Macroscopic Quantum Tunneling of Magnetization of Single Ferrimagnetic Nanoparticles of Barium Ferrite

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Presented are switching field measurements of individual ferrimagnetic and insulating BaFeCoTiO nanoparticles containing about $10^5 \mu_B$ at very low temperatures (0.1–6 K). For temperatures higher than 0.4 K, the quantitative agreement with the Néel-Brown theory of thermal activated magnetization reversal allowed us to identify unambiguously the magnetization reversal of uniform rotation. Below 0.4 K, strong deviations from this model are evidenced which are quantitatively in agreement with the predictions of the theory of macroscopic quantum tunneling of magnetization in the low dissipation regime. [S0031-9007(97)04527-4]

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Observation of the quantum behavior of a macroscopic variable has remained a challenging problem [1]. Today, only very few macroscopic systems show agreement with theoretical predictions. Among them, there are Josephson junctions and SQUIDs where quantum tunneling between two macroscopically distinct current states has been observed [2]. After a slow evolution during the last decades, macroscopic quantum tunneling (MQT) in magnetism constitutes a very rich and fascinating field of research.

In single-domain nanoparticles, strong exchange interactions align the magnetic moments parallel to each other. These particles can be described by a macroscopic order parameter: the magnetic moment of the particle. Under the effect of an applied field, the rotation of such a moment can be described by an energy function having two minima which correspond to the two states of opposite moment direction. The energy barrier between these states is due to magnetocrystalline and/or shape anisotropy. At zero field, this energy barrier (proportional to the particle volume) is much too high to observe magnetization reversal. However, the barrier can be lowered by applying a magnetic field in the opposite direction of the particle magnetization. When the applied field is close to the switching field $H_{\rm sw}^0$, for which the barrier vanishes, thermal fluctuations can drive the system above the barrier. At very low temperature, it was shown theoretically that there is also the possibility of tunneling through the energy barrier [3].

Until now, quantum tunneling of magnetization (QTM) was mostly studied by measuring the temperature dependence of magnetic relaxation after an abrupt change in the applied magnetic field. At high temperature, when energy barriers are overcome by thermal activation, magnetic relaxation strongly depends on temperature. At low enough temperature, when thermal activation becomes extremely weak, magnetic relaxation should in principle vanish. Nevertheless, this is not always the case and sev-

eral systems relax almost independently of temperature at low temperature [4]. This phenomenon was sometimes systematically attributed to QTM. However, as pointed out by Barbara *et al.* in Ref. [4], too naive interpretations of relaxation experiments in complex systems may lead to spurious conclusions, especially when the experiments have been done down to 2 K only. In particular, power-law distributions of energy barriers $n(E) \propto E^{-\delta}$ can simulate QTM [5]. Several processes giving such power-law distributions at low temperatures have been identified [6–9].

In order to avoid these complications, some groups tried to study the magnetization reversal of *individual singledomain* particles or wires. Most of these studies were done by using magnetic force microscopy at room temperature [10]. To our knowledge, only three groups could study magnetization reversal of small particles and wires at low temperatures [11-13]. However, their measurements lacked the ability to identify the classical regime described by the Néel-Brown theory of thermal activated magnetization reversal [14] and showed that such small particles and wires were still too complex (too large, defects due to surface roughness, oxidation, etc.). The agreement with the classical theory of Néel and Brown constitutes the precondition for the experimental observation of MQT.

In this Letter, we present single particle measurements on 10–20 nm particles of BaFeCoTiO. These particles are single-crystalline disks with hexagonal contour. We found that above 0.4 K, the magnetization reversal of these particles is unambigously described by a thermally activated rotation of the particle's moment over a well defined anisotropy energy barrier, as originally proposed by Néel and Brown [14]. At lower temperature, strong deviations are evidenced which compare quantitatively to the predictions of the existing MQT theory without dissipation. Details on measuring technique, sample deposition, and a

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review of the Néel-Brown theory are reported in Ref. [15] and references therein.

The BaFe_{12-2x}Co_xTi_xO₁₉ nanoparticles have a strong uniaxial magnetocrystalline anisotropy depending on the Co-Ti substitution [16]. We studied compositions with $0 \le x \le 0.8$. The measurements presented in this Letter were obtained with x = 0.8.

