Energetics of ³He States in ⁴He Films

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We report measurements of the NMR spin-lattice relaxation time, T_1 , of ³He in ⁴He films for 0.03 < T < 0.60 K as a function of ⁴He coverage of 0.1 layer of adsorbed ³He. The results show thermally activated behavior for T > 0.25 K and yield the energy difference, $\delta\epsilon$, between the ³He ground state and the first excited state; $\delta\epsilon$ shows substantial structure as a function of ⁴He coverage.

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³He atoms bound to a thin ⁴He film constitute a system of remarkable richness. As in the case for bulk ⁴He [1], the lowest state available to a single 3 He atom in a ⁴He film is one in which the ³He resides at the surface of the ⁴He film [2,3]. This is due to the combined effect of the substrate potential and ³He-⁴He interactions. In the dilute limit the ³He atoms in the surface state form a quasi-two-dimensional gas [4-7] which is degenerate for temperatures below the Fermi temperature. The effective potential defined by the substrate and the ⁴He also produce bound states of higher energy for the ³He in the film [4-7]. This spectrum of states is expected to be sensitive to the ⁴He coverage, n_4 [3]. For the present work, we have used NMR to study the dynamics of the ³He in mixture films and by this means have measured the energy separation, $\delta\epsilon$, between the ground and first excited state of the ³He as a function of n_4 . We find that $\delta\epsilon$ shows substantial structure.

In these experiments, we have carried out measurements of the spin-lattice relaxation time T_1 of ³He on a superfluid ⁴He film as a function of ⁴He coverage n_4 for $0.27 < n_4 < 0.53$ atom/Å² [8], and temperature T for 0.03 < T < 0.60 K. The ³He coverage is fixed at n_3 =0.0066 atom/Å² (~0.1 layer). Such a ³He system is well described as a 2D weakly interacting Fermi liquid [4-7] with Fermi temperature $T_F \sim 0.24$ K. In earlier work for T < 0.25 K, the measured relaxation rate $T_1^{-1}(T)$ was observed [8] to behave as $T_1^{-1}(T) \sim A$ $+B/\sqrt{T}$. Here, for T > 0.25 K, we find T_1^{-1} $\sim \exp(-\Delta/T)$ with characteristic energy Δ . We interpret Δ to be the energy gap between the Fermi level of the ³He in the ground state and an excited state of the ³He in the film [4].

The substrate used for this experiment is Nuclepore [9], polycarbonate filter material, which provides most of the 1.77 m² (\pm 10%) sample cell surface area. The measurements we report here are made by use of pulsed NMR [6] in a 2-T external field ($\omega/2\pi \sim 62.9$ MHz). The temperatures are achieved by use of a dilution refrigerator and measured with a Speer 100- Ω carbon resistor previously calibrated against a ³He melting curve thermometer [10]. The spin-lattice relaxation time T_1 is measured by spin-echo techniques using a series of $\frac{1}{2}\pi$ -

 $\tau - \frac{1}{2} \pi - \tau_0 - \pi$ rf-pulse sequences as a function of τ for $\tau_0 = 0.3$ msec. The amplitude of the spin echo from the ³He system is directly proportional to the magnetization which has recovered after a time τ following the first $\frac{1}{2} \pi$ rf pulse. For the range of ⁴He coverages and temperatures discussed here, the decay of the spin-echo height with τ is well described by a single exponential over one to two decades in echo height with a characteristic time T_1 . The magnetization and the spin-spin relaxation time T_2 are measured by use of $\frac{1}{2} \pi - \tau - \pi$ spin-echo pulse sequences.

Figure 1 shows measurements of the spin-lattice relaxation rate T_1^{-1} as a function of $1/\sqrt{T}$ (0.03 < T < 0.60 K) for several ⁴He coverages. Two temperature regions can be identified. For T < 0.25 K, $T_1^{-1}(T)$ is a linear function [8] of $1/\sqrt{T}$; $T_1^{-1} = A + B/\sqrt{T} \equiv W_{LT}$. The coefficient *B* has been shown to have intriguing n_4 dependence which apparently is correlated with the amount of



