Dimuons from Gauge Fermions Produced in $p\bar{p}$ Collisions

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In a supersymmetry scenario with a mass hierarchy $m_{\tilde{g}} \approx m_{\tilde{q}} > m_{\tilde{u}} > m_{\tilde{l}}$, gluino-scalar-quark pair production followed by the decay chain $\tilde{g} \to \tilde{q}\bar{q} (\bar{q}q), \tilde{q} \to \tilde{\omega}q, \tilde{\omega} \to \tilde{\mu}\nu (\mu\tilde{\nu}), \tilde{\mu} - \mu\tilde{\gamma}$ leads to like-sign and unlike-sign dimuons with comparable rates and possibly little accompanying hadronic activity; such events will often contain strange particles. Predictions are made for the dimuon distributions. The possible relevance to dimuon observations by Arnison et al., is addressed.

PACS numbers: 13.85.Qk, 11.30.Pb, 12.35.Eq

In experiments at the CERN $p\bar{p}$ collider, anomalous events are found^{1,2} which are unexplained by standard model sources. Of particular theoretical interest are the monojet plus missing transverse momentum (\bar{p}_T) events reported by Arnison et al. (UA1 Collaboration)¹ which have been interpreted³⁻⁵ as possible evidence for the production of supersymmetric particles.⁶ If scalar quarks (s-quarks) (\tilde{q}) or gluinos (\tilde{g}) are strongly produced, then their decays to photinos $(\tilde{\gamma})$ could explain the \overline{p}_T , since the photino interacts feebly and would be undetected by the calorimeters. Three specific supersymmetric scenarios have been suggested, namely (i) $\tilde{g}\tilde{g}$ production³ with masses $m_{\tilde{g}} > m_{\tilde{g}}$ $\approx 40 \text{ GeV}$ and $\tilde{g} \rightarrow q\bar{q}\tilde{\gamma}$ decays; (ii) $\tilde{q}\tilde{g}$ production⁴ with masses $m_{\tilde{q}} \approx 100 \text{ GeV}$, $m_{\tilde{g}} \approx 3 \text{ GeV}$, $\tilde{q} \rightarrow q\tilde{\gamma}$ decays, and a long-lived gluino; (iii) $\tilde{q}\bar{\tilde{q}}$ and $\tilde{q}\tilde{g}$ production⁵ with $m_{\tilde{g}} > m_{\tilde{q}} \approx 40$ GeV and $\tilde{q} \rightarrow q \tilde{\gamma}$ decays. In this Letter we address striking consequences of scenario (iii) involving dilepton events.

In grand-unified supersymmetry models with scalar particle (s-particle) mass relations $m_{\tilde{l}} = m_{\tilde{a}}$ and $m_{\tilde{e}}$ $= m_{\tilde{W}} = m_{\tilde{B}}$ at large scales $\mu \sim O(10^{16} \text{ GeV})$ coming from soft supersymmetry breaking, the masses at low scales $\mu \sim O(M_W)$ are calculable from the renormalization-group equations.⁷ For $m_{\tilde{g}} > m_{\tilde{q}}$ tight mass constraints are obtained⁸:

$$m_{\bar{g}}/m_{\bar{q}} \le 1.1, \quad m_{\bar{l}}/m_{\bar{q}} \le 0.45,$$

 $m_{\bar{v}}/m_{\bar{v}} \simeq 0.15,$ (1a)

which in scenario (iii) imply that

$$m_{\tilde{q}} \sim 40 \text{ GeV}, \quad m_{\tilde{l}} \sim 18 \text{ GeV},$$

 $m_{\tilde{g}} \sim 45 \text{ GeV}, \quad m_{\tilde{\gamma}} \sim 6 \text{ GeV}.$ (1b)

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This approximate value of the scalar electron (selectron) mass is already below the lower bound set by e^+e^- experiments,⁹ namely $m_{\tilde{e}} > 22$ GeV.

The present limit on the lowest W-fermion-Higgsfermion $(\tilde{\omega})$ mass from e^+e^- experiments^{9,10} is $m_{\tilde{e}} > 22$ GeV. As recently stressed by Hall and Raby,¹¹ it is possible that an $\tilde{\omega}$ is lighter than the squarks, thus permitting $\tilde{q} \rightarrow q \tilde{\omega}$ decay, with subsequent $\tilde{\omega}$ decays

$$\tilde{\omega} \to e \tilde{\nu}_e \to e (\nu_e \tilde{\gamma}), \quad \tilde{\omega} \to \tilde{e} \nu_e \to (e \tilde{\gamma}) \nu_e.$$
 (2)

Here we assume that $\tilde{\nu} \rightarrow \nu \tilde{\gamma}$ is the dominant $\tilde{\nu}$ decay mode.¹² The $\tilde{\omega} \rightarrow e\bar{p}_T$ branching fraction is 0.33.