In order to confirm the single-domain character of our particles, we studied the magnetization reversal of each particle as a function of the applied field direction. Influence of temperature and time on the statistics of the magnetization reversal was studied by waiting time and switching field experiments. Via the waiting time measurements, we had direct access to the switching probability. At given temperature, the magnetic field was increased to a waiting field which was close to the switching field. Then, we measured the elapsed time until the magnetization switched. This process was repeated several hundred times, in order to obtain a waiting time histogram. The integral of this histogram gave the switching probability. Regarding switching field measurements, the applied field was ramped at a given rate v = dH/dt, and the field value was stored as soon as the sample magnetization switched. Then, the field ramp was reversed and the process was repeated. After several hundred cycles, switching field histograms were established, allowing us to obtain the mean switching fields $H_{\rm sw}$ and the width σ (root mean square deviation). Both types of measurements can be studied as a function of the applied field direction which is defined by the angle θ between the easy axis of magnetization and the field direction.

In order to summarize the quasistatic magnetization measurements performed on a $10^5 \mu_B$ BaFeCoTiO nanoparticle, called particle I, we present in Fig. 1 the angular dependence of the reversal field H_{sw} . This dependence fits to the famous Stoner and Wohlfarth astroid showing that the magnetization reversal is a *rotation at the unison* [17]. The magnetocrystalline anisotropy field $\mu_0 H_a$, found by these measurements for particles with a Co_{0.8}Ti_{0.8} substitution, is about 0.4 T.

Between 0.4 and 6 K, waiting time and switching field measurements on all BaFeCoTiO nanoparticles were in complete agreement with the Néel-Brown theory: (i) exponential probabilities of not switching with mean waiting times following an Arrhenius law and (ii) mean switching fields and widths of the switching field distribution following the model of Kurkijärvi [18] [Eqs. (1) to (5) in Ref. [15]]. In Fig. 2, we demonstrate this agreement by a scaling plot of $H_{sw}(v, T)$. For T > 0.4 K, the data of $H_{sw}(v,T)$ could be aligned on the master curve being a straight line. The adjustments allowed us to determine all parameters of the model of Kurkijärvi, namely, E_0 being the height of the energy barrier at $H = 0, H_{sw}^0$ being the switching field at T = 0 K, and τ_0 being the prefactor of the Arrhenius law [see Eq. (3) in Ref. [15]]. Knowing these parameters, the model of Kurkijärvi pre-



FIG. 1. Switching field $H_{sw}(\theta')$ of the BaFeCoTiO particle I as a function of the angle θ' measured between the applied field direction and the in-the-SQUID-plane-projected easy axis of magnetization, at T = 0.2 K. The continuous line is the prediction of the Stoner-Wohlfarth model. Note that the easy axis of magnetization of this particle is out of the SQUID plane by about 20° which leads to a rounding of the astroid near zero angle.

dicts the switching field distribution [the width σ is given by Eq. (5) in Ref. [15]]. Again, a good agreement between theory and measurements was found for T > 0.4 K (Figs. 3 and 4).

This agreement could be confirmed by studying the angular dependence of E_0 following the prediction of the Stoner-Wohlfarth model [17,19]. The number of spins *S* in the nanoparticle can be estimated by $S \approx E_0/(2\mu_B\mu_0 H_{\rm sw}^0)$. We found $S \approx 10^5$ and 10^6 for particles I and II, respectively. Finally, the angular dependence



FIG. 2. Typical scaling plots of the mean switching fields H_{sw} for particle I. The applied field was swept at an angle of $\theta = 79^{\circ}$. The measurements were done at field sweeping rates v between 0.01-120 mT/s and temperatures between 0.13-2.5 K. Insets: Same data of $H_{sw}(v, T)$ and same scales but the real temperature T is replaced by an effective temperature T^* which restores the scaling below 0.4 K (see Fig. 5).



FIG. 3. Temperature dependence of the width of the switching field distribution σ for $\mu_0 dH/dt = 10$ mT/s and at three different angles of the applied field for particle I of about $10^5 \mu_B$. Full points were measured on particle II of about $10^6 \mu_B$ at $\theta \approx 20^\circ$. Lines: prediction of the Kurkijärvi model.

of τ_0 followed well the prediction of Coffey *et al.* [20]. The phenomenological damping constant α from the Gilbert's equation could be found: $\alpha \approx 10^{-3}$ [21] which corresponds to the low damping regime, expected for insulating particles and justifying the comparison with the theory of QTM in the low dissipation regime.

