## Energetics of  $3$ He States in  $4$ He Films

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We report measurements of the NMR spin-lattice relaxation time,  $T_1$ , of <sup>3</sup>He in <sup>4</sup>He films for  $0.03 < T < 0.60$  K as a function of <sup>4</sup>He coverage of 0.1 layer of adsorbed <sup>3</sup>He. The results show thermally activated behavior for  $T > 0.25$  K and yield the energy difference,  $\delta \epsilon$ , between the <sup>3</sup>He ground state and the first excited state;  $\delta \epsilon$  shows substantial structure as a function of <sup>4</sup>He coverage.

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 $3$ He atoms bound to a thin  $4$ He film constitute a system of remarkable richness. As in the case for bulk  ${}^{4}$ He [1], the lowest state available to a single  ${}^{3}$ He atom in a  $4$ He film is one in which the  $3$ He resides at the surface of the  ${}^{4}$ He film [2,3]. This is due to the combined effect of the substrate potential and  ${}^{3}$ He- ${}^{4}$ He interactions. In the dilute limit the  ${}^{3}$ He atoms in the surface state form a quasi-two-dimensional gas [4-7] which is degenerate for temperatures below the Fermi temperature. The effective potential defined by the substrate and the <sup>4</sup>He also produce bound states of higher energy for the  $3$ He in the film [4-7]. This spectrum of states is expected to be sensitive to the <sup>4</sup>He coverage,  $n_4$  [3]. For the present work, we have used NMR to study the dynamics of the  ${}^{3}$ He in mixture films and by this means have measured the energy separation,  $\delta \epsilon$ , between the ground and first excited state of the <sup>3</sup>He as a function of  $n_4$ . We find that  $\delta \epsilon$ shows substantial structure.

In these experiments, we have carried out measurements of the spin-lattice relaxation time  $T_1$  of <sup>3</sup>He on a superfluid <sup>4</sup>He film as a function of <sup>4</sup>He coverage  $n_4$  for  $0.27 < n_4 < 0.53$  atom/ $\AA^2$  [8], and temperature T for  $0.03 < T < 0.60$  K. The <sup>3</sup>He coverage is fixed at  $n_3$ =0.0066 atom/ $A^2$  ( $\sim$ 0.1 layer). Such a <sup>3</sup>He system is well described as a 2D weakly interacting Fermi liquid [4-7] with Fermi temperature  $T_F \sim 0.24$  K. In earlier work for  $T < 0.25$  K, the measured relaxation rate  $T_1^{-1}(T)$  was observed [8] to behave as  $T_1^{-1}(T) \sim A$  $+B/\sqrt{T}$ . Here, for  $T > 0.25$  K, we find  $T_1^{-1}$  $-\exp(-\Delta/T)$  with characteristic energy  $\Delta$ . We interpret  $\Delta$  to be the energy gap between the Fermi level of the  ${}^{3}$ He in the ground state and an excited state of the  $3$ He in the film  $[4]$ .

The substrate used for this experiment is Nuclepore [9], polycarbonate filter material, which provides most of the 1.77 m<sup>2</sup> ( $\pm$ 10%) sample cell surface area. The measurements we report here are made by use of pulsed NMR [6] in a 2-T external field  $(\omega/2\pi \sim 62.9 \text{ MHz})$ . The temperatures are achieved by use of a dilution refrigerator and measured with a Speer 100- $\Omega$  carbon resistor previously calibrated against  $a<sup>3</sup>$ He melting curve thermometer [10]. The spin-lattice relaxation time  $T_1$  is measured by spin-echo techniques using a series of  $\frac{1}{2} \pi$ -  $\tau$ - $\frac{1}{2}$   $\pi$ - $\tau$ <sub>0</sub>- $\pi$  rf-pulse sequences as a function of  $\tau$  for  $\tau_0$ =0.3 msec. The amplitude of the spin echo from the <sup>3</sup>He system is directly proportional to the magnetization which has recovered after a time  $\tau$  following the first  $\frac{1}{2} \pi$ rf pulse. For the range of  $4$ He coverages and temperatures discussed here, the decay of the spin-echo height with  $\tau$  is well described by a single exponential over one to two decades in echo height with a characteristic time  $T<sub>1</sub>$ . The magnetization and the spin-spin relaxation time  $T_2$  are measured by use of  $\frac{1}{2} \pi$ - $\tau$ - $\pi$  spin-echo pulse sequences.

