## Measurement of  $\Lambda_{\text{QCD}}$  from  $v_{\mu}$ -Fe Nonsinglet Structure Functions at the Fermilab Tevatron

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The CCFR Collaboration presents a measurement of scaling violations of the nonsinglet structure function and a comparison to the predictions of perturbative QCD. The value of  $\Lambda_{\text{QCD}}$ , from the nonsinglet evolution with  $Q^2 > 15 \text{ GeV}^2$  and in the modified minimal-subtraction renormalization scheme, is found to be  $210\pm 28(stat) \pm 41(syst)$  MeV.

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Deep inelastic lepton scattering (DIS) experiments have provided some of the most precise tests of perturbative quantum chromodynamics (PQCD). One critical prediction is the  $Q^2$  dependence of the nonsinglet structure function  $xF_3$ ; until now this prediction has not met the test of experimental comparison [1]. PQCD predicts the amount of scaling violation (the  $Q^2$  dependence)

from the measured  $x$  dependence of structure functions at fixed  $Q^2$ , and one additional unknown: the strong coupling parameter  $\alpha_s$  [2]. Since the structure functions are directly measured, the magnitude of the observed scaling violations can be compared to the predictions and simultaneously measured  $\alpha_s$  or  $\Lambda_{\text{QCD}}$ .

Structure functions evolve in PQCD according to the equations [2]

$$
\frac{dF^{NS}(x, Q^2)}{d\ln Q^2} = \frac{a_S(Q^2)}{\pi} \int_x^1 P_{qq}(z, a_s) F^{NS} \left(\frac{x}{z}, Q^2\right) dz \,,\tag{1}
$$

$$
\frac{dF^{S}(x,Q^{2})}{d\ln Q^{2}} = \frac{\alpha_{S}(Q^{2})}{\pi} \int_{x}^{1} [P_{qq}(z,a_{s})F^{S}(x/z,Q^{2}) + P_{qG}(z,a_{s})G(x/z,Q^{2})]dz ,
$$
\n(2)

where  $Q^2$  is the square of the four-momentum transfer to the nucleon,  $x$  is the fractional momentum carried by the struck quark, and the  $P_{IJ}$  are the predicted "splitting functions" [2]. The nonsinglet evolution depends only on the measured structure functions, the known splitting function, and  $\alpha_s$ . The singlet equation is more complicated: Its evolution is coupled with that of the gluons. Only the nonsinglet evolution can be computed independent of assumptions about the dependence of the gluon distribution on x and  $Q^2$ . Because  $P_{qq}(z)$  passes through zero, the left-hand side of Eq. (1) is predicted to pass through zero at about  $x \approx 0.11$ , independent of  $\alpha_s$ . [This statement is valid in leading order; in next-to-leading order, all curves parametrized by differing  $\Lambda_{\text{QCD}}$  (in the modified minimal-subtraction scheme) pass through a com-

mon point near zero at  $x \approx 0.11$  [3].] A comparison of this prediction with experiment is a fundamental test of PQCD which has not yet been demonstrated.

Neutrino experiments on heavy targets can perform this test with the nonsinglet structure function  $xF_3$ . The high statistics CDHSW data [4] do not agree well with the predicted dependence of the scaling violations on  $x$ , although the authors state that the discrepancies are within their systematic errors. Previous CCFR data lacked the statistical power to offer a conclusive test [5].

Currently the most precise deep inelastic tests of PQCD have been obtained from muon scattering data [6] using the singlet structure function  $F_2$ . These experiments have claimed good agreement with the theory.

0031-9007/93/71 (9)/1307 (4)\$06.00 1993 The American Physical Society However, since the evolution of  $F_2$  is coupled to that of the gluon structure function, and since the gluon distributions are not directly measured, corresponding tests of PQCD and determination of  $\Lambda_{\text{OCD}}$  necessarily depend on assumptions regarding the  $x$  dependence of the gluon density.

We report here measurement of scaling violation in structure functions  $F_2$  and  $xF_3$  from new data taken in the high energy, high flux Fermilab Tevatron quadrupole triplet neutrino beam line. The data for the structure function  $xF_3$  contain sufficiently high statistics and control of systematic uncertainties to address the scaling violation predictions of PQCD, and to permit measurement of  $\Lambda_{\text{QCD}}$  with comparable precision to that of recent muon experiments, but without assumptions about gluons.

Measurements of the scaling violations are sensitive to miscalibrations of either the hadron or muon energies  $(E_{\text{had}}$  or  $E_{\mu}$ ). For example, a +1% miscalibration in  $E_{\text{had}}$  ( $E_{\mu}$ ) can cause approximately a -50 (+50) MeV mismeasurement of  $\Lambda_{\text{QCD}}$ . Since these errors enter with opposite signs, if both  $E_{\text{had}}$  and  $E_{\mu}$  were in error by the same amount (e.g.,  $+1\%$  or  $-1\%$ ), the error in  $\Lambda_{\text{QCD}}$ would be small. Therefore, while it is important that the hadron and muon energy calibrations and resolution functions be well known, it is crucial that the calibration of  $E_{\text{had}}$  relative to  $E_{\mu}$  or the energy scales be cross calibrated to minimize energy uncertainty as a source of error.

