Limit on the Tau Neutrino Mass

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A limit on the tau neutrino mass $M_{v_{\tau}}$ is obtained from a study of tau decays in the reaction $e^+e^- \rightarrow \tau^+\tau^-$ at center-of-mass energies ~10.6 GeV. The result is based on an end-point analysis of the invariant mass spectrum of the decay products in the decay modes $\tau^- \rightarrow 3h^-2h^+v_{\tau}$ and

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 $\tau \longrightarrow 2h^{-}h^{+}2\pi^{0}v_{\tau}$. The data sample used in this analysis contains 1.77×10^{6} tau pairs, corresponding to an integrated luminosity of 1.92 fb⁻¹, and is substantially larger than previous data samples used to place a limit on $M_{v_{\tau}}$. The limit obtained for both five-hadron modes together is 32.6 MeV at 95% C.L.

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Massive neutrinos have been invoked as a possible explanation for a rich variety of outstanding problems in particle physics and astrophysics, and they are often features of extensions of the standard model [1]. Most studies placing a limit on the tau neutrino mass M_{ν_r} have used the spectrum of the invariant mass of the measured tau decay products M_X . The maximum attainable M_X in a given tau decay mode is a function of M_{ν_r} . This measurement is most sensitive to events with $M_X \sim M_\tau$ since this is where the spectrum varies most dramatically as a function of M_{ν_τ} . The tau decay modes with the least energy available for the tau neutrino are generally more sensitive to M_{ν_τ} and recent studies have concentrated on high-multiplicity tau decays largely for this reason.

The most stringent published result, $M_{v_{\tau}} < 31$ MeV at 95% C.L. from the ARGUS experiment [2], was originally obtained from a sample of twelve (later expanded to twenty) candidate tau-pair events in which one tau decayed via $\tau^- \rightarrow 3h^- 2h^+ v_{\tau}$ [3]. The candidate event with the highest invariant mass was removed to account for possible background contamination.

The analysis presented here uses data obtained with the CLEO-II detector [4] at the Cornell e^+e^- storage ring (CESR) at center-of-mass energies $E_{c.m.} \sim 10.6 \text{ GeV}$ with an integrated luminosity of 1.92 fb⁻¹, corresponding to 1.77×10^6 tau pairs. At these energies, tau leptons are pair-produced chiefly via the process $e^+e^- \rightarrow \gamma^* \rightarrow \tau^+\tau^-$, and the decay products of each tau are typically distinguishable from one another. A novel feature of this analysis, made possible by the excellent electromagnetic calorimetry of the CLEO-II detector, is the inclusion of a recently observed high-multiplicity tau decay mode containing neutral pions, $\tau^- \rightarrow 2h^-h^+2\pi^0v_{\tau}$ [5]. The decay mode $\tau^- \rightarrow 3h^-2h^+v_{\tau}$ is also investigated in this study.

The aim of this analysis is to obtain as clean an event sample as possible since a single background event near the end point can falsely lower the final limit. Potential backgrounds are minimized by selecting the event topology in which one tau decays leptonically $(\tau^+ \rightarrow e^+ v_e \bar{v}_\tau \text{ or} \tau^+ \rightarrow \mu^+ v_\mu \bar{v}_\tau)$ and the lepton is isolated by at least 90° from the hadronic decay products of the other tau, which decays into five hadrons and a low energy neutrino (the X side). The additional selection criteria which further purify the sample are listed below. They utilize all charged particles and any neutral energy deposits in the calorimeter which are isolated by more than 10° from a charged particle and which satisfy $|\cos\theta| < 0.95$, where θ is the angle with respect to the beam axis.

Exactly four or six charged particles (depending on the

decay mode) emanating from the interaction region are required. Events with two charged particles consistent with having come from either a photon conversion, a π^0 Dalitz decay, or a K_S^0 decay are removed. The total energy contained in neutral energy deposits unassociated with either charged particles or neutral pions is required to be less than 600 MeV. In the hemisphere defined by a 90° cone around the lepton, this total energy must be less than 100 MeV in each of the barrel and end-cap regions, defined by $|\cos\theta| < 0.71$ and $0.71 < |\cos\theta| < 0.95$, respectively. In the opposite hemisphere, this total energy must be less than 200 MeV in each region. The total energy of the detected particles on the X side must satisfy $E_X < E_{c.m.}/2$.