Figure <sup>1</sup> shows measurements of the spin-lattice relaxation rate  $T_1^{-1}$  as a function of  $1/\sqrt{T}$  (0.03 <  $T$  < 0.60 K) for several <sup>4</sup>He coverages. Two temperature regions can be identified. For  $T < 0.25$  K,  $T_1^{-1}(T)$  is a linear function [8] of  $1/\sqrt{T}$ ;  $T_1^{-1} = A + B/\sqrt{T} = W_{LT}$ . The coefficient B has been shown to have intriguing  $n_4$  dependence which apparently is correlated with the amount of



FIG. 1.  $T_1^{-1}$  vs  $T^{-1/2}$  for various  $n_4$ . For  $T < 0.25$  K, Tion 1.  $T_1 = \frac{87}{100}$  various  $n_4$ . For  $T \le 0.25$  K<br> $T_1^{-1}(T) \sim A + B/\sqrt{T}$ . The dot-dashed lines are straight-line its for  $T_1^{-1} \sim T^{-1/2}$ . For  $T > 0.25$  K,  $T_1^{-1}(T)$  increases exbonentially with temperature. Coverages:  $0.217 \text{ Å}^{-2}$  (solid triangles), 0.290 Å<sup>-2</sup> (circles), 0.339 Å<sup>-2</sup> (diamonds), 0.362  $\AA$ <sup>-2</sup> (squares), and 0.400  $\AA$ <sup>-2</sup> (open triangles).

superfluid in the <sup>4</sup>He film [8]. For  $T > 0.25$  K,  $T_1^{-1}(T)$ increases dramatically with temperature. For simplicity, we assume that the observed deviation of the relaxation rate from  $W_{LT}$  is due to the addition of another relaxation rate,  $W_{HT}$ , which is associated with the mechanism<br>of relaxation for  $T > 0.25$  K. Thus  $T_1^{-1} \sim W_{LT} + W_{HT}$ .

We find that the rate  $W_{HT}$  is well described by an exponential,  $W_{HT}$  –  $\exp(-\Delta/T)$ , as shown in Fig. 2, with  $\Delta$ dependent on  $n_4$ . The values of  $W_{HT}$  shown in Fig. 2 are obtained from data like that shown in Fig. <sup>1</sup> by subtraction:  $W_{HT} = T_1^{-1}(T) - W_{LT}$ , where we assume  $W_{LT}$  retains its  $\sqrt{T}$  character even for  $T > T_F$  [11]. This exponential behavior of  $W_{HT}$  should not be confused with the exponential behavior seen by others [12,13] in  $T_1(T)$ in the gas phase, which is dominated by wall relaxation. Here,  $W_{HT}$  is not due to the evaporation of <sup>3</sup>He from the mixture film. Measurements of the magnetization  $M(T)$ as a function of temperature show that the evaporation process is observable for  $T \geq 0.60$  K with a measured [14] binding energy  $-6\pm 1$  K, which is substantially larger than the average value of  $\Delta$   $\sim$  1.8 K (our result for the binding energy is consistent with the known value  $\sim$  5 K [13,14]). Furthermore, since  $T_1$  of the vapor phase of  ${}^{3}$ He is longer than that of the film, the evaporation process is expected to cause the relaxation rate of the film to decrease exponentially [13,14] with increasing temperature; this is contrary to the behavior observed in Fig. 2.

