

## Phonon-Assisted Double Exchange in Perovskite Manganites

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Measurements of the temperature dependence of the thermoelectric power and the resistivity of  $^{18}\text{O}/^{16}\text{O}$  isotope-exchanged  $(\text{La}_{1-x}\text{Nd}_x)_{0.7}\text{Ca}_{0.3}\text{MnO}_3$  samples have confirmed the existence of vibronic electronic states below  $T_c$  in the narrow range of bandwidths where static, cooperative Jahn-Teller (J-T) deformations are suppressed and dynamic J-T deformations introduce vibrational modes into the interatomic spin-spin interactions. A giant isotope effect on  $T_c$  is related to a mass-enhanced change in both the density and mobility of the mobile charge carriers at  $T_c$ . [S0031-9007(98)05628-2]

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Conventional theories of interatomic spin-spin interactions in magnetic materials neglect atomic vibrations. The only exception was postulated [1] some years ago to account for the ferromagnetism found in the perovskite, single-valent system  $\text{LaMn}_{1-x}\text{Ga}_x\text{O}_3$  on suppression by Ga of the *static*, cooperative Jahn-Teller (J-T) deformation of the high-spin Mn III ions found in  $\text{LaMnO}_3$ . It was pointed out that the cooperative oxygen vibrations of a *dynamic* J-T coupling would coordinate empty and half-filled Mn III  $\sigma$ -bonding orbitals alternating on opposite sides of an oxygen atom to give an isotropic ferromagnetic superexchange interaction. In 1951, Zener [2] had postulated that the observed [3] ferromagnetic order and metalliclike temperature dependence of the resistivity below  $T_c$  in the perovskite, mixed-valence system  $\text{La}_{1-x}\text{Ca}_x\text{MnO}_3$  was due to a real charge transfer (a double-exchange mechanism) within Mn III-O-Mn IV pairs that preserved both the spin angular momentum and the intra-atomic Hund's field coupling between the localized spin of a  $t^3$  configuration ( $S = \frac{3}{2}$ ) and the spin of the  $e$  electron shared between the two Mn atoms of a pair. For global ferromagnetism to occur in Zener's model, pair diffusion without any activation energy is assumed implicitly to be rapid compared to a spin-relaxation time. Not understood at the time was how a motional enthalpy  $\Delta H_m = 0$  might arise. On the other hand, in a double-exchange model that avoids the introduction of vibronic states, de Gennes [4] assumed that the mobile electrons occupy a narrow  $\sigma^*$  band of  $e$ -orbital parentage and that, if they are bound, they generate a local spin alignment.

The data reported for the perovskite manganites shows that the ferromagnetic transition at  $T_c$  is coupled to a drop in resistivity at a first-order phase change (see [5,6], for example). The unusual transport properties below  $T_c$  are suggestive of a vibronic state [7]. We have recently provided experimental evidence [8] for a transition from polaronic to metallic electronic behavior with increasing hydrostatic pressure in a temperature interval  $T_{c0} < T < T_c$  in  $\text{La}_{0.85}\text{Sr}_{0.15}\text{MnO}_3$ , which exhibits charge ordering at temperatures  $T < T_{c0}$  [9]. The unusual electronic behavior occurs in the compositional

range where  $T_c$  increases sharply with increasing width of the  $\sigma^*$  band. Variations  $60 < T_c < 360$  K have been found for the Curie temperatures of the  $R_{0.7}A_{0.3}\text{MnO}_3$  perovskites ( $R$  = rare earth,  $A$  = alkaline-earth atoms) over a narrow range of bandwidths [5]. In this Letter, we compare thermoelectric-power measurements made at ambient pressure and resistivity data under different pressure on  $^{18}\text{O}/^{16}\text{O}$  isotope-exchanged samples to show conclusively the mass dependence of the unusual electronic behavior below  $T_c$  in the  $O$  (orthorhombic) phase. This comparison also demonstrates that the giant isotope effect on  $T_c$  found for  $\text{La}_{1-x}\text{Ca}_x\text{MnO}_3$  ferromagnets [10] is due to changes not only in the mobility of polaronic charge carriers, but also in their density above  $T_c$ , with changes in the oxygen mass  $M$ .

