

## Superparamagnetic Spin Dynamics Studied Using Selective Excitation Double Mössbauer Spectroscopy

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A detailed study of spin dynamics in a 6 nm  $\text{Fe}_3\text{O}_4$  ferrofluid using a substantially improved selective excitation double Mössbauer (SEDM) experimental technique has led to the unambiguous separation of static disorder, collective excitations, and moment reversals. Superparamagnetic spin flips have been observed through the appearance of an additional line in the SEDM spectrum, defining the energy transitions during relaxation, with frequencies of  $2.5 \pm 0.3$  MHz at 70 K to  $9.7 \pm 1.0$  MHz at 110 K. SEDM offers a precise window into the dynamics and blocking behavior of fine particle systems.

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The basic building block of a superparamagnetic fine particle system is an exchange-coupled assembly of magnetic moments no larger than a single magnetic domain [1]. If, for simplicity, this particle can be described as having a single axis along which the magnetization prefers to lie, then the energy necessary to tilt the moment away from this easy axis by an angle  $\theta$  can be written as  $E = -KV \cos^2(\theta)$ , where  $K$  is the anisotropy constant of the particle and  $V$  is its volume. At high temperatures, when the thermal energy ( $kT$ ) is very much larger than the energy barrier  $KV$ , the moment can adopt any orientation within the particle and thermal fluctuations cause the average magnetization to be zero. As the temperature is lowered, the continuous tumbling is gradually replaced by  $180^\circ$  moment flips between the two easy directions. With decreasing temperature, the time between these superparamagnetic reversals increases until it is comparable to the measuring time of an experiment; below this temperature,  $T_B$ , the moment will appear to be stationary, or blocked. Once  $kT \ll KV$ , the probability of a magnetization reversal in a given time becomes vanishingly small, and a large particle magnetization is observed. Although no longer superparamagnetic, the moment direction continues to fluctuate about the easy axis, causing the observed particle moment to be slightly reduced. These small amplitude collective excitations can be viewed as the particle moment rocking in its potential well [2]. The amplitude of the collective excitations diminishes with temperature until the particle moment is ultimately frozen along its easy axis and the system is static.

In real fine particle systems, the situation is complicated by the presence of interparticle interactions and a distribution of particle sizes. Interactions arise because particles are generally close enough to be affected by the dipole fields from neighboring particles. These fields tend to cause a reduction in the effective anisotropy,  $K$  [3], modifying  $T_B$  and contributing to static magnetic disorder. In addition, any distribution of particle sizes will smear out the simple behavior described above. At any given temperature, the smallest particles will be superparamagnetic,

while others undergo collective excitations and the largest particles are essentially static. The blocking temperature becomes more difficult to define in the presence of a broad particle size distribution as various measuring techniques exhibit differing sensitivities to regions of the size distribution. For example, magnetization is dominated by the response of the larger, slower particles, while the majority of the susceptibility comes from particles close to their blocking temperature. A final complication arises from the chemical or grinding procedures used to prepare most fine particle systems. These lead to the introduction of varying degrees of static disorder which can further affect  $K$  and also build in a static disorder contribution that can mimic the dynamic disorder that arises from collective moment fluctuations.

In principle, transmission Mössbauer spectroscopy can be used to distinguish the contributions from static disorder, collective excitations, and superparamagnetic reversals. However, interplay between the various effects can mean that the deconvolution is not unique. For example, it is possible to obtain fully self-consistent fits to the spectra of Invar, a disordered Fe-Ni alloy, in terms of a purely relaxation based model [4]; however, no magnetic relaxation effects are in fact present, and the temperature dependence in the spectra is due solely to chemical disorder [5]. When the effects of a broad particle size distribution are included, the problem becomes much worse. A typical solution is to fit the spectra with two broadened static forms: a magnetic component to allow for the larger particles below  $T_B$  and a paramagnetic component for the smaller particles that are above  $T_B$ . The blocking temperature for the whole sample is then defined as the point where the two components have equal areas [6]. This procedure is unsatisfactory; primarily because it is invalid and generally yields poor fits to the data, but also because the derived blocking temperatures are not consistent with those extrapolated from susceptibility measurements [6] as the temperatures at which the paramagnetic component appears depend on the particle size distribution [7].

