Sympathetic Cooling of Trapped Ions: A Laser-Cooled Two-Species Nonneutral Ion Plasma

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Sympathetic cooling of trapped ions has been demonstrated in an experiment where 198 Hg⁺ ions were confined in a Penning ion trap with laser-cooled 9 Be⁺ ions. 198 Hg⁺ temperatures below 1 K were achieved. Ion plasma sizes, shapes, and rotation frequencies were measured. Dramatic changes in the 9 Be⁺ plasma were observed when the 198 Hg⁺ ions were introduced into the trap. These observations are consistent with the prediction of centrifugal separation for ions of different charge-to-mass ratios.

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The techniques of trapping and laser cooling have led to dramatic improvements in recent measurements and future prospects for precision spectroscopy.^{1,2} However, the number of species which can be directly laser cooled is limited by the availability of tunable, narrow-band sources and by more fundamental problems such as complicated level structure (as in molecules) or the absence of optical structure (as in protons and negative atomic ions). In addition, the laser-cooling process itself strongly perturbs the levels of an atom or ion. The cooling laser must be turned off during the interrogation time to avoid light shifts (ac Stark shifts) and broadening many orders of magnitude larger than achievable linewidths. In the most accurate experiment to date,³ the linewidth of a radio frequency transition in ${}^{9}\text{Be}^{+}$ was limited (≥ 0.025 Hz) by the necessity to restrict interrogation times $(\leq 20 \text{ s})$ in order to minimize heating that occurred when the cooling laser was turned off. In principle, linewidths substantially less than 0.001 Hz should be possible on transitions in trapped ions.

Sympathetic cooling,^{1,4,5} where one species is cooled by interaction with a second, directly cooled species, offers a solution to these problems. In the present experiments, spectroscopy of continuously cooled ¹⁹⁸Hg⁺ ions was made possible by confining them in a trap together with laser-cooled ⁹Be⁺ ions. The 313-nm radiation used to cool the Be⁺ ions did not seriously perturb the Hg⁺ ions since this wavelength is far from any resonance in Hg⁺. We estimate that the fractional light shift in the ²⁰¹Hg⁺ hyperfine separation would be less than 5×10^{-18} under conditions similar to those in the present experiment.

Although sympathetic cooling was noted previously in experiments with different isotopes of magnesium ions^{1,4} we report here the first measurements of temperatures and spatial distributions for a two species, magnetically confined, nonneutral plasma. In addition, the present experiments have demonstrated that radial diffusion of the sympathetically cooled species is prevented. One interesting feature of such a plasma, that the species with higher mass-to-charge ratio moves radially to the outside of the lighter (or more highly charged) species,^{6,7} was observed. The present results appear to have a direct bearing on proposed experiments to store and cool antiprotons at very low energies⁸⁻¹⁰ and may be important in other experiments where two or more species of different charge-to-mass ratio are simultaneously present in the trap.¹¹ Different considerations lead to separation of species in rf traps.¹²

The experiments were carried out using a Penning ion trap¹³ with hyperbolically shaped electrodes. The endcap-to-endcap spacing was 0.51 cm and the innerring diameter was 0.83 cm. The trap and vacuum system were at room temperature for all of the measurements except one where the trap was cooled to 77 K. A magnetic field near 1.43 T was used for all of the measurements. Be⁺-ion plasmas (or "clouds") were created in the trap by use of a beam of electrons to ionize beryllium atoms which were evaporated from a tungsten filament wrapped with beryllium wire. Hg⁺ ions were loaded into the trap by ionizing mercury vapor leaked into the vacuum system through a variable leak valve while the Be⁺ ions were being laser cooled.

Three laser systems were used to cool and probe the ions. A frequency-doubled dye laser beam with a power of approximately 50 μ W at 313 nm was directed through a hole in the ring electrode and used to cool the Be⁺ ions on the $2s^2S_{1/2}$ to $2p^2P_{3/2}$, $m_J = \pm \frac{1}{2}$ to $m_J = \pm \frac{3}{2}$, transition.¹ The photons backscattered by the Be⁺ ions were collected and counted. This signal was used for all of the measurements on the Be⁺ ions. A second 313-nm source was directed through another hole in the ring. When tuned to the $2s^2S_{1/2}$ to $2p^2P_{3/2}$, $m_J = \pm \frac{1}{2}$ to $m_J = -\frac{1}{2}$, transition, this probe beam depopulated the $m_J = \pm \frac{1}{2}$ state and thus caused a decrease in the scattered light from the cooling beam.¹ The ion-cloud sizes and shapes were measured by observing this signal for different positions of the probe beam. The ion-cloud rotation frequencies were obtained through the Doppler shift by measuring the frequency of the probe laser which produced maximum depopulation.¹⁴ A third laser system¹⁵ produced a few microwatts of tunable power at 194 nm. The positions and velocities of the Hg⁺ ions in the trap were measured by collecting and counting the 194-nm photons scattered when the frequency was tuned through the $6s^2S_{1/2}$ to $6p^2P_{1/2}$, $m_J = -\frac{1}{2}$ to $m_J = +\frac{1}{2}$ transition in the ion. Microwaves tuned to the $\Delta m_J = 1$ transition in the ground state prevented depletion of the $m_J = -\frac{1}{2}$ ground state by optical pumping.¹⁶ For both Be⁺ and Hg⁺ the temperatures were determined by measuring the Doppler contribution to the frequency width of the observed signal as the appropriate laser was tuned through resonance.¹⁴ An example of the signal from a Hg⁺-ion cloud whose cyclotron temperature has been sympathetically cooled to near 1 K is shown in Fig. 1.

