Origin of Two-Electron, One-Photon K-X-Ray Transitions*

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Hartree-Fock energy and intensity calculations show that the two-electron, one-photon $K^2 - L^2 - x$ -ray transitions recently reported are due to $1s^{-2} \rightarrow 2s^{-1}2p^{-1}$ electric dipole transitions. The mechanism which we use to describe the $1s^{-2}$ \rightarrow $2s^{-1}2p^{-1}$ transition is based on a "shake-down" model.

Recently Wölfli ${et}$ ${al.}^1$ have reported evidenc of two-electron, one-photon $K^2 - L^2 - x - ray$ transitions in heavy-ion collisions. An observation of analogous $L^2 - M^3$ Auger electrons has been reported by Afrosimov $et al.²$ Nothing prevents, in principle, doubly ionized inner-shell hole states of an atom from decaying by radiative or radiationless transitions which result in the simultaneous filling of the two holes. Previous work' gives one-electron selection rules for such radiative transitions but estimates of the probability of such transitions in the case of a doubly ionized K shell have to our knowledge not been given. Dow and Franceschetti' briefly discuss the simultaneous filling of two L holes by two conduction-band electrons in simple metals. Re- α cently Nagel *et al.*⁵ have pointed out that the experimental $K^2 - L^2$ transition energies obtained by perimental K^2 – L^2 transition energies obtained by
Wölfli *et al*. are in disagreement with 1s^{–2} – 2p^{–2} energies obtained from experimental and Hartree-Fock hypersatellite and satellite transition energies.

The purpose of this Comment is to show that $1s^{-2}$ - $2s^{-1}2p^{-1}$ electric dipole x-ray transitions (defined as $K\alpha\alpha^h$, see Fig. 1) should be observable in heavy-ion collisions where an extensive production of double-K-hole states occurs. We compare our intensity estimates and our results of Hartree-Fock energy calculations with the observations of Wölfli $et al.¹$ and find reasonable agreement. The mechanism for the $1s^{-2}$ - $2s^{-1}2p^{-1}$ transition is described in terms of a "shakedown" model, similar to the model⁶ which is used to interpret shifts of autoionizing lines in electron-atom collisions near threshold.

It has been suggested that shake-off and configuration mixingin the final state are responsible for some $low\text{-}energy$ structures below the characteristic lines in x -ray spectra.⁷ The shakeoff occurs as a consequence of the change in the average potential acting on the electrons when the vacancy transfers from an inner to an outer shell. This change could also be responsible for a shake-

down of a second electron whenever there are two inner-shell holes available initially. The result would be high-energy structures considerably above the characteristic line in x-ray spectra. For the case of initial $1s^02s^22p^n$ states, electric dipole transitions to $1s^2 2s^2 p^{n-1}$ states would be possible, whereas transitions to final $1s^22s^22p^{n-2}$ states would be parity forbidden. In the following we shall consider the intensity, $I(K\alpha\alpha^h)$, of these transitions with respect to the intensity $I(K\alpha^h)$ of hypersatellite transitions between $1s^02s^22p^n$ and $1s2s2p^{n-1}$ states

It can be shown that the total hypersatellite xray transition rate is given by

$$
T(1s^{0}2s^{2}2p^{n} + 1s2s^{2}2p^{n-1})
$$

= $\frac{4}{6}\alpha^{3}\omega_{1}^{3}nD_{1}(1s2p)^{2}$ (1)

in the frozen-core approximation and in atomic

FIG. 1. Energy diagram showing the decay of doublyionized K-shell states by the K^2 -KL hypersatellite ($K\alpha^h$) transitions and by the competing K^2-L^2 two-electron, one-photon ($K\alpha\alpha^h$) x-ray transitions. The K-L characteristic $(K\alpha)$ x-ray transition is also shown to scale.

units. ω_1 is the average $K\alpha^h$ transition energy and $D_1(1s2p)$ is the $2p \rightarrow 1s$ electric dipole radial integral. The rate for $1s^02s^22p^n + 1s^22s^2p^{n-1}$ transitions is zero in the frozen-core approximation. However, if we take the relaxation of the electron cloud into account we get in the lowest order

$$
T(1s^02s^22p^n + 1s^22s2p^{n-1})
$$

$$
= \frac{4}{9} \alpha^3 \omega_2^3 n D_0 (1s2s)^2 D_1 (1s2p)^2, \qquad (2)
$$

since the 2s orbital of the $1s^{0}2s^{2}2b^{n}$ configuration is not orthogonal to the 1s orbital of the $1s^22s2p^{n-1}$ configuration. $D_0(1s2s)$ is the 1s2s monopole radial overlap integral and ω_2 is the average $K\alpha\alpha^h$ transition energy. Hence, we obtain the branching ratio

$$
I(K\alpha\alpha^{\prime\prime})/I(K\alpha^{\prime\prime})=(\omega_2/\omega_1)^3D_0(1s2s)^2,
$$
 (3)

which attributes the $K\alpha\alpha^h$ intensity to the shake down of the 2s electron into a 1s hole.