There must be zero or two neutral pions (depending on the decay mode), with $2N_{\pi^0}$ photon showers used uniquely in their reconstruction, and each candidate π^0 must satisfy the requirement that $|m_{\pi^0} - m_{\gamma\gamma}| < 20$ MeV (the resolution on m_{π^0} is ~7 MeV). The constituent photon showers of each π^0 must be in the barrel region and have energy $E_{\gamma} > 60$ MeV. In addition, they must be less than 60° apart and have shower shapes consistent with those of photons. Each candidate π^0 is fitted to the nominal π^0 mass and accepted only if the χ^2 probability of the fit is greater than 0.05.

The kinematics dictate that the magnitude of the summed vector momenta of the observed tau decay products in the tau rest frame on the X side, p^* , must be small. This rest frame is approximated using $E_{c.m.}$, M_{τ} , and the direction of the summed momenta of these decay products in the laboratory rest frame. For the decay mode $\tau^- \rightarrow 3h^-2h^+v_{\tau}$, $p^* < 0.4$ GeV is required. For the decay mode $\tau^- \rightarrow 2h^-h^+2\pi^0v_{\tau}$, this requirement is made more restrictive, $p^* < 0.15$ GeV, in order to reduce the background from $\tau^- \rightarrow 2h^-h^+\pi^0v_{\tau}$ events. Finally, since the signal events produce three undetected neutrinos, the total visible energy of charged and isolated neutral particles must satisfy $E_{vis} < 0.85E_{c.m.}$, assuming all charged particles are pions and all neutral particles are photons.

Potential background comes from other processes which imitate the desired final states [primarily twophoton interactions and the hadronic interactions $(e^+e^- \rightarrow q\bar{q})$ and $(e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B})$] the bulk of which do not satisfy the selection criteria listed above. To further reduce the background from two-photon events, the total transverse momentum must satisfy $|\Sigma \mathbf{p}_t| > 200$ MeV. To minimize the background from hadronic interactions in which particles may have escaped detection, the vector of the missing momentum in the event cannot be directed inside a 20° cone around the beam axis.

Hadronic interactions containing D^* and/or D mesons which decay into high-multiplicity final states represent a particularly potential form of background. This is due to the similarity in mass of the tau and the D^* or D meson, which enables such hadronic events to have $M_X < M_\tau$ when a charged kaon is misidentified as a charged pion. Moreover, semileptonic D decays with undetected decay products (e.g., $D^+ \rightarrow K_L^0 l^+ v_l$) can mimic leptonic tau decays. To eliminate this source of background a χ^2 probability with 2 degrees of freedom, P_{y^2} , is formed using the $D^* - D$ mass difference and the \hat{D} mass, where D is either D^0 or D^+ and where the K^- mass is assigned to one of the charged particles on the X side. The resolutions on these quantities are well known from previous studies [6]. Only events with $P_{\chi^2} < 10^{-5}$ are accepted. One event passing all the $\tau \rightarrow 3h^{-2}h^+v_{\tau}$ selection criteria is removed with $P_{\chi^2}=0.99$ and a five-pion invariant mass of 1808 ± 4 MeV. The application of this criterion changes the event selection efficiency by less than 1% of itself and does not distort the M_X spectrum. The final event sample is shown in Fig. 1(a). Note that all of these events satisfy $M_X < M_{\tau}$.