The detector was absolutely calibrated using charged particle test beams. A hadron beam, at several different energies, was directed into the target carts at different positions. Each beam particle was momentum analyzed to about 1%. These data were used to calibrate the calorimeter to about 1% and to determine the calorimeter resolution function [7]. In two test runs, separated by 3 yr, the energy calibration constant, normalized to muon response, varied by  $\approx 0.3\%$ . Normalization of the calorimetric energy to the muon response removes timedependent calibration changes in the calorimeter. Test beam muons were used to calibrate the toroid spectrometer to  $\approx (0.5\% - 0.6\%)$ , and to determine the resolution function for muons [71.

The relative calibration of  $E_{\text{had}}$  to  $E_{\mu}$  was checked from the v data by plotting  $\langle E_{\text{vis}} \rangle^{\text{DATA}} / \langle E_{\text{vis}} \rangle^{\text{MC}}$  as a function of  $y = E_{\text{had}}/E_{\text{vis}}$ .  $((E_{\text{vis}})^{\text{MC}})$  is the visible energy analog to the data from a Monte Carlo simulation of the experiment.) If the hadron and muon energy scales are correct, the ratio will be unity for all  $y$ . If not, the two energy scales must be adjusted. To satisfy this constraint,<br>calibration adjustments of  $E_{\mu} \rightarrow 0.995E_{\mu}$  and  $E_{\text{had}}$  $\rightarrow 1.016E_{\text{had}}$  were chosen; these adjustments are consistent with the known calibration uncertainty. Figure <sup>1</sup> shows the relative calibration after adjustment of these two parameters. The error on the relative calibration remains  $(20.5\%)$  the dominant systematic error in the determination of  $\Lambda_{\text{OCD}}$ . Finally the angular resolution of



FlG. 1. The relative calibration after the adjustment. We plot  $E_v^{\text{DATA}}/E_v^{\text{MC}}$  as a function of y. Adjustments of  $E_\mu$  $\rightarrow 0.995E_{\mu}$  and  $E_{\text{had}} \rightarrow 1.016E_{\text{had}}$  were made to make the calibration unity for all  $\nu$ .

the muon in charged current events was determined from a sample of straight-through beam muons [3j.

We used a modified version of the Duke and Owens program to do a next-to-leading order (NLO) QCD analysis, in the modified minimal-subtraction  $(\overline{MS})$ scheme ( $\Lambda_{\text{QCD}}$  in this scheme has been denoted as  $\Lambda_{\overline{\text{MS}}}\text{D}$ ) with target mass correction [8]. Applying cuts  $Q^2 > 15$ GeV<sup>2</sup> to eliminate the nonperturbative region and  $x < 0.7$ to remove the highest  $x$  bin (where resolution corrections are sensitive to Fermi motion), best QCD fits to the data were obtained as illustrated in Fig. 2 and discussed below.

A good visual representation of structure function evolution compares the magnitude of the  $Q<sup>2</sup>$  dependence of the data in each  $x$  bin with the dependence predicted by the fit. This is shown by plotting the "slopes"  $(=d \ln x F_3/d \ln Q^2)$  as a function of x. Figure 3 shows our new data along with the curve through the points pre-



FIG. 2. The  $xF_3$  data (statistical errors) and the best QCD fit. Cuts of  $Q^2 > 15$  GeV<sup>2</sup> and  $x < 0.7$  were applied for an NLO-QCD fit including target mass corrections.



FIG. 3. The slopes of  $xF_3(=d \ln xF_3/d \ln Q^2)$  for the CCFR data, with statistical errors only, are shown as circles. The curve is a prediction from perturbative QCD with target mass correction. The slopes for  $F_2$  (squares) in the region  $x > 0.4$ are also shown (with x values shifted by  $+2\%$  for clarity).

dicted by the theory. More specifically the values shown in Fig. 3 result from power law fits to both data and theory over the  $Q^2$  range of the data. The logarithmic slopes of the data agree well with the QCD prediction throughout the entire  $x$  range. This observation is independent of calibration adjustments of about  $\pm 1\%$ . At low-x values the data agree well with predictions independent of the value of  $\Lambda_{\overline{\text{MS}}}$ . This is the first confirmation of the QCD prediction for scaling violations which is independent of assumptions about the gluon distributions and valid over the entire  $x$  range.

