Majorana Neutrinos and the Production of the Right-Handed Charged Gauge Boson

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A possibility of a very clean signature for the production of W_R^{\pm} is pointed out. If the right-handed neutrino is lighter than W_R^{\pm} , left-right symmetric gauge theory predicts the decay $W_R^+ \rightarrow \mu^+ \mu^+ + 2$ hadronic jets, with the branching ratio $\simeq 3\%$. The lack of neutrinos in the final state and the absence of a sizable background make W_R^{\pm} rather easy to detect (if it exists). Detailed predictions regarding the production and decay rates of W_R^+ are presented.

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In recent years left-right symmetric models¹ have emerged as a popular extension (or alternative) of the standard electroweak theory. Parity nonconservation, being due to the spontaneous symmetry breaking, in these models becomes a low-energy phenomenon which ought to disappear at energies sufficiently above the mass M_R of the right-handed charged gauge boson W_R^+ . Although some possible indirect low-energy tests of this idea do exist, the only clear and unambiguous confirmation of left-right symmetry would be the production and identification of the right-handed gauge bosons. In this Letter we point out the possibly unusually clean signal for the production of the right-handed charged boson, which would also directly test the Majorana nature of the neutrinos. As we show below, a nontrivial fraction of W_{R}^{+} 's possibly decay into the final state consisting of two antimuons and two hadronic jets, without neutrinos so that there is no loss of energy whatsoever. Furthermore, such a process is almost free from any background and could therefore serve as a direct and clean test of W_{R}^{+} production.

The model.—In order to be more specific we briefly review the main features of the theory. The gauge group is $SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L}$, which requires the existence of the heavier gauge bosons $W_{R^{\pm}}$ and Z_{2} , besides the usual ones: $W_{L^{\pm}}$ and Z_1 . To the lowest order in $(M_L/M_R)^2$, one has the following relation, given here only for illustration, between the neutral and charged gauge boson masses²:

$$M_{\mathbf{z}_{1}}^{2} \simeq \frac{M_{L}^{2}}{\cos^{2}\theta_{W}}; \quad M_{L}^{2} = \frac{\pi\alpha}{G_{F}\sqrt{2}\sin^{2}\theta_{W}};$$

$$M_{\mathbf{z}_{2}}^{2} = 2 \frac{\cos^{2}\theta_{W}}{\cos^{2}\theta_{W}} M_{R}^{2}.$$
(1)

Clearly the properties of W_L^{\pm} and Z_1 are not dramatically changed compared with the standard

model; furthermore, relation (1) guarantees the right-handed charged gauge boson W_{R}^{\pm} to be substantially lighter than Z_2 . For example, for $\sin^2\theta_{\rm W} \simeq 0.25$, $M_R \simeq (1/\sqrt{3})M_{Z_2}$.

As shown by Mohapatra and one of us (G.S.), the smallness of the neutrino mass is related to the maximality of parity nonconservation in weak interactions. Namely, ν_R becomes a heavy Majorana neutral lepton N with $m_N \sim M_R$ and ν_L is the light Majorana neutrino ν with $m_{\nu} \sim 1/M_R$. As a result of negligible mixings between ν_L and ν_R and very small $W_L - W_R$ mixing (< 10⁻³), the righthanded gauge boson is coupled only to the heavy lepton N, and not to the neutrino. This is the crucial feature, responsible for our main result discussed below.

Although the scale of parity restoration, i.e., M_R , cannot be predicted by the theory, current experimental data allow M_R to be quite low,³⁻⁵ thus encouraging the direct search for W_R and Z_{2} . Let us now discuss the production and decay rates for these particles, with the emphasis on the more interesting case of W_R^+ .

Neutral gauge boson Z_2 .—The signature is not spectacular. Take $M_{Z_2} = 300 \text{ GeV}$, $\sin^2 \theta_W = 0.25$. The computation gives for the total decay width³

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$$\Gamma_{Z_2} \simeq 9 - 10 \text{ GeV}, \tag{2}$$

with the decay branching ratios

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$$B(Z_2 \rightarrow \nu\nu) \simeq 1\%, \quad B(Z_2 \rightarrow NN) \simeq 9\%,$$

$$B(Z_2 \rightarrow \mu^+\mu^-) \simeq 2\%, \quad B(Z_2 \rightarrow \bar{u}u) \simeq 7\%, \quad (3)$$

$$B(Z_2 \rightarrow \bar{d}d) \simeq 14\%.$$

where we assume $2m_N < M_{Z_2}$ and ignore the phasespace corrections. The cross section for the production of Z_2 in the pp collider is found to be³

$$B(Z_2 \to \mu^+ \mu^-) \sigma \simeq 3 \times 10^{-38} \text{ cm}^2$$
 (4)

at $\sqrt{s} = 800$ GeV. Thus, under optimal luminosity

of 10^{33} cm⁻² sec⁻¹ at the future Collider Beam Accelerator (CBA), it would imply a few events per day.