The partial widths for $\tilde{q} \rightarrow q \tilde{\omega}$ and $\tilde{q} \rightarrow q \tilde{\gamma}$ decays in



FIG. 1. Branching fraction for the decays $\tilde{q} \rightarrow q \tilde{\omega}$ vs the $\tilde{\omega}$ mass for $m_{\tilde{a}} = 40$ GeV. A mixing angle $\beta = \pi/4$ in Eq. (3) and equal initial \tilde{q}_L and \tilde{q}_R populations are assumed.

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the light- m_q approximation are

$$\Gamma(\tilde{q}_L \to q\tilde{\omega}) = \frac{1}{4} \alpha \frac{\sin^2 \beta}{\sin^2 \theta_W} m_{\tilde{q}} \left[1 - \left(\frac{m_{\tilde{\omega}}}{m_{\tilde{q}}} \right)^2 \right]^2,$$

$$\Gamma(\tilde{q}_R \to q\tilde{\omega}) = 0,$$
(3)

$$\Gamma(\tilde{q} \to q\tilde{\gamma}) = \frac{1}{2} \alpha e_q^2 m_{\tilde{q}} [1 - (m_{\tilde{\omega}}/m_{\tilde{q}})^2]^2,$$

where $\sin^2\beta$ is the *W*-fermion, Higgs-fermion mixing. The expected $\tilde{u} \rightarrow d\tilde{\omega}$ and $\tilde{d} \rightarrow u\tilde{\omega}$ branching fractions from Eq. (3), based on equal initial \tilde{q}_L and \tilde{q}_R populations of mass 40 GeV, are shown in Fig. 1 versus $m_{\tilde{\omega}}$ for mixing angle $\beta = \pi/4$. For $m_{\tilde{q}} - m_{\tilde{\omega}} \ge 5$ GeV, the $\tilde{d} \rightarrow u\tilde{\omega}$ decay mode occurs at the $\ge 20\%$ level.

In $p\overline{p}$ collisions dilepton events would result from $\tilde{\omega}^{\pm}$ through the following subprocesses:

$$q\bar{q} \to \tilde{\omega}^+ \tilde{\omega}^-,$$
 (4a)

$$gg, q\bar{q}' \to \tilde{q}\bar{\tilde{q}}',$$
 (4b)

$$qg \rightarrow \tilde{q}\tilde{g},$$
 (4c)

$$gg, q\bar{q} \to \tilde{g}\tilde{g},$$
 (4d)

$$qq' \rightarrow \tilde{q}\tilde{q}',$$
 (4e)

$$a\overline{a}' \to \tilde{\omega}\tilde{g},$$
 (4f)

$$gq \to \tilde{\omega}\tilde{q}',$$
 (4g)

where q represents either a quark or antiquark and q' may differ from q. The strong decay

$$\tilde{g} \to \tilde{q}\bar{q}, \bar{\tilde{q}}q$$
 (5)

followed by $\tilde{q} \rightarrow q\tilde{\omega}$ leads to both $\tilde{\omega}^+ \tilde{\omega}^-$ and $\tilde{\omega}^\pm \tilde{\omega}^\pm$ final states in Eq. (4). We evaluated the $\tilde{\omega}$ -pair production cross sections in $p\bar{p}$ collisions at $\sqrt{s} = 630$ GeV, as in the work of Barger and co-workers,^{13,14} folding in the $\tilde{q} \rightarrow q\tilde{\omega}$ branching fractions of Fig. 1. Only the \tilde{q}_L contribute to $\tilde{\omega}\tilde{\omega}$ production; the appropriate statistical factors are taken into account. With masses \tilde{q} (40) and \tilde{g} (40+ ϵ), the cross sections obtained for $m_{\tilde{\omega}} = 25$ (35) GeV are given in Table I. The

TABLE I. $\tilde{\omega}$ -pair production cross sections at $\sqrt{s} = 630$ GeV for $m_{\tilde{\omega}} = 25$ (35) GeV.

