absence of Cu [1]. Understanding the pairing mechanism in Sr<sub>2</sub>RuO<sub>4</sub> could therefore provide important insight into the origin of unconventional superconductivity in general, and that of the HTSC in particular. Since a related compound, SrRuO<sub>3</sub>, is a ferromagnet, it was suggested [2] that Sr<sub>2</sub>RuO<sub>4</sub> is a triplet superconductor in which the pairing is mediated by ferromagnetic paramagnons. Experimental support for spin triplet pairing comes from Knight shift (KS) [3] and elastic neutron scattering (ENS) measurements [4], while muon spin resonance [5] provides evidence for a broken time-reversal symmetry in the SC state. However, the momentum dependence of the superconducting gap is still unclear. While originally a *p*-wave symmetry, belonging to the *E<sub>u</sub>* representation of the *D<sub>4h</sub>* point group, was proposed for the superconducting gap [2,6],  $\Delta(\mathbf{k}) \sim k_x + ik_y$ , recent specific heat [7], thermal conductivity [8], penetration depth [9], and nuclear magnetic resonance [10] experiments suggest the presence of line nodes in  $\Delta(\mathbf{k})$  and thus pairing with higher orbital momentum.

The spin susceptibility,  $\chi(\mathbf{q}, \omega)$ , is an important input parameter for any theory ascribing the pairing mechanism in Sr<sub>2</sub>RuO<sub>4</sub> to the exchange of spin fluctuations. In this Letter we present a scenario for the momentum and frequency dependence of  $\chi(\mathbf{q}, \omega)$ , both in the normal and superconducting states. In the normal state, we find a peak in  $\text{Im}\chi$  whose momentum position is close to that reported by Sidis *et al.* [11] in inelastic neutron scattering (INS) experiments. Our results for  $\text{Re}\chi$  agree with the prediction by Mazin and Singh [12] of a peak in the normal state static susceptibility,  $\chi(\mathbf{q}, \omega = 0)$ , around  $\mathbf{q} = (2\pi/3, 2\pi/3)$ . We show that for triplet pairing in the superconducting state the in-plane,  $\chi_{\pm} = (\chi_{xx} + \chi_{yy})/2$ , and out-of-plane,  $\chi_{zz}$ , components of the dynamic spin susceptibility are qualitatively different. In particular, we predict that a *resonance peak*, similar to the one observed

in the HTSC [13], appears in  $\chi_{zz}$ , but is absent in  $\chi_{\pm}$ . Since no resonance peak exists for spin singlet pairing, it is an important signature of spin triplet superconductivity.

Contributions to the dynamic spin susceptibility in Sr<sub>2</sub>RuO<sub>4</sub> come from three electronic bands which are derived from the Ru 4d-*xy*, -*xz*, and -*yz* orbitals. A comparison of angle-resolved photoemission (ARPES) [14] and de Haas-van Alphen (dHvA) [15] experiments with band-structure calculations [16] shows a substantial hybridization only between the *xz* and *yz* orbitals, with a resulting holelike ( $\alpha$  band) and electronlike Fermi surface (FS) ( $\beta$  band), while the decoupled *xy* orbitals give rise to the electronlike  $\gamma$  band [17]. Thus the electronic structure of Sr<sub>2</sub>RuO<sub>4</sub> can be described by the tight-binding Hamiltonian

$$\mathcal{H} = \sum_{\mathbf{k}, \sigma} \epsilon_{\mathbf{k}}^{xy} c_{\mathbf{k}, \sigma}^{\dagger} c_{\mathbf{k}, \sigma} + \sum_{\mathbf{k}, \sigma} \epsilon_{\mathbf{k}}^{xz} a_{\mathbf{k}, \sigma}^{\dagger} a_{\mathbf{k}, \sigma} + \sum_{\mathbf{k}, \sigma} \epsilon_{\mathbf{k}}^{yz} b_{\mathbf{k}, \sigma}^{\dagger} b_{\mathbf{k}, \sigma} - \sum_{\mathbf{k}, \sigma} (t_{\perp} a_{\mathbf{k}, \sigma}^{\dagger} b_{\mathbf{k}, \sigma} + \text{H.c.}), \quad (1)$$

