Nuclear Temperatures and the Population of Particle-Unstable States of 6 Li in 40 Ar-Induced Reactions on 197 Au at E/A = 60 MeV

J. Pochodzalla, ^(a) W. A. Friedman, ^(b) C. K. Gelbke, W. G. Lynch, and M. Maier National Superconducting Cyclotron Laboratory, Michigan State University, East Lansing, Michigan 48824

and

D. Ardouin, H. Delagrange, H. Doubre, C. Grégoire, A. Kyanowski, W. Mittig, A. Péghaire, J. Péter, F. Saint-Laurent, Y. P. Viyogi,^(c) and B. Zwieglinski^(d) Laboratoire Grand Accélérateur National d'Ions Lourds, 14021 Caën Cédex, France

and

G. Bizard, F. Lefèbvres, and B. Tamain Laboratoire de Physique Corpusculaire, Université de Caën, 14032 Cäen Cédex, France

and

J. Québert

Centre d'Etudes Nucléaires de Bordeaux, 33170 Gradignan Cédex, France (Received 22 April 1985)

Correlations between coincident alpha particles and deuterons emitted in ⁴⁰Ar-induced reactions on ¹⁹⁷Au at E/A = 60 MeV were measured. The relative populations of particle-unstable states of ⁶Li were extracted. The measured spectra are consistent with a mean nuclear temperature at emission of $T \approx 5$ MeV. Limitations of temperature measurements via the population of excited states are discussed.

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Complex-particle emission in intermediate- and high-energy nucleus-nucleus collisions presents a problem of such complexity that recourse to statistical methods seems appropriate. Statistical-model calculations are often based on the assumption of particle emission from equilibrated subsets of nucleons.¹⁻⁴ In specifying the phase space of decay configurations, inmedium corrections are nearly always neglected and the *asymptotic* nuclear states (bound and unbound) are used. Such calculations make specific predictions about the relative populations of ground and excited states of the emitted fragments. Indeed, in each model a unique relation exists between the relative population of states and the temperature at the point at which the particles leave the equilibrated subsystem. In principle, this "emission temperature" can be deduced from the relative population of excited states.

An approach of this nature involving a measurement of the relative population of ground and particle-stable excited states was recently used⁵ to determine the emission temperature for ¹⁴N-induced reactions on ¹⁰⁷Ag at E/A = 35 MeV. Surprisingly few ⁶Li, ⁷Li, and ⁷Be nuclei were observed in particle-stable excited states. This observation was interpreted to imply emission temperatures $T \le 1$ MeV, significantly smaller than either the temperature of the compound nucleus or the temperature parameters which characterize the kinetic-energy spectra of these light nuclei.⁵ However, the relative population of ground and *long*- *lived* excited states can be altered by the sequential decay of primary fragments produced in particleunbound states⁵ or by neutron-induced deexcitations⁶ which can occur after emission from an equilibrated system. In order to reduce the effects from sequential decay, it is desirable to investigate the population of *short-lived* particle-unstable states.

We have measured the population of particleunbound states of ⁶Li for ⁴⁰Ar-induced reactions on ¹⁹⁷Au at E/A = 60 MeV. For this heavier projectiletarget combination, complicating surface and finiteparticle-number effects should be reduced, and a higher degree of thermalization might be expected. Inclusive cross sections, measured for ⁴⁰Ar + ¹⁹⁷Au collisions over a large range of energies and fragment masses, were interpreted in terms of statistical emission mechanisms.⁷

The experiment was performed at the Laboratoire Grand Accélérateur National d'Ions Lourds, at Caën. A gold target of 10-mg/cm² areal density was irradiatby a beam of ⁴⁰Ar of E/A = 60 MeV incident energy. The size of the beam spot on target was approximately 1×2 mm². Light particles ($Z \le 3$) were detected by a close-packed hexagonal array of ΔE -E telescopes, each consisting of a 400- μ m-thick Si detector and a 10-cm-thick NaI detector. The center of the hodoscope was positioned at a laboratory angle of 30°. Each telescope subtended a solid angle of 0.46 msr; the angular separation between adjacent telescopes was 4.2°. energy calibrations of the hodoscope, established for all isotopes with $Z \leq 3$, are accurate to within 2%. A complete description of the experimental details will be given elsewhere.