	$\sigma(\tilde{\omega}^+\tilde{\omega}^-)$ (nb)	$\sigma(\tilde{\omega}^+\tilde{\omega}^+) + \sigma(\tilde{\omega}^-\tilde{\omega}^-)$ (nb)
(a)	0.14 (0.13)	0
(b)	0.18 (0.03)	0.05 (0.006)
(c)	0.18 (0.03)	0.18 (0.03)
(d)	0.07 (0.01)	0.07 (0.01)
(e)	0.02 (0.002)	0.02 (0.003)
(f)	0.01 (0.004)	0.01 (0.004)
(g)	0.01 (0.001)	0
Total	0.55 (0.20)	0.33 (0.05)

 $\tilde{\omega}^+ \tilde{\omega}^-$ give $l^+ l^- \bar{p}_T$ events¹¹ and $\tilde{\omega}^+ \tilde{\omega}^+$ give $l^+ l^+ \bar{p}_T$ events. The above \tilde{q} and \tilde{g} masses give an estimated cross section for monojets with missing $p_T > 40$ GeV of order 200 pb, which would be reduced by detection efficiency factors; should the monojet signal prove to be smaller than this, the \tilde{q} and \tilde{g} masses would have to be raised and our $\tilde{\omega}\tilde{\omega}$ signals reduced accordingly.

Provided that the \tilde{g} and \tilde{q} are approximately degenerate in mass, the \tilde{q} and $\overline{\tilde{q}}$ from Eq. (5) will have approximately the \tilde{g} momentum, and the \overline{q} or q will be soft. To the extent that $\tilde{\omega}$ is close in mass to \tilde{q} , the qfrom $\tilde{q} \rightarrow q \tilde{\omega}$ decay will also have low p_T . Hence, all mechanisms above have the potential to lead to "quiet" dileptons, with little associated hadronic activity [the subprocess (a) of Eq. (4) always gives quiet dileptons]. This is a feature of many of the dimuon events reported by Arnison *et al.*¹⁵

The \tilde{g} decay in Eq. (5) is flavor blind, and so $\tilde{u}\bar{u}$, $d\bar{d}$, $\tilde{s}\,\bar{s}$, and $\tilde{c}\,\bar{c}$ final states are about equally probable. Since the decay $c \rightarrow s$ also leads to strange quarks, the final state of subprocess (c) is likely to contain strange particles. In this connection it is interesting to note that UA1 finds¹⁵ one $\mu^+\mu^+\Lambda$ event and one $\mu^-\mu^-\bar{\Lambda}$ event with little hadronic p_T .

Next we consider the kinematics of dimuon events resulting from $\tilde{\omega}$ pair production and decay. All of the subprocesses in Eq. (4) give comparable momenta to the $\tilde{\omega}$, so we specialize to subprocess (c) which gives the largest same-sign dilepton rate. The major difference in the various sources is the amount of hadronic activity accompanying the dimuons, which will be small in the case that \tilde{g} and $\tilde{\omega}$ are close to \tilde{q} in mass. We here take masses $\tilde{q}(40)$, $\tilde{g}(40+\epsilon)$, $\tilde{l}(20)$, and $\tilde{\gamma}(6)$ with the two choices $\tilde{\omega}(25)$ and $\tilde{\omega}(35)$. We impose transverse-momentum and rapidity acceptance cuts on the muons used by the UA1 collaboration¹⁵:

$$|p_{T1}|, |p_{T2}| > 3 \text{ GeV}, \quad |p_{T1}| + |p_{T2}| > 10 \text{ GeV},$$

(6)
 $|\eta_1| < 1.2, \quad |\eta_2| < 1.8.$

Predicted distributions are shown in Fig. 2 for the dimuon invariant mass $m(\mu\mu)$, the cluster transverse mass¹⁶ $M_T(\mu\mu,\bar{p}_T)$, the azimuthal difference $\Delta\phi(\mu\mu)$ between the muons in the transverse plane, and the transverse momenta of the individual muons $p_T(\mu)$, the dimuon pair $p_T(\mu\mu)$, and the hardest jet $p_T(j_1)$ defined with use of the UA1 jet algorithm for overlapping jets. The \bar{p}_T distribution is about the same as the $p_T(\mu\mu)$ distribution. In the calculations all transverse momenta are corrected, event by event, to include effects of multiple gluon emission by the incident partons, as in the work of Barger *et al.*¹⁷ The \bar{p}_T and $M_T(\mu\mu,\bar{p}_T)$ results include Gaussian experimental errors in \bar{p}_T with root mean square error of 4 GeV, as in Barger *et al.*¹⁸