The value of  $\Lambda_{\text{QCD}}$  resulting from the fit to  $xF_3$  data was 179  $\pm$  36 MeV, with a  $\chi^2$  of 53.5 for 53 degrees of freedom  $(\chi^2 = 53.5/53)$ . Varying the  $Q^2$  cuts does not significantly change  $\Lambda_{\text{QCD}}$ ; for  $Q^2 > 10 \text{ GeV}^2$ , the best fit gives  $\Lambda_{\text{QCD}} = 171 \pm 32$  MeV ( $\chi^2 = 66.4/63$ ); and for Q  $>$  5 GeV<sup>2</sup>,  $\Lambda_{\text{QCD}}$  = 170 ± 31 MeV ( $\chi^2$  = 83.8/80).

A more precise determination of  $\Lambda_{\text{QCD}}$  from the nonsinglet evolution is obtained by substituting  $F_2$  for  $xF_3$  at large values of x. The evolution of  $F_2$  should conform to that of a nonsinglet structure function in a region  $x$  $> x_{\text{cut}}$ , so long as  $x_{\text{cut}}$  is large enough that the effects of antiquarks, gluons, and the longitudinal structure function are negligible on its  $Q^2$  evolution. A conservative choice for  $x_{\text{cut}}$  is 1 beyond which the antiquarks are consistent with zero. Table I shows the antiquark content  $[\approx 0.5(F_2 - xF_3)]$  of the nucleon in our highest x bins. The table also shows the values of  $\Lambda_{\text{OCD}}$  from fits where  $F_2$  was substituted for  $xF_3$  in those bins. [We normalized  $F_2(x) = xF_3(x)$  for  $x > x_{\text{cut}}$ , an adjustment of < 3%.] For our best value of  $\Lambda_{\text{QCD}}$  from nonsinglet evolution we choose to substitute  $F_2$  for  $xF_3$  for  $x > 0.5$ . (The slopes for  $F_2$  in this region are also shown in Fig. 3.) This nonsinglet fit yields our best value:



FIG. 4. The slopes of  $F_2(=d \ln F_2/d \ln Q^2)$  for the CCFR data are shown (squares). The curve is a prediction from perturbative QCD.

$$
\Lambda_{\text{QCD}} = 210 \pm 28 \text{ MeV for } Q^2 > 15 \text{ GeV}^2.
$$
 (3)

Varying the  $x_{\text{cut}}$  from 0.5 to 0.4 does not significantly change  $\Lambda_{\text{QCD}}$ ; the above substitution yields  $\Lambda_{\text{QCD}}=216$  $\pm$  25 MeV with good fit. Using  $2xF_1$  instead of  $F_2$  in this fit changes  $\Lambda_{\text{QCD}}$  by +1 MeV.

We have also done preliminary QCD fits evolving  $F_2$ , and  $F_2$  and  $xF_3$  simultaneously. The quality of these fits s satisfactory; e.g., for  $\Lambda_{\text{QCD}} = 211$  MeV and  $G(x)$  $= A(1-x)^4$  at  $Q^0 = 5$  GeV<sup>2</sup>, the PQCD predictions fit  $F_2$  data well as illustrated in Fig. 4. Our  $F_2$  data resolve some of the earlier controversies concerning QCD evolution of  $F_2$  in nuclear targets [1]. The values of  $\Lambda_{QCD}$ from  $F_2$  fits are consistent with Eq. (3). It must be pointed out that any value of  $\Lambda_{\text{QCD}}$  from such a fit is correlated with the  $x$  dependences of the gluons and antiquark distributions.

The systematic errors on  $\Lambda_{\text{QCD}}$  are shown in Table II. The energy scale error comes from changing both the hadron and muon energies by 1% in the same direction. As explained above, the errors from a correlated energy

**TABLE I.** Antiquarks and substitution fits. Fraction of  $\bar{q}(x)$ with respect to  $xF_3$ , and the extracted  $\Lambda_{\overline{MS}}$  (in MeV) from nonsinglet fits, with  $Q^2 > 15$  GeV<sup>2</sup>, are shown.

$x$ Bin	$x\bar{q}(x)/xF_3(x)$	$\Lambda_{\overline{\rm MS}}$
No substitution		$179 + 36$
0.65	$-0.3 \pm 0.7\%$	$218 \pm 36$
0.55	$1.2 \pm 1.0\%$	$210 + 28$
0.45	$3.0 \pm 0.7\%$	$216 \pm 25$

TABLE II. Systematic errors in  $\Lambda_{\overline{MS}}$  measurement. The errors on  $\Lambda_{\overline{MS}}$  are in MeV. The last column presents nonsinglet fits with  $xF_3$  in the range  $x \le 0.50$  and  $F_2$  in the range  $0.50 < x \leq 0.70$ .

