

200 ps, i.e., approximately the same as the lifetime of the free  $\Lambda$  particle. In any event, the present experiment provides an upper limit of about  $20 \mu\text{b}$  for the  $0^\circ$  production cross section of other  $\gamma$ -emitting hypernuclear states in the ( $K^-$ ,  $\pi^-$ ) reaction at 1.7 GeV/c, and demonstrates conclusively that present technology is sufficient to measure such small cross sections in particle- $\gamma$  coincidence experiments with currently available kaon beams.

This work was supported by the U. S. Energy Research and Development Administration under Contracts No. EY-76-C-02-0016 and No. EY-76-S-02-2894.

<sup>(a)</sup>Present address: Physics Department, University of Notre Dame, Notre Dame, Ind. 46556.

<sup>(b)</sup>Present address: Lawrence Livermore Laboratory, Livermore, Calif. 94550.

<sup>1</sup>A. Bamberger *et al.*, Phys. Lett. **36B**, 412 (1971), and Nucl. Phys. **B60**, 1 (1973).

<sup>2</sup>M. Bedjidian *et al.*, Phys. Lett. **62B**, 467 (1976).

<sup>3</sup>H. Feshbach and A. K. Kerman, in *Preludes in Theoretical Physics*, edited by A. De-Shalit, H. Feshbach, and L. Van Hove (North-Holland, Amsterdam, 1966), p. 260.

<sup>4</sup>H. J. Lipkin, Phys. Rev. Lett. **14**, 18 (1965).

<sup>5</sup>C. Chasman, K. W. Jones, and R. A. Ristinen, Nucl. Instrum. Methods **37**, 1 (1965).

<sup>6</sup>C. L. Wang *et al.*, to be published.

<sup>7</sup>A. Gal, J. M. Soper, and R. H. Dalitz, Ann. Phys. (N.Y.) **72**, 445 (1972).

### Difference in Analyzing Powers for ( $p, t$ ) Reactions Due to a Phase Change of Interference between Direct and Indirect Processes in Two-Nucleon Transfer Reactions

K. Yagi, S. Kunori, Y. Aoki, Y. Higashi, J. Sanada, and Y. Tagishi

*Institute of Physics and Tandem Accelerator Center, The University of Tsukuba, Ibaraki 300-31, Japan*

(Received 14 September 1977)

A marked difference between analyzing powers for reactions  $^{128}\text{Te}(p, t)^{126}\text{Te}(2_1^+)$  and  $^{110}\text{Pd}(p, t)^{108}\text{Pd}(2_1^+)$  with polarized protons has been observed, while the ground-state transitions have shown similar analyzing powers. The difference is accounted for as a result of a phase change of the interference between direct and inelastic multistep processes in two-neutron pickup reactions. The origin of this phase change is elucidated on the basis of the microscope description of the collective quadrupole oscillation of nuclei.

The interference between a direct process and inelastic multistep processes (nucleon transfer followed by inelastic scattering and the inverse) in two-nucleon transfer reactions is quite sensitive to the nuclear structure involved. The neutron-number ( $N$ ) dependence of this type of interference in excitation of the first  $2^+$  ( $2_1^+$ ) states has been extensively studied for the nuclei of  $N \approx 82-50$  by using ( $p, t$ ) reactions on the isotopes of  $^{A+2}\text{Nd}(A+2=150-142)$ ,  $^{1,2} \text{Te}(A+2=130-122)$ ,  $^{3,4} \text{Sn}(118, 116)$ ,  $^{3,5} \text{Cd}(116-112)$ ,  $^{3,5}$  and  $\text{Pd}(110-104)$ .<sup>5,6</sup> In consequence, a phase change from constructive to destructive interference has been found in the Pd isotopes.<sup>6</sup> The phase change has been interpreted as a result of a sign change of the form factor of the direct transfer process in going from Te, Sn, and Cd to Pd isotopes on the basis of the BCS and quasiparticle-RPA (random-phase approximation) model.<sup>6,7</sup>

The experimental and theoretical results mentioned above are all due to the measurements of the differential cross sections of the ( $p, t$ ) reac-

tions leading to the ground states ( $0_g^+$ ) and the  $2_1^+$  states. Measurements of analyzing powers for ( $p_{\text{pol}}, t$ ) reactions leading to the same  $2_1^+$  states are expected to provide a sensitive probe to detect whether the nature of the interference is constructive or destructive. Such measurements are of fundamental importance in understanding the microscopic structure of vibrational characters<sup>5</sup> of nuclei as well as the reaction dynamics of the processes.

