

## Properties of Orbitally Excited Heavy-Light ( $Q\bar{q}$ ) Mesons

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Orbitally excited heavy-light ( $Q\bar{q}$ ) mesons are potentially important as tools for tagging the flavors and momenta of ground-state pseudoscalars detected through weak decays. We use heavy-quark symmetry supplemented by insights gleaned from potential models to estimate masses and widths of  $p$ -wave  $B$ ,  $B_s$ , and  $D_s$  mesons. We generalize these results to higher excitations.

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Incisive study of particle-antiparticle mixing and  $CP$  violation for neutral  $B$  mesons requires that the quantum numbers of the meson be identified at the time of production. That identification can be made by observing the decay of a  $B$  or  $\bar{B}$  produced in association with a particle of opposite  $b$  number whose decay signals the flavor of the neutral  $B$  of interest. The efficiency of flavor identification might be dramatically enhanced if the neutral  $B$  under study were self-tagging [1].

Charmed mesons have been observed as (strong) decay products of orbitally excited ( $c\bar{q}$ ) states, through the decays  $D^{**} \rightarrow \pi D$  and  $D^{**} \rightarrow \pi D^*$  [2]. The charge of the pion emitted in the strong decay signals the flavor content of the charmed meson. If significant numbers of  $B$  mesons are produced through one or more narrow excited ( $\bar{b}q$ ) states, the strong decay  $B^{**\pm} \rightarrow B^{(*)0}\pi^\pm$  tags the neutral meson as ( $\bar{b}d$ ) or ( $b\bar{d}$ ), respectively.

The primary application of  $B^{**}$  tagging would be in the search for the expected large  $CP$ -violating asymmetry in ( $B^0$  or  $\bar{B}^0$ )  $\rightarrow J/\psi K_S$  decay [3].  $B^{**}$  tagging may also resolve kinematical ambiguities in semileptonic decays of charged and neutral  $B$  mesons by choosing between two solutions for the momentum of an undetected neutrino. In hadron colliders and  $Z^0$  factories, kinematic tagging may make practical high-statistics determinations of the form factors in semileptonic weak decay, and enable precise measurements of  $V_{cb}$  and  $V_{ub}$  [4,5].

In this Letter, we estimate the masses, widths, and branching fractions of orbitally excited  $B$ ,  $D_s$ , and  $B_s$  states from the properties of corresponding  $K$  and  $D$  levels. Our results show that one requirement for the utility of  $B^{**}$  tagging, narrow resonances, is likely to be met by the  $B_2^*$  and  $B_1$ . Experiment must rule on the strength of these lines and the ratio of signal to background.

For hadrons containing a heavy quark  $Q$ , quantum chromodynamics displays additional symmetries in the limit as the heavy-quark mass  $m_Q$  becomes large compared with a typical QCD scale [6]. These heavy-quark symmetries are powerful aids to understanding the spectrum and decays of heavy-light ( $Q\bar{q}$ ) mesons. Because  $m_b \gg \Lambda_{\text{QCD}}$ , heavy-quark symmetry should provide an excellent description of the  $B$  and  $B_s$  mesons. It is plausible that properties of  $D$  mesons, and even  $K$  mesons, should also reflect approximate heavy-quark symmetry.

One essential idea of the heavy-quark limit is that the

spin  $\vec{s}_Q$  of the heavy quark and the total (spin + orbital) angular momentum  $\vec{j}_q = \vec{s}_q + \vec{L}$  of the light degrees of freedom are separately conserved [7]. Accordingly, each energy level in the excitation spectrum of ( $Q\bar{q}$ ) mesons is composed of a degenerate pair of states characterized by  $j_q$  and the total spin  $\vec{J} = \vec{j}_q + \vec{s}_Q$ , i.e., by  $J = j_q \pm \frac{1}{2}$ . The ground-state pseudoscalar and vector mesons, which are degenerate in the heavy-quark limit, correspond to  $j_q = \frac{1}{2}$ , with  $J = 0$  and 1. Orbital excitations lead to two distinct doublets associated with  $j_q = L \pm \frac{1}{2}$ .

