

Observation of Quasibound States of the Neutron in Matter

K.-A. Steinhauser, A. Steyerl, and H. Scheckenhofer

Fakultät für Physik, Technische Universität München, D-8046 Garching, Germany

and

S. S. Malik

Fakultät für Physik, Technische Universität München, D-8046 Garching, Germany, and Physics Department, University of Rhode Island, Kingston, Rhode Island 02881

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Quasistationary states of ultracold neutrons have been observed in a double-hump potential barrier. This potential barrier was created by sandwiching a thin film of aluminum between two thin copper films. Measurements of reflection from and transmission through such composite films displayed clear resonances. The resonance positions and widths are in agreement with calculations.

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This paper reports unambiguous observations of the existence of quasistationary states of the neutron in matter. That the effective nuclear scattering potential could lead to such states was first pointed out by Kagan.¹ Seregin² subsequently proposed that an arrangement of thin films (with appropriate thickness and made of materials having different values of the effective nuclear potential) could constitute a double-hump potential barrier in which neutrons with energies $\sim 10^{-7}$ eV could form quasibound states. The quantum characteristics of states in such a potential region can be obtained by solving a one-dimensional Schrödinger equation involving only the neutron wave-vector component, k_z , perpendicular to the potential barrier. In semiclassical (WKB) approximation, the values of k_z for which such states are formed are given by

$$k_z \cong (\pi/d)(n + \frac{1}{2}), \quad (1)$$

where d is the width of the potential well enclosed by the two humps, and n is a positive integer including 0. Also,

$$k_z = [2m(E_n - V)]^{1/2}/\hbar, \quad (2)$$

where m denotes the neutron mass, E_n the kinetic energy corresponding to the neutron velocity component in z direction, and

$$V = 2\pi\hbar Nb/m, \quad (3)$$

the scattering potential at the bottom of the well. N and b , respectively, are the number density (in inverse cubic centimeters) and the coherent-scattering length of the medium.

In the experiment reported here, values of k_z could be varied with use of the "gravity diffractometer"^{3,4} for ultracold neutrons. As shown in

Fig. 1, the ultracold neutron beam produced by the neutron turbine facility⁵ at the Forschungsreaktor Munich (Garching) is guided (via neutron guides) to the entrance slit system of the gravity diffractometer. The diffractometer, in brief, consists of entrance and exit slit systems (slits of 2 cm width together with beam stops) and three neutron mirrors, two vertical and one horizontal. The entrance and exit slit height corresponds to the maxima of the neutron flight parabolae for the incoming and exiting beam. In these conditions the entrance slit is imaged on the exit slit. The vertical position of the horizontal mirror (measured from the slit height, or, more precisely, from the center of gravity of the maxima for the set of incident neutron trajectories capable of passing the system) measures the fall height, z , of the neutron. The value of k_z , then, is given by

$$k_z = (m/\hbar)(2gz)^{1/2}, \quad (4)$$

where g is the acceleration due to gravity.

In the normal operation of the gravity diffractometer, shown in Fig. 1, the center of the first vertical mirror, A , was fixed at fall heights between 50 and 60 cm. The height, z , of the horizontal mirror, B , was varied. In order to maintain the focusing condition, the horizontal position of the second vertical mirror, C , requires specific adjustment. The reflected intensity was measured using a BF_3 detector depleted in ^{10}B content and arranged 80 cm below the exit slit. Thus, the neutrons gain enough energy in the gravitational field to be able to penetrate the thin detector window (0.1 mm Al).