where  $c_{\mathbf{k}}^{\dagger}$ ,  $a_{\mathbf{k}}^{\dagger}$ ,  $b_{\mathbf{k}}^{\dagger}$  are the fermionic creation operators in the *xy*, *xz*, and *yz* bands, with spin  $\sigma$ , respectively. The normal state tight-binding dispersions are given by [16]

$$\epsilon_{\mathbf{k}}^i = -2t_x \cos k_x - 2t_y \cos k_y + 4t' \cos k_x \cos k_y - \mu, \quad (2)$$

with  $(t_x, t_y, t', \mu) = (0.44, 0.44, -0.14, 0.50)$  eV,  $(0.31, 0.045, 0.01, 0.24)$  eV,  $(0.045, 0.31, 0.01, 0.24)$  eV for the  $i = xy, xz, yz$  bands, respectively, and  $t_{\perp}$  reflecting the hybridization between the *xz* and *yz* bands. After diagonalizing the Hamiltonian, Eq. (1), we obtain the energy dispersions for the  $\gamma$  and hybridized  $\alpha$  and  $\beta$  bands

$$\epsilon_{\alpha, \beta}(\mathbf{k}) = \epsilon_{\mathbf{k}}^{\pm} \mp \sqrt{(\epsilon_{\mathbf{k}}^{\pm})^2 + t_{\perp}^2}, \quad \epsilon_{\gamma}(\mathbf{k}) = \epsilon_{\mathbf{k}}^{xy}, \quad (3)$$

with  $\epsilon_{\mathbf{k}}^{\pm} = (\epsilon_{\mathbf{k}}^{xz} \pm \epsilon_{\mathbf{k}}^{yz})/2$ . By fitting the area and shape of the  $\alpha$  and  $\beta$  FS to those observed by ARPES [14] and dHvA experiments [15], we obtain  $t_{\perp} \approx 0.1$  eV; the Fermi surfaces for all three bands are shown in Fig. 1.

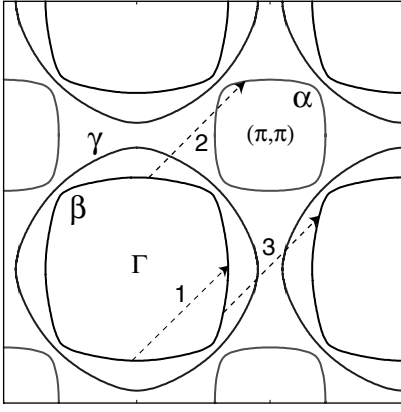


FIG. 1. Fermi surfaces of  $\text{Sr}_2\text{RuO}_4$  in the extended Brillouin zone. The arrows show quasiparticle excitations with nesting wave vector  $\mathbf{Q}_i = (0.72\pi, 0.72\pi)$  and lattice constant  $a = 1$ .

The superconducting gap for unitary spin triplet pairing can be written as

$$\Delta_{\zeta\eta}(\mathbf{k}) = [\mathbf{d}(\mathbf{k}) \cdot \boldsymbol{\sigma} i \sigma_2]_{\zeta\eta}, \quad (4)$$

where  $\boldsymbol{\sigma}$  are the Pauli matrices. We assume that spin-orbit coupling locks the  $\mathbf{d}$  vector along the crystal  $\hat{c}$  axis, i.e.,  $\mathbf{d} \parallel \hat{z} \parallel \hat{c}$ , consistent with KS [3] and ENS [4] experiments. In the following, we consider a superconducting gap with “ $f_{xy}$ -wave” ( $E_u$ ) symmetry,

$$d_z(\mathbf{k}) = \Delta(\mathbf{k}) = \Delta_0 \sin k_x \sin k_y (\sin k_x + i \sin k_y), \quad (5)$$

which was shown [18] to be consistent with the low-temperature power laws observed in specific heat and thermal conductivity experiments. Our conclusions are, however, insensitive to the detailed form of the gap function for triplet pairing. We take  $\Delta_0 \approx 1$  meV as reported by Andreev point-contact spectroscopy [19].