*Masses.*—The leading corrections to the spectrum prescribed by heavy-quark symmetry are inversely proportional to the heavy-quark mass. We may write the mass of a heavy-light meson as

$$M(nL_J(j_q)) = M(1S) + E(nL(j_q)) + \frac{C(nL_J(j_q))}{m_Q}, \quad (1)$$

where  $n$  is the principal quantum number and  $M(1S) = [3M(1S_1) + M(1S_0)]/4$  is the mass of the ground state. The excitation energy  $E(nL(j_q))$  has a weak dependence on the heavy-quark mass.

Let us focus first upon the  $j_q = \frac{3}{2}$  states observed as narrow  $D\pi$  or  $D^*\pi$  resonances. We appeal to potential models to estimate how the excitation spectrum varies with heavy-quark mass. Although nonrelativistic potential models have obvious limitations for systems that include light quarks, we find that the Buchmüller-Tye potential [8] gives a good account of the observed  $K$ ,  $D$ , and  $D_s$  levels. The potential-model spectra can also serve as templates for unobserved states, particularly those along the leading Regge trajectory.

According to Eq. (1), the masses of the strange and charmed mesons with  $j_q = \frac{3}{2}$  are given by

$$\begin{aligned} M(2P_2)_K - M(1S)_K &= E(2P)_K + \frac{C(2P_2)}{m_s}, \\ M(2P_1)_K - M(1S)_K &= E(2P)_K + \frac{C(2P_1)}{m_s}, \\ M(2P_2)_D - M(1S)_D &= E(2P)_D + \frac{C(2P_2)}{m_c}, \\ M(2P_1)_D - M(1S)_D &= E(2P)_D + \frac{C(2P_1)}{m_c}, \end{aligned} \quad (2)$$

where we have suppressed the  $j_q$  label for brevity. Upon identifying  $E(2P)_D = E(2P)_K - \delta$ , where  $\delta = 32$  MeV is

TABLE I. Masses (in MeV) predicted for the  $2P(\frac{3}{2})$  levels of the  $B$ ,  $D_s$ , and  $B_s$  systems. Underlined entries are Particle Data Group averages [9] used as inputs.

Meson family	$K$	$D$	$B$	$D_s$	$B_s$
$M(1S)$	<u>794.3</u>	<u>1973.2</u>	<u>5313.1</u>	<u>2074.9</u>	5409.1 <sup>a</sup>
Level shift $\delta$	0	32	42	56	67
$M(2^+(\frac{3}{2}))$	<u>1429 ± 6</u>	<u>2459.4 ± 2.2</u>	5767	2537	5846
$M(1^+(\frac{3}{2}))$	<u>1270 ± 10</u>	<u>2424 ± 6</u>	5755	2502	5834
$M(2^+(\frac{3}{2})) - M(1^+(\frac{3}{2}))$	159	35	12	35	12

<sup>a</sup>Assuming that  $M(1S) = M(1S_0) + 34.5$  MeV, as in the  $B$  system. The pseudoscalar mass,  $M_{B_s} = 5374.6$  MeV, is the weighted mean of the ALEPH and CDF values [10].

determined from the potential-model spectra, we are left with four linear equations in the five unknowns  $E(2P)_K$ ,  $C(2P_2)$ ,  $C(2P_1)$ ,  $m_s^{-1}$ , and  $m_c^{-1}$ .

The  $K$ - and  $D$ -meson masses we use as experimental inputs are displayed in Table I. There is no ambiguity about the  $2^+(\frac{3}{2})$  levels. We identify  $D_1(2424)$  as a  $j_q = \frac{3}{2}$  level because it is narrow, as predicted [11,12] by heavy-quark symmetry. We follow Ito *et al.* [13] in identifying  $K_1(1270)$  as the  $1^+(\frac{3}{2})$  level, because that assignment gives a consistent picture of masses and widths.