FIG. 1. T_1^{-1} vs $T^{-1/2}$ for various n_4 . For T < 0.25 K, $T_1^{-1}(T) \sim A + B/\sqrt{T}$. The dot-dashed lines are straight-line fits for $T_1^{-1} \sim T^{-1/2}$. For T > 0.25 K, $T_1^{-1}(T)$ increases exponentially with temperature. Coverages: 0.217 Å⁻² (solid triangles), 0.290 Å⁻² (circles), 0.339 Å⁻² (diamonds), 0.362 Å⁻² (squares), and 0.400 Å⁻² (open triangles).

superfluid in the ⁴He film [8]. For T > 0.25 K, $T_1^{-1}(T)$ increases dramatically with temperature. For simplicity, we assume that the observed deviation of the relaxation rate from $W_{\rm LT}$ is due to the addition of another relaxation rate, $W_{\rm HT}$, which is associated with the mechanisms of relaxation for T > 0.25 K. Thus $T_1^{-1} \sim W_{\rm LT} + W_{\rm HT}$.

We find that the rate $W_{\rm HT}$ is well described by an exponential, $W_{\rm HT} \sim \exp(-\Delta/T)$, as shown in Fig. 2, with Δ dependent on n_4 . The values of $W_{\rm HT}$ shown in Fig. 2 are obtained from data like that shown in Fig. 1 by subtraction: $W_{\rm HT} = T_1^{-1}(T) - W_{\rm LT}$, where we assume $W_{\rm LT}$ retains its \sqrt{T} character even for $T > T_F$ [11]. This exponential behavior of $W_{\rm HT}$ should not be confused with the exponential behavior seen by others [12,13] in $T_1(T)$ in the gas phase, which is dominated by wall relaxation. Here, $W_{\rm HT}$ is not due to the evaporation of ³He from the mixture film. Measurements of the magnetization M(T)as a function of temperature show that the evaporation process is observable for $T \ge 0.60$ K with a measured [14] binding energy $\sim 6 \pm 1$ K, which is substantially larger than the average value of $\Delta \sim 1.8$ K (our result for the binding energy is consistent with the known value ~ 5 K [13,14]). Furthermore, since T_1 of the vapor phase of ³He is longer than that of the film, the evaporation process is expected to cause the relaxation rate of the film to decrease exponentially [13,14] with increasing temperature; this is contrary to the behavior observed in Fig. 2.

To enhance our understanding of this relaxation rate $T_1^{-1}(T)$, we assume that $W_{LT} \sim n_0 W_0$, where n_0 and W_0 are respectively the temperature-dependent density and relaxation rate of the ³He spins in the ground state; $W_0(T)$ retains the form [8] $a+b/\sqrt{T}$. This is a reason-



FIG. 2. $\log_{10}(W_{\rm HT})$ vs 1/T for several ⁴He coverages. $W_{\rm HT} \sim \exp(-\Delta/T)$. Δ is given by the slopes of the straight-line fits (dot-dashed lines) for $\log_{10}(W_{\rm HT}) \sim 1/T$. Coverages: 0.217 Å⁻² (solid triangles), 0.290 Å⁻² (circles), 0.339 Å⁻² (diamonds), 0.362 Å⁻² (squares), and 0.400 Å⁻² (open triangles).

able assumption since, generally, the bulk relaxation rate T_1^{-1} is proportional to the density of ³He for classical or degenerate ³He liquid [15]; this proportionality is consistent with earlier measurements of T_1 done in mixture films for ³He coverages $0.1 < d_3 < 0.5$ layer [7]. Similarly, we take $W_{\rm HT} \sim n_1 W_1$, where n_1 and W_1 are respectively the density and the relaxation rate of ³He spins in the excited state. As the temperature is increased, a fraction of the ³He spins are thermally promoted into an excited state in the film, providing an additional channel for relaxation (Fig. 3). Assuming that the exchange rate W_E between the two states is faster than W_0 and W_1 [16], $T_1^{-1}(T) \sim n_0 W_0 + n_1 W_1$.