Error	$xF_3$ alone	$xF_3+F_2$
Energy scale	$+9$	±19
Relative calibration	±48	±36
$\frac{\Delta \sigma^{\nu N}}{\Delta \sigma^{\bar{\nu} N}/\sigma^{\nu N}}$	±11	± 6
	±20	±2
Total systematic	$+54$	±41

change tend to cancel, resulting in an error of  $\approx 10$ MeV. The largest error comes from a possible miscalibration of  $E_{\text{had}}$  with respect to  $E_{\mu}$ . The statistics of the relative calibration data allow a 0.6% variation of the two energy scales from the ideal which results in a 48 MeV systematic error (36 MeV for the fit with  $F_2$ ). The last two errors come from varying the two assumptions of the absolute normalization. The fit with  $xF_3$  alone shows a greater dependence on these assumptions because it is formed from differences of neutrino and antineutrino event sums, while  $F_2$  is derived from the sum of the two. Finally, using radiative correction due to Bardin *et al.* [9] instead of due to De Rujula *et al.* [9] gave a shift in  $\Lambda_{\text{QCD}}$ of about 5 MeV in preliminary studies.

In summary, we have presented new high energy, high statistics precision measurements of the scaling violations in  $xF_3$  and  $F_2$ . The data provide the first observation of the nonsinglet structure function evolution consistent with QCD, and yield  $\Lambda_{\text{QCD}}(MS) = 210 \pm 28 \text{(stat)} \pm 41 \text{(syst)}$ MeV. The measured  $\Lambda_{\text{QCD}}$  corresponds to a strong coupling constant at the Z<sup>0</sup> pole of  $\alpha_S(M_Z) = 0.111$  $\pm 0.002 \pm 0.003$  [10]; the theoretical uncertainty due to scale dependence in this measurement of  $\alpha_S$  is estimated to be about  $\pm 0.004$  [10]. Our measurement of  $\alpha_s$  from the evolution of the nonsinglet structure function agrees well with that obtained from the evolution of the singlet structure function from the charged lepton scattering-a combined NLO-QCD fit to the SLAC and BCDMS data yields  $\alpha_S(M_Z) = 0.113 \pm 0.003$  (expt)  $\pm 0.004$  (theor) [11]. These DIS measurements of  $\alpha_s$  also agree well with those of  $e^+e^-$  experiments [12]: The value of  $\alpha_s(M_Z)$  from the  $Z<sup>0</sup>$  event shape averaged over the LEP and SLC experiments is  $0.120 \pm 0.006$  (expt+theor); the value of  $\alpha_s(M_Z)$  from the  $\Gamma(Z \rightarrow \text{hadrons})$  averaged over LEP

experiments is  $0.130 \pm 0.012$  (expt+theor).

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- [I] S. R. Mishra and F. Sciulli, Annu. Rev. Nucl. Part. Sci. 39, 259 (1989).
- [2] G. Altarelli and G. Parisi, Nucl. Phys. 8126, 298 (1977).
- [3] W. C. Leung, Ph.D. thesis, Columbia University, 1992 (Nevis Report No. 276); P. Z. Quintas, Ph.D. thesis, Columbia University, 1992 (Nevis Report No. 277).
- [4] P. Berge et al., Z. Phys. C 49, 187 (1991).
- [5] E. Oltman et al., Z. Phys. C 53, 51 (1992).
- [6] A. C. Benvenuti et al., Phys. Lett. B 195, 97 (1987): A. C. Benvenuti et al., Phys. Lett. B 223, 490 (1989); A. C. Benvenuti et al., Phys. Lett. B 237, 592 (1990).
- [7] Calorimeter: W. K. Sakumoto et al., Nucl. Instrum. Methods Phys. Res., Sect. A 294, 179 (1990); Spectrometer: B. J. King et al., Nucl. Instrum. Methods Phys. Res., Sect. A 302, 254 (1991).
- [8] A. De Veto et al., Phys. Rev. D 27, 508 (1983).
- [9] D. Yu. Bardin et al., Report No. JINR-E2-86-260, 1986 (unpublished); A. De Rujula et al., Nucl. Phys. B154, 394 (1979).
- [10] The extraction of  $\alpha_s$  at the  $Z^0$  from the reported  $\Lambda_{\text{OCD}}$ , with 4 quark flavors, follows Reviews of Particle Properties, Phys. Rev. D 45, Sl (1992); also see A. D. Martin et al., Phys. Lett. B 266, 173 (1991).
- [11]M. Virchaux and A. Milsztajn, Phys. Lett. B 274, 221 (1992).
- [12] A compilation of  $\alpha_s$  measurements from  $e^+e^-$  experiments, and the averaging of various LEP/SLC experiments to yield the quoted values of  $\alpha_s$  can be found in S. Bethke, in Proceedings of the Dallas HEP Conference, August, 1992, Dallas (to be published).