To proceed, we choose a value for the charmed-quark mass,  $m_c$ . We consider two sets of parameters inspired by  $J/\psi$  and  $\Upsilon$  spectroscopy:  $m_c = 1.48$  GeV,  $m_b = 4.8$  GeV [8] and  $m_c = 1.84$  GeV,  $m_b = 5.18$  GeV [14]. Both solutions [ $C(2P_2) = (0.0495, 0.06155)$  GeV<sup>2</sup>,  $C(2P_1) = (-0.0029, -0.00358)$  GeV<sup>2</sup>,  $E(2P)_K = (0.4844, 0.48445)$  GeV,  $m_s = (0.33, 0.41)$  GeV] yield reasonable values for the strange-quark mass. Their implications for the  $B$ ,  $D_s$ , and  $B_s$  levels are consistent within 2 MeV. The average values are presented in Table I. Including the variation of excitation energy represented by the parameter  $\delta$  has lowered the masses by 7, 26, and 32 MeV for the  $B$ ,  $D_s$ , and  $B_s$  states.

Our prediction for the  $1^+$   $D_s$  meson lies 34 MeV below the level observed [9,15] at  $2536.5 \pm 0.8$  MeV. We take the discrepancy between calculated and observed masses as a measure of the limitations of our method.

The  $2P(\frac{1}{2})$   $D$  mesons have not yet been observed, so we cannot predict the masses of other heavy-light states by this technique. Splitting within the multiplet can be estimated using Eq. (1) from the kaon spectrum alone. The small splitting between  $K_0^*(1429)$  and  $K_1(1402)$  implies that the  $1^+(\frac{1}{2})$  and  $0^+(\frac{1}{2})$  levels should be nearly degenerate in all the heavy-light systems. Chiral symmetry and heavy-quark symmetry combined suggest that the heavy-light  $j_q = \frac{1}{2}$   $p$ -wave states should have large widths for pionic decay to the ground states [16]. This will make the discovery and study of these states challenging, and will limit their utility for  $B^{**}$  tagging.

*Decay widths.*—Consider the decay of an excited heavy-light meson  $H$ , characterized by  $L_J(j_q)$ , to a heavy-light meson  $H'(L'_J(j'_q))$ , and a light hadron  $h$  with spin  $s_h$ . The amplitude for the emission of  $h$  with orbital angular momentum  $\ell$  relative to  $H'$  satisfies certain symmetry relations because the decay dynamics becomes in-

dependent of the heavy-quark spin in the  $m_Q \rightarrow \infty$  limit of QCD [11]. The decay amplitude can be factored [12] into a reduced amplitude  $\mathcal{A}_R$  times a normalized 6- $j$  symbol,

$$\mathcal{A}(H \rightarrow H'h) = (-1)^{s_Q + j_h + J' + j_q} C_{j_h, J, j_q}^{s_Q, j'_q, J'} \mathcal{A}_R(j_h, \ell, j_q, j'_q),$$

where

$$C_{j_h, J, j_q}^{s_Q, j'_q, J'} = \sqrt{(2J' + 1)(2j_q + 1)} \begin{Bmatrix} s_Q & j'_q & J' \\ j_h & J & j_q \end{Bmatrix}$$

and  $\vec{j}_h \equiv \vec{s}_h + \vec{\ell}$ . The coefficients  $C$  depend only upon the total angular momentum  $j_h$  of the light hadron, and not separately on its spin  $s_h$  and the orbital angular momentum wave  $\ell$  of the decay. The two-body decay rate may be written as

$$\Gamma_{j_h, \ell}^{H \rightarrow H'h} = (C_{j_h, J, j_q}^{s_Q, j'_q, J'})^2 p^{2\ell+1} F_{j_h, \ell}^{j_q, j'_q}(p^2), \quad (3)$$