For spin triplet pairing, and isotropic spin fluctuations, the unrenormalized band susceptibility is given by [20]

$$\chi_{ij}^{rs}(\mathbf{p}) = -\frac{1}{2} \sigma_{\zeta\eta}^i \sigma_{\tau\delta}^j T \sum_{\mathbf{k}, m} \mathcal{A}_{\mathbf{k}, \mathbf{q}}^{rs} \{G_{\eta\tau}^r(\mathbf{l}) G_{\delta\zeta}^s(\mathbf{l} + \mathbf{p}) - [F_{\zeta\tau}^r(\mathbf{l})]^* F_{\eta\delta}^s(\mathbf{l} + \mathbf{p})\}, \quad (6)$$

where  $r, s = \alpha, \beta, \gamma$  are band indices,  $\mathbf{p} = (\mathbf{q}, i\omega_n)$ ,  $\mathbf{l} = (\mathbf{k}, i\nu_m)$  are four-vectors, and

$$G_{\eta\tau}^r(\mathbf{l}) = -\delta_{\eta\tau} \frac{i\nu_m + \epsilon_r(\mathbf{k})}{\nu_m^2 + E_r^2(\mathbf{k})}, \quad (7)$$

$$F_{\eta\tau}^r(\mathbf{l}) = \frac{\Delta_{\eta\tau}(\mathbf{k})}{\nu_m^2 + E_r^2(\mathbf{k})}$$

are the normal and anomalous Greens functions, respectively, with  $E_r(\mathbf{k}) = \sqrt{\epsilon_r^2(\mathbf{k}) + |\Delta_{\mathbf{k}}|^2}$ . The hybridization between the bands is reflected in

$$\mathcal{A}_{\mathbf{k}, \mathbf{q}}^{rs} = \frac{1}{2} \pm \frac{\epsilon_{\mathbf{k}}^- \epsilon_{\mathbf{k}+\mathbf{q}}^- + t_{\perp}^2}{2\sqrt{(\epsilon_{\mathbf{k}}^-)^2 + t_{\perp}^2} \sqrt{(\epsilon_{\mathbf{k}+\mathbf{q}}^-)^2 + t_{\perp}^2}}, \quad (8)$$

where the upper (lower) sign applies to  $rs = \alpha\alpha, \beta\beta$  ( $rs = \alpha\beta, \beta\alpha$ ),  $\mathcal{A}^{\gamma\gamma} = 1$ , and  $\mathcal{A}^{rs} = 0$  otherwise. In what follows we distinguish between  $\chi_{ij}^{\text{hyb}} = \chi_{ij}^{\alpha\alpha} + \chi_{ij}^{\beta\beta} + 2\chi_{ij}^{\alpha\beta}$ , which arises from intra- and interband quasiparticle transitions in the  $\alpha$  and  $\beta$  bands, and  $\chi_{ij}^{\gamma} \equiv \chi_{ij}^{\gamma\gamma}$  due to quasiparticle excitations in the  $\gamma$  band. Note that the out-of-plane susceptibility,  $\chi_{zz}(\mathbf{p})$ , and in-plane susceptibility,  $\chi_{\pm}(\mathbf{p})$ , differ in the form of their superconducting coherence factors, which as we show below, give rise to their *qualitatively* different frequency and momentum dependence. Finally, the bare susceptibility, Eq. (6), in correlated electron systems is renormalized by an effective quasiparticle interaction,  $U$ , and one has in random-phase approximation (RPA)

$$\bar{\chi}_{ij}^{\text{hyb}, \gamma} = \chi_{ij}^{\text{hyb}, \gamma} (1 - U \chi_{ij}^{\text{hyb}, \gamma})^{-1}. \quad (9)$$

In Fig. 2 we present the normal state susceptibility,  $\chi_{\text{NS}} = (\chi_{zz} + 2\chi_{\pm})/3$ , obtained from Eq. (6) with  $\Delta_0 = 0$

for  $\omega = 6.0$  meV along the momentum path shown in the inset. In the vicinity of  $(\pi, \pi)$ ,  $\chi_{\text{NS}}^{\text{hyb}}$  exhibits peaks at  $\mathbf{Q}_i$  and  $\mathbf{P}_i$ , arising from the nesting properties of the  $\alpha$  and  $\beta$  bands, while  $\chi_{\text{NS}}^{\gamma}$  provides only a weakly  $\mathbf{q}$ -dependent background [21]. Moreover, for  $q \rightarrow 0$  the form of  $\text{Im}\chi_{\text{NS}}^{\text{hyb}} \sim q^{-1}$  reflects the predominantly one-dimensional (1D) character of the  $xz, yz$  bands, while  $\text{Im}\chi_{\text{NS}}^{\gamma} \sim \omega/q$  arises from a cylindrical  $xy$  band.