In the phase diagram of Fig. 1 for the perovskites  $\text{Ln}_{0.7}\text{Ca}_{0.3}\text{MnO}_3$ , the structure changes from  $O'$  [orthorhombic ( $c/a < \sqrt{2}$ )] to  $O$  [orthorhombic ( $c/a > \sqrt{2}$ )] with increasing room-temperature tolerance factor  $t = (A\text{-O})/\sqrt{2}$  (Mn-O), where  $A\text{-O}$  and Mn-O are the equilibrium bond lengths. A larger thermal expansion of the  $A\text{-O}$  equilibrium bond length makes  $t(T)$  increase

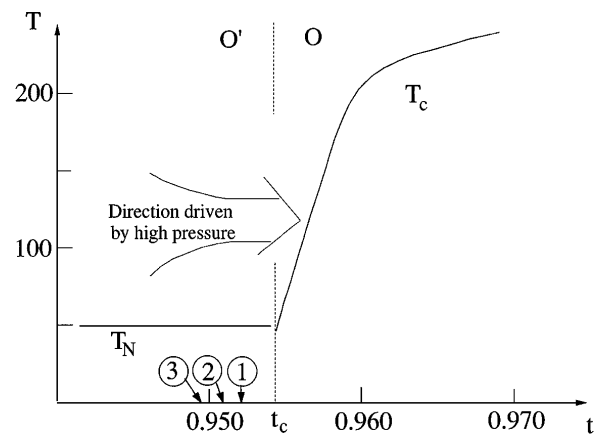


FIG. 1. The variation of  $T_c$  with room-temperature tolerance factor  $t \equiv (A\text{-O})/\sqrt{2}$  (Mn-O), where the  $A\text{-O}$  and Mn-O equilibrium bond lengths are the sums of empirical ionic radii of an  $\text{AMnO}_3$  perovskite; in this diagram,  $A = R_{0.7}\text{Ca}_{0.3}$ .

gradually with temperature  $T$ ; an unusually high compressibility of the Mn-O bond makes hydrostatic pressure  $P$  move the  $O'$  to  $O$  transition at room temperature from  $t_c$  to a lower effective  $t$  [6]. In the  $O'$  phase, the  $e$ -orbital degeneracy of the high-spin Mn III:  $t^3e^1$  configuration is removed by a cooperative, static J-T deformation that orders the occupied  $e$  orbital into the  $a$ - $b$  plane; the charge carriers are localized at single Mn sites as Mn IV ions and move as small polarons in the Mn III matrix. In this phase, superexchange spin-spin interactions are dominant, and a canted-spin ferromagnetism is observed below the magnetic-ordering temperature  $T_N$ . In the  $O$  phase, the  $e$ -orbital degeneracy may be lifted by either dynamic, cooperative J-T deformations, or by transformation of the  $e$  electrons into itinerant  $\sigma^*$ -band electrons. An unusual electronic state has been found below the Curie temperature  $T_c$  in the  $O$  phase [7]; it would appear to be associated with a dynamic J-T lifting of the  $e$ -orbital degeneracy as a transitional state between the static J-T orbital ordering in the  $O'$  phase and the itinerant-electron state appearing at higher values of  $t$ . In order to probe this transitional state further, we use pressure to induce an  $O'$  to  $O$  transition; it is in the  $O$  phase near this transition that the peculiar properties of the unusual electronic state are maximized.