where  $p$  is the three-momentum of the decay products in the rest frame of  $H$ . Heavy-quark symmetry does not predict the reduced amplitude  $\mathcal{A}_R$  or the related  $F_{j_h, \ell}^{j_q, j'_q}(p^2)$  for a particular decay. Once determined from the charmed or strange mesons, these dynamical quantities may be used to predict related decays, including those of orbitally excited  $B$  mesons. For each independent decay process, we assume a modified Gaussian form

$$F_{j_h, \ell}^{j_q, j'_q}(p^2) = F_{j_h, \ell}^{j_q, j'_q}(0) \exp(-p^2/\kappa^2) \left[ \frac{M_\rho^2}{M_\rho^2 + p^2} \right]^\ell, \quad (4)$$

and determine the overall strength of the decay and the momentum scale  $\kappa$  by fitting existing data. The final factor moderates the  $p^\ell$  threshold behavior of the decay amplitude at high momenta [17].

In writing (3) we have ignored  $1/m_Q$  corrections to heavy-quark symmetry predictions for decay rates, except as they modify the momentum  $p$  of the decay products. We assume that the momentum scale  $\kappa$  of the form factor in (4) is typical of hadronic processes ( $\approx 1$  GeV) and that it varies little with decay angular momentum  $\ell$ .

The decays  $2P(\frac{3}{2}) \rightarrow 1S(\frac{1}{2}) + \pi$  are governed by a single  $\ell = 2$  amplitude. To evaluate the transition strength  $F_{2,2}^{3/2, 1/2}(0)$ , we fix  $\Gamma(D_2^* \rightarrow D\pi) + \Gamma(D_2^* \rightarrow D^*\pi) = 25$  MeV, as suggested by recent experiments [2]. This determines all pionic transitions between the  $2P(\frac{3}{2})$  and  $1S(\frac{1}{2})$  multiplets. The results are shown in Table II; the predicted

TABLE II. Decay rates of the  $2P(\frac{3}{2})$  heavy-light mesons.

Transition	Width (MeV)	
	Calculated	Observed <sup>a</sup>
$D_2^*(2459) \rightarrow D^*\pi$	9 <sup>b</sup>	
$D_2^*(2459) \rightarrow D\pi$	16 <sup>b</sup>	
$D_2^*(2459) \rightarrow D\eta$	$\sim 0.1$	
$D_2^*(2459) \rightarrow D^*\rho$	3	
$D_2^*(2459) \rightarrow D\rho$	< 1	
$D_2^*(2459) \rightarrow \text{all}$	28	$19 \pm 7$
$D_1(2424) \rightarrow D^*\pi$	11	
$D_1(2424) \rightarrow D^*\rho$	< 1	
$D_1(2424) \rightarrow D\rho$	6	
$D_1(2424) \rightarrow \text{all}$	18	$20_{-5}^{+9}$
$D_{s2}^*(2537) \rightarrow D^*K$	< 1	
$D_{s2}^*(2537) \rightarrow DK$	7	
$D_{s2}^*(2537) \rightarrow D_s\eta$	$\sim 0.1$	
$D_{s2}^*(2537) \rightarrow \text{all}$	7	
$D_{s1}(2502) \rightarrow D^*K$	< 1	< 4.6
$B_2^*(5767) \rightarrow B^*\pi$	11	
$B_2^*(5767) \rightarrow B\pi$	10	
$B_2^*(5767) \rightarrow B^*\rho$	3	
$B_2^*(5767) \rightarrow B\rho$	< 1	
$B_2^*(5767) \rightarrow \text{all}$	24	
$B_1(5755) \rightarrow B^*\pi$	16	
$B_1(5755) \rightarrow B^*\rho$	1	
$B_1(5755) \rightarrow B\rho$	3	
$B_1(5755) \rightarrow \text{all}$	20	
$B_{s2}^*(5846) \rightarrow B^*K$	< 1	
$B_{s2}^*(5846) \rightarrow BK$	1	
$B_{s2}^*(5846) \rightarrow \text{all}$	2	
$B_{s1}(5834) \rightarrow B^*K$	< 1	
$K_2^*(1429) \rightarrow K^*\pi$	12	25
$K_2^*(1429) \rightarrow K\pi$	27	50
$K_2^*(1429) \rightarrow K\rho$	12	9
$K_2^*(1429) \rightarrow K\omega$	3	3
$K_2^*(1429) \rightarrow \text{all}$	55	
$K_1(1270) \rightarrow K^*\pi$	6	14
$K_1(1270) \rightarrow K\rho$	38 <sup>c</sup>	38
$K_1(1270) \rightarrow K\omega$	7	10
$K_1(1270) \rightarrow \text{all}$	51	

<sup>a</sup>1992 Particle Data Group values [9].