To enhance our understanding of this relaxation rate  $T_1^{-1}(T)$ , we assume that  $W_{LT} \sim n_0W_0$ , where  $n_0$  and  $W_0$ are respectively the temperature-dependent density and relaxation rate of the  ${}^{3}$ He spins in the ground state;  $W_0(T)$  retains the form [8]  $a+b/\sqrt{T}$ . This is a reason-



FIG. 2.  $log_{10}(W_{\text{HT}})$  vs  $1/T$  for several <sup>4</sup>He coverages.  $W_{\text{HT}} \sim \exp(-\Delta/T)$ .  $\Delta$  is given by the slopes of the straight-line  $\lambda$  H<sub>T</sub>  $\sim$  exp(b) 2/1). As given by the slopes of the straight-line<br>fits (dot-dashed lines) for log<sub>10</sub>( $W_{\text{HT}}$ )  $\sim$  1/T. Coverages: 0.217<br> $\lambda$ <sup>-2</sup> (solid triangles), 0.290  $\lambda$ <sup>-2</sup> (circles), 0.339  $\lambda$ <sup>-2</sup> (diamonds), 0.362 Å  $^{-2}$  (squares), and 0.400 Å  $^{-2}$  (open triangles).

able assumption since, generally, the bulk relaxation rate  $T_1^{-1}$  is proportional to the density of <sup>3</sup>He for classical or degenerate  $3$ He liquid [15]; this proportionality is consistent with earlier measurements of  $T_1$  done in mixture films for <sup>3</sup>He coverages  $0.1 < d_3 < 0.5$  layer [7]. Similarly, we take  $W_{HT} \sim n_1 W_1$ , where  $n_1$  and  $W_1$  are respectively the density and the relaxation rate of  $3$ He spins in the excited state. As the temperature is increased, a fraction of the  ${}^{3}$ He spins are thermally promoted into an excited state in the film, providing an additional channel for relaxation (Fig. 3). Assuming that the exchange rate  $W_E$ between the two states is faster than  $W_0$  and  $W_1$  [16],  $T_1^{-1}(T) \sim n_0W_0+n_1W_1$ .

Next, we investigate the temperature dependence of  $n_0$ and  $n_1$ . By modeling the film to have discrete energy levels  $\epsilon_0$  and  $\epsilon_1$ , we can solve [17] for the chemical potential of the  ${}^{3}$ He, using a Fermi distribution, at fixed number N, and energy separation  $\delta \epsilon = \epsilon_1 - \epsilon_0$ . This yields  $n_0$  and  $n_1$  as a function of temperature. N is the total number of <sup>3</sup>He atoms,  $N/A = n_0 + n_1$ ; A is the surface area. In the temperature range of the measurements done here,  $n_0(T) \sim 1 - \exp(-\Delta/T)$  whereas  $n_1(T) \sim \exp(-\Delta/T)$ ;  $\Delta$ is approximately the energy separation between the Fermi level and the excited state. Consequently, the observed relaxation rate can be written as  $T_1^{-1}(T)$  $\approx W_0(T) + W_1(T) \exp(-\Delta/T)$  [18]. The rate  $W_1$ , which characterizes the mechanisms of relaxation from the excited state, may be a function of temperature. However, any anticipated temperature dependence in  $W_1$  is weak compared with the exponential behavior of  $n_1(T)$ . Thus, for the purpose of extracting the energies  $\Delta$ , we assumed that  $W_1(T)$  is independent of temperature [19]. We find that the relaxation rate in the excited state is typically 50 times larger than that of the ground state,  $W_1 \sim 50 W_0$  $[20]$ .