The composition  $(\text{La}_{0.25}\text{Nd}_{0.75})_{0.7}\text{Ca}_{0.3}\text{MnO}_3$ , which we have characterized elsewhere [6,7], lies at the position No. 1 in Fig. 1. Two additional samples with different  $t$  factors, marked No. 2 and No. 3 in Fig. 1, were prepared:  $(\text{La}_{0.2}\text{Nd}_{0.8})_{0.7}\text{Ca}_{0.3}\text{MnO}_3$  and  $(\text{La}_{0.15}\text{Nd}_{0.85})_{0.7}\text{Ca}_{0.3}\text{MnO}_3$ . Isotope exchange of sample No. 1 was carried out in a furnace with two identical, parallel ceramic tubes passing  $^{16}\text{O}$  and  $^{18}\text{O}$  gas separately with identical gas flows. Two pieces cut from the same  $(\text{La}_{0.25}\text{Nd}_{0.75})_{0.7}\text{Ca}_{0.3}\text{MnO}_3$  pellet were put in the same heating zone of the furnace. The two samples were first loaded at 950 °C for 72 h with  $^{16}\text{O}$  or  $^{18}\text{O}$ , furnace cooled over 24 h, and then weighed precisely. An exchange of samples between the two tubes was followed by the same annealing procedure; the isotope exchange, as determined by the weight change, was 79%  $^{16}\text{O}$  to  $^{18}\text{O}$  and 73%  $^{18}\text{O}$  to  $^{16}\text{O}$ . Each of the samples No. 1–No. 3 has a tolerance factor  $t < t_c$ . A four-probe method was used to measure the resistivity  $\rho(T)$  under high pressure in a self-clamped pressure cell with silicone oil as the pressure-transfer medium. The thermoelectric power  $\alpha(T)$  was measured in a home-built apparatus. We have taken  $T_c$  to be the temperature at which  $d\rho/dT = 0$ ; the error in this reading of  $T_c$  has been shown to be within  $\pm 0.5$  K. In a test for thermal hysteresis of  $T_c$ , all samples were measured on cooling to 12 K before being measured on warming for each pressure applied. The connection between the  $T_c$  defined as above from the first-order transition and the Curie temperature from magnetic susceptibility has been well-established [5,6]. Therefore, we are able to monitor the ferromagnetic Curie temperature by measuring the transition in resistivity.

Figure 2 compares the  $\alpha(T)$  curves for the two oxygen isotopes of sample No. 1. We have shown elsewhere

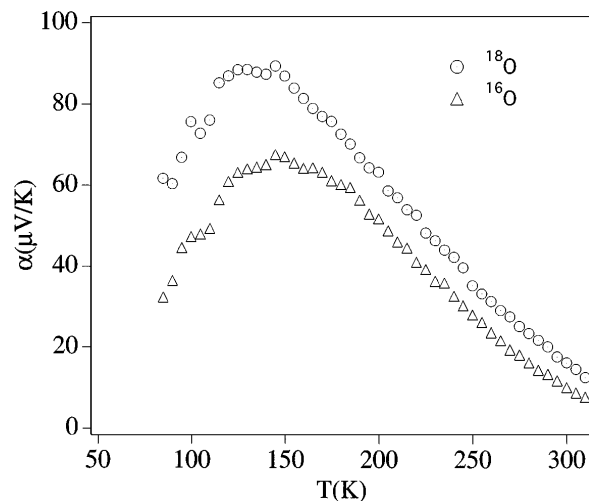


FIG. 2. Temperature dependence of the thermoelectric power for the two isotopes of sample No. 1.

[6] that the increase in  $\alpha(T)$  with decreasing temperature  $T > T_c$  is due to a trapping out of mobile charge carriers (polarons), and that for samples with  $t > t_c$  the Curie temperature  $T_c$  increases sensitively with the concentration of mobile polarons just above  $T_c$  as  $t$  increases. The polaronic character above  $T_c$  has been confirmed by neutron diffraction [11,12] and other spectroscopic techniques [13,14]. The increase in the maximum value of  $\alpha(T)$  on replacing  $^{16}\text{O}$  by  $^{18}\text{O}$  means a reduction in the concentration of mobile polarons just above  $T_c$  and is equivalent to a reduction in  $t$ . We have found a similar isotope effect on  $\alpha(T)$  in samples with  $t > t_c$  but it diminishes with increasing  $t > t_c$ . It follows that at least part of the giant isotope effect on  $T_c$  previously reported [10] is due to an increased trapping energy of the polarons above  $T_c$  with increased oxygen mass  $M$ . However, any mass dependence of the ferromagnetic coupling below  $T_c$  remains to be demonstrated.

In order to identify any additional mass dependence of the interatomic ferromagnetic exchange below  $T_c$ , we turned to measurements of  $\rho(T)$  under pressure, Figs. 3 and 4. We used enough pressure to make  $t$  of all our samples cross  $t_c$ , where a maximum of the mass dependence is expected. We summarize in Fig. 5 the measured values of  $T_c$ . The transition at  $d\rho/dT = 0$  found for pressures  $P < P_c$  in the range  $40 < T < 50$  K appears to be second order as it shows no hysteresis.

