Evidence from α Decay That Z = 82 Is Not Magic for Light Pb Isotopes

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To resolve the reported anomalous behavior of the α -decay rates of ^{186,188,190,192}Pb we determined more accurate α -decay branches for these isotopes. Our data result in α -decay reduced widths whose dependence on N is similar to that observed for other elements. However, contrary to the expectation of a shell effect at Z = 82, this new information indicates lead nuclei to be less hindered toward α decay than mercury isotopes. It appears that midway between N = 82 and N = 126 the proton number of 82 is not magic.

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Alpha-decay transitions between ground states of doubly even nuclei are taken to represent unhindered decays. Reduced widths for these *s*-wave transitions behave in a regular fashion as a function of both neutron and atomic number. They are largest for nuclei two or four particles beyond a closed shell (with sharp minima at the shell) and they then decrease as the next closure is approached. The *s*-wave widths for ^{186, 188, 190, 192}Pb, however, have been reported¹ to behave anomalously, i.e., they purportedly increase by a factor of 30 between ¹⁸⁶Pb (N = 104) and ¹⁹²Pb (N = 110) instead of decreasing as one nears N = 126. Theoretical calculations^{2, 3} have not reproduced this unusual behavior.

In Ref. 1, the [electron-capture $(EC) + \beta^+$] strengths were deduced from K x-ray intensities. A number of corrections are involved in such determinations. A more precise method entails the use of a known $(EC + \beta^+)$ decay scheme. To obtain more reliable α -branching ratios we undertook the investigation of the $(EC + \beta^+)$ decay schemes of these neutron-deficient lead isotopes in conjunction with studies of their α -decay properties. Results for ¹⁹²Pb, ¹⁹⁰Pb, and ¹⁸⁸Pb have been published in Toth *et al.*,⁴ Ellis-Akovali *et al.*,⁵ and Toth *et al.*,⁶ respectively. Herein we present new information on ¹⁸⁶Pb and discuss the partial α half-lives for all four isotopes within the overall framework of α -decay rates for even-even nuclei with $Z \ge 78$.

While ^{188, 190, 192}Pb had been produced in ¹⁶O +¹⁸⁰W bombardments at the Oak Ridge isochronous cyclotron, the machine parameters are such that the intense ${}^{16}O^{5+}$ beam could not be accelerated to a sufficiently high energy to induce the reaction $^{180}W(^{16}O, 10n)$. The recent availability of energetic heavier ions from the Holifield Heavy Ion Research Facility allowed us to produce ¹⁸⁶Pb in the reaction 160 Dy(35 S, 6n) by bombarding a 2.92mg/cm²-thick dysprosium metal foil enriched in 160 Dy to 78.9% with 200-MeV 32 S ions. As in the earlier studies,⁴⁻⁶ reaction products were mass separated with the UNISOR (University Isotope Separator at Oak Ridge) on-line facility, collected onto an automated tape system, and transported to a counting station. Singles and coincidence γ -ray data were accumulated simultaneously with a largevolume Ge(Li) detector and a γ -x detector. A Si(Au) surface-barrier detector was used for α particle counting. All three detectors were placed in calibrated geometries so that absolute counting rates could be determined. Production and collection cycles were 20 s in duration while the counting time was broken up into four 5-s intervals.

The α spectrum, shown in Fig. 1(a), is dominated by the single group known^{7,8} to belong to ¹⁸⁶Pb α decay. The energy of this peak was determined to



FIG. 1. (a) Singles α -particle spectrum and (b) total coincidence x-ray spectrum, measured at A = 186.

be 6335 ± 10 keV; previously measured energies are 6320 ± 20 (Ref. 7) and 6332 ± 10 keV (Ref. 8). The α group decayed with a half-life of 4.7 ± 0.1 s in agreement with the value of 4.79 ± 0.05 s reported by Schrewe *et al.*⁸ but in disagreement with the value 8 ± 2 s published by Le Beyec *et al.*⁷ The two less intense peaks in Fig. 1(a) belong to the ¹⁸⁶Pb α -decay daughter, ¹⁸²Hg (see e.g., Hansen *et al.*⁹), and to ¹⁸⁶Tl (see Ijaz *et al.*¹⁰).