<sup>b</sup>Sum fixed at 25 MeV.

<sup>c</sup>Input value.

rates are stable as the momentum scale  $\kappa$  ranges from 0.8 to 1.2 GeV. SU(3) determines the strengths of  $K$  and  $\eta$  transitions [18]. The predictions agree well with what is known about the  $L = 1$   $D$  and  $D_s$  states [19]. The ratio  $\Gamma(D_2^* \rightarrow D\pi)/\Gamma(D_2^* \rightarrow D^*\pi) = 1.8$  is consistent with the Particle Data Group average,  $2.4 \pm 0.7$  [9], and with a recent CLEO measurement,  $2.1 \pm 0.6 \pm 0.6$  [20].

Increasing the  $D_{s1}$  and  $D_{s2}^*$  masses by 34 MeV to match the observations of  $D_{s1}$  increases each of the partial widths for those states by 1 or 2 MeV. The narrow width observed for  $D_{s1}$  is consistent with the prediction from heavy-quark symmetry. This suggests that mixing of the narrow  $2P(\frac{3}{2})$  level with the broader  $2P(\frac{1}{2})$  state

TABLE III. Properties of the  $3D(\frac{5}{2})$  heavy-light mesons.

State	Mass (MeV)	Width (MeV)
$K_3^*$	1770	190
$K_2$	1770	100
$D_3^*$	2830	240
$D_2$	2830	140
$D_{s3}^*$	2880	100
$D_{s2}$	2880	60
$B_3^*$	6148	180
$B_2$	6148	170
$B_{s3}^*$	6198	100
$B_{s2}$	6198	90

[11,12] is negligible. This pattern should hold for  $B$  and  $B_s$  as well. We have also applied heavy-quark dynamics to the decays of the  $2P(\frac{3}{2})$  strange mesons. The pionic transition rates given in Table II are somewhat lower than the experimental values, but the ratios agree well with experiment.

Decays of the  $2P(\frac{3}{2})$  states into a vector meson plus a  $1S(\frac{1}{2})$  level are governed by three independent decay amplitudes characterized by  $(j_h, \ell) = (2, 2)$ ,  $(1, 2)$ , and  $(1, 0)$ . SU(6) symmetry identifies the  $(2, 2)$  transition strength with the  $F_{2,2}^{\frac{3}{2}, \frac{1}{2}}(0)$  for pion emission. The two new amplitudes occur in a fixed combination that should be dominated by the  $\ell = 0$  amplitude. We have to evaluate one new transition strength,  $F_{1,0}^{\frac{3}{2}, \frac{1}{2}}(0)$ . Lacking measurements of partial widths for vector-meson emission in the charmed states, and encouraged by the pattern of pionic decay widths for the strange resonances, we use the decay rate  $\Gamma(K_1(1270) \rightarrow \rho + K) = 37.8$  MeV to fix  $F_{1,0}^{\frac{3}{2}, \frac{1}{2}}(0)$ . We smear the expression (3) for the partial width over a Breit-Wigner form to take account of the 150-MeV width of the  $\rho$  resonance. The resulting estimates for the  $\rho$  transitions are also shown in Table II. Rates for  $K^{**} \rightarrow K\omega$  decays follow by SU(3) symmetry.