Below 0.4 K several of the smallest particles showed strong deviations from the Néel-Brown model. These deviations were a saturation of the thermal dependence of H_{sw} and σ , and a faster field sweeping rate (v = dH/dt) dependence H_{sw} than given by the Néel-Brown model (see Figs. 2 and 3). In order to investigate the possibility that the low temperature deviations are due to an escape from the metastable potential by MQT, a common method is to replace the real temperature Tby an effective temperature $T^*(T)$ in order to restore the scaling plot. In the case of MQT, $T^*(T)$ should



FIG. 4. Switching fields distributions for several temperatures as a function of $\varepsilon = 1 - H_{sw}/H_{sw}^0$. The applied field was swept at an angle of $\theta = 79^{\circ}$ and at a rate of $\mu_0 dH/dt =$ 60 mT/s. The lines are predictions of the Kurkijärvi model showing a good agreement for T > 0.4 K. All parameters of the Kurkijärvi model were found by the scaling plot in Fig. 2.

saturate at low temperatures. Indeed, we found that the ansatz of $T^*(T)$ as shown in the inset of Fig. 5, can restore unequivocally the scaling plot demonstrated by a straight master curve (inset of Fig. 2). The flattening of T^* corresponds to a saturation of the escape rate Γ which is a necessary signature of MQT. As measurements at zero temperature are impossible, we investigated the effective temperature at our lowest measuring temperature and defined the crossover temperature between thermally activated and the quantum regime by $T_c = T^*$ at $T \approx 0.12$ K (see inset of Fig. 5).

The angular dependence of the crossover temperature of a ferromagnetic particle [22] was considered by several authors [23–25]. As the BaFeCoTiO particles have a strong uniaxial anisotropy and weak in-plane anisotropy, we compared our measurements by taking into account only uniaxial anisotropy [24]:

$$T_c(\theta) \propto \mu_0 H_a \varepsilon^{1/4} |\cot \theta|^{1/6} (1 + |\cot \theta|^{2/3})^{-1},$$
 (1)

where $\mu_0 H_a$ is the anisotropy field given in Tesla and $\varepsilon = (1 - H/H_{sw}^0)$. The proportionally coefficient of Eq. (1) is of the order of unity and depends on the approach of the calculation [25]. Our measured angular dependence of $T_c(\theta)$ is in excellent agreement with this prediction (Fig. 5). The normalization value $T_c(45^\circ) = 0.31$ K compares well with the theoretical value of about 0.2 K. This quantitative agreement of the crossover temperature versus an external parameter strongly suggests MQT in these BaFeCoTiO particles.

Measurements on other particles with anisotropy between $H_a = 0.3$ and 1 T showed that $T_c(\theta)$ is about proportional to H_a . Furthermore, we found that, for a given anisotropy field H_a , $T_c(\theta)$ decreases for bigger particles (see particle II in the inset of Fig. 5) which is also in agreement with Eq. (1) as $T_c(\theta)$ is proportional to $\varepsilon^{1/4}$



FIG. 5. Angular dependence of the crossover temperature T_c for particle I. The line is given by Eq. (1). The values are normalized by $T_c(45^\circ) = 0.31$ K. Inset: Effective temperature T^* as a function of the real temperature T at three different angles of the applied field. Full points were measured on the particle II, of about $10^6 \mu_B$.

(for a bigger particle, ε must be smaller in order to measure a magnetization switching in the same time window, which is fixed by the field sweeping rate v). Finally, the width of the switching field distribution should be constant in the quantum regime which is also verified by our measurements (Figs. 3 and 4).

The agreement with the Néel-Brown theory was obtained recently for the first time on 20 nm Co particles of similar quality [15]. However, no clear quantum effects were found down to 0.2 K. This was not surprising for two reasons: (i) The calculated crossover temperature for such a particle is smaller than 0.2 K and (ii) the dissipation effects due to conduction electrons may strongly reduce quantum effects which should not be the case in insulating BaFeCoTiO particles having a very small damping factor $\alpha = 10^{-3}$.

The ultimate proof for MQT in a magnetic nanoparticle would be the observation of level quantization of its collective spin state which was recently evidenced in molecular Mn₁₂ and Fe₈ clusters having a collective spin state S = 10 [26]. In our case of $S = 10^5$, the field separation associated to the level quantization is rather small: $\Delta H = H_a/2S \approx 0.002$ mT. Future measurements should focus on the level quantization of collective spin states of $S = 10^2$ to 10^4 .

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