Analyzing powers for the reactions  $^{128}\text{Te}(p_{\text{pol}}, t)^{126}\text{Te}(0_g^+ \text{ and } 2_1^+)$  and  $^{110}\text{Pd}(p_{\text{pol}}, t)^{108}\text{Pd}(0_g^+ \text{ and } 2_1^+)$  were measured at  $E_p = 22.0$  MeV. The nuclei  $^{128}\text{Te}$  and  $^{110}\text{Pd}$  were chosen as targets because the previous measurements of the differential cross sections showed that the  $^{128}\text{Te}(p, t)^{126}\text{Te}(2_1^+)$  transition<sup>3,4</sup> had constructive interference while  $^{110}\text{Pd}(p, t)^{108}\text{Pd}(2_1^+)$ <sup>6</sup> had destructive. A polarized proton beam was produced with a Lamb-shift ion source<sup>8</sup> and was accelerated with the University of Tsukuba 12UD Pelletron. The beam intensity was about 50 nA on target and

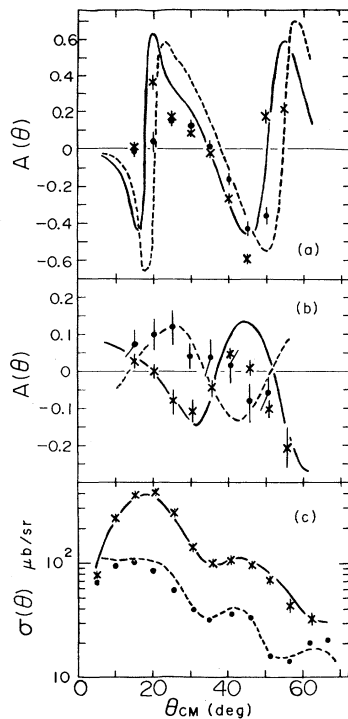


FIG. 1. Experimental and calculated analyzing powers  $A(\theta)$  and cross sections  $\sigma(\theta)$  for reactions  $^{128}\text{Te}(p, t)$ ,  $^{126}\text{Te}(p, t)$  and  $^{110}\text{Pd}(p, t)$  at  $E_p = 22.0$  MeV. The  $0_g^+$  transitions are in (a) and the  $2_1^+$  transitions in (b) and (c). The crosses [circles] are for  $^{128}\text{Te}(p, t)$  [ $^{110}\text{Pd}(p, t)$ ] transitions. The solid [dashed] curves are CCBA calculations of  $A(\theta)$  and  $\sigma(\theta)$  for the  $^{128}\text{Te}(p, t)$  [ $^{110}\text{Pd}(p, t)$ ] transitions.

the degree of polarization of the proton beam was  $(85 \pm 2)\%$ . The  $^{128}\text{Te}$  and  $^{110}\text{Pd}$  targets were enriched metallic films of  $0.5 \text{ mg/cm}^2$  thickness. The emitted tritons were analyzed with a magnetic spectrograph and detected with a silicon position-sensitive detector mounted in the focal plane. The energy resolution was 40 keV with an angular spread of  $\Delta\theta = \pm 1.5^\circ$ .

Angular distributions of the analyzing powers  $A(\theta)$  are shown in Figs. 1(a) and 1(b). The most striking features of the  $A(\theta)$  observed are the following: (i) A pronounced difference exists between the  $A(\theta)$  for  $^{128}\text{Te}(p_{\text{pol}}, t)^{126}(2_1^+)$  and  $^{110}\text{Pd}(p_{\text{pol}}, t)^{108}(2_1^+)$  transitions, viz., the sign of the analyzing power is almost opposite in the two cases [Fig. 1(b)]; (ii) on the other hand, the  $A(\theta)$  for the  $^{128}\text{Te}(p_{\text{pol}}, t)^{126}(0_g^+)$  transition is quite similar to that for the  $^{110}\text{Pd}(p_{\text{pol}}, t)^{108}(0_g^+)$  transition [Fig. 1(a)].