With increasing pressure  $P$ , a first-order phase change occurs a little below 2 kbar in the  $^{16}\text{O}$  sample No. 1 and a little below 11 kbar in the  $^{18}\text{O}$  sample No. 1; the dramatic onset of a thermal hysteresis at  $T_c$  is taken to mark a  $t(P) \approx t_c$  at  $P = P_c$ . It follows that the  $^{18}\text{O}$  sample No. 1, which has a larger  $P_c$ , is equivalent to the  $^{16}\text{O}$  sample No. 1, but with a lower effective tolerance factor  $t$  as was also deduced from the  $\alpha(T)$  data. At a pressure  $P = 11$  kbar  $> P_c$ , a giant isotope coefficient  $d \ln T_c / d \ln M = 4.9$  has been obtained; it is about 6 times

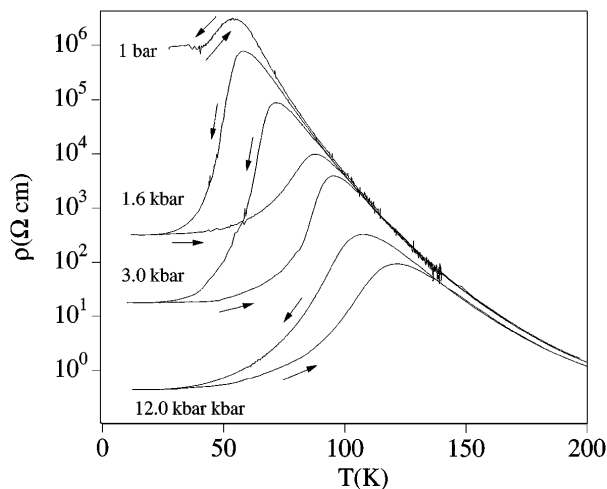


FIG. 3. The resistivity versus temperature for  $^{16}\text{O}$  sample No. 1 under different pressures; the pressure labeled is taken from the value at  $T_c$ . A high noise level made measurement of the resistivity below 30 K not meaningful in the phases without a first-order transition.

larger than that reported [10] for  $\text{La}_{0.8}\text{Ca}_{0.2}\text{MnO}_3$ . However, this giant coefficient may reflect only the change in the density of mobile charge carriers in the paramagnetic state; the  $\alpha(T)$  data have shown an important mass dependence of the mobile polaron density above  $T_c$ . To probe the mass dependence of the electronic state below  $T_c$ , we note that for  $t > t_c$  both the hysteresis width  $\Delta T_c = T_c(\text{warming}) - T_c(\text{cooling})$  and the coefficient  $dT_c/dP$  are mass dependent. The maximum  $\Delta T_c \approx 27$  K for  $^{16}\text{O}$  and 19 K for  $^{18}\text{O}$  occurs at  $P = P_c$ ; at a  $P > P_c$ ,  $\Delta T_c$  and  $dT_c/dP$  are reduced significantly on going from  $^{16}\text{O}$  to  $^{18}\text{O}$ , Fig. 5(a). To clarify whether this reduction is due to a pressure dependence or a mass dependence of  $\Delta T_c$  and  $dT_c/dP$ , we did pressure experiments on samples No. 2 and No. 3. According to Fig. 1, a higher  $P_c$  is to be expected for these samples with smaller tolerance factor  $t$  than for the  $^{16}\text{O}$  sample No. 1. As shown in Fig. 5(b),

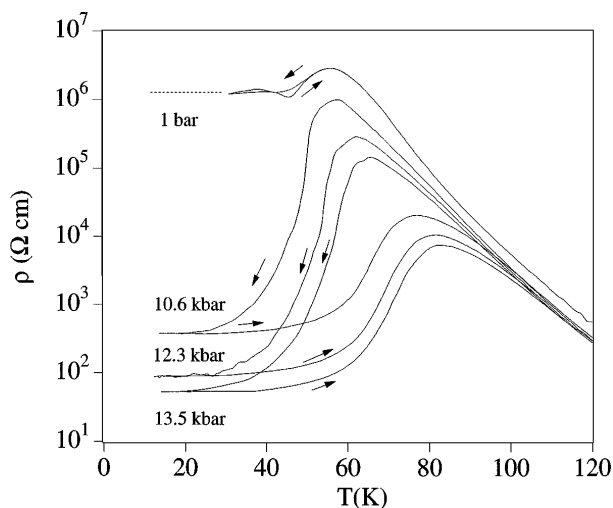


FIG. 4. The resistivity versus temperature for  $^{18}\text{O}$  sample No. 1 under different pressures as in Fig. 3.