We note that the $\tilde{\omega}(25)$ and $\tilde{\omega}(35)$ cases are qualita-



FIG. 2. Predicted distributions in dimuon events resulting from $\tilde{q}\tilde{g}$ production and the decays $\tilde{g} \rightarrow \tilde{q}\bar{q}$, $\tilde{q} \rightarrow \tilde{\omega}q$, $\omega \rightarrow \tilde{\mu}\nu(\mu\tilde{\nu})$, and $\tilde{\mu} \rightarrow \mu\tilde{\gamma}$, with $m_{\tilde{g}} \approx m_{\tilde{q}} = 40$ GeV, and $m_{\tilde{\omega}} = 35$ GeV (solid curves), 25 GeV (dashed curves). These calculations for $p\bar{p}$ collisions at $\sqrt{s} = 630$ GeV include the acceptance cuts of Eq. (5). The vertical arrows denote data values of the UA1 $\mu^+\mu^+\Lambda$ and $\mu^-\mu^-\Lambda$ events (Ref. 15). The predicted \bar{p}_T distribution is about the same as that for $p_T(\mu\mu)$.

tively similar in all distributions but $M_T(\mu\mu, \bar{p}_T)$ and $p_T(j_1)$. The heavier- $\tilde{\omega}$ case has much softer accompanying jets. The hardest jet has $p_T < 10$ GeV in more than 90% of events for $\tilde{\omega}(35)$ and in less than 20% of events for $\tilde{\omega}(25)$.

The characteristics of the distributions in Fig. 2 can be used in the search for $\tilde{\omega}$ pair production, once sufficient statistics have accumulated. By requirement of muon isolation, the heavy-quark backgrounds from $c\overline{c}$, $b\overline{b}$, and $t\overline{b}$ production¹⁹ can be suppressed relative to the $\tilde{\omega}\tilde{\omega}$ signal; this is especially the case for like-sign dimuons where these backgrounds are much smaller in the absence of large $B^0-\overline{B}^0$ mixing.

The decays of Z bosons are a potential source of unlike-sign dileptons^{11, 20, 21}:

$$Z \to \tilde{\mu}\bar{\tilde{\mu}} \to \mu^+ \mu^- \tilde{\gamma}\tilde{\gamma}, \tag{7a}$$

$$Z \to \tilde{\omega}^+ \tilde{\omega}^- \to \mu^+ \mu^- \nu \bar{\nu} \tilde{\gamma} \tilde{\gamma}. \tag{7b}$$

Here we omit the phase-space-suppressed $Z \rightarrow \tilde{q}\tilde{\tilde{q}}$ contribution. The rate for (7a) is determined by the s-particle masses, whereas the rate for (7b), which is a component of subprocess (a) in Eq. (4), depends also²⁰ on the mixing angle β . For six mass-degenerate scalar lepton (s-lepton) flavors at 20 GeV, and six degenerate s-quark flavors at 40 GeV, the predicted branching fractions are

$$B(Z \to \tilde{\mu}\tilde{\bar{\mu}}) \simeq 0.01,$$

$$B(Z \to \tilde{\omega}^+ \tilde{\omega}^+) \simeq 0.10$$
(8)

for $m_{\tilde{\omega}} = 25-35$ GeV and mixing angle $\beta = \pi/4$. The corresponding total width from Z decay to s-particles is $\Delta\Gamma \simeq 0.8$ GeV. The distributions from this $\tilde{\omega}$ -pair source are fairly similar to those in Fig. 2.