A cold, single-species ion cloud in a Penning trap with hyperbolic electrodes should assume a nearly spheroidal shape with constant density inside the cloud and an abrupt drop in density at the edge.^{14, 17, 18} The eccentricity of the spheroid is determined by the trapping voltage, magnetic field, and rotation frequency. Any cloud in thermal equilibrium will exhibit uniform rotation. The rotation frequency is a measure of the density and of the angular momentum of the ions.¹⁷⁻²¹ It can be partially controlled by varying the torque applied to the cloud by the cooling laser. Observed rotation frequencies were well below those corresponding to the maximum stable density of ions in the trap, the Brillouin density.²⁰ The mechanism which limits the frequency is not clearly understood, but it may depend upon trap asymmetries.^{18, 19, 22} For precision spectroscopy, high rotation velocities and the accompanying Doppler shifts should be avoided by working at low densities.



FIG. 1. Observed fluorescence from a Hg⁺-ion cloud cooled to approximately 1 K by interaction with a laser-cooled Be⁺ cloud. The horizontal axis is the frequency of a laser tuned through the $6s^2S_{1/2}$ $(m_J = -\frac{1}{2})$ to $6p^2P_{1/2}$ $(m_J = +\frac{1}{2})$ transition in Hg⁺. The room-temperature Doppler width of this transition is about 1.4 GHz.

A dramatic change in the rotation frequency (and thus the density) and the shape (away from spheroidal) of the Be⁺ cloud occurred when Hg⁺ ions were introduced into the trap. With only Be⁺ in the trap, rotation frequencies up to nearly 200 kHz could be achieved. The single-particle rotation (magnetron) frequency was measured to be only 9.4 kHz with -1.5V on the ring, so the observed frequencies were due primarily to the space-charge fields. With Hg⁺ and Be⁺ in the trap, the largest observed rotation frequency was 21 kHz. The measured size and shape of a Be+ cloud with and without Hg^+ is shown in Fig. 2(a). Adding the Hg⁺ ions decreased the rotation frequency by a factor of 2. A larger change in density and shape of a Be⁺ cloud is shown in Fig. 2(b). Figures 2(a) and 2(b) are the smallest and largest clouds examined. In all cases the Be⁺ clouds were prolate spheroids without the Hg⁺ and oblate and nonspheroidal with Hg⁺ present. The Hg⁺ clouds appeared disk shaped with diameter-to-length ratios of 6 to 1 or larger.

Clearly, the Hg⁺ ions applied a substantial torque to the Be⁺ ions. For all of the Hg⁺ clouds measured, the axial bounce frequency (equal to twice the axial length divided by the rms axial velocity) was approximately equal to the rotation frequency. This condition is consistent with axial asymmetries of the trap and resultant resonant particle transport limiting the rota-tion frequency.^{18, 22} No definitive evidence is available, however, to exclude other mechanisms²³ from limiting the rotation frequency with the exception of drag due to background gas. Cooling of the trap electrodes to 77 K, which substantially lowered the residual mercury pressure, caused no change in measured rotation frequencies. Despite the presence of a torque on the Hg⁺ ions, they remained in the trap for several hours unless the cooling was interrupted. If the cooling laser was blocked or tuned off resonance the Hg⁺ ions were lost in several minutes, demonstrating that Hg⁺ confinement was dependent on the torque applied to the Hg⁺ ions by the laser via the coupling to the Be⁺ ions.

Measured Hg⁺ temperatues ranged from 0.4 to 1.8 K and Be⁺ temperatures ranged from less than 0.05 to 0.2 K. The temperature difference between the two species may be a result of the thermal coupling between the directly laser-cooled Be⁺ ions and the indirectly cooled Hg⁺ ions being weak, due to centrifugal separation. Also, the axial temperature of the Be⁺ ions should be higher than the transverse temperature because of photon recoil,¹⁴ and this could cause the Hg⁺-ion temperature to take on some intermediate value.

