

**van Megen and Underwood Reply:** The central issue of the Comment of Zeng *et al.* [1] concerns the reduction of the scaling time  $\tau_\beta$  with increasing  $\phi$  in the glass phase ( $\phi > \phi_c$ ). First, we stress that  $\tau_\beta$ , which enters a relaxation function of the form  $F(\tau) = f(\tau/\tau_\beta)$  anticipated by Zeng *et al.*, should not be interpreted as a characteristic time associated with a particular physical relaxation process. Indeed such an interpretation is precluded on the basis of the fractal decay indicated by the power law predicted for the early part of the  $\beta$  process [2]. For this stage the intermediate scattering function  $f(q, \tau)$  can be written as

$$f(q, \tau) = f_c(q) + h(q)(\tau/t_0)^{-a}, \quad (1)$$

where  $t_0$  specifies the absolute time scale. This  $\phi$  independent result follows from Eqs. (19) to (22) of Ref. [3]. In mode coupling theory (MCT),  $\tau_\beta$  represents the crossover from the  $\beta$  to the  $\alpha$  process; the latter describes structural relaxation towards equilibrium, characterized by the time scale  $\tau_\alpha$ . Below  $\phi_c$  structural relaxation slows with increasing  $\phi$  so that  $\tau_\alpha$  and also  $\tau_\beta$  increase.

In the glass phase ( $\phi > \phi_c$ ) the  $\alpha$  process arrests and here  $\tau_\beta$  marks the crossover from the above power law to the plateau,

$$f(q, \infty) = f_c(q) + h(q)|\sigma|^{1/2}(1-\lambda)^{-1/2}, \quad (2)$$

where the separation parameter  $\sigma = c(\phi - \phi_c)/\phi_c$ ,  $c \approx 1.2$  and the exponent  $a$  is related transcendently to the exponent parameter  $\lambda$  [see Eq. (2.51a) of Ref. [2]]. It follows that  $\tau_\beta$  varies as  $|\sigma|^{-1/2a}$ . The reduction in  $\tau_\beta$  with increasing  $\phi$  (or  $\sigma$ ) is a consequence of the concomitant increase in the asymptote  $f(q, \infty)$  and occurs irrespective of whether relaxation to the plateau proceeds by the above power law or the illustrative stretched exponential used by Zeng *et al.*

The stretched exponential

$$f(\tau) = A \exp[-(\tau/\tau_k)^\beta] \quad (3)$$

results in a more featureless range of scaling than that seen in the data (Fig. 8 of Ref. [3]). Bartsch *et al.* [4] have already shown that relaxation data similar to ours cannot be satisfactorily explained in terms of stretched exponentials. One reason for this is that our relaxation curves (Figs. 6 and 8 of Ref. [3]) expressed in terms of  $\log \tau$  are convex over time windows as large as 3 orders of magnitude. The stretched exponential function [Eq. (3)], on the other hand, is convex for  $\tau/\tau_k \gg 1$ , where the function is close to zero. Consequently, in the figure of Zeng *et al.*, convex curvature is apparent only over intervals smaller than one decade. Our data, therefore, illustrate that a more complete description of the relaxation to the plateau is given by a power law rather than by a stretched exponential.

Zeng *et al.* state that we should have determined  $f_c(q)$  and  $\phi_c$  experimentally. We stress that we have measured both these quantities.  $\phi_c$  has been identified as the concentration where the fluid structure is arrested on the ex-

perimental time scale and also as that where homogeneous nucleation is suppressed. The nonergodicity parameter  $f_c(q)$  has been determined by three independent methods; first, from the long time value of  $f(q, \tau)$  (Fig. 4 of Ref. [5]); second, from the mean-squared amplitude of fluctuations of the intensity of the scattered light (Fig. 5 of Ref. [3]); and third, from the amplitude of the  $\alpha$  process for  $\phi < \phi_c$  (Fig. 2 of Ref. [6]). Different procedures yield consistent results with accuracy levels of 1% and 5% for  $\phi_c$  and  $f_c(q)$ , respectively. In seeking optimum MCT fits to our relaxation data  $\phi_c$  (or  $\sigma$ ) and  $f_c(q)$  are varied only within these tolerances. The only unconstrained parameter is the absolute time scale, which is not specified by the theory. It then becomes a matter of semantics whether or not  $\phi_c$  and  $f_c(q)$  are regarded as fit parameters.

Finally, we can summarize our results in terms of MCT as follows: All our measured relaxation functions outside the microscopic transients can be described by the basic version of MCT to an accuracy of (10–15)% using a single fitting parameter  $t_0$ . The error margins reflect to some extent our experimental uncertainties but also systematic errors of the theory. This description extends over 4 to 5 decades in time, holds for a significant spread of  $q$  values and  $\alpha$  relaxation times that vary over 5 decades for the 8 concentrations analyzed. In particular, our estimates of  $\tau_\beta$  obtained by fitting the MCT master functions to the scaled data for  $\phi > \phi_c$  allow us to confirm the predicted value of the exponent  $a = 0.301$  to an accuracy of about  $\pm 0.03$ . This uncertainty slightly exceeds that obtained for  $a$  from the tolerance, determined from our data below the glass transition ( $\phi < \phi_c$ ), in the exponent parameter  $\lambda$ . Our results confirm that  $\tau_\beta$  increases as  $\phi_c$  is approached from either side.

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