

**Ferrell and Bhattacharjee Respond:** We recently noted<sup>1</sup> the necessity of including the bulk viscosity in second-sound damping. This contribution is  $B_{\psi}' = (\rho_s/\rho_n)D_1$ , where  $D_1$  is the *background component* of the first-sound damping. The latter is taken to be proportional to  $\rho_n/\rho$ .  $\rho_{s,n}$  and  $\rho$  are the superfluid, normal fluid, and total fluid density, respectively. Ahlers and Hohenberg<sup>2</sup> "agree that the correction discussed by FB should appear below  $T_\lambda$ " but assert that "its size has been severely overestimated." They base this assertion on an incorrect interpretation of the experimental first-sound data of Chase,<sup>3</sup> exhibited in Fig. 1. The solid curve shows the theoretically expected first-sound damping, separated into its critical<sup>4</sup> and background components. At the  $\lambda$  point the background, shown by the dashed curve, is equal to  $2.0 \times 10^{-17}$  sec<sup>2</sup>/cm. This corresponds to the value  $D_1 = 5.0 \times 10^{-4}$  cm<sup>2</sup>/sec that we used in Ref. 1.

It is true that the experimental value for the total  $D_1$  does vary by a factor of 2.4 in the reduced-temperature interval  $0.01 \leq |t| \leq 0.03$ , in satisfactory accord with the theoretical curve. But the rise in the total  $D_1$  as  $|t|$  decreases from  $|t| = 0.03$  is almost entirely due to the onset of the critical first-sound damping. Ahlers and Hohenberg<sup>2</sup> mistakenly include the critical component of  $D_1$  and therefore should find a  $B_{\psi}'$  bigger than we found, and *not smaller*, as they assert. The critical part of  $D_1$  comes from the relaxation of the longitudinal component of the order parameter.<sup>4</sup> Its connection with  $D_2$  is rather more complicated than Ahlers and Hohenberg<sup>2</sup> seem to appreciate, because of the opposing transport of superfluid and normal fluid, as noted by Khalatnikov.<sup>5</sup> The relaxational contributory contribution to  $D_2$  cancels completely in the background region and sets in only weakly as the  $\lambda$  point is approached.<sup>6</sup>

Ahlers and Hohenberg<sup>2</sup> want to drop  $B_{\psi}$  from the damping. But  $B_{\psi}$  and  $B_{\psi}'$  are distinctly separate contributions and occur differently in the equations of motion. Dropping  $B_{\psi}$  would furthermore be inconsistent with the excellent agreement with experiment that we found for our theory<sup>7</sup> of the  $\lambda$ -point first-sound attenuation using  $B_{\psi} = 1.0 \times 10^{-4}$  cm<sup>2</sup>/sec. Being a massless Goldstone mode, the transverse component of the order parameter can be expected to be temperature independent below the  $\lambda$  point. We further note

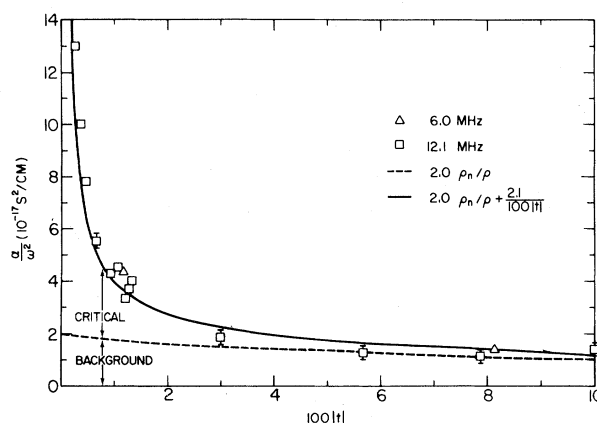


FIG. 1. Measurements by Chase (Ref. 3) of  $\alpha/\omega^2$  vs reduced temperature for two different frequencies  $\omega/2\pi$ .  $\alpha$  is the amplitude attenuation coefficient in nepers per centimeter. The theoretically expected  $\alpha/\omega^2$  (solid curve) is decomposed into its background component (dashed curve) and critical component (Ref. 4).

that their neglect of  $\rho^2\xi_3 - 2\rho\xi_1$ , which we do not neglect, is unjustified and leads to erroneous conclusions.

In conclusion, we believe that our calculation of the normal-fluid bulk-viscosity contribution to second-sound damping should stand as presented.<sup>1</sup>

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<sup>1</sup>R. A. Ferrell and J. K. Bhattacharjee, Phys. Rev. Lett. **51**, 487 (1983).

<sup>2</sup>G. Ahlers and P. C. Hohenberg, preceding Comment [Phys. Rev. Lett. **52**, 313 (1984)].

<sup>3</sup>C. E. Chase, Proc. Roy. Soc. London, Ser. A **220**, 116 (1953); see also erratum at bottom of p. 198 of Phys. Fluids **1**, 193 (1958).

<sup>4</sup>R. A. Ferrell and J. K. Bhattacharjee, Phys. Rev. B **23**, 2434 (1981).

<sup>5</sup>I. M. Khalatnikov, Zh. Eksp. Teor. Fiz. **57**, 489 (1969) [Sov. Phys. JETP **30**, 268 (1970)].

<sup>6</sup>R. A. Ferrell and J. K. Bhattacharjee, Phys. Rev. B **24**, 5071 (1981).

<sup>7</sup>R. A. Ferrell and J. K. Bhattacharjee, Phys. Rev. Lett. **44**, 403 (1980), and Phys. Rev. B **28**, 121 (1983), Fig. 9.