A measurement of beam intensity with horizontal mirror, B , as nickel-coated glass mirror of 10 cm $\times$ 20 cm yielded 45 counts per hour (about

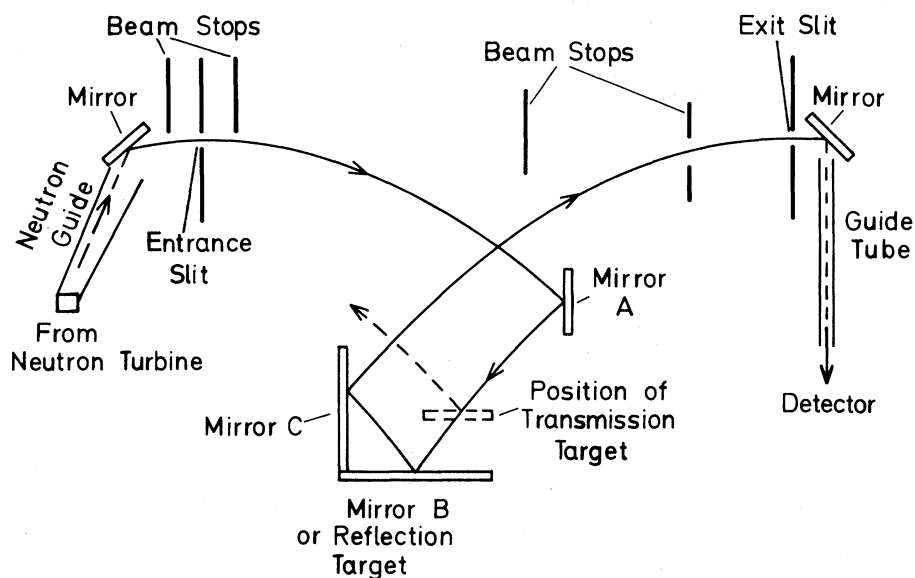


FIG. 1. Experimental arrangement showing the positions of the multilayered targets. For reflection measurements, the target acts as the horizontal mirror, *B*, of the mirror system of the gravity diffractometer. The entrance and exit slit (together with beam stops) define and analyze the ultracold neutron beam. A change in the fall height is achieved by a change in vertical target position.

one-half of the value measured previously^{3,4}) with a small negative slope (0.18 counts/h cm) at higher values of z . The dispersion in the value of k_z , convoluted with the analyzer (exit) slit resolution as determined by the slit width, was measured by varying the vertical exit slit position. The full width at half maximum (FWHM) of the resolution curve determined in this way was 3 cm, the same as in Refs. 3 and 4 and consistent with the value $\Delta k_z/k_z = \frac{1}{2}\Delta z/z \approx 1\%$ obtained by a Monte Carlo simulation of neutron passage through the instrument.⁴

The properties of the neutron beam reflected from a double-hump potential barrier were studied by replacing the mirror *B* by a target of the same size and consisting of thin films of aluminum and copper deposited on glass substrate. The double-hump potential well is created by sandwiching an Al film (nominal thickness 860 Å) between two Cu films of 240 Å each. These films were evaporated on the glass substrate one at a time, monitoring the thickness by the frequency of a quartz crystal. During the evaporation the substrate was continuously rotated in such a way as to limit variations of film thickness over the sample extension to <3%. The outer Cu layer was protected from oxidation by an additional 100-Å-thick Al film. The total thickness of the layers determined by an optical-interference microscope

was found to agree with the quartz-crystal data.

The intensity reflected from the target measured as a function of fall height is shown in Fig. 2. The data show a clear reflection minimum at $z = 108.5$ cm. The solid line in Fig. 2 represents the calculation of the reflected intensity obtained by solving the Schrödinger equation for the multi-step potential region due to the Al-Cu-Al-Cu-glass media, as depicted in the inset of Fig. 2. A thickness of 881 ± 2 Å was required for the width of the potential well between the two humps for $n=1$ (second level) for the position of the calculated minimum to coincide with the observed value at 108.5 cm, in reasonable agreement with the optical microscope and quartz-oscillator data of 860 Å. The fitted value 225 ± 5 Å for the Cu-film thickness is slightly less than the nominal value of 240 Å. The observed width (FWHM) of 7.5 cm (7.7 neV) corresponds to a lifetime of the state of the order of $\hbar/\Gamma = 2 \times 10^{-7}$ s. The depth of the minimum, should reach almost the background level of 12.4 ± 0.4 counts/h. There is only a slight enhancement due to the instrumental resolution of 2 neV. The observations, however, indicate a noticeable gap between the calculated minimum 13.8 ± 0.4 counts/h and the observed value 17.4 ± 0.7 counts/h. Possible reasons for this discrepancy are discussed later.