Next, we investigate the temperature dependence of n_0 and n_1 . By modeling the film to have discrete energy levels ϵ_0 and ϵ_1 , we can solve [17] for the chemical potential of the ³He, using a Fermi distribution, at fixed number N, and energy separation $\delta \epsilon = \epsilon_1 - \epsilon_0$. This yields n_0 and n_1 as a function of temperature. N is the total number of ³He atoms, $N/A = n_0 + n_1$; A is the surface area. In the temperature range of the measurements done here, $n_0(T) \sim 1 - \exp(-\Delta/T)$ whereas $n_1(T) \sim \exp(-\Delta/T)$; Δ is approximately the energy separation between the Fermi level and the excited state. Consequently, the observed relaxation rate can be written as $T_1^{-1}(T)$ $\simeq W_0(T) + W_1(T) \exp(-\Delta/T)$ [18]. The rate W_1 , which characterizes the mechanisms of relaxation from the excited state, may be a function of temperature. However, any anticipated temperature dependence in W_1 is weak compared with the exponential behavior of $n_1(T)$. Thus, for the purpose of extracting the energies Δ , we assumed that $W_1(T)$ is independent of temperature [19]. We find that the relaxation rate in the excited state is typically 50 times larger than that of the ground state, $W_1 \sim 50 W_0$ [20].

Within the context of this model, the slopes of Fig. 2 provide a direct measure [21] of the energy separation Δ



FIG. 3. Schematic illustration of the two states available to the ³He. n_0 and W_0 are respectively the density and the relaxation rate of the ³He spins in the ground state. n_1 and W_1 are respectively the density and the relaxation rate of the ³He spins in the first excited state. The exchange rate between the two states, W_E , is assumed to be much greater than either W_0 or W_1 .



FIG. 4. (a) $\Delta \text{ vs } n_{4}$. Δ is the energy separation between the Fermi level of the ³He in the ground state and the first excited state. The evolution of $\Delta(n_4)$ shows a minimum of 1.22 K at $n_4 \approx 0.34$ Å⁻². (b) $\delta\epsilon$ vs n_4 . $\delta\epsilon$ is the energy separation between the ground and the first excited state of the ³He in the film. The solid circles are the energies obtained using NMR techniques. $\delta\epsilon(n_4)$ shows a minimum of ~ 1.5 K; at our highest ⁴He coverage $\delta\epsilon \sim 1.7$ K. The ³He coverage ~ 0.1 layer. Also shown here are energies as given from heat-capacity measurements (triangles) for $d_3 \approx 0.3$ layer from Ref. [4].

between the Fermi level and the excited state in the film. In Fig. 4(a), we present the energies Δ as a function of ⁴He coverage n_4 . Δ has considerable structure as a function of n_4 ; Δ has a minimum for $n_4 \approx 0.34$ atom/Å² and a local maximum for $n_4 \approx 0.41$ atom/Å². By adding the Fermi energy to Δ , we obtain the energy separation between the ground and the excited state $\delta \epsilon \equiv \epsilon_1 - \epsilon_0$. To accomplish this, we note that the magnetization is found to be well described by a 2D ideal Fermi gas, with a degeneracy temperature which shows a weak ⁴He-coverage dependence. This degeneracy temperature is within 10% of the Fermi temperature T_F [4]. Consequently, we approximate the Fermi temperature at each ⁴He coverage by the degeneracy temperature. Figure 4(b) shows the variation of this energy separation, $\delta\epsilon$, as a function of ⁴He coverage.

The values for the excitation energy $\delta\epsilon(n_4)$ have been obtained on a much finer n_4 grid than the earlier heatcapacity results of Bhattacharyya, DiPirro, and Gasparini [4] [Fig. 4(b)] which were at a somewhat higher ³He coverage, $d_3 \approx 0.3$ layer. When one accounts for the difference in ³He coverage, the absolute values of the energies are quite consistent for the two different techniques.

These data should be useful in testing emerging theories for ³He in mixture films. Recent theoretical work by Pavloff and Treiner [3] and by Epstein and Krotscheck [22] has explored the properties of ³He in ⁴He films. In the case of thin ⁴He films, these workers predict structure in the evolution of the energy levels ϵ_i with n_4 ; this is generally consistent with the energetics we report here. Each calculation yields a local minimum in $\delta \epsilon$ qualitatively similar to our observations. In the limit of large n_4 , Pavloff and Treiner predict two bound states at the ⁴He surface with $\delta \epsilon \simeq 1.8$ K; the first excited state is expected to remain at the film surface for modest ³He coverage. In the same limit Epstein and Krotscheck predict a single surface state for which the energy difference between this surface state and the lowest state in the ⁴He film is ≈ 1.4 K. The agreement between the theory and our measurements is encouraging. Finite ³He coverage calculations are needed.

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peratures, the chemical potential of both phases was assumed to be that of an ideal gas.

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