Given the torque due to the Hg^+ ions, the counteracting torque due to the laser on the Be^+ ions, and the temperature difference between the two clouds, it is not unreasonable to expect some shear. In a uni-



FIG. 2. (a) Measured Be⁺- and Hg⁺-ion-cloud shapes. The magnetic field is along the z axis. The Be⁺ cloud, which contained about 800 ions, is shown with and without the Hg⁺ present. The measured rotation frequencies were 41 kHz without Hg⁺ [corresponding to a density, $n(Be^+) = 3.9 \times 10^7 \text{ cm}^{-3}$] and 20 kHz with Hg⁺ present $[n(Be^+) = 1.9 \times 10^7 \text{ cm}^{-3}$, $n(Hg^+) = 1.6 \times 10^7 \text{ cm}^{-3}$]. The solid lines drawn through the data points conform to the theoretically predicted and separately confirmed spheroidal shape for Be⁺ alone but are drawn without consideration of theoretical shapes for Be⁺ and Hg⁺ together. The edges of the clouds were measured with an uncertainty of about 25 μ m. (b) Measured cloud shapes for a Be⁺ cloud which contained about 12000 ions and a Hg⁺ cloud which was larger in radial extent than the aperture through the ring electrode (diameter $\simeq 2100 \ \mu$ m). The measured rotation frequencies were 73 kHz without Hg⁺ [$n(Be^+) = 7.0 \times 10^7 \text{ cm}^{-3}$] and 18 kHz with Hg⁺ $[n(Be^+) = 1.8 \times 10^7 \text{ cm}^{-3}, n(Hg^+)]$ = $1.5 \times 10^7 \text{ cm}^{-3}$]. (c) Theoretically predicted shapes for cold Be⁺ and Hg⁺ clouds under conditions similar to those in (a).

formly rotating cloud, the Doppler shift and thus the observed optical resonance frequency should be a linear function of the radial distance from the center of the cloud. Figure 3 shows the observed resonance frequency for a Be^+ cloud, confined in the trap together



FIG. 3. Measured resonance frequency in Be^+ as a function of the transverse position (perpendicular to the trap axis) of the probe laser beam. These measurements, done with Hg⁺ ions present in the trap, placed a limit on the amount of shear in the Be⁺ cloud. The statistical error in the data points is smaller than the size of the points.

with a Hg⁺ cloud, as a function of the transverse position of the probe laser beam. Fitting the data in Fig. 3 with a rotation frequency $\omega = \omega_r + \Delta \omega (r/r_{cl})$, where r_{cl} is the cloud radius, implies that $|\Delta \omega / \omega_r| < 0.3$. Indeed, to the extent that the data suggest that shear is present, it appears that the outer edge of the cloud is rotating faster than the middle. No evidence for shear was observed in a similar measurement on Hg⁺ ions or in the comparison of the frequencies between the two species.

The measured shapes of the Be+- and Hg+-ion clouds were compared to numerical calculations based on a zero-temperature theory which balances magnetic, space-charge, and external electric forces. 6, 17, 24 The calculation used measured values for the trapping voltage, magnetic field, rotation frequency, and relative cloud diameters to predict shapes. A zerotemperature theory should be applicable when the ratio of the Debye length to the dimensions of the ion cloud is small. In the present experiments this ratio was typically less than 0.1. The theoretical prediction of complete radial separation of the ion clouds was not definitively tested since all of the probing of ion position was done in a direction perpendicular to the axis of the trap. Changes in collection efficiency for the 194-nm fluorescence as the beam position was moved prevented the use of count rate as a measure of the Hg⁺ cloud thickness along the laser-beam direction. The theory^{6, 24} suggests that the heavier Hg⁺ ions should be found in a torus around the lighter Be⁺ ions as shown in Fig. 2(c).

These experiments have demonstrated the effectiveness of sympathetic cooling and point the way toward applications such as use in high-resolution spectroscopy and antiproton accumulation and storage. They have also allowed observation of some of the characteristics of a cold, magnetically confined, two-species nonneutral plasma. Significant features include the dramatic change in the shape of the Be⁺-ion cloud when the Hg⁺ ions are introduced into the trap, the temperature difference between the laser-cooled Be⁺ ions and the sympathetically cooled Hg^+ ions, and the substantial torque exerted on the Be^+ cloud by the Hg⁺ ions. A few features, including the source of the torque on the Hg⁺ ions, are not clearly understood and may limit the number of ions that can be stored in a trap. Such techniques may be applicable to cooling neutral particles in a trap.25

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