A second target with Cu-Al-Cu film thicknesses

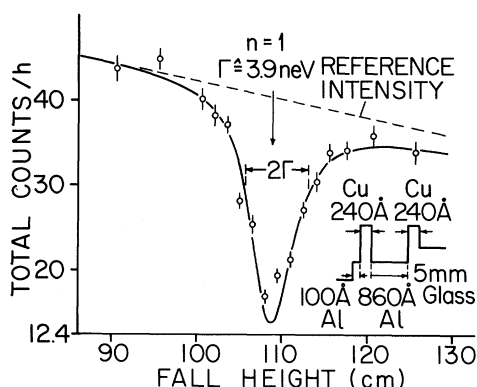


FIG. 2. Reflected intensity measured as a function of the fall height for a target with nominal layer thicknesses: Al (100 Å), Cu (240 Å), Al (860 Å), and Cu (240 Å). The substrate is glass. Potential functions representing these layers are shown in the inset. The intensity minimum at 108.5 cm corresponds to $n=1$ (the second stationary state). The solid curve is an exact solution of the one-dimensional Schrödinger equation for the multistep potential representing the target and includes the instrumental resolution broadening.

selected to allow observation of the third stationary state ($n=2$) showed similar reflection characteristics.

A transmission target was prepared by evaporation of Al (110 Å), Cu (180 Å), Al (1670 Å), Cu (180 Å), and Al (110 Å) on a substrate assembled from eight well-polished 5×5 -cm² silicon crystals of 0.25-mm thickness. Silicon was chosen because of its low absorption cross section and because it can be polished well down to sufficiently small thicknesses to achieve a transparency of $\sim 70\%$ in the wavelength range investigated. This target was installed 16 cm above mirror *B* (Fig. 1), thus enabling separation of the transmitted and reflected beams. The measured transmission data are shown in Fig. 3. The data show two resonances ($n=1$ and $n=2$). The line positions (74 and 99 cm) and widths (3.4 and 5.9 cm) are fairly well represented by the solid fitted curve for the following layer thicknesses: central Al layer, 1663 ± 3 Å; Cu barriers, 190 ± 5 Å. The step in the transmission curve at $z=85$ cm is due to different optimal settings of mirror *A* (Fig. 1), and consequently different incident beam intensities, at lower and higher fall heights. As in the reflection measurements, a discrepancy with expectation is observed in the resonance intensity, since the transmission maxima are lower than calculated.

The Breit-Wigner width for the n th quasista-

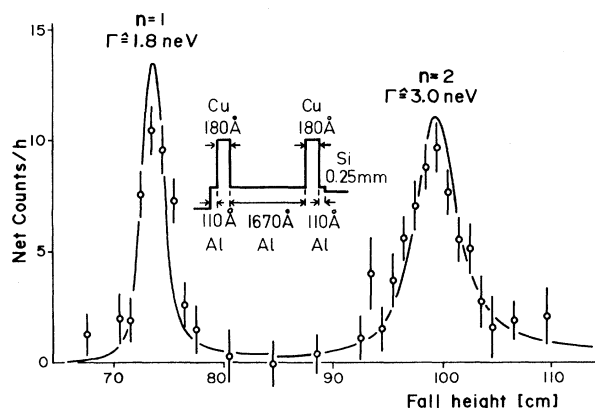


FIG. 3. Transmission data for a target with nominal layer thicknesses: Al (110 Å), Cu (180 Å), Al (1670 Å), Cu (180 Å), and Al (110 Å). The substrate is silicon of 0.25-mm thickness. The two resonances observed correspond to $n=1$ and $n=2$. The data are compared to the solid curve calculated for a multistep potential.