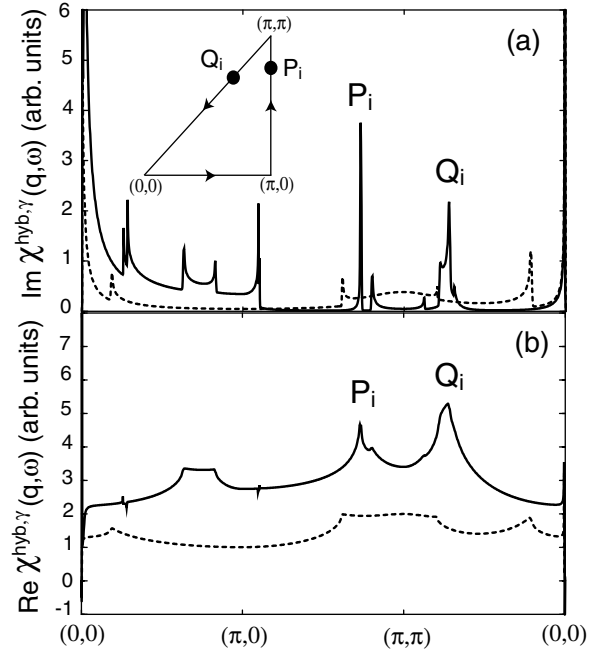


FIG. 2.  $\mathbf{q}$  scans of (a)  $\text{Im}\chi_{\text{NS}}^i$ , and (b)  $\text{Re}\chi_{\text{NS}}^i$  for  $i = \text{hyb}$  (solid line) and  $i = \gamma$  (dashed line) at  $\omega = 6.0$  meV and  $T = 1.0$  meV. Inset (a): Path of  $\mathbf{q}$  scan with filled circles showing nesting wave vectors  $\mathbf{Q}_i$  and  $\mathbf{P}_i$ .

In Fig. 3 we present the RPA susceptibility,  $\bar{\chi}_{\text{NS}}$ , in the normal state. A fit of our results, Eq. (9), to the measured  $\omega$  dependence of  $\text{Im}\chi_{\text{NS}}$  at  $\mathbf{Q}_i$  (see inset) yields  $U = 0.175$  eV [22] in agreement with Ref. [12]. Because of the  $\mathbf{q}$  structure of  $\text{Re}\chi_{\text{NS}}^{\text{hyb}}$  (Fig. 2b), and the weak  $\mathbf{q}$  dependence of  $U$  [12],  $\text{Im}\bar{\chi}_{\text{NS}}^{\text{hyb}}$  is reduced from its bare value for small  $\mathbf{q}$ , but still possesses peaks at  $\mathbf{Q}_i$  and  $\mathbf{P}_i$ . In contrast,  $\bar{\chi}_{\text{NS}}^{\gamma}$  is strongly suppressed for all  $\mathbf{q}$ . Thus, the experimentally observed peak close to  $\mathbf{Q}_i$  arises primarily from  $\text{Im}\bar{\chi}_{\text{NS}}^{\text{hyb}}$  and the strongest SC pairing most likely occurs between electrons in the  $\beta$  band.

In Fig. 4a we present the frequency dependence of  $\text{Im}\chi^{\text{hyb}}$  at  $\mathbf{Q}_i$  in the normal and superconducting states. There exist three channels for quasiparticle excitations with wave vector  $\mathbf{Q}_i$  which contribute to  $\text{Im}\chi^{\text{hyb}}$ , as indicated by arrows in Fig. 1. In the normal state all three channels are excited in the low frequency limit, which yields  $\text{Im}\chi_{\text{NS}}^{\text{hyb}} \sim \omega$ , in agreement with our numerical results in Fig. 4a. The dominant contribution to  $\text{Im}\chi^{\text{hyb}}$ , both in the normal and the superconducting states, arises from excitations of type (3), since (i) they are intraband  $xz$  (or  $yz$ ) transitions and thus independent of  $t_{\perp}$ , and (ii) the FS exhibits the largest nesting in this region of momentum space.