a  $P_c(\text{No. 3}) > P_c(\text{No. 2}) > P_c(\text{No. 1})$  is observed, and the maximum  $\Delta T_c \approx 27$  K of all  $^{16}\text{O}$  samples is nearly pressure independent. Moreover, the coefficients  $dT_c/dP$ , which are labeled in Fig. 5, are reduced under pressure, but they remain higher than that of the  $^{18}\text{O}$  sample No. 1. Comparison of these parameters for  $^{18}\text{O}$  sample No. 1 and  $^{16}\text{O}$  sample No. 3 is particularly significant as  $P_c$  is nearly the same in the two samples. This comparison rules out any pressure dependence on  $\Delta T_c$  and  $dT_c/dP$ . We have thus demonstrated that both the thermal hysteresis width  $\Delta T_c$  and  $dT_c/dP$  found in the ferromagnetic perovskite manganites are mass dependent.

To interpret the mass dependence of  $\Delta T_c$  and  $dT_c/dP$ , we refer to the virial theorem and the observation [6] that the compressibility of the Mn-O bond is greater than that of the A-O bond, where  $A = (\text{La}_{1-x}\text{Nd}_x)_{0.7}\text{Ca}_{0.3}$  in our samples. For a central-force  $r^{-1}$  potential energy, the virial theorem states that  $2\langle T \rangle + \langle V \rangle = 0$ , where  $\langle T \rangle$  and  $\langle V \rangle$  are the mean kinetic and potential energies of the system. We have argued that the anomalously large compressibility of the Mn-O bond reflects a double-well potential of the equilibrium Mn-O bond length that can be expected to occur where there is a discontinuous change in the mean kinetic energy of the electronic system. Although a discontinuous change in the kinetic energy of the electronic system may be expected on passing from polaronic to itinerant electronic behavior on lowering  $T$

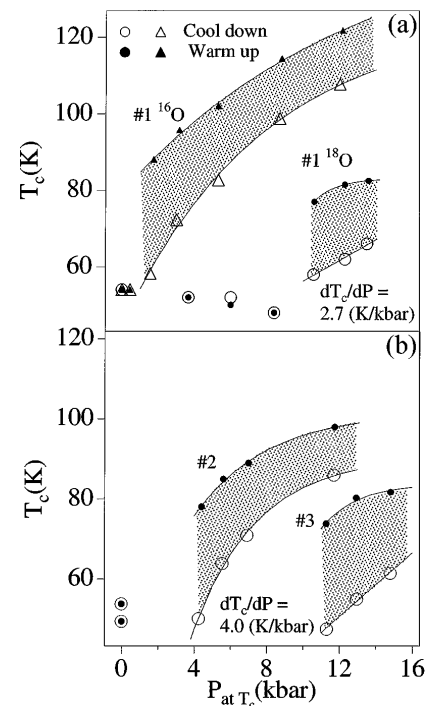


FIG. 5. The pressure dependencies of  $T_c$  (warming) and  $T_c$  (cooling) taken from  $d\rho/dT = 0$  and fit to an exponential function: (a) for  $^{16}\text{O}$  and  $^{18}\text{O}$  sample No. 1 from Figs. 3 and 4; (b) for samples No. 2 and No. 3. The labeled  $dT_c/dP$  values were taken from  $T_c$  (cooling) and fit to a linear curve at  $P = P_c$  for  $^{18}\text{O}$  sample No. 1 and sample No. 3.