Monte Carlo studies [7] of the acceptance show that it is nearly constant as a function of M_X for the decay mode $\tau \xrightarrow{-} 3h^{-}2h^{+}v_{\tau}$, but increases linearly with increasing



FIG. 1. (a) A histogram of the invariant masses of the measured tau decay products, M_X , for the final data sample of candidate $\tau^- \rightarrow 3h^-2h^+v_\tau$ and $\tau^- \rightarrow 2h^-h^+2\pi^0v_\tau$ events. The superimposed curve is the expected distribution for M_X at $M_{v_\tau}=0$. (b) A plot of those individual events satisfying $M_X > 1.65$ GeV, represented by their M_X values with error bars corresponding to the resolution on M_X . The triangles correspond to candidate $\tau^- \rightarrow 3h^-2h^+v_\tau$ events and the squares to $\tau^- \rightarrow 2h^-h^+2\pi^0v_\tau$ events. The vertical dashed line corresponds to $M_X=M_\tau$ and the vertical dotted line to M_X $=M_\tau - M_{v_\tau}^{95}$, where $M_{v_\tau}^{95}$ is the final limit of 32.6 MeV. (c) A plot of the likelihood function obtained from the final data sample. The most likely value for M_{v_τ} is compatible with zero within less than one sigma.

 M_{χ} for the decay mode $\tau^- \rightarrow 2h^-h^+ 2\pi^0 v_{\tau}$ due primarily to the $p^* < 0.15$ GeV requirement. The combined acceptance and reconstruction efficiencies are found to be $(7.2 \pm 0.2)\%$ and $(0.79 \pm 0.03)\%$ for the decay modes $\tau^- \rightarrow 3h^-2h^+v_{\tau}$ and $\tau^- \rightarrow 2h^-h^+2\pi^0v_{\tau}$, respectively (statistical errors only).

Estimation of the non-tau background in the data sample uses simulated event samples consisting of events from hadronic and two-photon interactions. No events remain after applying all the selection criteria to each of these samples. More stringent limits on the background from hadronic interactions have been estimated using portions of the data which are predominantly comprised of such events. Events which have seven or more charged particles constitute such an event sample and are used to estimate the background from hadronic interactions as (0.16 ± 0.03) events and (0.01 ± 0.01) events for the modes $\tau \longrightarrow 3h^-2h^+v_\tau$ and $\tau \longrightarrow 2h^-h^+2\pi^0v_\tau$, respectively (statistical errors only). This estimate is verified by studying the effect of removing or greatly loosening certain signal selection criteria. In both modes, this alteration results in a small number of events classified as background (defined as $M_X > 2$ GeV) entering the final sample, consistent with the number predicted from events with seven or more charged particles.

When the selection criteria are applied to a sample of simulated $e^+e^- \rightarrow \tau^+\tau^-$ events (excluding the decay modes $\tau^- \rightarrow 3h^-2h^+v_\tau$ and $\tau^- \rightarrow 2h^-h^+2\pi^0v_\tau$), the resulting event samples have some contamination due to the decay modes $\tau^- \rightarrow 3h^- 2h^+ \pi^0 v_{\tau}$ and $\tau^ \rightarrow 2h^{-}h^{+}\pi^{0}v_{\tau}$. The background coming from τ^{-} $\rightarrow 3h^{-}2h^{+}\pi^{0}v_{\tau}$, where the π^{0} is not detected, can only increase the final limit, since the omission of the π^0 decreases M_X further below M_{τ} . On the other hand, background from $\tau^- \rightarrow 2h^-h^+\pi^0 v_{\tau}$, with spurious neutral energy deposits forming a fake π^0 , could artificially increase M_X and falsely lower the final limit [8]. However, although studies of simulated $\tau \rightarrow 2h^{-}h^{+}\pi^{0}v_{\tau}$ events show that an estimated 0.6 ± 0.3 events (statistical error only) will enter the final $\tau \rightarrow 2h^{-}h^{+}2\pi^{0}v_{\tau}$ data sample in this fashion, each of the simulated events upon which this estimation is based had $M_X < 1550$ MeV. Hence this channel is only capable of producing < 0.35events at 90% C.L. in the region $M_X > 1550$ MeV and is not likely to falsely lower the final limit.

The tau neutrino mass limit is determined from a likelihood function which consists of a theoretical estimate of the five-pion invariant mass spectrum convoluted with detector resolution and acceptance functions, where the latter is incorporated as a function of M_X and is determined from studies of simulated event samples. The likelihood is calculated event by event as a function of M_{v_r} . The final likelihood curve is a product of the individual event likelihoods and is shown in Fig. 1 (c). The default KORALB [9] spectral function and the most recent value of the tau mass [10] are used in its calculation. The 95%

TABLE I. The size of the final event samples, the 95% C.L. limit on $M_{\nu_{\tau}}$ after correction for systematic efforts, $M_{\nu_{\tau}}^{95}$, and the estimated Monte Carlo probability of having obtained this limit, $P_{\rm MC}$, for each of the studied decay modes and for the published ARGUS result. The errors on $P_{\rm MC}$ are statistical only.