The  $(p_{\text{pol}}, t)$  transitions to the  $0_g^+$  and  $2_1^+$  states are analyzed in terms of coupled-channel Born-approximation (CCBA) calculations.<sup>9</sup> Under the

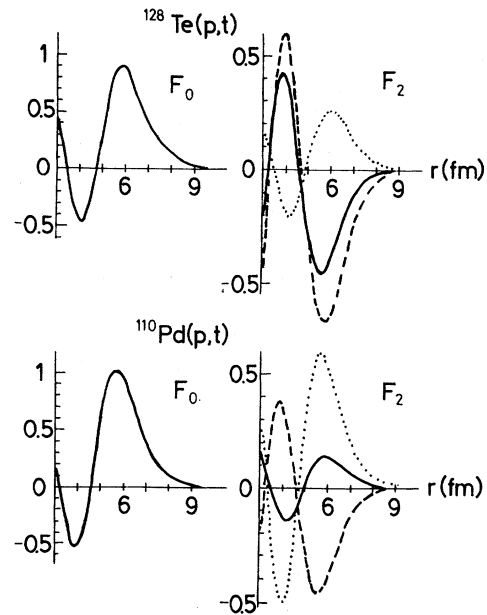


FIG. 2. Radial dependence of transfer form factors  $F_0(0_g^+ \rightarrow 0_g^+)$  and  $F_2(0_g^+ \rightarrow 2_1^+)$ . On the right side for the  $F_2$ , dashed and dotted curves show the contributions from the RPA forward- and backward-scattering amplitudes, respectively, and solid curves are sums of the two contributions.

BCS and quasiparticle-RPA model the nuclear wave functions for the  $0_g^+$  and  $2_1^+$  states are constructed by using both the monopole pairing interaction and the  $Q$ - $Q$  interaction.<sup>10</sup> Details on the procedure are found in Refs. 4, 5, 7, and 11. Transfer form factors  $F_0(0_g^+ \rightarrow 0_g^+)$  and  $F_2(0_g^+ \rightarrow 2_1^+)$  together with the contributions to  $F_2(0_g^+ \rightarrow 2_1^+)$  from the RPA forward- and backward-scattering amplitudes are shown in Fig. 2. Form factors for transitions between the  $2_1^+$  states are assumed to be proportional to those of the ground-states transitions as in the cases of Refs. 4 and 6.

It should be noted that the radial form factor  $F_2(0_g^+ \rightarrow 2_1^+)$  at the nuclear surface ( $r \sim 6 \text{ fm}$ ) changes its sign in going from  $^{128}\text{Te}(p, t)$  to  $^{110}\text{Pd}(p, t)$ , while the other form factors  $F_0(0_g^+ \rightarrow 0_g^+)$  and  $F_L(2_1^+ \rightarrow 2_1^+)$  do not. The sign change is ascribed to an increase of the contribution from the backward-scattering amplitudes in the Pd isotopes (Fig. 2). This change can be traced to the sign change in the spectroscopic amplitude for the direct transfer process,<sup>12</sup>

$$B(jj'; 0_g^+(A+2) \rightarrow 2_1^+(A)) \\ = \sqrt{5}[-V_j V_{j'} x(jj') + U_j U_{j'} y(jj')],$$

where the  $x$ 's and  $y$ 's are the forward- and backward-scattering amplitudes in RPA, respective-

ly, and  $V_j(U_j)$  is the occupied (unoccupied) amplitude of the  $j$  orbit. The amplitude  $B$  is determined by the competition between the forward contributions  $VVx$  and the backward contributions  $UUy$ . The latter exceeds the former<sup>13</sup> in the case of the Pd isotopes because (i) the  $UU$  are larger than the  $VV$  near the beginning of the major shell  $N=50-82$ , and (ii) the  $y$ 's become considerably large because of an increase of ground-state correlations in the Pd isotopes; indeed deformation parameters  $\beta_2$  for the quadrupole oscillation of the Pd isotopes are as large as<sup>14</sup>  $\beta_2=0.25$ . The spectroscopic amplitude for the inelastic transition in the multistep processes is expressed as

$$B(jj'; 0_g^+ \rightarrow 2_1^+(A)) \\ \propto U_j V_j x(jj') + V_j U_j y(jj').$$

Therefore the inelastic form factor at the nuclear surface does not change its sign in going from Te to Pd isotopes.<sup>13</sup> Actual calculations for the analyzing power and cross section for the  $2_1^+$  state of <sup>108</sup>Pd are done by the use of the form factor  $F_2(0_g^+ \rightarrow 2_1^+)$  which has been determined<sup>6</sup> by fitting the experimental  $2_1^+$  cross section for 52-MeV protons.<sup>15</sup>

Optical-potential parameters for protons are obtained from the work of Becchetti and Greenlees<sup>16</sup> and those for tritons are from Flynn *et al.*<sup>17</sup> Calculated analyzing powers are shown in Figs. 1(a) and 1(b). The essential features of the experimental analyzing powers described in (i) and (ii) (similarity between the two  $0_g^+$  transitions and difference between the two  $2_1^+$  transitions) are well reproduced by the calculations, although there is room for improvement in fitting the  $2_1^+$  analyzing powers.<sup>18</sup> In addition, the  $2_1^+$  cross sections [Fig. 1(c)] are also well reproduced by the CCBA calculations both in angular distributions and intensities.