We report here data from a modified Mössbauer technique: selective excitation double Mössbauer (SEDM) spectroscopy. This method relies on Mössbauer analyzing the radiation reemitted from the sample following resonant pumping into a selected hyperfine state. Static disorder, collective excitations, and moment reversals can be completely distinguished as they each yield a distinct and unambiguous signature. The data presented here on a 6.0 nm magnetite ferrofluid [8] show static disorder at the lowest temperatures ( $T \sim 20$  K), the growth of collective excitations by 40 K, and the clear onset of moment reversals at  $54 \pm 3$  K.

Figure 1 shows conventional transmission Mössbauer spectra at various temperatures. At 20 K the moments are static (confirmed below by SEDM) and the six-line pattern is broadened by static disorder. As the temperature is raised, the lines develop an increasing asymmetry, broadening towards the center of the pattern, with the effect being strongest for the outer lines. This behavior is due to collective excitations and can be described using a model originally proposed by Mørup [2]. By 60 K, a central component due to particles undergoing spin flips is apparent, and the collective excitation description is inadequate. With further temperature increases, the central component grows to dominate the spectrum. If the equal-area criterion is applied to these data, a blocking temperature of  $70 \pm 5$  K is obtained, in severe disagreement with

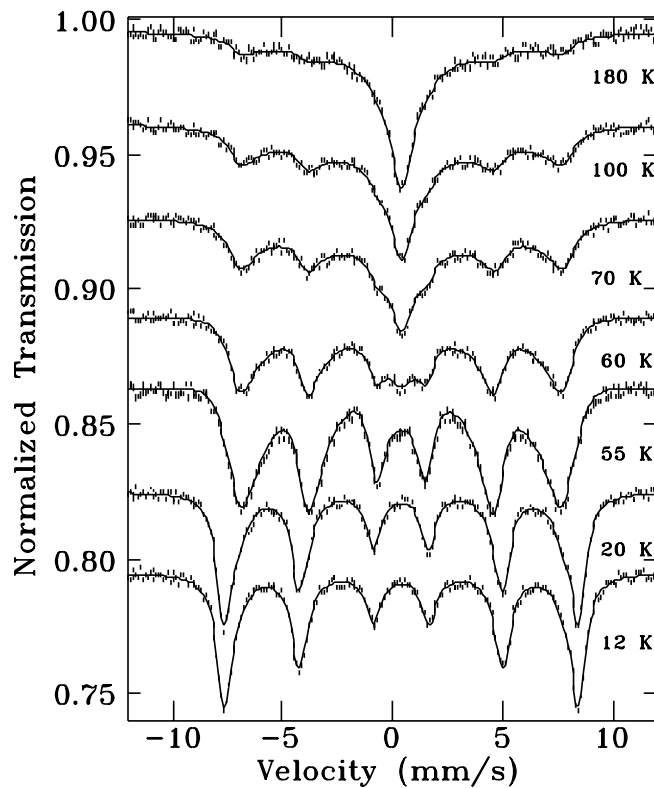


FIG. 1. Typical transmission Mössbauer spectra of a 6.0 nm  $\text{Fe}_3\text{O}_4$  ferrofluid. Solid lines are fits using a multistate relaxation model with a distribution of particle sizes [7].

the extrapolation of frequency dependent  $\chi_{ac}$  data which yields  $T_B = 55 \pm 2$  K [7].

The difficulties in analyzing the data in Fig. 1 derive from the similarity of static and dynamic effects, combined with a distribution of particle sizes. Static disorder leads to broad lines, while collective excitations simply cause *additional* broadening and shifts. When a range of particle sizes are present, a wide range of fluctuation amplitudes will be observed at a given temperature, leading to a further contribution to the line broadening. Once spin flips start occurring in the smallest particles, the collective excitation model fails. However simple spin-flip models [9] cannot account for the contribution of the larger particles until much higher temperatures are reached ( $T \gg T_B$ ) and all of the particles are undergoing spin flips. As a result, for the region of primary interest around  $T_B$ , neither model works. Some of these limitations have recently been eliminated by a many-state relaxation model that includes the effects of a size distribution and correctly describes the crossover from collective excitations to spin flips [7]. This model yields  $T_B = 55 \pm 5$  K, fully consistent with the value extrapolated from  $\chi_{ac}$  data.

