## Symmetry of the Gap in B12212 from Photoemission Spectroscopy

In a recent Letter, Shen et al. [1] detected a large anisotropy of the superconducting gap in  $Bi_2Sr_2CaCu_2O_8$ (Bi2212), consistent with  $d$ -wave symmetry from photoemission spectroscopy. Moreover, they claim that the change in their spectra as a function of aging is also consistent with such an interpretation. In this Comment, I show that the latter statement is not entirely correct, in that the data as a function of aging are inconsistent with a d-wave gap but are consistent with an anisotropic swave gap (assuming impurity scattering can be treated as in Ref. [2]).

In Ref. [1], the data show that the gap is close to zero along the (1,1) direction and maximum along the (1,0) direction, just as expected for a gap with  $d_{x^2-y^2}$ symmetry. As the sample ages, the gap becomes nonzero along  $(1,1)$ . This is attributed by them to poorer k resolution due to impurity scattering. This brings up the interesting question of what one theoretically expects for the excitation gap as a function of impurities. I do this for two cases where a spherical Fermi cylinder is assumed for simplicity's sake. For the  $d$ -wave case, the gap is assumed to be  $\Delta \cos(2\phi)$  and for the anisotropic s-wave case,  $\Delta |\cos(2\phi)|$ . Thus, the modulus of the gap is the same, the only difference being the symmetry of the gap under rotations.

The self-energy equations at  $T = 0$  in the Born approximation are [2,3]

$$
\tilde{\omega} = \omega + \frac{\Gamma}{2\pi} \int_0^{2\pi} d\phi' \frac{\tilde{\omega}}{[\tilde{\Delta}(\phi')^2 - \tilde{\omega}^2]^{1/2}}, \qquad (1)
$$

$$
\tilde{\Delta}(\phi) = \Delta(\phi) + \frac{\Gamma}{2\pi} \int_0^{2\pi} d\phi' \frac{\tilde{\Delta}(\phi')}{[\tilde{\Delta}(\phi')^2 - \tilde{\omega}^2]^{1/2}}, \quad (2)
$$

where  $\Gamma$  is the strength of the impurity scattering. These solutions are then used to determine the angle-resolved density of states:

$$
N(\phi,\omega) = N_0 \operatorname{Im}\left(\frac{\tilde{\omega}}{[\tilde{\Delta}(\phi)^2 - \tilde{\omega}^2]^{1/2}}\right),\tag{3}
$$

where  $N_0$  is the density of states in the normal state. The excitation gap is where  $N$  first becomes nonzero. For the d-wave case, this is zero for all  $\phi$  as soon as  $\Gamma$  is nonzero. Instead, the excitation gap employed here is the same as that defined in Ref. [1], that is, where the value of  $N/N_0$  first becomes equal to  $\frac{1}{2}$ . These result are summarized in Fig. 1. As can be seen, the  $d$ -wave case is qualitatively inconsistent with the data, since it becomes rapidly gapless as  $\Gamma$  increases. In contrast, the anisotropic s-wave case gives a behavior consistent with the data, with the gap becoming isotropic (equal to  $\Delta/2$ ) in the large  $\Gamma$  limit.

A final remark is that the gap equations have not been resolved  $(\Delta$  was treated as fixed). One can easily



FIG. 1. Excitation gap as a function of position on the Fermi surface for various impurity concentrations for  $d$ -wave case and anisotropic s-wave case. The lines are labeled by values of  $\Gamma/\Delta$ . The solid points are data from Ref. [1].

calculate the reduction of  $T_c$  with  $\Gamma$ 

$$
\ln\left(\frac{T_{c0}}{T_c}\right) = c\bigg[\psi\bigg(\frac{1}{2} + \frac{\Gamma}{2\pi T_c}\bigg) - \psi\bigg(\frac{1}{2}\bigg)\bigg],\qquad (4)
$$

where  $T_{c0}$  is  $T_c$  for the pure system and c is 1 for the *d*-wave case and  $1 - 8/\pi^2 \sim 0.19$  for the *s*-wave case. Similarly,  $\Delta$  decreases as  $\Gamma$  increases with the effect being much larger in the  $d$ -wave case. This makes the  $d$ -wave case even more inconsistent with the data.

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