## Coherent Enhancement of the Hot-Electron Mean Free Path by Superlattice Transmission Resonances

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We report a strong enhancement of the optical responsivity in GaAs/A16aAs multi-quantum-well infrared detectors. This is explained by a resonant increase in the hot-electron mean free path as a result of the coherent transmission resonances in the continuum states above the energy barriers of the superlattice.

PACS numbers: 73.40.Kp, 72.20.Jv

There has been a great deal of interest recently in studying the continuum resonances above the energy barriers in multi-quantum-well superlattices, <sup>1-5</sup> as well as hot-electron transport<sup>6</sup> and capture into quantum as hot-electron transport<sup>6</sup> and capture into quantum<br>wells.<sup>7-11</sup> We discuss here the direct determination of the hot-electron mean free path  $L$  for an electron which is photoexcited out of a doped GaAs quantum well, transports above the superlattice energy barriers, and is subsequently recaptured into a distant well. Using a novel infrared photoconductivity technique, we have observed, for the first time, a striking enhancement in the low-temperature L (relative to the high-temperature  $L$ ), caused by the coherent resonances in the continuum states.

The two samples used in the study were grown using molecular-beam epitaxy and had the following structures. Sample  $A$  had a 50-period superlattice consisting of 45-Å GaAs wells (doped  $n = 1 \times 10^{18}$  cm<sup>-3</sup>) and 320 Å of undoped  $Al_{0.28}Ga_{0.72}As$  barriers; these were sandwiched between GaAs contact layers  $(n = 1 \times 10^{18})$ cm<sup> $-3$ </sup>). Sample *B* was similar except the wells were 38

Å and the barriers were 328 Å of  $Al<sub>0.36</sub>Ga<sub>0.64</sub>As$ . These were processed into  $200-\mu m$ -diam mesas and the substrate polished at 45° to allow (as required by the quantum-mechanical selection rules) a component of the optical electric field perpendicular to the superlattice.  $12, 13$ 

The measured  $12$  room-temperature-normalized absorption coefficient  $\alpha$  for photoexcitation of an electron from the single bound state in the well to the lowest con-<br> $\frac{1}{2}$  is above in Fig. 1. inuum state above the barrier,  $4,14,15$  is shown in Fig. 1 for both samples (dashed curve). For comparison we also show the photoconductive responsivity spectra  $(R)$ measured at  $T = 20$  K (using the apparatus described previously  $(13-15)$ . The shift of the responsivity curves to higher energy is a result of the lower temperature. For sample A the  $T=20$  K responsivity spectrum is also narrower than the  $T = 300$  K absorption spectrum as a result of the lower temperature. The fact that this is not the case for crystal  $B$  is due to the excited state being higher in the continuum and hence broader in energy.

The low-temperature bias dependence of the respon-



FIG. 1. Normalized absorption  $\alpha$  and responsivity R spectra (measured at  $T = 300$  and 20 K, respectively) for two crystals A and B. The actual peak values are as follows:  $\alpha_A = \alpha_B$  $=$  2000 cm<sup>-1</sup>,  $R_A$  = 0.55 A/W, and  $R_B$  = 0.44 A/W.



FIG. 2. Responsivity as a function of bias voltage for different temperatures. Sample A was measured at a wavelength  $\lambda = 7.8$   $\mu$ m while B was measured at  $\lambda = 6.4$   $\mu$ m.

sivities clearly shows a striking resonance enhancement (Fig. 2). These data were taken using infrared radiation having a wavelength near the peak of the responsivity spectra ( $\lambda$  = 7.8 and 6.4  $\mu$ m for samples A and B, respectively). Note that as the temperature is increased the resonance enhancement decreases in amplitude and disappears by  $T = 70$  K and that the  $T = 20$  and 70 K curves cross. Thus, surprisingly there is a bias for which the high-temperature responsivity is actually larger than the low-temperature responsivity. We will show later that this large enhancement is due to a coherent resonance of the photoexcited electron transmission coefficient in the continuum state above the  $Al_xGa_{1-x}As$  energy barriers.