Figure 1 shows the measured α -d correlation function, R(q), defined by

$$\sigma_{\alpha d}(\mathbf{p}_{\alpha}, \mathbf{p}_{d}) = C \sigma_{\alpha}(\mathbf{p}_{\alpha}) \sigma_{d}(\mathbf{p}_{d}) [1 + R(q)].$$
(1)

Here, $\sigma_{\alpha d}$ and σ_{α} , σ_d denote the two-particle and single-particle inclusive cross sections for alpha particles and deuterons, respectively; \mathbf{p}_{α} and \mathbf{p}_d are the laboratory momenta; q is the momentum of relative motion; and C is a normalization constant which is determined by the requirement that R(q) = 0 for q = 160-200 MeV/c. The measured correlation function exhibits two maxima corresponding to the T=0, $J^{\pi}=3^+$ state in ⁶Li at 2.186 MeV ($\Gamma=24$ keV, $\Gamma_{\alpha}/\Gamma_{\text{tot}}=1.00$) and the overlapping T=0, $J^{\pi}=2^+$ states at 4.31 MeV ($\Gamma=1.3$ MeV, $\Gamma_{\alpha}/\Gamma_{\text{tot}}=0.97$), and at 5.65 MeV ($\Gamma=1.9$ MeV, $\Gamma_{\alpha}/\Gamma_{\text{tot}}=0.74$).⁸

The coincidence yield resulting from the decay of excited ⁶Li nuclei was obtained by the assumption that the α -d coincidence yield is given by $Y_{\alpha d} = Y_{6_{\text{Li}}} + Y_b$, where $Y_{6_{\text{Li}}}$ denotes the yield from decaying ⁶Li nuclei and Y_b denotes the "background" yield. The background yield was assumed to be given by $Y_b = CY_{\alpha}Y_d[1 + R_c(q)]$, where Y_d and Y_{α} are the singles yields and $R_c(q)$ corresponds to the correlation function expected from the Coulomb repulsion of the two coincident particles.^{9,10} This background is indicated by the solid curves in Fig. 1. Yields of particle-unstable excited ⁶Li nuclei, shown in Fig. 2, were extracted by binning of the experimental yield with respect to the kinetic energy in the ⁶Li rest frame and



FIG. 1. Correlation function for coincident deuterons and alpha particles for ⁴⁰Ar-induced reactions on ¹⁹⁷Au at E/A = 60 MeV. The curve is explained in the text.

subtraction of the background yield shown in Fig. 1.

The yield $Y_{6Li}(E^*)$ is related to the energy spectrum, dn(E)/dE, in the ⁶Li center-of-mass frame by the equation

$$Y_{6_{\text{Li}}}(E^*) = \int \epsilon(E^*, E) \frac{dn(E)}{dE} dE.$$
 (2)

Here, $\epsilon(E^*, E)$ is the efficiency function for the response of the hodoscope to α -*d* pairs arising from the decay of excited ⁶Li nuclei; *E* and *E*^{*} denote the actual and measured excitation energies, respectively.

The efficiency function for our hodoscope was calculated for the precise geometry, light-particledetection thresholds ($E_d \ge 15$ MeV, $E_\alpha \ge 40$ MeV), and detector energy resolution that was determined during the experiment. In these calculations, the parent nucleus, ⁶Li^{*}, was assumed to decay isotropicalin its rest frame. The laboratory energy spectra and angular distributions of excited ⁶Li nuclei were constrained to be identical to the spectra shown in Fig. 3 for the emission of particle-stable ⁶Li nuclei. Because of the high detection thresholds for particle-stable Li nuclei, it was necessary to extrapolate the measured cross sections toward lower energies. For this extrapolation, simple analytic functions were fitted to the data. Two different extrapolations are shown in the figure. The calculated yields are insensitive to the detailed form of these parametrizations, provided that they reproduce the measured ⁶Li cross sections.



FIG. 2. Energy spectrum resulting from the decay of particle-unbound states in ⁶Li. The curves correspond to thermal distributions, T = 1, 2.5, 5, 10, and 20 MeV in Eq. (2), taking the response of the hodoscope into account.



FIG. 3. Energy spectra of particle-stable ⁶Li nuclei and two examples of cross-section parametrizations used for the calculations of the hodoscope response. The parametrizations were of the form $d^2\sigma/dEd\Omega = CE'^{1/2}\exp(-E'\sin^2\theta/T_1 - E^*/T_2)$, with $E' = E - V_c$, $E^* = E'\cos^2\theta + E_0$ $-2(E'E_0)^{1/2}\cos\theta$, and $E_0 = mv_0^2/2$; *m* is the mass of ⁶Li. The solid curves correspond to the parameters $T_1 = 17.7$ MeV, $T_2 = 40.1$ MeV, $v_0/c = 0.16$, and $V_c = 30$ MeV; the dashed curves correspond to $T_1 = 19.5$ MeV, $T_2 = 29.7$ MeV, $v_0/c = 0.186$, and $V_c = 0$.