In the superconducting state excitations (1)–(3) possess nonzero threshold energies,  $\omega_{cn}$  with  $n = 1, 2, 3$ , that are determined by the momentum dependence of the order parameter and the shape of the Fermi surface. Specifically,  $\omega_{cn} = |\Delta_{\mathbf{k}}| + |\Delta_{\mathbf{k}+\mathbf{Q}_i}|$ , where  $\mathbf{k}$  and  $\mathbf{k} + \mathbf{Q}_i$  both lie on the Fermi surface, as shown in Fig. 1. For the band parameters chosen, we obtain  $\omega_{c1} \approx 0.15\Delta_0$ ,  $\omega_{c2} \approx 0.8\Delta_0$ ,

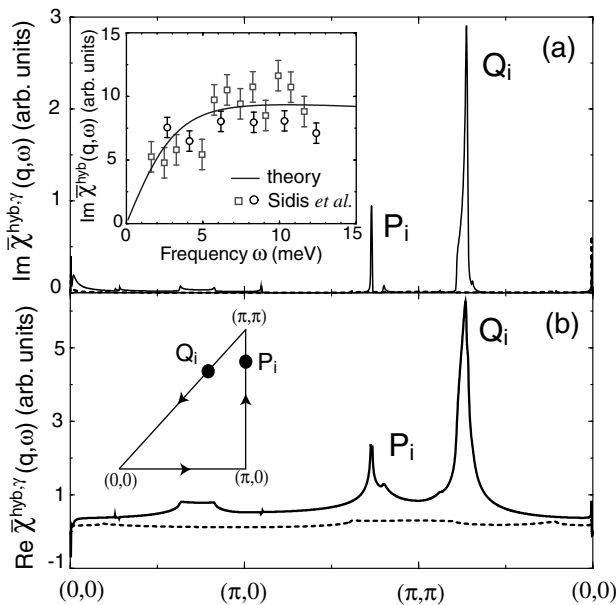


FIG. 3.  $\mathbf{q}$  scans for  $\bar{\chi}_{\text{NS}}^{\text{hyb}}$  (solid line) and  $\bar{\chi}_{\text{NS}}^{\gamma}$  (dashed line) for the same parameters as shown in Fig. 2. Inset (a): Fit of  $\text{Im}\bar{\chi}^{\text{hyb}}$  at  $\mathbf{Q}_i$  to the data of Ref. [11];  $\text{Im}\bar{\chi}$  is multiplied by a mass enhancement factor  $m^*/m_{\text{band}} \sim 4$  in agreement with dHvA experiments [15,23].

and  $\omega_{c3} \approx 2.1\Delta_0$ . Since excitations (1)–(3) are well separated in frequency, we can identify their relative contribution to  $\text{Im}\chi_{zz,\pm}^{\text{hyb}}$ . While  $\omega_{c1}$  cannot be observed in the frequency dependence of  $\text{Im}\chi_{zz,\pm}^{\text{hyb}}$  due to the negligible spectral weight of excitation (1),  $\omega_{c2}$  and  $\omega_{c3}$  can clearly be identified. The large spectral weight of excitation (3) likely makes  $\omega_{c3}$  the experimentally observable spin gap. Moreover, due to the superconducting coherence factors which appear in the calculation of  $\chi_{zz,\pm}^{\text{hyb}}$ , the overall frequency dependencies of the in-plane and out-of-plane components of  $\text{Im}\chi^{\text{hyb}}$  are *qualitatively* different. Specifically, since  $\text{Re}(\Delta_{\mathbf{k}}\Delta_{\mathbf{k}+\mathbf{q}}^*)$  is negative for transition (3), but positive for transition (2),  $\text{Im}\chi_{zz}^{\text{hyb}}$  ( $\text{Im}\chi_{\pm}^{\text{hyb}}$ ) exhibits a sharp jump at  $\omega_{c3}$  ( $\omega_{c2}$ ) and increases continuously at  $\omega_{c2}$  ( $\omega_{c3}$ ). Consequently,  $\text{Re}\chi_{zz}^{\text{hyb}}$  ( $\text{Re}\chi_{\pm}^{\text{hyb}}$ ) possesses a logarithmic divergence at  $\omega_{c3}$  ( $\omega_{c2}$ ).