In order to obtain the hot-electron mean free path L from these data we first express the responsivity to a 'good approximation as  $^{14,11}$  $\frac{e^{(-2at)}}{2}$  = 25% is the quantum efficiency (including the reflection off the top metal contact) and  $g$  is the optical gain derived below. The probability  $p$  of an electron generated at  $x_0$  traveling distance x is  $p = (1/L)$  $-e^{-x^2}/2 = 25\%$  is the quantum emclency (including<br>the reflection off the top metal contact) and g is the opti-<br>cal gain derived below. The probability p of an electron<br>generated at  $x_0$  traveling distance x is  $p = (1/L)$ <br> transport distance  $\Delta x$  for an electron generated between 0 and *l* and collected at *l* is

$$
\Delta x = \int_{x_0}^{l} (x - x_0) p \, dx + \int_{l}^{\infty} (l - x_0) p \, dx. \tag{1}
$$

For uniformly generated electrons, the average transport distance  $\Delta x_{av}$  is given by

$$
\Delta x_{\rm av} = \frac{1}{l} \int_0^l \Delta x \, dx_0 \,. \tag{2}
$$

Thus, the normalized transport or optical gain  $g = \Delta x_{av}/l$ 1S

$$
g = \left(\frac{L}{l}\right) \left[1 - \left(\frac{L}{l}\right) (1 - e^{-l/L})\right],\tag{3}
$$

where for our sample the superlattice length is  $l = 1.8$  $\mu$ m. Using Eq. (3) together with the data from Fig. 2



FIG. 3. Experimental hot-electron mean free path L (for both samples A and B) as a function of bias voltage, for  $T = 20$ and 70 K.

we can obtain the bias dependence of the hot-electron mean free path  $L$  (shown in Fig. 3). Note that the striking resonance in  $L$  is even more pronounced than the corresponding enhancement in the responsivity. This is due to the exponential relation between  $g$  and  $L$ .

We now analyze the origin of this resonance in  $L$ . As discussed previously,  $15,16$  the hot-electron mean free path is very long (i.e., many periods) in these structures and thus the transport of the photoexcited electron above the top of the energy barriers is in a quasiequilibrium condition. That is, on the average the energy gained from the potential drop through the superlattice is approximately balanced by the energy loss to LO phonons (having an energy  $\hbar \omega_0$ ). Thus, an electron will propagate with an energy  $n\omega_0$ . Thus, an electron will propagate with an average energy  $\Delta E \approx \frac{1}{2} \hbar \omega_0$  above the top of the energy barriers (as schematically illustrated in Fig. 4). This is possible since the short electron LO-phonon emission ime<sup>17-19</sup>  $\tau_{LO}$  = 170 fs is comparable to the transit time across a period. One can calculate the bias-dependent mean free path  $L(V)$  for this transport in terms of the hot-electron superlattice transmission coefficient  $T(V)$ using

$$
L(V) = v(V)\tau_w(V)T(V)\,,\tag{4}
$$

$$
v(V) = \mu E / [1 + (\mu E / v_s)^2]^{1/2}, \qquad (5)
$$

$$
\tau_w(V) = (\tau - \tau_0)(v/v_s) + \tau_0, \qquad (6)
$$

where  $v(V)$  is the velocity of the hot electrons (given in terms of the mobility<sup>20</sup>  $\mu$  = 500 cm<sup>2</sup>/Vs, the electric field erms of the mobility<sup>20</sup>  $\mu$  = 500 cm<sup>2</sup>/V s, the electric held<br>E = V/l, and the saturation velocity<sup>21</sup>  $v_s$  = 1×10<sup>7</sup> cm/s, and  $\tau_w(V)$  is the well recapture time [given in terms of the high-  $(\tau)$  and low-bias  $(\tau_0)$  values<sup>22</sup>]. This dependence on v accounts for the expected increase in  $\tau_w$  as the transit time and hence capture rate decreases. The linear dependence of L on  $T(V)$  [shown in Eq. (2)] is a simplification obtained from the expected linearity of the velocity on  $T(V)$ . That is, the velocity is approximately proportional to the superlattice energy bandwidth  $\delta E$ 



FIG. 4. Schematic superlattice band diagram showing electron transport and phonon emission.

(i.e.,  $v \propto \delta E$ ), <sup>23</sup> which is in turn proportional to the transmission coefficient [i.e.,  $\delta E \propto T(V)$ ]. <sup>24</sup> In contrast,  $\tau_w$  is not expected to depend strongly on  $T(V)$  since it is primarily a single-quantum-well property describing the capture of the hot electron from the lowest continuum state above the top of the well into a quantum-well bound state.