The excitation energy spectrum dn/dE for thermally emitted ⁶Li nuclei is given by

$$\frac{dn(E)}{dE} = Ne^{-E/T} \cdot \sum_{i} \left[\frac{(2J_i + 1)\Gamma_i/2\pi}{(E - E_i)^2 + \Gamma_i^2/4} \frac{\Gamma_{\alpha,i}}{\Gamma_i} \right], \quad (3)$$

where N is a normalization constant and the sum includes the three T=0 excited states of ⁶Li below 10 MeV excitation energy. Equation (3) corresponds to the phase-space modifications arising from the α -d interaction¹¹

$$\frac{dn}{dE} = \frac{1}{\pi} \sum_{J} (2J+1) e^{-E/T} \frac{\partial \delta_{J}(E)}{\partial E}, \qquad (4)$$

if the energy dependence of the phase shifts, $\delta_J(E)$, is dominated by a series of resonances. For narrow resonances, the relative yields are given by

$$\exp(-E_i/T)(2J_i+1)\Gamma_{\alpha,i}/\Gamma_i.$$
(5)

Calculations based on Eqs. (2) and (3) are shown in Fig. 2 for a variety of emission temperatures. The calculations were normalized to reproduce the experimental yield over the energy range of $T_{c.m.} = 0.3-1.2$ MeV. The spectral shapes are sensitive to emission temperatures smaller than the level separation; higher emission temperatures are more difficult to distinguish. The experimental yields are consistent with an emission temperature of $T \approx 5$ MeV. This value is lower than the temperature parameter $T \approx 20$ MeV which characterizes the energy spectra of complex nuclei emitted at intermediate rapidity,⁷ but higher than the one reported⁵ for ¹⁴N-induced reactions at E/A = 35 MeV.

At this point, we wish to caution that temperatures deduced from measurements of the relative population of states may have large uncertainties whenever the primary population ratio is altered by secondary processes. To demonstrate this, we consider the population ratio of two states separated by the excitation energy ΔE . If the primary population ratio R $= C \exp(-\Delta E/T)$ is altered by a factor α , and if the resulting ratio is then interpreted in terms of a temperature T', i.e., $C \exp(-\Delta E/T') = \alpha R$, one obtains $T' = T/(1 + T/\beta)$, with $\beta = -\Delta E/\ln(\alpha)$. Only in the limit $\beta >> T$ will T' agree with the temperature T; if, on the other hand, $\beta \ll T$, one obtains $T' = \beta$ $= -\Delta E/\ln(\alpha)$, independent of T. Large values of β can be achieved by selection of states whose population is not altered after emission from the equilibrated system and/or by comparison of states which are widely separated in energy. If one cannot ensure that α is close to unity (or else that the value of α is precisely known), the population ratios will only be useful for $T \leq \Delta E$.

The ground state, in particular, can be strongly fed by the sequential decay of primary fragments. From our measurements we obtain a population ratio $\sigma_1/\sigma_0 = 0.8 \pm 0.2$, where σ_0 denotes the integrated cross section for particle-stable ⁶Li and σ_1 denotes the integrated cross section of ⁶Li emitted in the 2.186-MeV state. If one ignored the complication of sequential decay, this ratio would indicate a temperature of $T' = 2.2 \pm 0.7_{-0.6}^{+0.7}$ MeV. The measured population ratio can also result from an emission temperature of 5 MeV and a secondary enhancement of the ground-state population by a factor of 1.7.

The present investigation confirms that particleunstable states of light nuclei are strongly populated in intermediate-energy nucleus-nucleus collisions. The shape of the experimental excitation energy spectrum is consistent with a thermal distribution characterized by an emission temperature of $T \approx 5$ MeV. Higher temperatures cannot be ruled out with certainty since the interpretation of the data becomes uncertain for $T \gg \Delta E$. The extent to which the spectrum is influenced by processes which occur after emission requires further detailed investigations.

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^(a)On leave from the Max-Planck-Institut für Kernphysik, Heidelberg, Federal Republic of Germany.

^(b)Permanent address: Department of Physics, University of Wisconsin, Madison, Wis. 53706.

(c)Permanent address: Bhabha Atomic Research Center,

Calcutta, India.

- ^(d)Permanent address: Institute for Nuclear Science, Warsaw, Poland.
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¹⁰The curves in Fig. 1 correspond to $r_0 = 8$ fm. For $q \ge 100$ MeV/c the background has been extrapolated, requiring $R_c(q \to \infty) = 0$. Our conclusions do not depend critically on this specific choice of background.

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