To properly examine a magnetic fine particle system, an experimental technique which can unambiguously separate the effects of static disorder, collective excitations, and superparamagnetic spin flips is needed. In addition, no external magnetic field which might bias moment orientations and dynamics should be present. These requirements can be met by selective excitation double Mössbauer spectroscopy. In this technique, instead of measuring the absorption as the  $\gamma$  energy is swept across a wide range of values (see, for example, Fig. 1), the sample is pumped at a fixed, single energy, and the reemitted radiation is analyzed.

Long counting times, energy calibration difficulties, and instrumental unreliability have resulted in limited use of SEDM since its discovery [10–12]. We have resolved many of these problems by employing a small, transducer-mounted conversion electron detector (CED) containing a 99%  $^{57}\text{Fe}$  enriched stainless steel foil [13] as our energy detector. The CED is a much more efficient means of energy detection and yields a much greater signal to background ratio than the conventional approach of Doppler shifting a single line absorber in front of a proportional counter. In addition, specialized digital circuitry ensures a consistent energy calibration and phase locks the motion of the two transducers, eliminating interruptions for the biweekly energy calibrations previously employed. As a result, our spectrometer runs continuously, and combined with the greatly improved performance of the CED, our system yields a 1000-fold [10] to 5000-fold [11] improvement in effective counting time when compared with previous experimental configurations. This makes SEDM a practical technique for use in the study of magnetic relaxation effects.

The SEDM data shown in Fig. 2 were obtained using a modest 1 GBq  $^{57}\text{CoRh}$  source. The leftmost line in the

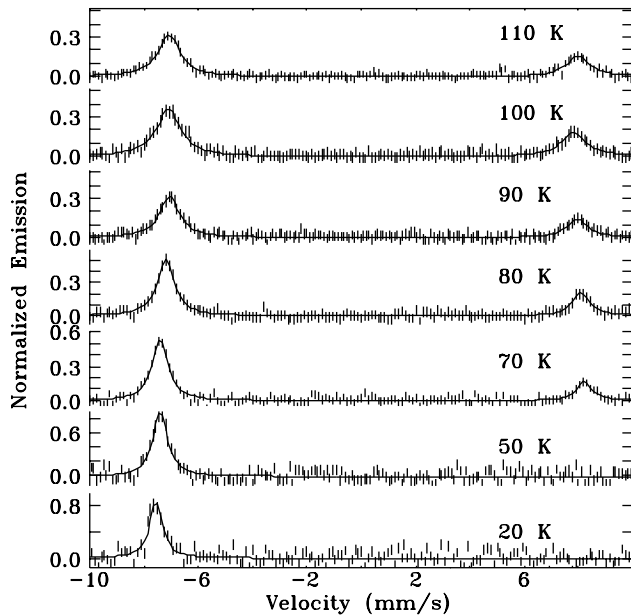


FIG. 2. SEDM spectra of a 6.0 nm  $\text{Fe}_3\text{O}_4$  ferrofluid. At each temperature, the pump energy was centered on the line at the left. The appearance of the peak at positive velocities indicates the onset of superparamagnetic moment reversals.

spectrum was pumped as it has the largest absorption cross section, thus maximizing the signal and reducing collection times. Sample temperatures of 20 to 200 K were obtained with a closed cycle refrigeration system. Typical counting times were 20 days.

The static magnetic field present at the  $^{57}\text{Fe}$  nucleus in a magnetically ordered material induces hyperfine splittings in the  $I_g = 1/2$  ground state and the  $I_e = 3/2$  excited state. Selection rules ( $\Delta m_I = 0, \pm 1$ ) mean that only six of the possible eight transitions are allowed, and a six-line spectrum is observed by transmission Mössbauer spectroscopy (see, for example, the 12 K spectrum in Fig. 1). The left-right symmetry in the spectrum means that the sign of the magnetic field cannot be determined and so superparamagnetic spin flips, which involve a sign reversal in the field, cannot be observed directly. By contrast, the state-specific pumping used in SEDM explicitly breaks this symmetry. If the constant velocity drive is set to an energy corresponding to the leftmost line in the 12 K spectrum in Fig. 1, then the  $m_{I_g} = -1/2 \rightarrow m_{I_e} = -3/2$  transition is driven and the  $m_{I_e} = -3/2$  excited state is populated. The selection rules allow only a single transition from the  $m_{I_e} = -3/2$  state, and so in a material with a unique, static field, e.g.,  $\alpha\text{-Fe}$ , the radiation reemitted when the excited nucleus returns to the ground state is at the same energy as the pump, and SEDM yields a single sharp line at the pump energy. Static disorder leads to a broadened absorption line and the reemitted radiation reflects a convolution between the source linewidth and the hyperfine field distribution. A broader reemission line is observed. However this line can be substantially narrower than that observed by transmission as only part of the distribution is

probed [5]. A typical static SEDM spectrum is shown at the bottom of Fig. 2 for the ferrofluid studied here at 20 K.