The right-handed charged gauge boson W_R^{\pm} .—Its decay patterns and signatures depend crucially on whether N is lighter than W_R^{\pm} or not.⁶ We make, what we believe, a reasonable assumption: $m_N < M_R$ (it is equivalent to a commonly used premise $m_t < m_W$ in the standard model).

In this case, ignoring the phase-space corrections, we obtain for three generations of fermions

$$B(W_R^+ \rightarrow N_\mu \mu^+) \simeq 8\%$$
.

We have also assumed that the charged and doubly charged Higgs bosons are not lighter than W_R ; relaxing this would change the branching fraction $B(W \rightarrow Nl)$ by at most 1%.

A few words are needed here regarding mass differences and mixings among different *N*'s. The combined limit on the product of mixings and mass differences comes from lepton flavor-changing processes, such as $\mu \rightarrow e\gamma$. Namely, one estimates²

$$\frac{\Gamma(\mu - e\gamma)}{\Gamma(\mu - e\nu\overline{\nu})} \simeq \frac{\alpha}{\pi} \left(\frac{M_L}{M_R}\right)^4 \left(\sin\theta_R \cos\theta_R \frac{m_{Ne}^2 - m_{N\mu}^2}{M_R^2}\right)^2, \quad (5)$$

where for simplicity we specify to two generations only; θ_R is the Cabibbo leptonic mixing angle in the right-handed sector. Taking $(M_L/M_R)^2 \gtrsim \frac{1}{10}$, as to make W_R accessible to direct production, we get

$$\sin(2\theta_R)\Delta m_N^2/M_R^2 \lesssim 10^{-5}, \qquad (6)$$

a rather stringent limit. It means that we can safely ignore intergenerational mixings in the production and decay of W_R^+ .

Now, N's being Majorana leptons they decay equally often into leptons or antileptons. There-fore⁷

$$B(N_{\mu} \rightarrow \mu^{+}X^{-}) = B(N_{\mu} \rightarrow \mu^{-}X^{+}) \simeq 50\%$$
 (7)

and so, with the branching ratio of about 4%, W_R^+ decays into

$$W_R^+ - \mu^+ \mu^+ \bar{q} q', \qquad (8)$$

where the quarks in the final state form hadronic jets $(\bar{q}q' = \bar{u}d \text{ or } \bar{c}s \text{ or } \bar{t}b)$. The above process would serve as a very clean signal for W_R^+ pro-



FIG. 1. Total $pp \rightarrow W_R^{\pm}$ cross sections vs M_R at $\sqrt{s} = 800$ GeV. $\sin^2 \theta_W$ is chosen to be 0.25.

duction and, simultaneously, would be a direct test of the Majorana character of neutrinos. As a result of the absence of neutrinos, there is no energy loss in the final state, and so it is possible to reconstruct the W_R invariant mass. Furthermore, it is almost free from the background (see below).

Assume for the moment $M_R = 200 \text{ GeV}$, expected approximately if $M_{Z_2} \simeq 300 \text{ GeV}$ or so; let us also take $m_{N\mu} \simeq 100 \text{ GeV}$. Then one μ^+ has the energy of 75 GeV, and the other three particles have approximately $E_i \simeq 42$ GeV, a perfectly clean signature of W_R^+ production. In the rest of this paper we quantify the above point by presenting the results of the detailed calculation of production rates of W_R^+ , transverse momentum distributions of the primary and secondary leptons, and invariant mass distribution of the final lepton pair. To be as complete as possible we vary the W_R^+ mass in the range of experimental interest: 150 GeV $\leq M_R \leq 300$ GeV; we keep $m_N = 100$ GeV and at the end display the dependence on m_N .

We calculate the W_R production in the simple Drell-Yan picture. The rates for the relevant subprocesses are

$$\hat{\sigma}(u\overline{d} - W^{\dagger}) = \frac{1}{3} \left(\pi^2 \alpha / \sin^2 \theta_W \right) \delta(\hat{s} - M_R^2), \qquad (9)$$

and

$$\frac{d\hat{\sigma}}{d\hat{t}} \left(u \vec{d} - \mu^+ N \right) \\ = \frac{1}{3} \frac{\alpha \pi^2}{4 \sin^4 \theta_W \hat{s}^2} \frac{\hat{t} \left(\hat{t} - m_N^2 \right)}{(\hat{s} - M_R^2)^2 + M_R^2 \Gamma^2}.$$
(10)



FIG. 2. Transverse momentum distributions of the primary and secondary leptons from W_R production for pp collision at $\sqrt{s} = 800$ GeV. The case $M_R = 200$ GeV, $m_N = 100$ GeV, and $\sin^2\theta_W = 0.25$ is illustrated.