through  $T_c$ , which is the conventional interpretation of this transition, alternative transitions are also possible. For example, a polaron gas in equilibrium with regions of trapped polarons may transform to a vibronic phase in which the trapped polarons form extended Mn IV-rich domains as in a mobile charge-density wave within which larger polarons are organized. In order to distinguish between these possibilities, we consider the significance of  $\Delta T_c$ . At  $T_c$ , the Gibbs free energy  $\Delta G$  is identical for both the ferromagnetic and paramagnetic phases and the hysteresis  $\Delta T_c$  is due to an interface strain energy associated with the nucleation of the second phase as a result of the volume change  $\Delta V$  occurring at a first-order transition. Neutron-diffraction data [12,15] have corroborated the volume change  $\Delta V < 0$  on lowering the temperature at  $T_c$  in the  $O$  (orthorhombic) phase. Therefore,  $\Delta T_c$  can be used as an indicator of the relative magnitude of the volume change. The larger  $\Delta V$ , the larger  $\Delta T_c$ ; therefore, the larger  $\Delta T_c$  for  $^{16}\text{O}$  compared to  $^{18}\text{O}$  samples indicates a  $\Delta V(^{16}\text{O}) > \Delta V(^{18}\text{O})$ . This conclusion is also verified by the greater pressure sensitivity  $dT_c/dP$  for the  $^{16}\text{O}$  compared to the  $^{18}\text{O}$  sample.

If the electrons are itinerant, the tight-binding bandwidth  $W_0$  is mass independent. However, the Mott bandwidth for polaronic conduction [16] varies as  $W \sim W_0 \exp(-\gamma \varepsilon_b / \hbar \omega_0)$ , where  $\varepsilon_b$  is the polaron binding energy by a lattice optical mode of frequency  $\omega_0$  and  $\gamma$  is a constant; the polaron bandwidth is clearly mass dependent through  $\omega_0$ . The mean kinetic energy  $\langle T \rangle$  increases with the bandwidth; therefore, the mean kinetic energy of itinerant electrons should be independent of the oxygen mass  $M_0$ , whereas that of polarons decreases with decreasing  $\omega_0 \sim \sqrt{M_0}$ . It follows from the virial theorem that the volume of the ferromagnetic state below  $T_c$  is mass dependent if the electrons are polaronic, but is mass independent if they are itinerant. If, as is generally assumed, a polaronic to itinerant electronic transition occurs on cooling through  $T_c$ , then the mass dependence of  $\Delta T_c$  is due to the mass dependence of the paramagnetic-state volume since there would be no mass dependence of the volume of an itinerant-electron state. But from the virial theorem, the lower polaron kinetic energy of the  $^{18}\text{O}$  paramagnetic state would make  $\Delta V(^{18}\text{O}) > \Delta V(^{16}\text{O})$  for itinerant electrons below  $T_c$ , which is opposite to what is observed in our samples. We are, therefore, forced to conclude that the volume of the ferromagnetic state below  $T_c$  is more mass dependent than that of the paramagnetic state, the higher mobility of the charge carriers in the  $^{16}\text{O}$  ferromagnetic phase resulting in a smaller volume than is found in the  $^{18}\text{O}$  ferromagnetic phase. This conclusion requires retention of some form of polaronic phase below  $T_c$  at the crossover from static to dynamic Jahn-Teller site deformations. This requirement is consistent with the stabilization of a vibronic state below  $T_c$  in a small interval  $\Delta t$  above  $t_c$ .

In conclusion, the thermoelectric power measurements on  $^{16}\text{O}/^{18}\text{O}$  isotope samples confirm that the isotope shift

of  $T_c$  is partially due to a mass-dependent trapping out of mobile polarons in the paramagnetic state. Trapping out of mobile charge carriers indicates a segregation into hole-rich clusters within a hole-poor matrix in the paramagnetic state. Moreover, the pressure dependence of the resistivity shows a sharp transition from a second-order to a first-order transition at  $T_c$  on passing from the  $O'$  to the  $O$  phase. In addition, the observations of a mass dependence in both the thermal hysteresis width  $\Delta T_c$  and the coefficient  $dT_c/P$  indicate that lattice vibrations are involved in the transport properties of the ferromagnetic state in the  $O$  phase. This mass-dependent ferromagnetic state is understandable with a polaronic picture below  $T_c$ . With twofold-degenerate  $\sigma$ -bonding atomic orbitals occupied by one or less localized electron per atom, dynamic J-T deformations would introduce vibronic processes. Where vibronic processes among  $\sigma^*$ -band electrons occur in the presence of localized spins in  $\pi$ -bonding orbitals, the interatomic spin-spin exchange interactions are not independent of the oxygen-atom vibrational dynamics. These vibronic processes introduce a double-exchange component to the global ferromagnetic coupling above  $T_c$  that increases not only with the polaron density, but also with the polaron mobility, and hence, inversely with the root of the oxygen mass.

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