In conclusion, analyzing powers for  $(p_{\text{pol}}, t)$  reactions are very powerful for detecting the interference mode (phase) between direct and inelastic multistep processes in two-nucleon transfer reactions. The difference between constructive and destructive interference appears distinctly as a difference in sign of the analyzing powers. The phase change of the interference is attributed to the neutron-number dependence of the occupation probability of single-particle orbits and that of ground-state correlations of the quadrupole oscil-

lation of nuclei. In this sense the  $(p_{\text{pol}}, t)$  analyzing power is a sensitive probe for detecting the microscopic characteristics of collective oscillations of nuclei.

<sup>1</sup>K. Yagi, K. Sato, Y. Aoki, T. Udagawa, and T. Tamura, Phys. Rev. Lett. **29**, 1334 (1972).

<sup>2</sup>T. Udagawa, T. Tamura, and T. Izumoto, Phys. Lett. **35B**, 129 (1971).

<sup>3</sup>K. Yagi, Y. Aoki, C. Rangacharyulu, M. Matoba, and M. Hyakutake, Phys. Lett. **44B**, 447 (1973).

<sup>4</sup>T. Izumoto, Y. Aoki, C. Rangacharyulu, K. Yagi, M. Matoba, and M. Hyakutake, Phys. Lett. **57B**, 17 (1974).

<sup>5</sup>K. Yagi, Y. Aoki, T. Izumoto, S. Kunori, and M. Sano, in Proceedings of the International Conference on Nuclear Structure, Contributed Papers, Tokyo, 1977 (to be published), pp. 532, 533, 534.

<sup>6</sup>K. Yagi, Y. Aoki, M. Matoba, and M. Hyakutake, Phys. Rev. C **15**, 1178 (1977).

<sup>7</sup>T. Izumoto, Prog. Theor. Phys. **52**, 1214 (1974).

<sup>8</sup>Y. Tagishi, and J. Sanada, in *Fourth International Symposium on Polarization Phenomena in Nuclear Reactions, Zürich, 1975: Proceedings*, edited by W. Gruebler and V. König (Birkhauser Verlag, Basel, 1976), p. 860.

<sup>9</sup>M. Toyama and M. Igarashi, computer code TWOSTP; P. D. Kunz, computer code CHUCK (private communication).

<sup>10</sup>The  $Q-Q$  strength is chosen so as to reproduce the excitation energy of the  $2_1^+$  states.

<sup>11</sup>T. Udagawa, Phys. Rev. C **9**, 270 (1974).

<sup>12</sup>S. Yoshida, Nucl. Phys. **33**, 685 (1962).

<sup>13</sup>It can be proved that the  $x$ 's have the same sign as the  $y$ 's in the case of the collective lowest  $2^+$  ( $2_1^+$ ) state under the pairing plus  $Q-Q$  interactions; see, for example, S. Yoshida, Nucl. Phys. **38**, 380 (1962). In addition,  $V$  and  $U$  are defined as positive.

<sup>14</sup>P. H. Stelson and L. Grodzin, Nucl. Data, Sect. A **1**, 21 (1965).

<sup>15</sup>Because of large anharmonicity in the quadrupole oscillation of Pd isotopes, the RPA wave function is not very good for describing the  $2_1^+$  state. See Refs. 5 and 6 for details.

<sup>16</sup>F. D. Becchetti, Jr., and G. W. Greenlees, Phys. Rev. **182**, 1190 (1969).

<sup>17</sup>E. R. Flynn, D. D. Armstrong, J. G. Beery, and A. G. Blair, Phys. Rev. **182**, 1113 (1969).

<sup>18</sup>The inelastic multistep processes are expected to be the most important of the indirect processes because of the large inelastic-scattering cross sections in Pd and Te isotopes. However, the indirect effect due to sequential transfer processes should be evaluated in obtaining more accurate fitting.