The results collected in Table II show that both the  $B_2^*$  and the  $B_1$  states should be narrow, with large branching fractions to a ground state  $B$  or  $B^*$  plus a pion. These states should also have significant two-pion transitions that we have modeled by the low-mass tail of the  $\rho$  resonance. The strange states,  $B_{s2}^*$  and  $B_{s1}$ , are very narrow ( $\Gamma \lesssim 10$  MeV); their dominant decays are by kaon emission to the ground state  $B$  and  $B^*$ . The consistent picture of  $K_1$  and  $K_2^*$  decay rates supports the identification [13] of  $K_1(1270)$  as the  $2P_1(\frac{3}{2})$  level.

To assess the prospects for tagging  $B_s$ , we consider briefly the  $L = 2$  heavy-light mesons with  $j_q = \frac{5}{2}$ . Only the  $K$  mesons have been observed. The identification of the  $K_3^*(1770)$  as a  $3D_3(\frac{5}{2})$  level is clear. Two  $J^P = 2^-$  levels,  $K_2(1773)$  and  $K_2(1816)$ , are candidates for its partner [21]. Whatever the assignment for the  $3D_2(\frac{5}{2})$  level, the splitting within the  $j_q = \frac{5}{2}$  doublet will be very small for the  $D^{***}(2830)$ ,  $B^{***}(6148)$ ,  $D_s^{***}(2880)$ , and

$B_s^{***}(6198)$  systems.

To evaluate the transition strength  $F_{3,3}^{\frac{5}{2},\frac{1}{2}}(0)$  for pseudoscalar emission, we fix  $\Gamma(K_3^* \rightarrow K^*\pi) = 45$  MeV. As before, SU(6) symmetry determines the strength  $F_{3,3}^{\frac{5}{2},\frac{1}{2}}(0)$  for vector-meson emission. In the absence of measurements that would allow us to fix the other important decay amplitude, we have set  $F_{2,1}^{\frac{5}{2},\frac{1}{2}}(0) = 0$ . Our projections for vector-meson emission will therefore be underestimates. We summarize our expectations for the total widths of the  $3D(\frac{5}{2})$  states in Table III. The  $3D(\frac{5}{2})$   $B$  mesons will be broad ( $\approx 175$  MeV), but decay with about 20% probability to  $B_s$  and  $B_s^*$  by emitting a kaon. The favorable branching fraction means that it might be possible to use  $B_3^*$  and  $B_2$  decays to tag the  $B_s$ , in spite of the large total widths.

Properties of orbitally excited heavy-light mesons will test the validity of heavy-quark symmetry, which may offer new insight into the spectrum of strange mesons. If the narrow  $B_2^*$  and  $B_1$  are copiously produced with little background, efficient tagging of flavor and momentum may be at hand. Prospects for incisive  $B$  studies at high energies would then be dramatically enhanced [5].

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[1] M. Gronau, A. Nippe, and J. L. Rosner, Phys. Rev. D **47**, 1988 (1993).

[2] Observations of the  $L = 1$  charmed (and charmed-strange) mesons are reported in ARGUS Collaboration, H. Albrecht *et al.*, Phys. Lett. B **221**, 422 (1989); **230**, 162 (1989); **231**, 208 (1989); **232**, 398 (1989); **297**, 425 (1992); Tagged Photon Spectrometer Collaboration, J. C. Anjos *et al.*, Phys. Rev. Lett. **62**, 1717 (1989); CLEO Collaboration, P. Avery *et al.*, Phys. Rev. D **41**, 774 (1990); Phys. Lett. B **303**, 377 (1993); E687 Collaboration, P. L. Frabetti *et al.*, Report No. Fermilab-Pub-93/249-E (unpublished), determine  $\Gamma(D_2^*) = 24 \pm 7 \pm 5$  MeV,  $\Gamma(D_1) = 15 \pm 8 \pm 5$  MeV,  $\Gamma(D_{s1}) < 3.2$  MeV; CLEO Collaboration, G. Crawford *et al.*, contribution No. 282 to the XVI International Symposium on Lepton and Photon Interactions, 1993 (unpublished), find

$\Gamma(D_2^*) = 28_{-7}^{+8+6}$  MeV,  $\Gamma(D_1) = 20_{-5}^{+6+3}$  MeV,  $\Gamma(D_{s1}) < 2.3$  MeV.