In Fig. 4b we present the RPA susceptibility,  $\text{Im}\bar{\chi}_{zz,\pm}^{\text{hyb}}$ , in the superconducting state, assuming that  $U$  remains unchanged below  $T_c$ . Because of the logarithmic divergence of  $\text{Re}\chi_{zz}^{\text{hyb}}$  at  $\omega_{c3}$ ,  $\text{Im}\bar{\chi}_{zz}^{\text{hyb}}$  exhibits a *resonance* peak at

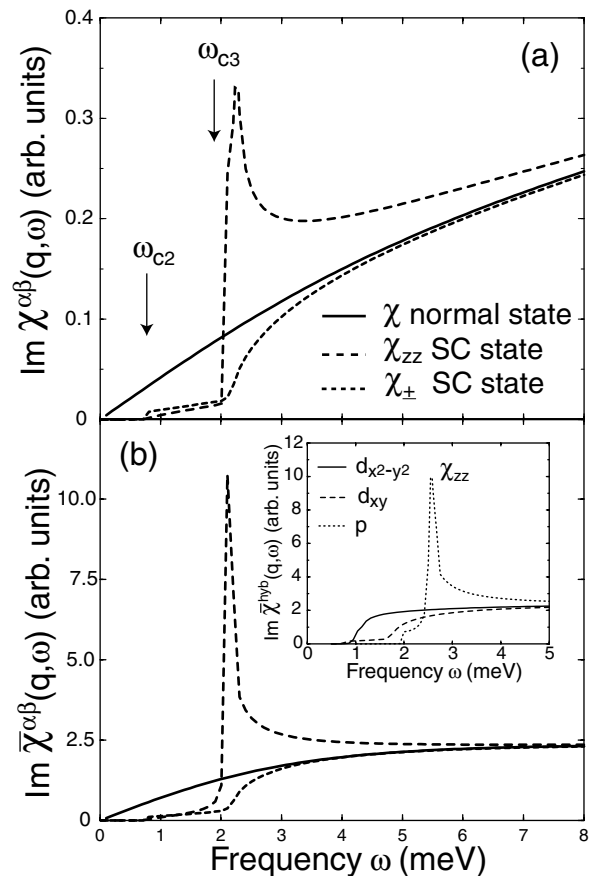


FIG. 4. Spin susceptibilities at  $\mathbf{Q}_i$  for the  $f_{xy}$ -wave state at  $T = 0$ : (a) bare susceptibility,  $\text{Im}\chi^{\text{hyb}}$ ; (b) RPA susceptibility,  $\text{Im}\bar{\chi}^{\text{hyb}}$ , for  $U = 0.175$  eV. The frequency integral of  $\text{Im}\bar{\chi}^{\text{hyb}}(\mathbf{Q}_i)$  up to 15 meV remains constant through  $T_c$ . Inset: For spin singlet states with  $d_{xy}$  or  $d_{x^2-y^2}$  symmetry  $\text{Im}\bar{\chi}_{zz}^{\text{hyb}}$  shows *no* resonance peak, contrary to the spin triplet  $p$ -wave state.

a frequency slightly below  $\omega_{c3}$ . In contrast,  $\text{Im}\bar{\chi}_{\pm}^{\text{hyb}}$  increases continuously above  $\omega_{c3}$ . The logarithmic divergence of  $\text{Re}\chi_{\pm}^{\text{hyb}}$  at  $\omega_{c2}$  is rapidly smoothed out for finite quasiparticle damping due to its small prefactor and is likely experimentally not observable. Thus, we predict that for triplet pairing  $\text{Im}\bar{\chi}_{zz}^{\text{hyb}}$  and  $\text{Im}\bar{\chi}_{\pm}^{\text{hyb}}$  possess *qualitatively* different frequency dependencies at  $\mathbf{Q}_i$  with only  $\text{Im}\bar{\chi}_{zz}^{\text{hyb}}$  exhibiting a resonance peak below  $\omega_{c3}$ . In contrast, a resonance peak was predicted in Refs. [24,25] for the in-plane component  $\text{Im}\bar{\chi}_{\pm}$ , but not for  $\text{Im}\bar{\chi}_{zz}$ . A comparison of our results for  $\chi_{zz,\pm}$  with those in [24,25] suggests that the SC coherence factors for  $\chi_{zz,\pm}$  have been interchanged in Refs. [24,25]. We obtain the correct  $\omega, q \rightarrow 0$  limit only for the SC coherence factors which appear in our results for  $\chi_{zz,\pm}$  in Eq. (6). In this case, we find that  $\text{Re}\chi_{zz}$  decreases below  $T_c$  when a SC gap opens, while  $\text{Re}\chi_{\pm}$  remains unchanged. As shown by Leggett [26], this result is a general property of any unitary state if  $\mathbf{d}||\hat{c}$ .