FIG. 3. Invariant-mass distribution of the lepton pair from the W_R cascade decays for a pp colliding beam at $\sqrt{s} = 800$ GeV. The cases $m_N = 100$ GeV and 150 GeV with $M_R = 200$ GeV and $\sin^2\theta_W = 0.25$ are illustrated.

Here the width Γ is given by the sum of partial widths for decays into fermion pairs,

$$\Gamma(W_R - f_1 \bar{f}_2) = (\frac{1}{12} C \alpha \sin^2 \theta_W M_R) \lambda^{1/2} (M_R^2, m_1^2, m_2^2) \left[1 - \frac{1}{2} \frac{m_1^2 + m_2^2}{M_R^2} - \frac{1}{2} \frac{(m_1^2 - m_2^2)^2}{M_R^4} \right], \tag{11}$$

with C = 1 for leptons and C = 3 for quarks, and $\lambda(x, y, z) = x^2 + y^2 + z^2 - 2xy - 2xz - 2yz$. For the choice of $M_R = 200$ GeV, $m_N = 100$ GeV, and m_t =20 GeV, the total width is about 5.3 GeV and the branching fraction for $W_R \rightarrow Nl$ is slightly reduced by kinematics from 8% to 6%. In calculating the inclusive production rates, the subprocess cross section, $\hat{\sigma}$, in Eqs. (9) and (10) must be convoluted with the momentum distributions of the quarks in the initial hadrons. We use the parametrization of Owens and Reya⁸ for the parton distributions evaluated at the mass scale $Q^2 = \frac{1}{2}\hat{s}$. For the secondary decay $N \rightarrow l+2$ jets, the momentum distribution of the lepton l in the rest frame of N is simply given by $dn/dp \propto p^2(3m_N - 4p)$ for $p < \frac{1}{2}M_R$. Figure 1 shows the W_{R}^{\pm} production cross sections versus M_R for the pp collider at $\sqrt{s} = 800$ GeV. At an integrated luminosity 10³⁹ cm⁻² accumulated approximately over one year for the future CBA, $10^4 W_R$ events could be produced for $M_R \approx 200$ GeV. These then give hundreds of same-sign dilepton events per year as discussed above for a reasonable branching fraction $B(W \rightarrow Nl) \approx 6\%$. In Fig. 2, useful p_T distributions for both primary and secondary leptons are illustrated. High invariant mass for the lepton pair is also expected as shown in Fig. 3.

A few words are in order regarding the background for this process. Previous calculations⁹ indicate that in the case of opposite-sign dimuons, the background turns out to be at least an order of magnitude below the W_R^+ signal. In our case, the only conceivable background would be from the heavy-quark decays and so, if anything, it should be lower for same-sign dimuons. Furthermore, because of small generational mixing we do not expect a lepton flavor-changing final state, such as μ^+e^+ , which should be equally present in the background. Therefore, an additional nice feature of this process is the absence of the competing background.

In conclusion, a reasonable assumption, $m_N \leq M_R$, allows for the exciting possibility of a very clean signal for the production of W_R^{\pm} , which crucially depends on the Majorana character of both left-handed and right-handed neutrinos. This offers a simultaneous possibility of confirming the idea of parity restoration at soon achievable energies and of directly testing the Majorana nature of neutrinos.

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⁵Recently, G. Beall, M. Bander, and A. Soni, Phys. Rev. Lett. <u>48</u>, 848 (1982), have argued the existence of the lower bound on M_R : $M_R \gtrsim 1.6$ TeV from the K_L - K_S mass difference. Their result is, however, applicable only to the special class of left-right symmetric theories characterized by the same left and right Cabibbo rotations. Even then, this bound is a function of the top-quark and Higgs-boson masses and could be quite lower. See R. N. Mohapatra, G. Senjanović, and M. D. Tran, to be published.

⁶The production of W_R^{\pm} was discussed before in Ref. 3. The clean signature we are stressing here was, however, not emphasized.

⁷Here we assume a small mass difference between N_i 's as to suppress processes such as $N_{\mu} \rightarrow N_e e\mu^+$ and as suggested by Eq. (6).

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