Decay mode	Sample size	$M_{v_{\tau}}^{95}$ (MeV)	Р _{МС} (%)
$\tau^- \rightarrow 3h^- 2h^+ v_{\tau}$	60	47.5	34.9 ± 0.8
$\tau \longrightarrow 2h^{-}h^{+}2\pi^{0}v_{\tau}$	53	33.7	4.3 ± 0.3
Combined	113	32.6	13.9 ± 0.6
ARGUS	20	31	0.041 ± 0.012

C.L. limit, $M_{v_{\tau}}^{95}$, is defined as the value of $M_{v_{\tau}}$ at which the integral of the likelihood curve reaches 95% of its total. This integral only covers positive neutrino masses in order to derive a conservative limit [11]. Table I provides a summary of the results obtained from the final data samples in the decay modes studied.

To compare these results to the ARGUS result it is informative to calculate the quantity P_{MC} , defined as the percentage of signal Monte Carlo experiments in which a 95% C.L. limit less than or equal to that of the data is obtained. Since each of these experiments is generated at zero neutrino mass with the same number of events as in the given data sample [12], P_{MC} may be interpreted as an estimate of the probability of obtaining a given $M_{v_{\tau}}^{95}$ for a given sample size. For simplicity, no detector simulation is used. The last column of Table I shows P_{MC} for the final event samples and for the most recent ARGUS result [13]. It is important to note that since this limit depends on a few events near the end point, and the yield of such events decreases rapidly as M_X approaches M_τ , one should not expect this limit to improve linearly with increasing sample size.

Systematic errors are estimated by varying the relevant quantity and observing its effect on the final limit. These estimated errors are then incorporated into the final limit using a Gaussian approximation [14]. The largest source of systematic error arises from the uncertainty in the dependence of the acceptance on M_X . This is estimated to contribute 5 MeV by varying the dependence within reasonable bounds. The uncertainty in the mass scale, known from D^0 decays [6], is estimated to contribute 1 MeV. The uncertainty in the mass resolution is estimated to contribute 1 MeV by varying the resolution within reasonable bounds. The slight distortion of the M_X spectra due to backgrounds from other tau decays is estimated to contribute 1 MeV from Monte Carlo studies. The uncertainty in the theoretical model of the decay is estimated to contribute 1 MeV by varying the default spectra function within reasonable bounds. Finally, the uncertainty on M_{τ} contributes 0.5 MeV [10].

In summary, using a substantially larger data sample than that used in previous studies, 95% C.L. limits on $M_{\nu_{\tau}}$ from the decay modes $\tau \longrightarrow 3h^{-}2h^{+}\nu_{\tau}$, τ^{-} $\rightarrow 2h^{-}h^{+}2\pi^{0}v_{\tau}$, and both five-hadron decay modes of 47.5, 33.7, and 32.6 MeV, respectively, have been obtained. These limits include the effects of systematic errors. Background has been estimated from both Monte Carlo studies and data, and was found to be substantially less than one event in the sensitive region of the final sample. This is the first time the decay mode τ^{-} $\rightarrow 2h^{-}h^{+}2\pi^{0}v_{\tau}$ has been used to set a limit on $M_{v_{\tau}}$.

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generated following a Gaussian distribution with mean and width given by the data. For the decay mode $\tau^- \rightarrow 3h^-2h^+v_{\tau}$, the average resolution on M_X is 9 MeV; for $\tau^- \rightarrow 2h^-h^+2\pi^0v_{\tau}$, 14 MeV.

[13] In order to mimic as closely as possible the ARGUS procedure, the value of P_{MC} for the ARGUS 20-event sam-

ple is calculated using 20-event Monte Carlo experiments from which the event with the largest M_X is removed.

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