Our results are insensitive to details of the electronic band structure or the symmetry of the gap function for spin triplet pairing. In particular, for a nodeless superconducting gap with “ $p$ -wave” symmetry [2],  $\Delta(\mathbf{k}) = \Delta_0(\sin k_x + i \sin k_y)$ , belonging to the  $E_u$  representation, the frequency and momentum dependence of  $\text{Im}\bar{\chi}_{zz,\pm}^{\text{hyb}}$  remain to a large extent unchanged from that shown in Fig. 4b (see inset); a resonance peak appears again only in  $\text{Im}\bar{\chi}_{zz}^{\text{hyb}}$ . In contrast, for spin singlet pairing the in-plane and out-of-plane susceptibilities are identical and no resonance peak exists in  $\text{Im}\bar{\chi}^{\text{hyb},\gamma}$ . In the inset of Fig. 4 we plot  $\text{Im}\bar{\chi}^{\text{hyb}}$  at  $\mathbf{Q}_i$  as a function of frequency for SC gaps with  $d_{x^2-y^2}$  symmetry,  $\Delta(\mathbf{k}) = \Delta_0(\cos k_x - \cos k_y)/2$ , and  $d_{xy}$  symmetry,  $\Delta(\mathbf{k}) = \Delta_0 \sin k_x \sin k_y$ , with  $\Delta_0 = 1$  meV. In both cases,  $\text{Im}\bar{\chi}^{\text{hyb}}$  increases continuously above  $\omega_{c3}$ , since  $\Delta(\mathbf{k})$  does *not* change sign for excitation (3) and no logarithmic singularity occurs in  $\text{Re}\chi^{\text{hyb}}$ . In contrast, for the FS geometry of the HTSC and a SC gap with  $d_{x^2-y^2}$  symmetry, one finds  $\Delta_{\mathbf{k}}\Delta_{\mathbf{k}+\mathbf{Q}} < 0$ , which as described above leads to a resonance peak at  $\mathbf{Q} = (\pi, \pi)$  [27]. A resonance peak is thus *not* an intrinsic property of singlet or triplet superconductivity, but arises from the interplay of FS topology and symmetry of the SC gap.

An additional contribution to  $\chi_{\pm}$  in the SC state can in principle come from a coupling of the spin density to in-plane fluctuations of  $\mathbf{d}$ . However, for the  $\mathbf{q}$ -independent coupling assumed in Ref. [24], we find that these fluctuation contributions (FC) are 3 orders of magnitude smaller than those coming from Eq. (6). Moreover, the spin-orbit coupling present in  $\text{Sr}_2\text{RuO}_4$  introduces a gap for in-plane fluctuations of  $\mathbf{d}$  which further suppresses the FC to  $\chi_{\pm}$  and renders them irrelevant.

In summary, we present a scenario for the spin susceptibility in the normal and SC states of  $\text{Sr}_2\text{RuO}_4$ . In the normal state we find a peak close to the experimentally observed position at  $\mathbf{Q}_i$ . For spin triplet pairing in the superconducting state we show that the momentum and frequency dependence of  $\text{Im}\bar{\chi}_{zz}$  and  $\text{Im}\bar{\chi}_{\pm}$  are *qualitatively*

different. We predict the appearance of a resonance peak in  $\text{Im}\bar{\chi}_{zz}$ , similar to the one observed in the HTSC, and its absence in  $\text{Im}\bar{\chi}_{\pm}$ . Finally, we show that no resonance peak exists for spin singlet pairing.

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