The onset of magnetic fluctuations has a significant impact on the SEDM spectrum. As collective excitations develop, the SEDM line broadens visibly (compare the 20 and 50 K SEDM spectra in Fig. 2). However, it is superparamagnetic spin flips that have the most dramatic effect: at 70 K a new line is clearly present in the SEDM spectrum. This line at  $\sim +8$  mm/s is due to the  $m_{I_e} = +3/2 \rightarrow m_{I_g} = +1/2$  transition and is present even though we have explicitly populated only the  $m_{I_e} = -3/2$  excited state. This is possible because when a spin flip occurs in a particle in which we have pumped a nucleus into the  $m_{I_e} = -3/2$  excited state, the field within that particle reverses, the projection of  $I_e$  onto that field changes sign, and the populated state becomes  $m_{I_e} = +3/2$ . This state then decays to give the line at  $\sim +8$  mm/s. The observation of a *sharp* line at +8 mm/s indicates that the moment reversal is instantaneous on the time scale of the SEDM measurement. This observation is consistent with estimates that the duration of the moment reversal process is  $\sim 0.1$  ns [14], much shorter than the time between reversals ( $\sim 100$  ns). The intensity ratio of the lines at  $\sim -8$  and  $\sim +8$  mm/s is related to the probability that a spin flip occurs during the lifetime of the excited state and is thus a direct indication of the rate at which spin flips happen. We emphasize that no amount of *static* disorder can lead to the appearance of this additional line. It can be caused only by  $180^\circ$  magnetization reversals.

To develop a quantitative description of the SEDM spectra, a model is needed. Using Sack's [15] stochastic quantum mechanical formalism, we have modeled both SEDM and transmission Mössbauer spectra. Transitions between two excited states have been used to describe the SEDM spectra, with the linewidth and relaxation rate as free parameters in a least-squares fit.

Results of fits to the data are shown in Fig. 3. A comparison between the observed linewidths and those obtained with an  $\alpha\text{-Fe}$  foil (dashed line in Fig. 3) clearly shows the effects of static disorder. The further increase in width above 30 K is due to collective excitations. This can be confirmed by treating the data at each temperature in Fig. 1 as broadened solely by a static hyperfine field distribution and using the derived distribution to fit the corresponding SEDM spectrum. While this procedure has been shown to work for purely static systems [5], it fails here, yielding lines that are too narrow. This misfit provides further evidence of the presence of collective excitations, and demonstrates that SEDM can be used to distinguish static and dynamic sources of line broadening.

Superparamagnetic spin flips occur with increasing frequency above  $T_B$ , going from  $2.5 \pm 0.3$  MHz at 70 K to  $9.7 \pm 1.0$  MHz at 110 K. A blocking temperature of  $T_B = 54 \pm 3$  K is extrapolated from a linear fit to the SEDM relaxation frequency, in excellent agreement with transmission Mössbauer and frequency dependent  $\chi_{ac}$

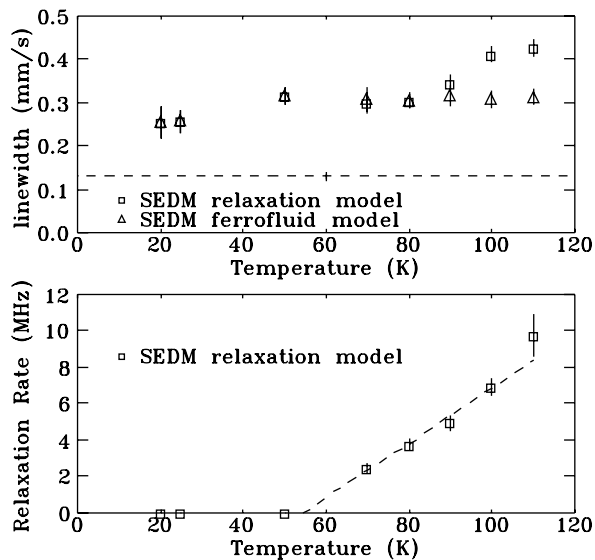


FIG. 3. Results of fits to the data in Fig. 2 using two SEDM models. Top: Linewidth (the dashed line shows the linewidth obtained by SEDM on  $\alpha$ -Fe). Bottom: Relaxation rate showing the onset of superparamagnetic spin flips above  $T_B = 54 \pm 3$  K.