- [3] C. Kim, J. L. Rosner, and C.-P. Yuan, Phys. Rev. D **42**, 96 (1990); **45**, 389(E) (1992); C. Dib, I. Dunietz, F. J. Gilman, and Y. Nir, Phys. Rev. D **41**, 1522 (1990).
- [4] M. Neubert, Phys. Lett. B **264**, 455 (1991); P. Cho and B. Grinstein, *ibid.* **285**, 153 (1992).
- [5] C. T. Hill, Report No. Fermilab-Conf-93-256/T (unpublished).
- [6] N. Isgur and M. B. Wise, Phys. Lett. B **232**, 113 (1989); for a review, see M. Neubert, Report No. SLAC-PUB-6263 (to be published).
- [7] E. Eichten and F. Feinberg, Phys. Rev. D **23**, 2724 (1981); W. E. Caswell and G. P. Lepage, Phys. Lett. B **167**, 437 (1986); E. Eichten, in *Proceedings of the 1987 International Symposium on Field Theory on the Lattice*, edited by A. Billoire *et al.* [Nucl. Phys. B (Proc. Suppl.) **4**, 170 (1988)]; G. P. Lepage and B. A. Thacker, *ibid.*, p. 199.
- [8] W. Buchmüller and S.-H. H. Tye, Phys. Rev. D **24**, 132 (1981). We take  $m_q = 0.3$  GeV,  $m_s = 0.45$  GeV,  $m_c = 1.48$  GeV, and  $m_b = 4.8$  GeV.
- [9] Particle Data Group, K. Hikasa *et al.*, Phys. Rev. D **45**, S1 (1992).
- [10] CDF Collaboration, F. Abe *et al.*, Phys. Rev. Lett. **71**, 1685 (1993), report the mass of the  $B_s$  meson as  $5383.3 \pm 4.5 \pm 5.0$  MeV; ALEPH Collaboration, D. Buskulic *et al.*, Report No. CERN-PPE/93-97 (unpublished) report  $5368.6 \pm 5.6 \pm 1.5$  MeV. See also OPAL Collaboration, P. D. Acton *et al.*, Phys. Lett. B **295**, 357 (1992).
- [11] N. Isgur and M. Wise, Phys. Rev. Lett. **66**, 1130 (1991).
- [12] A. F. Falk and M. Luke, Phys. Lett. B **292**, 119 (1992).
- [13] T. Ito, T. Morii, and M. Tanimoto, Prog. Theor. Phys. **90**, 419 (1993).
- [14] E. J. Eichten, K. Gottfried, T. Kinoshita, K. D. Lane, and T.-M. Yan, Phys. Rev. D **21**, 203 (1980).
- [15] CLEO Collaboration, J. Alexander *et al.*, Phys. Lett. B **303**, 377 (1993), confirm the  $1^+$  assignment.
- [16] W. A. Bardeen and C. T. Hill, Report No. Fermilab-Pub-93/59-T (unpublished).
- [17] This damping factor chiefly affects the  $f$ -wave contributions to the  $3D(\frac{5}{2})$  decay rates discussed below.
- [18] We take the  $\eta$  wave function to be  $(u\bar{u} + d\bar{d} - s\bar{s})/\sqrt{3}$ .
- [19] Dynamical models for these decays were explored by S. Godfrey and R. Kokoski, Phys. Rev. D **43**, 1679 (1991). The possibility of a significant  $s$ -wave contribution (at order  $1/m_Q$ ) to the decay  $D_1 \rightarrow D^*\pi$  was raised by Ming-Lu, M. B. Wise, and N. Isgur, *ibid.* **45**, 1553 (1992).
- [20] G. Crawford *et al.* (Ref. [2]).
- [21] LASS Collaboration, D. Aston *et al.*, Report No. SLAC-PUB-6031, 1993 (unpublished).