Gamma-ray spectra clearly showed the presence of ¹⁸¹Tl and ¹⁸⁶Hg (Béraud et al.¹¹ and Cole et al.¹²) produced in reactions involving charged-particle plus neutron evaporation, but no transition that could be assigned to ¹⁸⁶Pb on the basis of either half-like or K-x-ray coincidences. There was no indication of a short-lived component, consistent with a 4.7-s half-life, in the decay curve of the annihilation radiation peak. Thallium K x rays were also not observed. Here the situation was somewhat blurred by the presence of lead x rays due to fluorescence. The lead $K\alpha_2$ peak has an energy just 0.07 keV below that of the thallium $K\alpha_1$ x-ray group. (The thallium $K\alpha_2$ peak was masked by the much more intense mercury $K\alpha_1$ x rays.) However, the intensity of the lead $K\alpha_1$ x rays summed over the 20-s counting period, when corrected by the theoretical $K\alpha_1/K\alpha_2$ ratio, accounted for all of the events seen in the peak at 72.80 keV with no indication of thallium $K\alpha_1$ x rays. A small excess of 1624

counts in this peak was observed during the first 5-s counting interval, but it was adequately accounted for by the K-shell electron conversion of the E3374.0-keV transition associated^{11,12} with the 3.0-s ¹⁸⁶Tl isomer. Figure 1(b) illustrates the absence of thallium K x rays. It shows the total coincidence spectrum, in the neighborhood of the K-x-ray energy region, accumulated in the γ -x detector. While gold and mercury K x rays are seen in Fig. 1(b), there are no thallium x rays from either ¹⁸⁶Pb $(EC + \beta^+)$ or ¹⁸⁶Tl isomeric decay. [No transitions have been observed (Refs. 11 and 12 and present study) in coincidence with the ¹⁸⁶Tl E3 γ ray; if any exist their energies must be less than the thallium K-shell binding energy.] Finally, we note that the ¹⁸⁶Tl isomer apparently has a low spin.¹² One would therefore expect most of ¹⁸⁶Pb (EC + β^+) decay to proceed either directly or through intermediate states to this isomer. The decay curve for the 374.0-keV γ ray showed a single (3.0 ± 0.2) -s component with no hint of a parent-daughter, growth and decay, correlation, further indicating an absence of ¹⁸⁶Pb (EC + β^+) decay.

Our data therefore suggest a ¹⁸⁶Pb α /total branching ratio of 100%, a value which is much larger than the 2.4% branch estimated⁷ from expected cross sections for the production of ¹⁸⁶Pb in heavy-ion reactions. On the basis of their measured ¹⁸⁶Pb and ¹⁸⁹Pb α branches Hörnshoj *et al.*,¹ in their discus-

	E_{α} (keV)	$T_{1/2}$ (min)	α branch	δ^2 (MeV)	
		-, -		·	
		Current data ^a			
¹⁹² Pb	5112(5)	3.5(1)	$5.7 \times 10^{-5}(10)$	0.049 ± 0.014	
¹⁹⁰ Pb	5577(5)	1.2(1)	$9.0 \times 10^{-3}(20)$	0.094 ± 0.036	
¹⁸⁸ Pb	5980(5)	22(2)	0.22(7)	0.114 + 0.055	
¹⁸⁶ Pb	6.335(10)	4.7(1)	1.0	0.09	
¹⁸⁴ Pb					
	Earlier data				
¹⁹² Pb	5110 ^b	2.3(5)°	$6.9 \times 10^{-5} (24)^{d}$	0.094	
¹⁹⁰ Pb	5580(10)°	$1.2(2)^{c}$	$2.1 \times 10^{-3} (7)^{d}$	0.021 + 0.017	
¹⁸⁸ Pb	5980(10)°	$24.5(15)^{f}$	$3.3 \times 10^{-2}(11)^{d}$	0.015 + 8.882	
¹⁸⁶ Pb	$6320(20)^{g}$	8(2) ^h	$4.8 \times 10^{-2} d$	0.0028	
¹⁸⁴ Ph	$6632(10)^{i}$	$0.55(6)^{i}$	1 0(estimate)	0.06	

TABLE I. Alpha-decay properties of lead isotopes.

^aData are from Refs. 4–6, and this study.

^bRef. 14; other value: 5060(30) (Ref. 7).

^cRef. 7.

^dRef. 1.

^eRef. 7; other values: 5975(15) (Ref. 15); 5990(15) (Ref. 8).

sion of α widths, increased the ¹⁸⁶Pb ratio by a factor of 2, i.e., to 4.8%. This augmented branch is still much less than our value.