Figure 2 presents nonrelativistic Hartree-Fock Figure 2 presents nonrelativistic Hartree-Fock
(HF) energies⁸ for the $1s^{0}2s^{2}2p^{n} \rightarrow 1s^{2}2s2p^{n-1}$ electric dipole shake-down transitions as a function of the atomic number Z between Mg ($Z = 12$) and Ni $(Z = 28)$ for the case $n = 4$ and 6. The energies are given relative to twice the corresponding HF are given relative to twice the corresponding
energies for the 1s¹2s²2p" - 1s²2s²2p"^{- 1} transi tions. The energies of the parity-forbidden

Figure 3 displays the calculated relative shakedown rate as a function of Z using Eq. (3) for an initial configuration with $n = 4$. This relative rate is decreasing approximately as Z^{-2} , since The is decreasing approximately as Z , since $D_0(1s2s)^2 \approx 0.035Z^{-2}$ according to our HF calcula tions. The inverse of the most accurate experimental ratios with an error of 75% as reported by Wölfli *et al.*¹ are given for comparison

FIG. 2. Relative HF energies of one-photon K^2-L^2 x-ray transitions. Term-average HF energies are used in all the calculations except for the $(1s)^{-2}$ ${}^{1}S_0$ $(2s)$ ⁻¹(2p)⁻¹¹P₁ transition $(n=6, \text{ solid curve}).$ The notation in the figure refers to the subshells involved in the transitions. The measured values based on the data of Wölfli et al . (Ref. 1) for Ni-Fe, Ni-Ni, Fe-Fe, and Fe-Ni collisions are given for comparison.

FIG. 3. The branching ratio of K^2-L^2 ($K\alpha\alpha^h$) and K^2 -KL (K α ^h) transitions is given as a function of Z for an initial configuration with $n = 4$. The experimental data from Wölfli et al . (Ref. 1) are given for comparison.

(4)

In order to examine the validity of the shake-down model we relate the monopole interaction element $D_0(1s2s)$ to the change of the average HF potential in the shake-down transition. If the influence of the M orbitals on this potential difference is neglected, then the result is

$$
D_0(1s2s) = \frac{-R^0(2s1s1s1s) + R^0(2s2p1s2p) - \frac{1}{6}R^1(2s1s2p2p)}{\epsilon_{2s} - \epsilon_{1s}}.
$$

The 1s and 2s radial wave functions in $D_0(1s2s)$ are assumed to be the nonorthogonal solutions of the term-averaged HF equations for the final and initial configurations, respectively. The corre-
sponding one-electron energies are ϵ_{1s} and ϵ_{2s} . The values of the generalized Slater integrals R^k in Eq. (4) are not appreciably different if the L orbitals are taken from the final or initial state. The integral $R^0(2s1s1s1s)$ which dominates the numerator describes the change of the screening due to the filling of the 1s holes. The two other integrals describe the reduction of this screening due to the creation of the final $2p$ hole. Note that Eq. (4) is independent of the number of $2p$ electrons in the initial configuration. Our result indicates also that $D_0(1s2s)$ would not be affected very much by the multiplet splittings.

The intensity of $K\alpha\alpha^{h}$ is also influenced by final-state configuration interaction primarily because the $1s2s^22p^{n-1}$ and $1s^22s2p^{n-1}$ configura tions can mix. Assuming that the orbitals are solutions of the $1s^2 2s2p^{n-1}$ term-averaged HF equations, it can be shown that the interaction matrix element $\langle 1s2s^22p^{n-1}|H| 1s^22s2p^{n-1}\rangle$ is proportional to the exchange integral $R^1(2s1s2p2p)$ which appears in Eq. (4). The proportionality constant for any n and any term is smaller than 1 and can be either positive or negative. Since the absolute value of $R^1(2s1s2p2p)$ is only about 30% of that of $R⁰(2s1s1s1s)$ in the cases we have studied this configuration mixing does not change our shakedown results. However, we would like to stress that the relative intensity of $K\alpha\alpha^h$ may be sensitive to the detailed correlation between the two 1s electrons in the final state in analogy to the double-photoexcitation cross section of the K shell.¹⁰ Many configurations besides $1s2s^22p^{n-1}$ would be needed to describe this situation properly. Note also that the mixing due to the near degeneracy of the initial $1s^02s^22p^n$ and $1s^02s^02p^{n+2}$ configurations for $n \leq 4$ would suppress the initialstate energy.

In conclusion, we have shown that the shakedown rate of two-electron-one-photon K^2 - L^2 transitions relative to K^2 -KL hypersatellite transitions is of the order of 10^{-3} for $Z = 12$ and decreases approximately as Z^{-2} . Since there is a significant double- K ionization in many heavy- $\frac{1}{2}$ ion-atom collisions, $1s^{-2}$ \rightarrow $2s^{-1}2p^{-1}$ transitions should be observable. Our results support the available experimental evidence with regard to both energy and intensity.

*Work supported in part by the U. S. Energy Research and Development Administration under Contract No. $E(11-1)-2753.$

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