We conclude with some remarks on the possible relevance to UA1 dimuon observations:

(i) UA1 finds four like-sign and seventeen unlikesign dimuons¹⁵ with the acceptance cuts of Eq. (6). Some of these events can be identified with conventional physics sources such as Drell-Yan, ψ , and Y (which give $\mu^+\mu^-$ events with muons isolated from hadrons), and *bb*, $c\bar{c}$ (which give nonisolated muons). However, in addition there are like-sign events with both muons isolated and little hadronic activity (as well as unlike-sign events with isolated muons and jets) that may represent new physics; in the $\mu^+\mu^+\Lambda$ event, $m(\mu\mu) \approx 22$ GeV, and in the $\mu^-\mu^-\Lambda$ event $m(\mu\mu) \approx 14$ GeV. One e^+e^- candidate event with $m(ee) \approx 22$ GeV has also been reported.¹⁵

(ii) The 40-GeV s-quark supersymmetry scenario proposed to explain the UA1 monojets has the poten-

tial to give such isolated dileptons, both like-sign and unlike-sign. The dominant production subprocesses are $\tilde{\omega}^+ \tilde{\omega}^-$, $\tilde{q}\bar{\tilde{q}}'$, and $\tilde{q}\tilde{g}$ production with the decay chain $\tilde{g} \rightarrow \tilde{q}\bar{q} \ (q\bar{\tilde{q}}), \tilde{q} \rightarrow \tilde{\omega}q, \tilde{\omega} \rightarrow \tilde{\mu}\nu \ (\mu\tilde{\nu}), \tilde{\mu} \rightarrow \mu\tilde{\gamma}$. An $\tilde{\omega}$ mass between that of the s-quarks and s-leptons is necessary. Depending on the masses, and the contributing subprocesses, dilepton events with and without jets are possible. Figure 2 compares the model with the quiet UA1 same-sign dimuon events¹⁵; the situation that both events lie close together in $p_T(\mu\mu)$ and $\phi(\mu\mu)$ is admittedly somewhat unlikely in our model; future data with higher statistics will clarify its relevance.

(iii) The expected dimuon cross sections from $\tilde{\omega}$ pair production are obtained by multiplication of the $\sigma(\tilde{\omega}\tilde{\omega})$ values in Table I by $[B(\tilde{\omega} \rightarrow \mu \bar{p}_T)]^2 = \frac{1}{9}$ and the dimuon acceptance, which is about 0.5 for $\tilde{\omega}(25)$ and 0.7 for $\tilde{\omega}(35)$. The results obtained for $m_{\tilde{\omega}}$ = 25 (35) GeV are as follows:

 $\frac{\text{Source } \sigma(\mu^+\mu^-) \text{ (nb) } \sigma(\mu^+\mu^+) + \sigma(\mu^-\mu^-) \text{ (nb)}}{Z^0 \qquad 0.01 \ (0.01) \qquad 0}$ Hadronic 0.03 (0.004) 0.03 (0.003)

For an integrated luminosity of 400 nb⁻¹, expected by the end of the current CERN collider run, a number of dimuon events of $\tilde{\omega}$ -pair origin are possible.

(iv) The vertical arrows on the horizontal axis in Fig. 2 represent the data values for the UA1 $\mu^+\mu^+\Lambda$ and $\mu^-\mu^-\overline{\Lambda}$ events. The data values occur at probable regions for all distributions except $p_T(\mu\mu)$.

(v) It is natural to often find strange particles with dileptons of this origin due to the flavor-blind $\tilde{g} \rightarrow \tilde{q}\bar{q}$ decay.

(vi) If $\tilde{\omega}$ -pair production is a significant dilepton source, there must also exist similar μe events. The acceptance for electrons is more restrictive than that for muons so that $N(ee) < \frac{1}{2}N(\mu e) < N(\mu\mu)$. For $p_T(e) > 10$ GeV and muon acceptance given by Eq. (5), we estimate the event proportions $N(ee):N(\mu e)$ $:N(\mu\mu) \approx 1:8:8$ for $\tilde{\omega}(25)$ and 1:3:3 for $\tilde{\omega}(35)$.

(vii) Cross-section predictions are sensitive to the \tilde{q} and \tilde{g} masses, and those given here are illustrative rather than definitive. With $m(\tilde{q}) \approx 40$ GeV and $m(\tilde{g}) \approx 50$ GeV, the predicted rate for high- \bar{p}_T monojet and dijet events is somewhat large compared to present experimental indications (assuming a high detection efficiency). It may eventually be appropriate to increase the \tilde{q} and \tilde{g} masses, with consequent reduction in the supersymmetric dilepton rates.

We thank G. Bauer, D. Cline, and C. Rubbia for discussion of the UA1 data on dileptons and W. F. Long for assistance.

This research was supported in part by the University of Wisconsin Research Committee with funds granted by the Wisconsin Alumni Research Foundation, and in part by the U. S. Department of Energy under Contracts No. DE-AC02-76ER00881 and No. DE-FG02-87ER40173.

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