Since  $v(V)$  and  $\tau_w(V)$  are nearly constant at high bias they do not significantly affect the shape of the resonance in L, which is produced by the barrier transmission resonances. To calculate  $T(V)$ , consider an electron being transported through the superlattice and having an average energy  $\Delta E$  above the top of the barriers. Since, on the average, the electron will lose one or more phonons of energy per period, it will usually (with probability  $p_1$ ) traverse a single well (having a transmission coefficient  $t_1$ ), emit at least one phonon, and then incoherently traverse the next well (as schematically illustrated in Fig. 4 for the electron near well  $w_1$ ). However, some of the time (with probability  $p_2$ ) an electron can coherently traverse two quantum wells (transmission coefficient  $t_2$ ) with no energy loss (i.e., ballistically) and then emit sufficient phonons to return to an average energy  $\Delta E$ (schematically illustrated in Fig. 4 for the electron near well  $w_3$ ). It is this ballistic transport across a pair of wells which leads to the coherent transmission resonance in the mean free path. An exact calculation of the average superlattice transmission coefficient  $T(V)$  in terms of  $p_1, p_2, t_1$ , and  $t_2$  has been done.<sup>25</sup> However, one can use the much simpler expression (which agrees numerically to within a few percent) given below

$$
T(V) = [(1-p2) + p2t2(V)]N, \t(7)
$$

where  $N$  is the number of *pairs* of quantum wells traversed before recapture and where we have simplified the above expression using the calculated result  $t_1 \approx 1$ . This expression for  $T(V)$  is just the sum of the probability-weighted transmission coefficients multiplied together for N-independent events. The coherent transmission coefficient for a pair of wells,  $t_2(V)$ , is calculated  $2^6$  using the transfer-matrix method in an analogous way to that used for the transmission of a pair of barriers.<sup>27</sup> By now combining Eqs.  $(4)-(7)$  and solving self-consistently at each bias voltage using  $L(V)$  $=2l_pN(V)$  (where  $l_p = 365$  Å is the superlattice period) we can calculate the bias dependence of the mean free path. The result is shown in Fig. 5 for two values of the probability for coherent transport  $p_2 = 0.3$  and 0.05 which have been adjusted (together with  $\tau$ ) to give the best fit with experiment. The good agreement with the measurements shown in Fig. 3 is evident with the position, shape, and temperature dependence of the hotelectron mean free path  $L(V)$  being well explained. Note that, as previously mentioned, the high-field well recapture time  $\tau$  is significantly larger than the low-field value  $\tau_0$  and is, in fact, comparable to the electron tran-



FIG. 5. Calculated mean free path  $L$  as a function of bias voltage (for both samples  $A$  and  $B$ ). The well recapture times  $\tau$  and coherent probabilities  $p_2$  are indicated.

sit time  $\tau_T = l/v$  across the superlattice. This is the reason that the hot-electron mean free path is so long and thus the optical gain close to its maximum value of  $\frac{1}{2}$ 

The *ballistic* mean free path  $28,29$  is defined in terms of the coherent probability  $p_2$  using  $p_2 = \exp(-l_p/\Lambda_b)$ . Substituting  $p_2 = 0.3$  at  $T = 20$  K and  $p_2 = 0.05$  at  $T = 70$ K we determine  $\Lambda_b$  = 300 and 120 Å at these temperatures which is in satisfactory agreement with other determinations.  $28,29$  It is this coherent ballistic transport and the associated transmission resonances that is responsible for the unusual crossing of the different temperature and wavelength curves mentioned previously (Figs. 2 and 3).

In conclusion, we have presented the first direct measurement of a striking enhancement in the hot-electron recapture mean free path, and shown that it is caused by the coherent double-well transmission resonances in the superlattice continuum states. The strength of this resonance demonstrates that the hot electrons remain in the  $\Gamma$  valley as a results of the short phonon emission time  $(\tau_{LO} = 170 \text{ fs})$  and resulting rapid phonon energy loss. This new understanding of the transport physics can lead to improved quantum-well infrared photodetectors. 14, 15, 30, 31

We are grateful to G.A. Baraff, F. Beltram, and S. Luryi for helpful discussions.

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