

## Erratum: Spontaneous Symmetry Breaking in Single and Molecular Quantum Dots [Phys. Rev. Lett. 82, 5325 (1999)]

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In our recent Letter on spontaneous symmetry breaking in quantum dots (QD's), we displayed in Fig. 4 addition energies  $\Delta\varepsilon(N) = E(N+1) - 2E(N) + E(N-1)$ , where  $E(N)$  is the  $N$ -electron ground-state total energy, calculated with the spin-and-space unrestricted Hartree-Fock (sS-UHF) method. Subsequent to the publication of our Letter, we have performed further systematic sS-UHF calculations, with the use of larger harmonic-oscillator bases and an implementation of an extensive search for energy minima. While the behavior and magnitudes of  $\Delta\varepsilon$  shown in Fig. 4 of our Letter are maintained, as well as our finding pertaining to the prevalent violation of Hund's first rule, our improved calculations yield in certain instances different spin polarizations  $P \equiv N\uparrow - N\downarrow$ , where  $N\uparrow$  and  $N\downarrow$  ( $N\uparrow + N\downarrow = N$ ) are the number of electrons with up and down spins, respectively.

In Fig. 1 below, we display our new results for  $\Delta\varepsilon$  in a single QD with GaAs parameters, i.e.,  $\kappa = 12.9$ ,  $\hbar\omega_0 = 5$  meV, and  $m^* = 0.067m_e$  (corresponding to the top curve in Fig. 4 of our Letter). The results of our calculations (solid dots) for the spin polarization given in the inset of Fig. 1 exhibit violation of Hund's rule (open squares) for  $N = 4, 8, 9, 14, 15, 16, 18$ , and 22 (note that this violation appears already for  $N = 4$ ); however, as noted in our Letter, the addition energies display maxima at closed shells (i.e., at  $N = 6, 12$ , and 20), as well as at the midshell closures (i.e., at  $N = 4, 9$ , and 16). In general, the non-Hund ground-state minima are accompanied by energetically close spin isomers obeying Hund's rule, and vice versa (e.g., for  $N = 17$  the energy difference between the Hund,  $P = 3$ , and the non-Hund,  $P = 1$ , isomers is 0.05 meV).

For the corresponding case of a quantum dot molecule with  $\kappa = 12.9$ ,  $d = 70$  nm, and  $V_b = 10$  meV (third curve from the top in Fig. 4 of our Letter), our improved calculation yields  $P = 0$  for  $N = 14$  (unlike the earlier value of  $P = 2$ ), with all the other spin polarizations remaining unchanged.

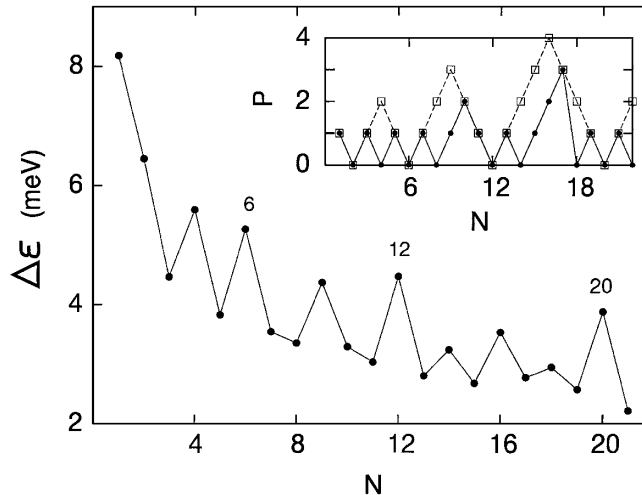


FIG. 1. sS-UHF results for the addition energies ( $\Delta\varepsilon$  vs  $N$ ) of a single QD ( $\hbar\omega_0 = 5$  meV,  $\kappa = 12.9$ ,  $m^* = 0.067m_e$ ). The inset displays the calculated (solid dots) spin polarizations,  $P \equiv N\uparrow - N\downarrow$ , as well as those (open squares) expected from Hund's first rule.