In discussing α -decay rates we consider them within the theoretical formalism developed by Rasmussen¹³ wherein decay probabilities are represented by a reduced width, δ^2 . Decay energies, half-lives, and α branches are needed to compute the reduced widths. In Table I we compare these quantities for ^{186, 188, 190, 192}Pb as obtained in our current investigations with data from Refs. 1, 7, and 8, and from Siivola¹⁴ and Hornshøj *et al.*¹⁵ Large discrepancies exist, not only for the ¹⁸Pb branching ratio, but for the ¹⁸⁸Pb and ¹⁹⁰Pb α branches as well. As a result, the corresponding widths are increased by factors of 32, 7, and 4.5. Our width for ¹⁹²Pb, on the other hand, is less than the value based on the earlier data because the nuclide's half-life is 3.5 min, rather than 2.3 min as reported by Le Beyec et al.⁷ and used in Ref. 1. Even though the ¹⁸⁴Pb α branch has not been measured we have included in Table I its half-life and decay-energy data⁸ and calculated a reduced width by assuming a branching ratio of 100%.

Figure 2 shows s-wave reduced widths for nuclei with Z from 78 to 100 plotted as a function of N. Information used to calculate the reduced widths for isotopes with $A \ge 196$ is taken from Refs. 16 and 17. Data for lead, mercury, and platinum nuclei are taken from Table I; Refs. 8, 9, and 15; and Schneider *et al.*¹⁸ and Ellis, Toth, and Carter,¹⁹ ^fRef. 15; other value: 26(2) (Ref. 7).

^gRef. 7; other value: 6332(10) (Ref. 8). ^hRef. 7; other value: 4.79(5) (Ref. 8).

ⁱRef. 8.

respectively. One sees in Fig. 2 the regularity of the reduced widths as a function of neutron number with the extremely sharp break at N = 126. This discontinuity has been shown (see, e.g., $Mang^{20}$) to be a shell-structure effect. A less pronounced minimum is seen at the subshell closure at N = 152. The lead anomaly is indicated by the dashed line which connects the ^{186, 188, 190, 192}Pb widths calculated from the earlier data summarized in Table I. The widths for ^{186, 188, 190, 192}Pb computed from our data are shown by the open points. It is clear that they have a dependence on N which is similar to that observed for other elements. However, these new data indicate neutron-deficient lead isotopes to be less hindered toward α decay than mercury isotopes, contrary to the expectation of a shell effect at Z = 82.

Our results seem to be related to the disappearance of the Z = 82 gap in the vicinity of N = 114which has been predicted²¹ on the basis of Hartree-Fock-Bogoliubov calculations of proton singleparticle energies, and to the existence of varying shapes in mercury and platinum isotopes in this mass region. In ^{182, 184, 186, 188}Hg it has been shown²² that well-deformed prolate bands cross the slightly oblate ($\epsilon \sim 0.1$) ground-state bands. Platinum nuclei with A < 190, on the other hand, are believed²³ to be prolate in their ground states. If one supposes that ^{186, 188, 190, 192}Pb also have slightly oblate ground states then α transitions from oblate mercury to prolate platinum isotopes would be expected to be



FIG. 2. Reduced widths for s-wave α transitions plotted as a function of N for isotopes with Z from 78 to 100. The dashed line connects widths for ^{186, 188, 190, 192}Pb calculated from earlier data. Open points for Z = 82, connected by the full line, are widths for ^{186, 188, 190, 192}Pb calculated from our experimental results.

hindered whereas lead α decays, which do not involve shape changes between the parent and daughter nuclei, would not be. (Low-lying 0⁺ excited states in ^{192, 194, 196, 198}Pb have been described²⁴ by oblate two-particle, two-hole configurations; their ground states, however, have been assumed to be spherical.) Further detailed calculations of α -decay rates incorporating shape changes are needed. If such theoretical results do indeed agree with our experimental observations, then the study of α -decay rates may prove to be a useful tool to deduce information concerning nuclear shapes. Finally, we note that the ¹⁸⁴Pb reduced width (see Table I) is appreciably smaller than our widths for ¹⁸⁶Pb and ¹⁸⁸Pb which seems to indicate the reappearance of the Z = 82 gap for N < 102.

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