tionary state at $E=E_n$ depends upon the probability, P , of tunneling through a potential barrier. In quasiclassical (WKB) approximation,

$$P = \exp\{-2d_b[2m(V_b - E_n)]^{1/2}/\hbar\}, \quad (5)$$

where V_b and d_b are the height and width of the barrier, respectively. For identical barriers defining the double hump the resonance lines are of nearly Lorentzian shape with a FWHM of $2\Gamma^* = \hbar\omega P/\pi$, where $\hbar\omega \simeq E_{n+1} - E_n$.^{2,6} For instance, for the resonance of Fig. 2 the respective calculated WKB width is $2\Gamma^* = 2.2$ neV. The exact treatment yields the value $2\Gamma = 5.1$ neV (for the nominal Cu film thickness) which agrees better with the measured value 7.7 neV. The difference can be explained if Cu film thickness is reduced (225 Å instead of 240 Å). Similar deviations between exact calculation and measurement were observed for the other resonances investigated.

As noted earlier, the experimental resonance extrema for all the targets are lower than the corresponding calculated and resolution broadened values. A poorer resolution than the 2 neV employed in the calculations can explain the difference. However, exit-slit scans at the position of reflectivity minimum and at the wings yielded a resolution (FWHM) of ~ 3 cm in agreement with the instrumental resolution. Unequal transparencies of the two potential barriers ($P_A \neq P_B$) would lead to nonzero reflectivity minima (and transmission maxima < 1), but the data would require $\sim 20\%$ deviations between P_A and P_B which are unlikely to exist. Departures from the rectangular

potential shape (due to diffusion mixing at the Al-Cu boundaries) would result in changes of level position and width, but not in reduced resonance amplitudes. Thus, a slight blurring of the potential boundaries by $\sim 80 \text{ \AA}$ would eliminate the small mismatch (by 2%) of theoretical and experimental level spacings in Fig. 3. A variation in layer thickness of $\sim 3\%$ is, however, insufficient to account for the reduced resonance amplitudes. Microscopic density fluctuations of surface micro-roughness would give rise to disorder scattering and, consequently, coherent-beam attenuation, similar to "absorption" (including nuclear capture and thermal inelastic scattering). Calculation shows that an enhancement of "absorption" in pure Al by a factor of $\sim 10^2$ – 10^3 could explain the data, but such strong scattering is unlikely to exist.

The optical analog of the double-hump potential barrier is the well-known Fabry-Perot interferometer. Thus, the present results indicate that a neutron Fabry-Perot interferometer with a resolution of 10^{-9} eV is feasible.

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High-Energy Photoproduction of the D^{*+}

P. Avery, J. Wiss, J. Butler,^(a) G. Gladding, M. C. Goodman,^(b)
T. O'Halloran, J. J. Russell, and A. Wattenberg
University of Illinois, Urbana, Illinois 61801

and

M. Binkley, J. Cumalat, I. Gaines, M. Gormley, R. L. Loveless,^(c) and J. Peoples
Fermi National Accelerator Laboratory, Batavia, Illinois 60510

and

M. S. Atiya, and S. D. Holmes, B. C. Knapp, W. Lee, and W. J. Wisniewski
Columbia University, New York, New York 10027
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Photoproduction of the D^{*+} have been observed where the D^{*+} decays via $D^{*+} \rightarrow \pi^+ D^0$ and the D^0 decays via $K^+ \pi^-$ and $K_s^0 \pi^+ \pi^-$. The D^{*+} , D^0 mass difference and the D^0 mass observed here are in excellent agreement with previous measurements of charmed mesons produced in e^+e^- annihilations. The photoproduced D^{*+} and D^{*-} signals are produced nearly equally at the level of about 100 nb/nucleon.

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We report on the observation of the D^{*+} (D^{*-}) produced in the wideband neutral beam at Fermilab. Both this beam and our detector have been described in a previous Letter.¹ Our exposure consisted of approximately 6×10^{11} photons with an energy greater than 50 GeV incident on a 2-cm-long scintillator target. The particles emerg-

ing from these interactions were analyzed by a large-acceptance magnetic spectrometer system (multiwire proportional chambers) which includes two multicell Cherenkov counters with pion thresholds of 6 and 12 GeV, a large lead-glass array for neutral detection, and a hadron calorimeter. The data described here were recorded under a