extrapolations of  $T_B$  [7]. The continued increase in fitted linewidth above 80 K as the relaxation frequency increases indicates that our model is too simple, as a correct description of the superparamagnetic processes should involve no linewidth variations. A distribution of relaxation frequencies for each moment size was used in a multilevel relaxation model to fit the ferrofluid transmission Mössbauer spectra [7]. Since transmission experiments are most sensitive to flip rates at or above the Larmor frequency and SEDM is sensitive to flip rates at or below the Larmor frequency, relaxation rates within the time scale of the SEDM measurement were used to fit the SEDM spectra in Fig. 2. The results in Fig. 3 show that a more consistent linewidth was obtained. This agreement between the two experiments strongly supports our description of the transmission Mössbauer spectra of fine particle systems.

In summary, substantial improvements to SEDM methodology have allowed us to characterize the defining magnetic phenomena of a fine particle system. At the lowest temperatures, moments are frozen along their easy axes and the material is easily described by a distribution of static magnetic fields from, for example, chemical disorder and dipole interactions. Collective excitations appear by 50 K and lead to significant, temperature dependent line broadening that exceeds that predicted by a static hyperfine field distribution. Clear evidence of moments undergoing a transition from collective excitations to superparamagnetism is given by the 70 K SEDM spectrum. The additional line is unequivocal evidence that moments are undergoing

simple  $180^\circ$  spin flips and that no other moment orientation process is responsible for the superparamagnetic behavior of these particles. Furthermore, the sharp lines indicate the reversal is abrupt. Relaxation frequencies of 2.5 to 10 MHz at temperatures of 70 to 110 K exhibit a gradual increase with temperature. Relaxation rates were measured directly without appealing to models of magnetic excitations, and are not influenced by particle size distributions.

Although collection times remain long, they are comparable to those necessary when using CEDs to study thin films and could easily be reduced by using a more intense source. With the unique ability to decouple static and slow dynamic magnetic effects, SEDM proves to be an ideal technique to distinguish the effects of interacting particles upon the blocking temperature.

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- [1] J.L. Dormann, D. Fiorani, and E. Tronc, in *Advances in Chemical Physics*, edited by I. Prigogine and Stuart A. Rice (Wiley, New York, 1997), Vol. XCVIII, p. 283.
  - [2] S. Mørup, *J. Magn. Magn. Mater.* **37**, 39 (1983).
  - [3] M.F. Hansen and S. Mørup, *J. Magn. Magn. Mater.* **184**, 262 (1998).
  - [4] D.G. Rancourt, H.H.A. Smit, and R.C. Thiel, *J. Magn. Magn. Mater.* **66**, 121 (1987).
  - [5] J. van Lierop and D.H. Ryan, *J. Appl. Phys.* **85**, 4518 (1999).
  - [6] E. Tronc, P. Prené, J.P. Jolivet, F. D'Orazio, F. Lucari, D. Fiorani, M. Godinho, R. Cherkaoui, M. Nogues, and J.L. Dormann, *Hyperfine Interact.* **95**, 129 (1995).
  - [7] J. van Lierop and D.H. Ryan, *J. Appl. Phys.* **87**, 6277 (2000).
  - [8] Ferrofluidics Corporation, 40 Simon Street, Nashua, NH 03061.
  - [9] M. Blume and J.A. Tjon, *Phys. Rev.* **165**, 446 (1968).
  - [10] Neil D. Heiman and J.C. Walker, *Phys. Rev.* **184**, 281 (1969).
  - [11] Bohdan Balko and Gilbert R. Hoy, *Phys. Rev. B* **10**, 36 (1974).
  - [12] D.C. Price and A.M. Stewart, *Hyperfine Interact.* **42**, 1157 (1988).
  - [13] L.X. Liao, D.H. Ryan, and Z. Altounian, *Rev. Sci. Instrum.* **64**, 679 (1993).
  - [14] D.H. Jones and K.K.P. Srivastava, *J. Magn. Magn. Mater.* **78**, 320 (1989).
  - [15] R.A. Sack, *Mol. Phys.* **1**, 163 (1958).