Within the context of this model, the slopes of Fig. 2 provide a direct measure [21] of the energy separation  $\Delta$ 



FIG. 3. Schematic illustration of the two states available to the  ${}^{3}$ He. n<sub>0</sub> and  $W_0$  are respectively the density and the relaxation rate of the <sup>3</sup>He spins in the ground state.  $n_1$  and  $W_1$  are respectively the density and the relaxation rate of the  ${}^{3}$ He spins in the first excited state. The exchange rate between the two states,  $W_E$ , is assumed to be much greater than either  $W_0$  or  $W_{\perp}$ .



FIG. 4. (a)  $\Delta$  vs  $n'$ <sub>4</sub>.  $\Delta$  is the energy separation between the Fermi level of the  ${}^{3}$ He in the ground state and the first excited state. The evolution of  $\Delta(n_4)$  shows a minimum of 1.22 K at  $n_4 \approx 0.34 \text{ Å}^{-2}$ . (b)  $\delta \epsilon$  vs  $n_4$ .  $\delta \epsilon$  is the energy separation between the ground and the first excited state of the 'He in the film. The solid circles are the energies obtained using NMR techniques.  $\delta \epsilon(n_4)$  shows a minimum of  $\sim$  1.5 K; at our highest <sup>4</sup>He coverage  $\delta \epsilon$  – 1.7 K. The <sup>3</sup>He coverage  $\sim$  0.1 layer. Also shown here are energies as given from heat-capacity measurements (triangles) for  $d_3 \approx 0.3$  layer from Ref. [4].

between the Fermi level and the excited state in the film. In Fig. 4(a), we present the energies  $\Delta$  as a function of <sup>4</sup>He coverage  $n_4$ .  $\Delta$  has considerable structure as a function of  $n_4$ ;  $\Delta$  has a minimum for  $n_4 \approx 0.34$  atom/ $\text{\AA}^2$  and a local maximum for  $n_4 \approx 0.41$  atom/ $\AA$ <sup>2</sup>. By adding the Fermi energy to  $\Delta$ , we obtain the energy separation between the ground and the excited state  $\delta \epsilon = \epsilon_1 - \epsilon_0$ . To accomplish this, we note that the magnetization is found to be well described by a 2D ideal Fermi gas, with a degeneracy temperature which shows a weak <sup>4</sup>He-coverage dependence. This degeneracy temperature is within 10% of the Fermi temperature  $T_F$  [4]. Consequently, we approximate the Fermi temperature at each  $4$ He coverage by the degeneracy temperature. Figure 4(b) shows the variation of this energy separation,  $\delta \epsilon$ , as a function of <sup>4</sup>He coverage.

The values for the excitation energy  $\delta \epsilon(n_4)$  have been obtained on a much finer  $n_4$  grid than the earlier heatcapacity results of Bhattacharyya, Dipirro, and Gasparini [4] [Fig. 4(b)] which were at a somewhat higher  ${}^{3}$ He coverage,  $d_3 \approx 0.3$  layer. When one accounts for the difference in  ${}^{3}$ He coverage, the absolute values of the energies are quite consistent for the two different techniques.

These data should be useful in testing emerging theories for  $3$ He in mixture films. Recent theoretical work by Pavloff and Treiner [3] and by Epstein and Krotscheck [22] has explored the properties of  $3$ He in  $4$ He films. In the case of thin  ${}^{4}$ He films, these workers predict structure in the evolution of the energy levels  $\epsilon_i$  with  $n_4$ ; this is generally consistent with the energetics we report here. Each calculation yields a local minimum in  $\delta \epsilon$  qualitatively similar to our observations. In the limit of large  $n_4$ , Pavloff and Treiner predict two bound states at the <sup>4</sup>He surface with  $\delta \epsilon \approx 1.8$  K; the first excited state is expected to remain at the film surface for modest  ${}^{3}$ He coverage. In the same limit Epstein and Krotscheck predict a single surface state for which the energy difference between this surface state and the lowest state in the <sup>4</sup>He film is  $\approx$ 1.4 K. The agreement between the theory and our measurements is encouraging. Finite  ${}^{3}$ He coverage calculations are needed.

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